

Quick Sort

i location is ~~element~~ index of one

Partition of
Page _____

→ Partition

→ Quicksort.

9	4	6	3	7	1	2	11	5
---	---	---	---	---	---	---	----	---

i i

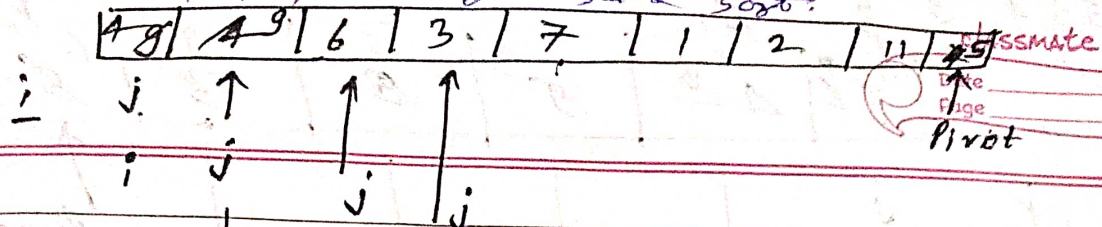
Pivot

i = set as pointer to NULL

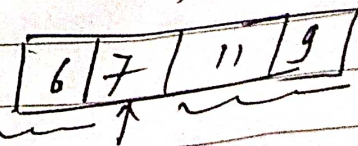
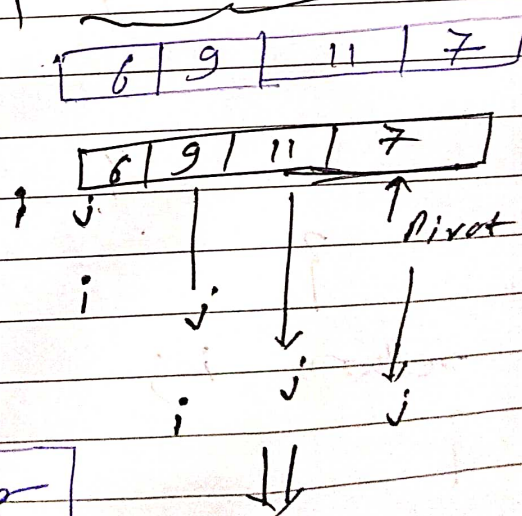
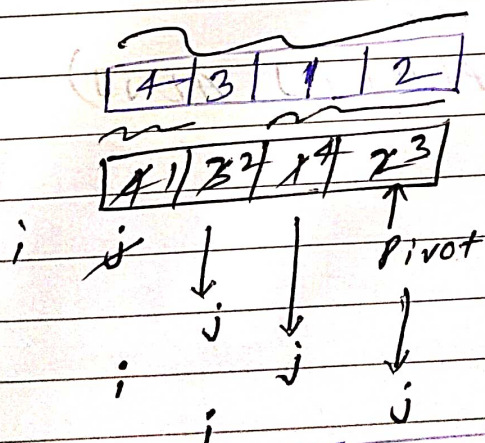
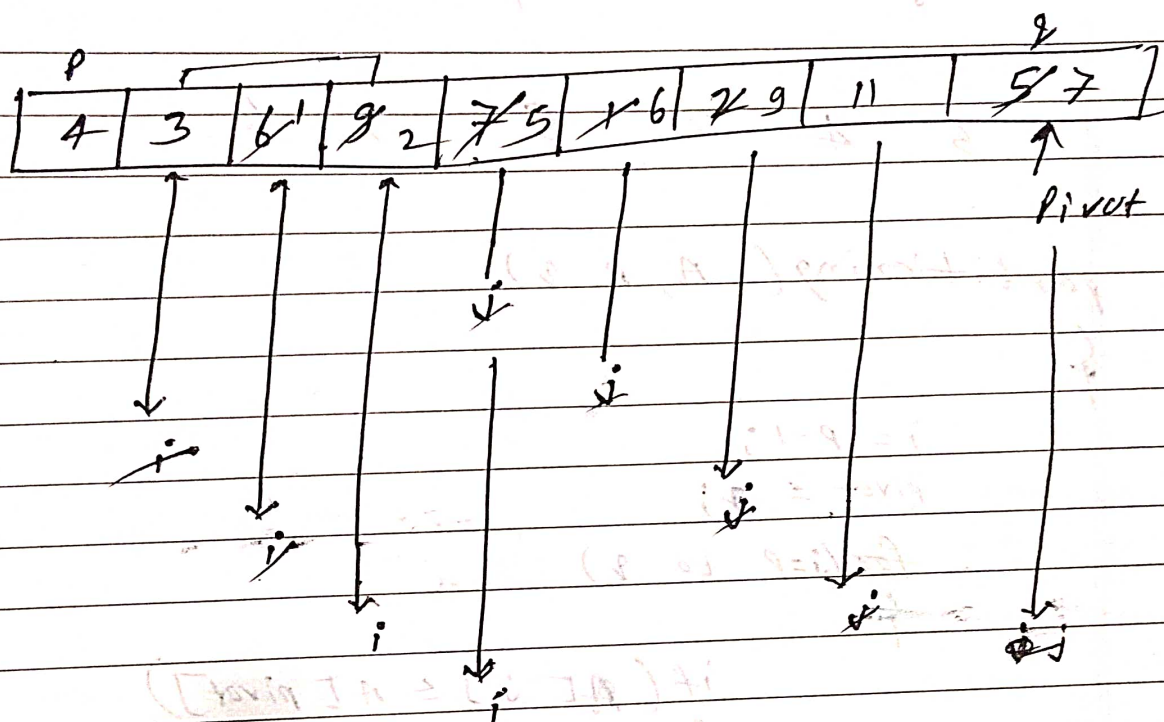
j = set pointer to list of element either from left, right side processing

