

DAA Assignment - 2

Ques 1 -

void func (int w)

{
 int j = 1, i = 0;

while (i < w)

 {
 i = j;

j++;

}

}

for j = 1 i = 1;

j = 2 i = 1+2;

j = 3 i = 1+2+3;

] m

$$\therefore 1+2+3+\dots < w$$

$$1+2+3+m < w$$

$$\frac{m(m+1)}{2} < w \rightarrow m \approx \sqrt{2w}$$

by summation 2 Method

$$\sum_{i=1}^m 1 \Rightarrow 1+1+\dots \sqrt{n} \text{ times}$$

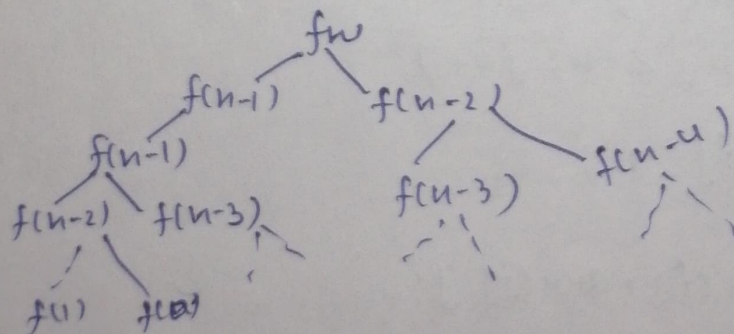
$$\therefore T(n) = \sqrt{n}$$

Ques 2 -

for fibonacci series -

$$f(n) = f(n-1) + f(n-2)$$

$$f(0) = 0 \quad f(1) = 1$$



∴ at every function call we get two function calls
for n levels.

we have $\Rightarrow 2 \times 2 \dots n$ times

$$\therefore T(n) = 2^n$$

Maximum Space Considering recursion

Stack

no of calls max = n

for each call we have space complexity $O(1)$

$$\therefore T(n) = O(n)$$

Ques - (a) $n \log n$:-

Quick Sort

void func [int arr[], int l, int k]

{
if ($l < k$)

{
int pi = partition(arr, l, k);

func(arr, l, $pi-1$);

func(arr, $pi+1$, k);

}

int partition (int arr[], int l, int k)

{
int pi = arr[k];

int u = (l-1);

for (int j = l; j <= k; j ++)

{
if (arr[j] < pi)

{
 u ++;

swap(arr[j], arr[u]);

}

swap(arr[u+1], arr[k]);
return $u+1$;

}

(b)

$$n^3 \div$$

Multiplication of two Square Matrix

for ($i=0$; $i < n$; $i++$)

{ for ($j=0$; $j < n$; $j++$)

{ for ($k=0$; $k < n$; $k++$)

{ $res[i][j] += a[i][k] * b[k][j]$;

(c)

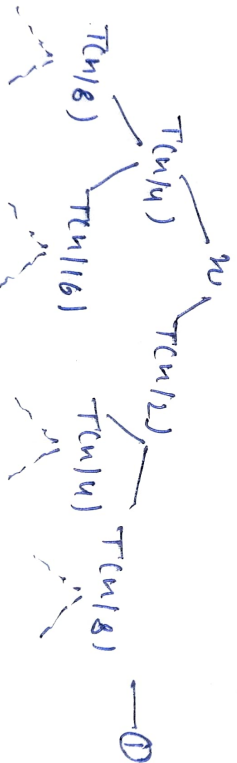
$\log(\log n)$

for ($i=2$; $i < n$; $i = i * i$)

{ $C++$;

