

NISTIR 8292 DRAFT SUPPLEMENT

Face Recognition Vendor Test (FRVT)

Part 4: MORPH - Performance of Automated Face Morph Detection

Mei Ngan
Patrick Grother
Kayee Hanaoka
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<https://www.nist.gov/programs-projects/face-recognition-vendor-test-frvt-ongoing>



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U.S. Department of Commerce
Gina M. Raimondo, Secretary

National Institute of Standards and Technology
James K. Olthoff, Performing the Non-Exclusive Functions and Duties of the Under Secretary of Commerce for Standards and Technology & Director, National Institute of Standards and Technology

FRVT MORPH Status and Changelog

Prior editions of this report are maintained on the FRVT MORPH website. The FRVT MORPH evaluation remains open to new algorithm submissions indefinitely. This report will be updated as new algorithms are evaluated, as new datasets are added, and as new analyses are included. Comments and suggestions should be directed to frvt@nist.gov.

July 27, 2021

- This report adds single-image and differential morph detection results for a new dataset of morphs created using the MIPGAN software provided by the Norwegian University of Science and Technology. See Sections 2.3, 4 and Figure 17.
- An updated version of the [FRVT MORPH API](#) document has been published. This update adds an optional input parameter to the function `detectMorphDifferentially()`. The additional parameter represents the time/age difference (in days) between a suspected morph and the live probe image.
- Interactive report cards for each algorithm have been published and linked from the results table on the [FRVT MORPH webpage](#). For example, https://pages.nist.gov/frvt/reportcards/morph/hdalbp_005_1.html.

April 16, 2021

- This report adds algorithm score distribution plots (Section 4.6) and APCER calibration plots (Section 4.7).
- This report updates the differential bona fide morph detection scores vs. elapsed time plots, now with results for both visa and mugshot bona fide datasets. See Section 4.9.
- Interactive report cards for each algorithm will be published and linked from the [FRVT MORPH webpage](#) in the coming weeks.

February 02, 2021

- This report updates the morph detection error metrics, attack presentation classification error rate (APCER) and bona fide classification error rate (BPCER), to incorporate when an algorithm fails to process an image. See Sections 3 and 4.1.2. Results in all tables and plots in this report and on our website reflect this change unless otherwise noted.
- This report includes single-image and differential morph detection results for three new datasets of morphs (Visa-Border, UNIBO Automatic Morphed Face Generation Tool v2.0, Twente) created using new and updated methods provided by the University of Twente and the University of Bologna. See Sections 2.3 and 4.
- This report adds differential morph detection results for the UNIBO Automatic Morphed Face Generation Tool v1.0 dataset. See Sections 2.3, 4.3, and Figure 12.
- This report replaces the term "match score" with "comparison score" where applicable to better align with standard terminology.

July 24, 2020

- This report adds results for one new algorithm (hdadfr-003) submitted by Hochschule Darmstadt. See Section 2.2.

June 3, 2020

- This report adds results for two new algorithms (hdadfr-002, hdalaplace-001) submitted by Hochschule Darmstadt. See Section 2.2.
- This report adds a new dataset to support assessment of image resolution on morph detection accuracy. See Section 2.3.

- This report documents initial analyses on the impact of image resolution on single-image morph detection accuracy. See Executive Summary and Section 4.5.

March 4, 2020

- This report has been formally published as NIST Interagency Report (NISTIR) 8292.

January 24, 2020

- This report adds results for seven new algorithms submitted by Hochschule Darmstadt and one new algorithm submitted by the Norwegian University of Science and Technology. See Section 2.2.
- This report includes results for a new dataset of morphs provided by the University of Lincoln. See Section 4.4.3.
- This report includes results for a new dataset of bona fide images, which includes 1) a set of high quality visa portraits for single-image morph detection and 2) a set of high quality visa portraits + a set webcam probes that exhibit moderately poor pose variations and background illumination for two-image differential morph detection. See Sections 2.3, 4.1.1, 4.2, and 4.3.
- Sample imagery for the new datasets have been added to Figures 2 and 3.
- The accuracy results in Tables 4.2 and 4.3 are now grouped by dataset and ordered by algorithm accuracy (APCER @ BPCER_m=0.01).
- This report documents new analyses, including 1) BPCER as a function of morph detection score threshold across visa and mugshot datasets and 2) for two-image differential morph detection, bona fide morph detection score as a function of time elapsed between the bona fide and probe image.
- We have migrated our website to a new platform that supports interactive plotting and sortable tables: https://pages.nist.gov/frvt/html/frvt_morph.html. Summary accuracy tables and DET plots are published on the website and will be updated as new results are available.

