# CS 1511 Homework 22

## Mathew Varughese, Justin Kramer, Zach Smith

### Fri, April 5

#### 43

If  $a = 0^n$ , Simon's algorithm still works. This is because if the function is one-to-one, and  $a = 0^n$ , after we compute  $|xz\rangle - > |x(y \oplus f(x))\rangle$  we can measure  $|(x \oplus a)|$  and see that it's equivalent to x. This will let us know that  $a = 0^n$ . We will therefore have correctly computed a. Or, if we continue Simon's algorithm, we will eventually be finding k linear equations for  $y \odot a = 0$  with a uniform string for y that makes this true. In this case, every single one of these y's will work. Solving the linear equations will give us that all values of a are 0, which is true.

**44 a.** To get the Bell state  $1/\sqrt{2} \mid 0\rangle + 1/\sqrt{2} \mid 1\rangle$ , Alice would apply Hadamard operation to her qubit. This will be when x = 0 and y = 0.

To get the Bell state  $1/\sqrt{2} \mid 0\rangle - 1/\sqrt{2} \mid 1\rangle$ , Alice can perform a multiplication by  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$  to her qubit after a Hadamard. This will be when x = 0 and y = 1.

To get the Bell state  $-1/\sqrt{2} \mid 0\rangle + 1/\sqrt{2} \mid 1\rangle$ , Alice can perform a CNOT gate operation to her qubit. This will be when x = 1 and y = 0.

To get the Bell state  $-1/\sqrt{2} \mid 0\rangle - 1/\sqrt{2} \mid 1\rangle$ , Alice can perform a multiplication by  $\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$  to her qubit before a CNOT gate operation. This will be when x = 1 and y = 1.

#### 44 b.

If x = 0 and y = 0, we get the original state  $1/\sqrt{2} \mid 00 \rangle + 1/\sqrt{2} \mid 11 \rangle$ 

If x = 0 and y = 1, we get the state  $1/\sqrt{2} \mid 00\rangle - 1/\sqrt{2} \mid 11\rangle$ 

If x = 1 and y = 0, we get the state  $1/\sqrt{2} \mid 10\rangle + 1/\sqrt{2} \mid 01\rangle$ 

If x = 1 and y = 1, we get the state  $1/\sqrt{2} \mid 01 \rangle - 1/\sqrt{2} \mid 10 \rangle$ 

#### 44 c.

When Bob measures his qubit b, the state of qubit a will collapse to state 0 or 1 with equal probability 1/2 of each occurring. If we then take a CNOT gate to qubits a and b and then a Hadamard gate operation on qubit a, we will see the x value as the "x coordinate" of the

resulting vector and the y value as the "y coordinate" of the resulting vector.