## CS 1511 Homework 15

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## 29.)

Let  $L \in BP \cdot NP$ .

 $\exists TM\ T$  and  $\exists Integer\ k$  such that:

 $\forall x \forall R \ \mathrm{T(x,R)} \ \mathrm{halts} \ \mathrm{in} \mid x \mid^k \mathrm{steps}$ 

 $x \in L \text{ iff } prob(T(x,R) \in 3\text{-SAT}) \ge 3/4$ 

 $x \notin L \text{ iff } prob(T(x,R) \in 3\text{-SAT}) \le 1/4$ 

First off, we will ignore the second tape in this T.

We will create our circuit C to accept two inputs (x,y) with x being an encoding of T.

The y will be hardwired to be our correct set R. Below is how we will build this correct set. If this machine is run  $n^2$  times, then the prob(T is wrong) becomes  $< 1/4^n$  according to statistics.

If we get wrong answers, we can simply throw them away. We build R from the correct set. By the union bound,  $\forall n, \exists R \text{ such that } \forall x \mid x \mid = n \text{ implies } T(x, R) \text{ is correct. We just need to find an R that works.}$ 

 $\exists C_n \text{ family of circuits } \{C_n\}_{n\geq 1} \text{ such that }$ 

 $L \in NP/Poly$