September 17, 2019

- This is the first FRVT MORPH report published as a draft for public comment. This report documents results for five morph detection algorithms over twelve datasets.

Executive Summary

Background

Face morphing and the ability to detect it is an area of high interest to photo-credential issuance agencies, companies, and organizations employing face recognition for identity verification. Face morphing is an image manipulation technique where two or more subjects' faces are morphed or blended together to form a single face in a photograph. Morphed photos can look very realistically like all contributing subjects. Morphing is easy to do and requires little to no technical experience given the vast availability of tools available at little or no cost on the internet and mobile platforms. If a morphed photo gets onto an identity credential for example, multiple, if not all constituents of the morph, can use the same identity credential. Morphs can be used to fool both humans [1] [2] and current face recognition systems [3], which presents a vulnerability to current identity verification processes.

FRVT MORPH Test Activity

The FRVT MORPH test provides ongoing independent testing of prototype face morphing attack detection (MAD) technologies. The evaluation is designed to obtain commonly measured assessment of morph detection capability to inform developers and end-users. FRVT MORPH is open for ongoing participation worldwide, and there is no charge to participate. The test opened in June 2018, and NIST has since received a number of morph detection algorithm submissions from international academic entities, including Hochschule Darmstadt, Norwegian University of Science and Technology, and University of Bologna.

The test leverages a number of datasets created using different morphing methods with goals to evaluate algorithm performance over a large spectrum of morphing techniques. Testing was conducted using a tiered approach, where algorithms were evaluated on low quality morphs created with readily accessible tools available to non-experts, morphs generated using automated morphing methods based on academic research, and high quality morphs created using commercial-grade tools. We'd like to get an assessment on the existence and extent of morph detection capabilities, and if there is indication of high accuracy, much larger datasets can be curated to support large-scale evaluation of the technology.

Results and Notable Observations

Ideally, it is important that morph detection technology produce very low false detection rates given the assumption that most transactions will be on legitimate photos that are not morphs. False detection rates need to be controlled, because additional amounts of resources will be required to adjudicate such errors. With that said, an initial automated morph detection capability with say ideally 0% false detection rates but high morph miss rates would still yield gains in operations compared to not having any morph detection capability at all.

- **Single-image Morph Detection:** In this use case, a single image is provided to the algorithm, and the software has to 1) make a decision on whether it thinks the image is a morph and 2) provide a confidence score on its decision.

To assess morph detection performance, two primary quantities are reported - the Attack Presentation Classification Error Rate (APCER) or morph miss rate and the Bona Fide Classification Error Rate (BPCER) or false detection rate (see Section 3). APCER and BPCER are reported both individually and as a tradeoff in the DET analysis in this report. For the algorithms submitted to this track thus far, morph miss rates generally remain very high (above 0.82) at a false detection rate of 0.01. This can be interpreted as "at the cost of incorrectly claiming that 1 in every 100 legitimate photos is a morph, the percentage of actual morphs that are not being correctly detected is above 82%". This is observed across all algorithms and all datasets tested, and is indicative of the technology maturity still being in its infancy for practical application. While large reductions in morph miss rates are observed when the false detection rate is relaxed to 0.1, the single-image morph detection algorithms evaluated often do not generalize well across different morphing methodologies, and morph detection with a single image in isolation remains a challenging research issue. *Section 4.2, 4.4*

Caveat: There is an exception to the generally high morph miss rates observed, which is the University of Bologna's algorithm (unibo-000) result against morphs created using techniques developed also by the University of Bologna in the UNIBO Automatic Morphed Face Generation Tool v1.0 and v2.0 datasets. Those particular datasets were generated using a set of sequestered source images and morphed using software that implemented techniques published in [3–6]. The unibo-000 algorithm's morph miss rate is 0.09 and 0.16 at a false detection rate of 0.01 on datasets

generated with their v1.0 and v2.0 tool respectively. While such results need to be caveated, it highlights an interesting data point which quantifies that morph detection software can be trained/designed to detect images created using a particular morphing process and confirms the importance of cross-database training and testing for the development and evaluation of morphing detection algorithms. *Section 4.2.2*

