

CS 1511 Homework 2

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3. (a)

$$E_{TM} = \{\langle M \rangle \mid M \text{ is a TM and } L(M) = \emptyset\}$$

Assume \exists TM R that decides E_{TM} .

Construct Turing Machine S that decides $HALT_{TM}$.

S = "On input $\langle M, w \rangle$ where M is a TM and w is a string:

1. Construct TM M' as follows:

M' = "On input x :

(a) Run M on input w

(b) If M accepts w , reject. Otherwise accept.

2. Run R on input $\langle M' \rangle$

3. If R accepts $\langle M' \rangle$ reject otherwise accept.

Assume that $\langle M, w \rangle \in HALT_{TM}$. Since $\langle M, w \rangle \in HALT_{TM}$, M halts on input w , so $L(M') = \Sigma^*$. Since $L(M') \neq \emptyset$, $\langle M' \rangle \notin E_{TM}$. Since R is a decider for E_{TM} , running input $\langle M' \rangle$ will cause R to reject $\langle M' \rangle$, so S will accept $\langle M, w \rangle$.

Assume that $\langle M, w \rangle \notin HALT_{TM}$. Since $\langle M, w \rangle \notin HALT_{TM}$, M does not halt on input w , so $L(M') = \emptyset$. Since $L(M') = \emptyset$, $\langle M' \rangle \in E_{TM}$. Since R is a decider for E_{TM} , running input $\langle M' \rangle$ will cause R to accept $\langle M' \rangle$, so S will reject $\langle M, w \rangle$.

4.

The holographic principle was developed after thorough debates about black holes between Stephen Hawking and Leonard Susskind. Susskind developed the principle, which states that a black hole takes in a three-dimensional and spreads it around its entire event horizon from an outside view. This is similar to a hologram where an object in one place is spread across a film. This principle also applies to the three-dimensional universe, where everything is laid out across a one-dimensional film at the edge of the universe. Furthermore, Hawking argued that black holes destroy information when objects pass into them. Susskind, who was correct, argued that black holes take in and outwardly radiate the information they take in, preserving it in its entirety.