Ans-

$$T(n) = T(n/4) + T(n/2) + C * n^2$$



level $0 \rightarrow n^2$

$$1 \rightarrow \frac{n^2}{4^2} + \frac{n^2}{2^2} = \frac{C * n^2}{16}$$

$$2 \rightarrow \frac{n^2}{8^2} + \frac{n^2}{16^2} + \frac{n^2}{4^2} + \frac{n^2}{8^2} = \left(\frac{5}{16}\right)^2 n^2 C$$

$$\text{max level} = \frac{n}{2^k} = 1$$

$$\Rightarrow k = \log_2 n$$

$$\therefore T(n) = \left[cn^2 + \left(\frac{5}{16}\right)n^2 + \left(\frac{5}{16}\right)^2 + \dots + \left(\frac{5}{16}\right) \log^4 n^2 \right]$$

$$T(n) = cn^2 \left[1 + \frac{5}{16} + \left(\frac{5}{16}\right)^2 + \dots + \left(\frac{5}{16}\right) \log^4 n \right]$$

$$T(n) = cn^2 \times 1 \times \left[\frac{1 - \left(\frac{5}{16}\right) \log^4 n}{1 - \frac{5}{16}} \right]$$

$$= cn^2 \times \frac{16}{5} \left[1 - \left(\frac{5}{16}\right) \log^4 n \right]$$

$$\therefore T(n) = O(n^2 c) \Rightarrow O(cn^2)$$

Ques-

Find few (u^o, v)

{

few $(u^o = j; u^o \leq w; i++)$

{

few $(j = 1; j \leq w; j++ = i)$

{

} }

for $u^o \quad j$

1

2

3

4

1+3+5
1+4+7
1+5+9

1
2
3
4

$$\sum_{u^o=1}^w \frac{(u-1)}{c}$$

$$\therefore T(n) = \frac{(n-1) + \frac{(n-1) + (n-1)}{2}}{2}$$

$$T(n) = n \left[1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right] - 1 \times n \left[1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right]$$

$$= n \log n - \log n$$

$$\therefore T(n) = O(n \log n)$$

$$\text{for } (i=2; i \leq w; i = \text{power}(i, k))$$

$$\left\{ \begin{array}{l} O(1) \end{array} \right\}$$

}

for $\rightarrow i$ 2^1 2^k 2^{k^2} 2^{k^3} \vdots 2^{k^m}

$$\text{where } 2^{k^w} \leq w$$

$$k^m = \log w$$

$$m \log k \log w$$

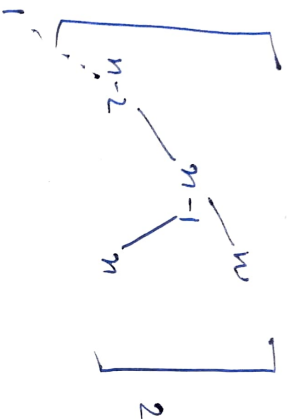
$$\therefore \sum_{i=1}^m 1$$

$$\Rightarrow 1 + \dots + m \text{ times}$$

$$\Rightarrow T(n) = O(\log k \log n)$$

Ques 7- Given Algo divides array in 99% & 1% part.

$$\therefore T(n) = T(n-1) + O(1)$$



'n' work is done at each level for merging.

$$T(n) = [T(n-1) + T(n-2) + \dots + T(1) + O(1)] \times n$$

$$T(n) = O(n^2)$$

$$\text{element} \quad \text{higher} = 2$$

$$\text{height} \quad \text{higher} = n$$

$$\therefore \text{diff} = n-2 \quad \therefore (n > 1)$$

- Ques- Considering for large values of n
- (a) $100 < \log \log n < \log n < (\log n)^2 < \sqrt{n} < n < n \log n < \log(n!) < n^2 < 2^n < 4^n < 2^{2^n}$
- (b) $1 < \log \log n < \sqrt{\log n} < \log n < \log 2n < 2 \log n < n < n \log n < 2n < 4n < \log(n!) < n^2 < n < 2 < \log 2n < 5n$
- (c) $96 < \log_8 n < \log 2n < 5n < n \log_6 n < n \log_2 n < \log(n!) < 8n^2 < 7n^3 < n! < 8^{2n}$