Image Resolution: We conducted an initial study on whether image resolution has an impact on single-image morph detection accuracy. The results show that some algorithms are able to take advantage of additional resolution in images and reduced error rates are observed as image resolution increases. For those algorithms, there appears to be diminishing returns in error reduction when the interocular distance (IOD) is larger than 600 pixels. These results are caveated with necessary assessments of APCER (morph miss rates) and BPCER (false detection rates) separately as a function of score threshold. Interestingly, we observe that while false detection rates decrease in higher resolution images (at equal thresholds), morph miss rates increase as resolution increases (at equal thresholds).

The implications of these initial results would mean for ecosystems that only expect and can enforce processing of images at high resolution, then the use of higher resolution photos would yield reductions in error rates, for some algorithms. But, consequently, in a morph detection system that is set to a threshold configured for higher resolution photos, if it encounters lower resolution photos, the system would expect 1) increased false detection rates but favorably, 2) decreased morph miss rates. Likewise, in a system that is configured at a threshold targeted for lower resolutions, when higher resolution photos are encountered, the system would observe, favorably, decreased false detection rates, but unfavorably, increased morph miss rates. The existence and magnitude of these observations vary between algorithms. *Section 4.5*

Printing and Scanning: The process of printing and scanning (printing a digital image onto paper, then scanning it back in) or re-digitalization is known to be one of the biggest challenges to morph detection. The process of printing and scanning photos is followed by a number of identity credential issuance entities (e.g. passports) worldwide in countries that rely on mail-in applications. Therefore, the use case of morph detection on printed and scanned photos is very relevant. We investigate the performance of algorithms on print and scanned photos using a subset of images (both morphs and nonmorphs) from the UNIBO Automatic Morphed Face Generation Tool v1.0 dataset, printed with an HiTi P310W photo printer, and scanned back in with a Fujitsu fi-7280 scanner at 300 PPI. For a majority of the algorithms, morph miss rates are low BUT false detection rates are extremely high, so the algorithms appear to be classifying most scanned photos as morphs, even when they're not. The unibo-000 algorithm results show that on the same set of morphed images that it was able to successfully detect originally as digital photos, once printed and scanned back in, morph miss rates increased by 49%. *Section 4.2.3*

- **Two-image Differential Morph Detection:** In this use case, two face photos are provided to the algorithm, the first being a suspected morph and the second image representing a known, non-morphed face image of one of the subjects contributing to the morph (e.g., live capture image from an eGate). The software has to 1) make a decision on whether it thinks the image is a morph and 2) provide a confidence score on its decision. This procedure supports measurement of whether algorithms can detect morphed images when additional information (the second photo) is provided. While morph miss rates are very high at a false detection rate of 0.01 (1 in 100) for all algorithms, notable results are observed for the hdaarcface-001 (and its subsequent updates, hdadfr-002 and hdadfr-003) algorithms. There are significant reductions in morph miss rates for hdaarcface-001 if the false detection rate is relaxed. At a false detection rate of 0.1 (1 in 10), morph miss rates are reduced to 17% or below across all datasets tested, which demonstrates better generalizability on different morphing methods when compared to the single-image morph detection algorithms tested to date.

We continue to expand our test to evaluate differential morph detection capabilities across a spectrum of morphing methods and types of imagery. *Section 4.3*

Future Work

FRVT MORPH will run continuously, and this report will be updated as new algorithms, datasets, analyses, and metrics are added.

Acknowledgements

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The authors are grateful to staff in the NIST Biometrics Research Laboratory for infrastructure supporting rapid evaluation of algorithms.

Disclaimer

Specific hardware and software products identified in this report were used in order to perform the evaluations described in this document. In no case does identification of any commercial product, trade name, or vendor, imply recommendation or endorsement by the National Institute of Standards and Technology, nor does it imply that the products and equipment identified are necessarily the best available for the purpose.

The data, protocols, and metrics employed in this evaluation were chosen to support morph detection research and should not be construed as indicating how well these systems would perform in applications. While changes in the data domain, or changes in the amount of data used to build a system, can greatly influence system performance, changing the task protocols could reveal different performance strengths and weaknesses for these same systems.