- Increment for element of i & proceed upto pivot element
- Increment of i only if $a[i] < a[\text{pivot}]$.

Q- Sort 9, 4, 6, 3, 7, 1, 2, 11, 5 using Quick Sort.



- ① i is only increment if $a[j] \leq a[\text{pivot}]$, then swap the elements $a[i]$ and $a[j]$.
- ② j is increment every time till it reaches to pivot location element.
- ③ If $a[j] == a[\text{pivot}]$, then swap $a[i]$ & $a[\text{pivot}]$.



- Initial Setting of i & pivot for an Array A , and setting of $i = j - 1$
1. Compare $A[j]$ & $A[\text{pivot}]$ as $a[j] \leq a[\text{pivot}]$, then increment $i = i + 1$ and swap of $A[i]$ & $A[j]$.
 2. j is incremented till it doesn't reach to pivot & increment in i due to $A[j] == A[\text{pivot}]$.
 3. If $A[j] == A[\text{pivot}]$ then swap $A[i]$ & $A[\text{pivot}]$.

Algorithm Quick Sort

Date _____

Page _____

QuickSort(p, q)

{

if ($p < q$) then

{

// Divide p into two subproblems

$j = \text{Partition}(A, p, q)$

// j is the position of the element.

// solve the subproblems

QuickSort($p, j-1$);

QuickSort($j+1, q$);

}

}

→ p is j setting
→ q is pivot setting

partitioning(A, p, q)

$i = p - 1$

$pivot = A[p]$

for($j = p$ to q)

{

if ($A[j] \leq A[pivot]$)

{

$i = i + 1$

swap($A[i], A[j]$)

