```
1. def coin_change(coins, amount):
  dp = [float('inf')] * (amount + 1)
  dp[0] = 0
  for coin in coins:
     for x in range(coin, amount + 1):
        dp[x] = min(dp[x], dp[x - coin] + 1)
  return dp[amount] if dp[amount] != float('inf') else -1
coins = [1, 2, 5]
amount = 11
print("Minimum coins required:", coin change(coins, amount))
2. def knapsack(values, weights, W):
  n = len(values)
  dp = [[0 \text{ for } x \text{ in } range(W + 1)] \text{ for } x \text{ in } range(n + 1)]
  for i in range(n + 1):
     for w in range(W + 1):
       if i == 0 or w == 0:
          dp[i][w] = 0
        elif weights[i-1] <= w:
          dp[i][w] = max(values[i-1] + dp[i-1][w-weights[i-1]], dp[i-1][w])
        else:
          dp[i][w] = dp[i-1][w]
  return dp[n][W]
values = [60, 100, 120]
weights = [10, 20, 30]
W = 50
```

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print("Maximum value in Knapsack =", knapsack(values, weights, W))
3. class Job:
  def init (self, id, deadline, profit):
     self.id = id
     self.deadline = deadline
     self.profit = profit
def job sequencing(jobs):
  jobs.sort(key=lambda x: x.profit, reverse=True)
  n = len(jobs)
  result = [False] * n
  job sequence = ['-1'] * n
  for i in range(len(jobs)):
     for j in range(min(n - 1, jobs[i].deadline - 1), -1, -1):
       if result[j] is False:
          result[j] = True
          job sequence[j] = jobs[i].id
          break
  return job sequence
jobs = [Job('a', 2, 100), Job('b', 1, 19), Job('c', 2, 27), Job('d', 1, 25), Job('e', 3, 15)]
print("Job sequence:", job_sequencing(jobs))
4. import heapq
def dijkstra(graph, start):
  queue = [(0, start)]
  distances = {vertex: float('inf') for vertex in graph}
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distances[start] = 0

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while queue:
     current distance, current vertex = heapq.heappop(queue)
     if current_distance > distances[current_vertex]:
       continue
     for neighbor, weight in graph[current_vertex].items():
       distance = current distance + weight
       if distance < distances[neighbor]:
          distances[neighbor] = distance
          heapq.heappush(queue, (distance, neighbor))
  return distances
graph = {
  'A': {'B': 1, 'C': 4},
  'B': {'A': 1, 'C': 2, 'D': 5},
  'C': {'A': 4, 'B': 2, 'D': 1},
  'D': {'B': 5, 'C': 1}
start vertex = 'A'
print("Shortest paths from", start_vertex, ":", dijkstra(graph, start_vertex))
5. import heapq
from collections import defaultdict
class Node:
  def init (self, freq, symbol, left=None, right=None):
     self.freq = freq
     self.symbol = symbol
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}

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self.left = left
     self.right = right
     self.huff = "
def huffman tree(symbols, freq):
  heap = [[weight, [symbol, "]] for symbol, weight in zip(symbols, freq)]
  heapq.heapify(heap)
  while len(heap) > 1:
     lo = heapq.heappop(heap)
     hi = heapq.heappop(heap)
     for pair in lo[1:]:
       pair[1] = '0' + pair[1]
     for pair in hi[1:]:
       pair[1] = '1' + pair[1]
     heapq.heappush(heap, [lo[0] + hi[0]] + lo[1:] + hi[1:])
  return sorted(heapq.heappop(heap)[1:], key=lambda p: (len(p[-1]), p))
symbols = ['A', 'B', 'C', 'D', 'E', 'F']
freq = [5, 9, 12, 13, 16, 45]
huffman code = huffman tree(symbols, freq)
print("Huffman Codes:")
for p in huffman code:
  print(f"Symbol: {p[0]}, Code: {p[1]}")
6. def container loading(weights, capacity):
  weights.sort()
  total weight = 0
  for weight in weights:
     if total weight + weight <= capacity:
       total weight += weight
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else:
       break
  return total weight
weights = [10, 20, 30, 40, 50]
capacity = 100
print("Maximum weight loaded:", container_loading(weights, capacity))
7. class Graph:
  def _init_(self, vertices):
     self.V = vertices
     self.graph = []
  def add_edge(self, u, v, w):
     self.graph.append([u, v, w])
  def find(self, parent, i):
     if parent[i] == i:
       return i
     return self.find(parent, parent[i])
  def union(self, parent, rank, x, y):
     root x = self.find(parent, x)
     root y = self.find(parent, y)
     if rank[root_x] < rank[root_y]:</pre>
       parent[root_x] = root_y
     elif rank[root x] > rank[root y]:
       parent[root_y] = root_x
     else:
       parent[root y] = root x
       rank[root_x] += 1
```

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def kruskal_mst(self):
     result = []
     i = 0
     e = 0
     self.graph = sorted(self.graph, key=lambda item: item[2])
     parent = []
     rank = []
     for node in range(self.V):
       parent.append(node)
       rank.append(0)
     while e \le self.V -
8. import heapq
def prim(graph, start):
  mst = []
  visited = set()
  min heap = [(0, start, None)]
  while min_heap:
     weight, current, prev = heapq.heappop(min heap)
     if current not in visited:
       visited.add(current)
       if prev is not None:
          mst.append((prev, current, weight))
       for neighbor, wt in graph[current].items():
          if neighbor not in visited:
```

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return mst
graph = {
  'A': {'B': 1, 'C': 4},
  'B': {'A': 1, 'C': 2, 'D': 5},
  'C': {'A': 4, 'B': 2, 'D': 1},
  'D': {'B': 5, 'C': 1}
}
start vertex = 'A'
print("Edges in MST:", prim(graph, start_vertex))
9. class Graph:
  def _init_(self, vertices):
     self.V = vertices
     self.graph = []
  def add_edge(self, u, v, w):
     self.graph.append([u, v, w])
  def find(self, parent, i):
     if parent[i] == i:
        return i
     return self.find(parent, parent[i])
  def union(self, parent, rank, x, y):
     root x = self.find(parent, x)
     root y = self.find(parent, y)
     if rank[root x] < rank[root y]:
        parent[root_x] = root_y
```