Institutional Review Board

The National Institute of Standards and Technology's Research Protections Office reviewed the protocol for this project and determined it is not human subjects research as defined in Department of Commerce Regulations, 15 CFR 27, also known as the Common Rule for the Protection of Human Subjects (45 CFR 46, Subpart A).

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1 The FRVT MORPH Activity

Face morphing and the ability to detect it is an area of high interest to a number of photo-credential issuance agencies and those employing face recognition for identity verification. Face morphing is an image manipulation technique where two or more subjects' faces are morphed or blended together to form a single face in a photograph. Morphed photos can look very realistically like all contributing subjects. If a morphed photo gets onto an identity credential for example, multiple, if not all constituents of the morph, can use the same identity credential. Morphs can be used to fool both humans [1] [2] and current face recognition systems [3], which presents a vulnerability to current identity verification processes. Figure 1 illustrates the impact of morphed photos on current algorithms from some of the leading face recognition algorithms (labeled as A, B, C, and D) submitted to the NIST Ongoing FRVT 1:1 Verification test. The overlap between the morph and genuine comparison score distributions, and the significant percentage of morph comparisons that would successfully authenticate at FMR=0.001 (1 in 1000) provides the basis for research into how to detect this form of image manipulation.

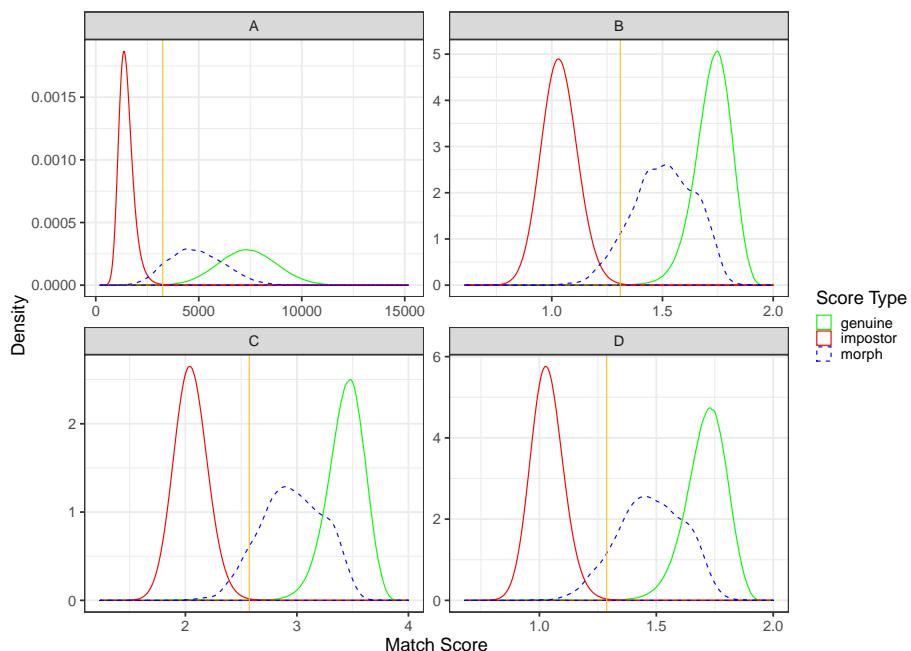


Figure 1: Morph comparison score distribution. The plot shows comparison score distribution for 1) genuine comparisons of photos of the same person (green) 2) imposter comparisons of photos of different people (red), and 3) morph comparisons of morphed photos with other photos of contributing subjects (blue). The gold line represents the score threshold at a false match rate (FMR) of 0.001. All comparison scores to the right of the gold line indicate that the algorithm thinks the photos are of the same person at that FMR threshold (e.g. successful authentication at an eGate).

The FRVT MORPH test will provide ongoing independent testing and measurement of prototype face morph detection technologies. The evaluation is designed to obtain an assessment of morph detection capability to inform developers and end-users, and will evaluate two separate tasks:

- Algorithmic capability to detect face morphing (morphed/blended faces) in still photographs:
 - Single-image morph detection of non-scanned photos, printed-and-scanned photos, and images of unknown photo format/origin;
 - Two-image differential morph detection of non-scanned photos, printed-and-scanned photos, and images of unknown photo format/origin. This procedure supports measurement of whether algorithms can detect morphed images when additional information, such as a live capture image, is provided.