}

}

return i

}

10

5

4

6

4

3

5

4



01



2

2

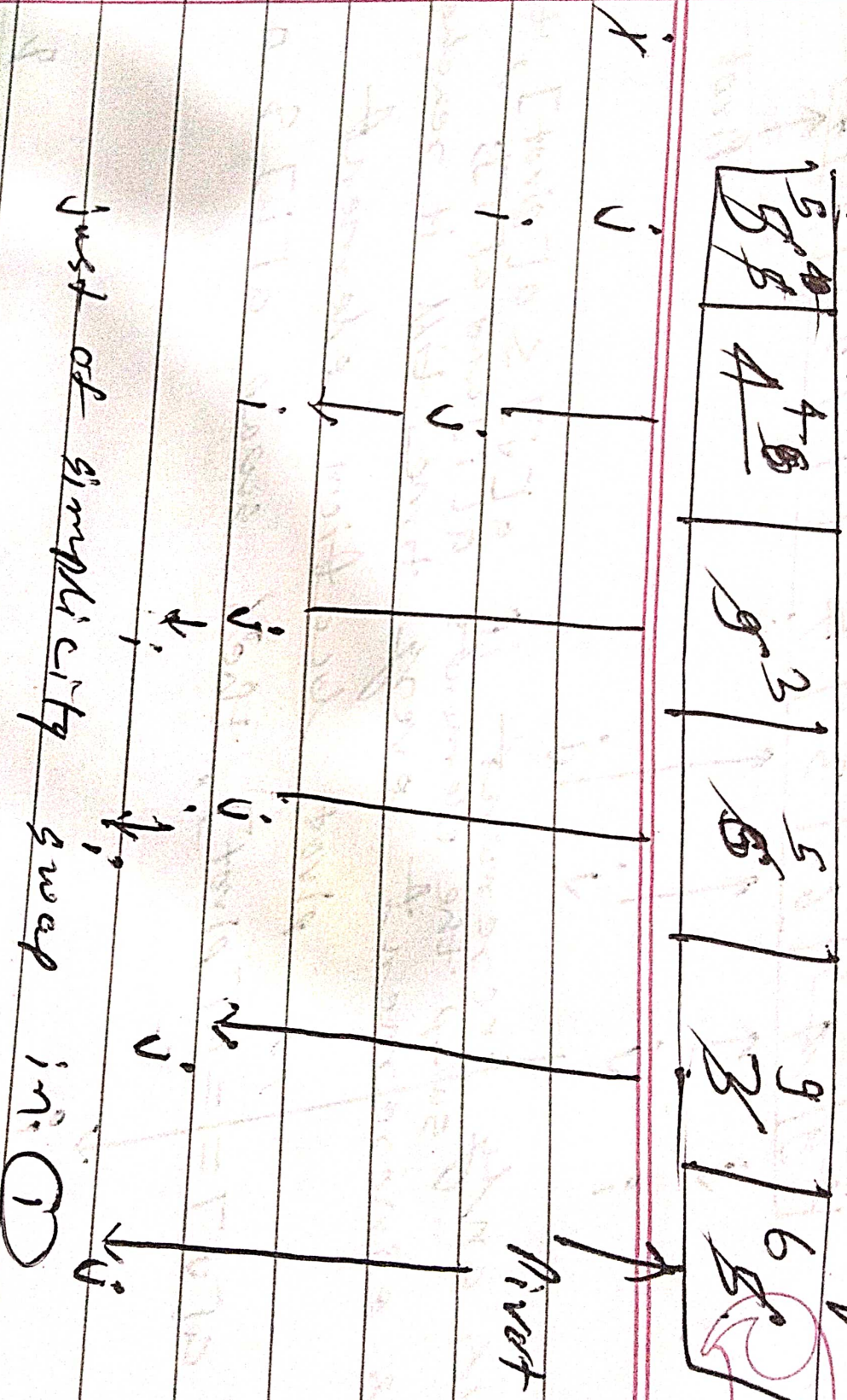


of

22

Date _____

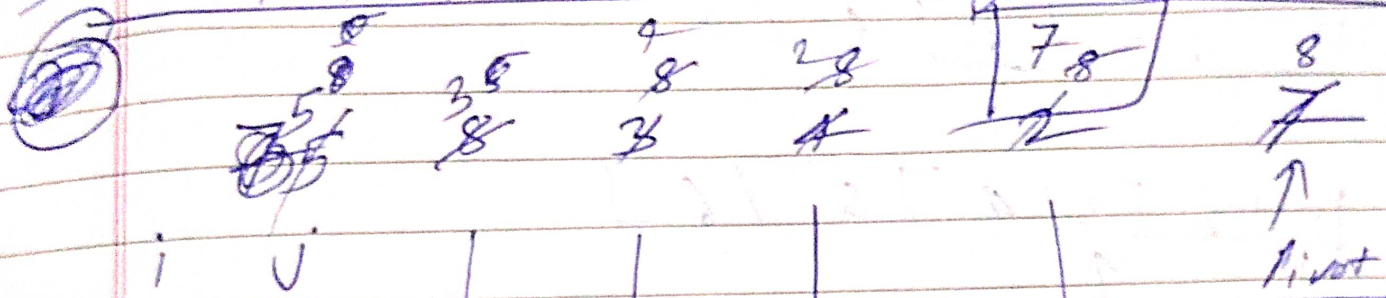
১১১১



just of simplicity sweep in (1)

Q:-

5, 8, 3, 4, 2, 7 Sort using Quick Sort



$$a[j] \leq a[\text{pivot}]$$

$$5 < 7$$

$$8 < 7$$

$$3 < 7$$

$$4 < 7$$

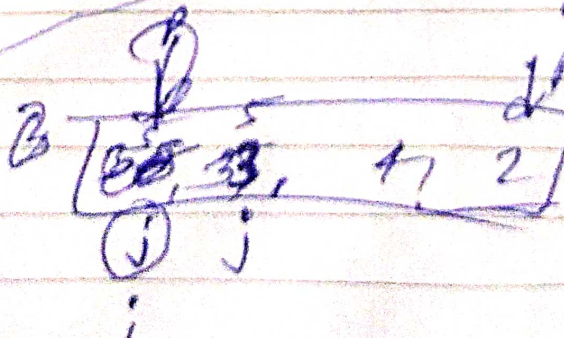
Notation
Big Oh
Omega
Theta

$$1 + 2 + \dots + n = \frac{n(n+1)}{2} = \frac{1}{2}n^2 + \frac{1}{2}n = O(n^2)$$

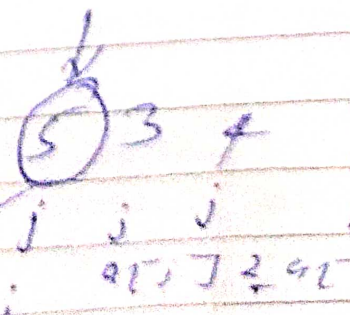
$$2 + 3 + 4 + 5 + 6 = \frac{n(n+1)}{2}$$

$$f(n) = m \lg(n)$$

$$f(n) = O(\lg(n))$$



Partition



$$[2] \{ 3, 4, 5 \}$$

Worst Case ~~Quick~~ Sort

classmate

Date

Page

$$O(n^2)$$

$$T(n) = T(n-1) + O(n)$$

Randomized Quick Sort

1 2 3 4 5 6

Place the elements in random order

(I)

1	3	2	6	4	5
---	---	---	---	---	---

(II)

1	2	3	4	5	6
---	---	---	---	---	---



Random pivot selection.

✓ Chances of getting reduced worst case time.

Complexity

1. Average Case Complexity

$$O(n \log_2 n)$$

2. Worst case $O(n^2)$, when elements are sorted to apply for quick sort.