- Face recognition algorithm resistance against morphing. The expected behavior from algorithms is to be able to correctly reject comparisons of morphed images against all constituents that contributed to the morph. The goal is to show algorithm robustness against morphing alterations when morphed images are compared against other images of the subjects used for morphing.

2 Methodology

2.1 Test Environment

The evaluation was conducted offline at a NIST facility. Offline evaluations are attractive because they allow uniform, fair, repeatable, and large-scale statistically robust testing. Testing was performed on high-end server-class blades running the CentOS Linux [7] operating system. The test harness used concurrent processing to distribute workload across dozens of computers.

2.2 Algorithms

The FRVT MORPH program is open to participation worldwide. The participation window opened in June 2018, and the test will evaluate algorithms on an ongoing basis. There is no charge to participate. The process and format of algorithm submissions to NIST are described in the FRVT MORPH Concept, Evaluation Plan, and Application Programming Interface (API) document [8]. Participants provide their submissions in the form of libraries compiled on a specified Linux kernel, which are linked against NIST's test harness to produce executables. NIST provides a validation package to participants to ensure that NIST's execution of submitted libraries produces the expected output on NIST's test machines.

This report documents the results of all algorithms submitted for testing to date. Tables 1 and 2 lists the participants who submitted algorithms to FRVT MORPH.

Participant Name	Short Name	Submission Sequence	Submission Date	Developer Notes
Hochschule Darmstadt	hdalbp	005 006	2018.11.29 2019.12.02	The idea behind the LBP implementation is based on HDA (http://dasec.h-da.de) / NTNU (https://www.ntnu.edu/nbl) approaches and published in [9–11].
Hochschule Darmstadt	hdaprnu	002 004	2019.04.09 2020.01.21	The idea behind the PRNU implementation is based on a HDA (http://dasec.h-da.de) / PLUS (http://www.wavelab.at) cooperation and published in [12, 13].
Norwegian University of Science and Technology	ntnussl	001 002	2019.07.08 2019.10.11	[14]
University of Bologna	unibo	000	2019.07.29	
Hochschule Darmstadt	hdabsif	004	2020.01.17	
Hochschule Darmstadt	hdalaplace	001	2020.04.01	

Table 1: FRVT MORPH Participants (Single-image Morph Detection)

Participant Name	Short Name	Submission Sequence	Submission Date	Developer Notes
Hochschule Darmstadt	hdawl	000 002	2019.03.29 2019.12.02	The hdawl submission is a weighted landmark analysis approach (i.e., difference of landmarks) and is based on the work described in [15, 16].
Hochschule Darmstadt	hdalbp	006	2019.12.02	The idea behind the LBP implementation is based on HDA (http://dasec.h-da.de) / NTNU (https://www.ntnu.edu/nbl) approaches and published in [9–11].
Hochschule Darmstadt	hdabsif	004	2020.01.17	
Hochschule Darmstadt	hdaarcface hdadfr hdadfr	001 002 003	2019.12.29 2020.04.01 2020.07.15	The idea behind the hdaarcface/hdadfr implementation is published in [17].
Hochschule Darmstadt	hdalaplace	001	2020.04.01	

Table 2: FRVT MORPH Participants (Two-image Differential Morph Detection)

2.3 Image Datasets

Testing was performed over a number of datasets created using various methods with goals to evaluate algorithm performance over a large spectrum of morphing techniques. Testing was conducted using a tiered approach, where algorithms were evaluated on

- **Tier 1:** Lower quality morphs created with readily accessible tools available to non-experts, such as online tools from public websites and free mobile applications. These morphs are created using low effort processes and are generally low quality and contain large amounts of morphing artifacts that are visible to the human eye.
- **Tier 2:** Morphs generated using automated morphing methods based on academic research and best practices. Automated methods allow for generation of morphs in large quantities for testing.
- **Tier 3:** Higher quality morphs created using commercial-grade tools with manual processes. These are high quality morphs with very minimal visible morphing artifacts.

All source images used to generate the morphs in the test datasets are frontal, portrait-style photos. Dataset information is summarized in Tables 3, 4, 5, and sample imagery is provided in Figure 2. For morph detection, each image is accompanied by an associated image label describing the image format/origin, which includes non-scanned photos, printed-and-scanned photos, and photos of unknown format.

- **Non-scanned photos:** Photos are digital images known to not have been printed and scanned from paper. There are a number of operational use-cases for morph detection on such digital images.
- **Printed-and-scanned photos:** While there are existing techniques to detect manipulation of a digital image, once the image has been printed and scanned from paper, it leaves virtually no traces of the original image ever being manipulated. So the ability to detect whether a printed-and-scanned image contains a morph warrants investigation.
- **Photos of unknown format:** In some cases, the format and/or origin of the image in question is not known, so images with “unknown” labels will also be tested.

2.3.1 Tier 1 - Low Quality Morphs

Dataset	Morphing Method	# Morphs	# Source Images	Image Size	Image Label	Notes
Online tool from website	Unknown	1183	558	300x400	NonScanned	The probe images used to evaluate differential MAD on this dataset are portrait quality images.

Table 3: Tier 1 datasets: morphs created with easily accessible, non-expert morphing software such as online tools from websites and mobile applications. All morphs are created with two subjects and subject alpha, where known, is 0.5 (i.e., each subject contributed equally to the morph). The image label represents the label that was provided to the algorithm while processing images from the particular dataset.

2.3.2 Tier 2 - Automated Morphs

Dataset	Morphing Method	# Morphs	# Source Images	Image Size	Image Label	Notes
Global Morph	Automated	1346	254	512x768	NonScanned	Entire source images are averaged after alignment and feature warping. Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are portrait quality images.
Local Morph	Automated	1346	254	512x768	NonScanned	Only the face area is averaged after alignment and feature warping; Subject A provides the periphery. Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are portrait quality images.

Local Morph Colorized Average	Automated	1346	254	512x768	NonScanned	Only the face area is averaged after alignment and feature warping. Subject A provides the periphery. Face area is adjusted to the average of Subject A's and Subject B's face color histograms. Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are portrait quality images.
Local Morph Colorized Match	Automated	1346	254	512x768	NonScanned	Only the face area is averaged after alignment and feature warping. Subject A provides the periphery. Face area is adjusted to match Subject A's color histogram. Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are portrait quality images.
Complete [18]	Automated	6376	233	900x1200, 1350x1350	NonScanned	
Splicing [18]	Automated	11966	233	900x1200, 1350x1350	NonScanned	
Combined [19]	Automated	12752	233	900x1200, 1350x1350	NonScanned	

UNIBO Automatic Morphed Face Generation Tool v1.0 [3–5]	Automated	2464	64	median: 696x928, min: 488x651, max: 788x1051	NonScanned	Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are informal photos, often with pose angle and illumination variations. These photos were often collected with a webcam and the subject looking at the camera.
DST	Automated	171	487	1350x1350, 900x1200, 512x768	NonScanned	Subject A provides the periphery. Faces are detected using the Viola-Jones [20] algorithm. Techniques including Delaunay triangulation are used to develop warpable meshes, which are rendered using affine warping. [21] is applied to remove morphing artifacts. Morphs were created using subjects of the same sex and ethnicity labels.
Image Resolution	Automated	19978 per image resolution	251 per image resolution	Median: 4612x6149 (1200 IOD), 2306x3075 (600 IOD), 577x769 (300 IOD), 289x385 (150 IOD), 145x193 (75 IOD)	NonScanned	Morphs were created using the UNIBO Automatic Morphed Face Generation Tool v2.0 [3–6] at the highest resolution (1200 IOD), then resized to lower resolutions. Morphs were created using subjects of the same sex and ethnicity labels.

Visa-Border	Automated	25727	51454		NonScanned	Morphs were created using the UNIBO Automatic Morphed Face Generation Tool v2.0 [3–6]. Morphs were created using subjects of similar age and with the same sex and nationality labels. Source images used for morphing are visa-like images from a global population, and the live probe images are border crossing photographs collected with a webcam of travelers entering the United States. The border crossing photos often have pose angle and illumination variations.
UNIBO Automatic Morphed Face Generation Tool v2.0 [3–6]	Automated	2464	64		NonScanned	Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are informal photos, often with pose angle and illumination variations. These photos were often collected with a webcam and the subject looking at the camera.

Twente	Automated	2464	64		NonScanned	Face landmarks are detected based on [22], and automatic post-processing/splicing is based on [23]. Morphs were created using subjects of the same sex and ethnicity labels. The probe images used to evaluate differential MAD on this dataset are informal photos, often with pose angle and illumination variations. These photos were often collected with a webcam and the subject looking at the camera.
MIPGAN-II [24,25]	Automated	2464	64		NonScanned	Morphs were created using subjects of the same sex and ethnicity labels. The pre-trained network models were fine-tuned on the source imagery used to generate the morphs. The probe images used to evaluate differential MAD on this dataset are informal photos, often with pose angle and illumination variations. These photos were often collected with a webcam and the subject looking at the camera.

Table 4: Tier 2 datasets: morphs created using various automated methods. All morphs are created with two subjects and subject alpha, where known, is 0.5 (i.e., each subject contributed equally to the morph). The image label represents the label that was provided to the algorithm while processing images from the particular dataset.

2.3.3 Tier 3 - High Quality Morphs

Dataset	Morphing Method	# Morphs	# Source Images	Image Size	Image Label	Notes
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Manual	Commercial Tools	323	825	640x640, 1080x1080	NonScanned	The probe images used to evaluate differential MAD on this dataset are portrait quality images.
Lincoln [26]	Automated + Manual	108	-	445x580	NonScanned	
Print + Scanned		61	64	600x600	Scanned	Morphs were created using the UNIBO Automatic Morphed Face Generation Tool v1.0, then printed using an HiTi 310W photo printer and scanned back in with a Fujitsu fi-7280 scanner @ 300 PPI.

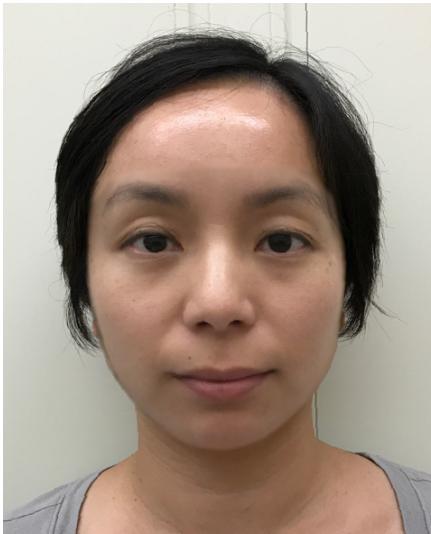
Table 5: Tier 3 datasets: morphs created using manual methods with commercial tools. All morphs are created with two subjects and subject alpha, where known, is 0.5 (i.e., each subject contributed equally to the morph). The image label represents the label that was provided to the algorithm while processing images from the particular dataset.

2.3.4 Other Datasets

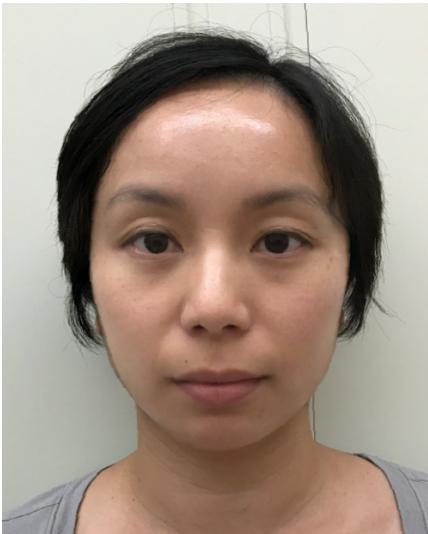
Dataset	# Source Images	Image Size	Image Label	Notes
Mugshots	1047389	499x588, 768x960, 800x1000, 1000x1330	NonScanned	The probe images used to evaluate differential MAD on this dataset are similarly, mugshot-style photos.
Visa	871984	320x320	NonScanned	The visa-like frontal images have geometry in good conformance with the ISO/IEC 19794-5 Full Frontal image type. Pose is generally excellent. The mean interocular distance (IOD) is 61 pixels. All of the images are live capture. The probe images used to evaluate differential MAD on this dataset are webcam photos collected with variations in pose, illumination, and background. See Border crossing webcam probes dataset for additional information.
Border crossing webcam probes	871984	Mostly 340x220	NonScanned	These webcam images are taken with a camera oriented by an attendant toward a cooperating subject. This is done under time constraints, so there are role, pitch and yaw angle variation. The background is not uniform and may contain furniture and windows. There is sometimes perspective distortion due to close range images. The mean IOD is 38 pixels. All of the images are live capture.

Table 6: Other datasets: additional bona fide images used to evaluate morph false detection rate.

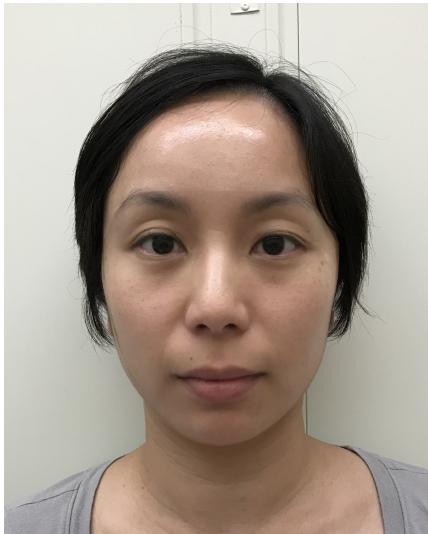




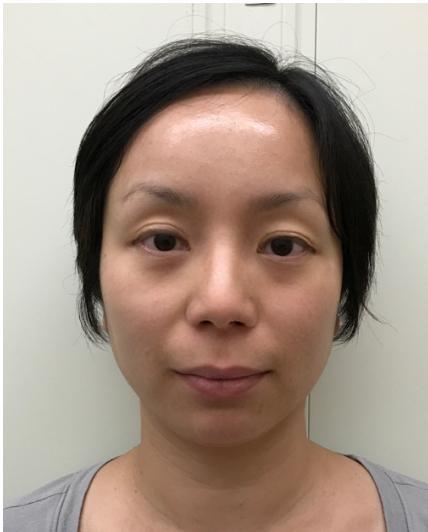
(i) Splicing



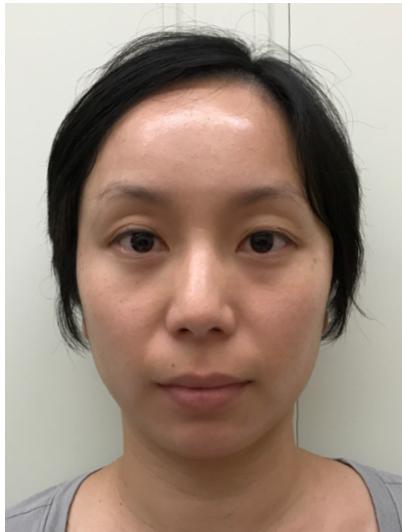
(j) Combined



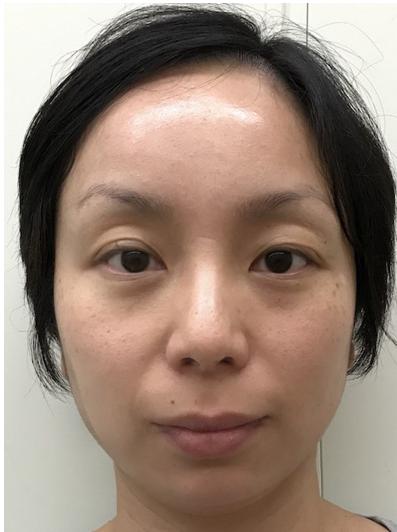
(k) UNIBO Automatic Morphed Face Generation Tool v1.0



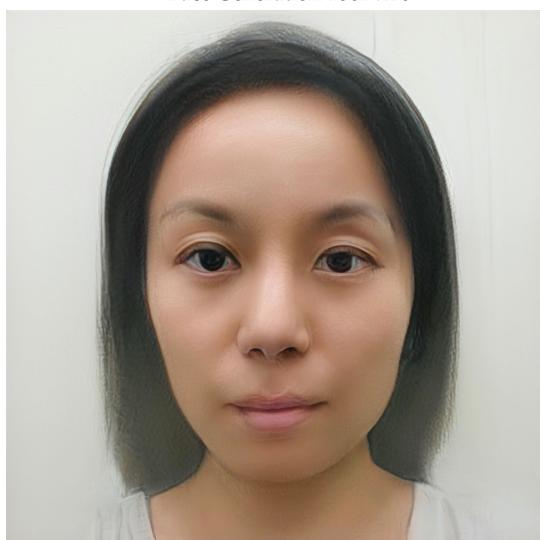
(l) DST



(m) UNIBO Automatic Morphed Face Generation Tool v2.0



(n) Twente



(o) MIPGAN-II



Figure 2: Samples of morphed imagery used in this report. Both subjects of the morphs are NIST employees.

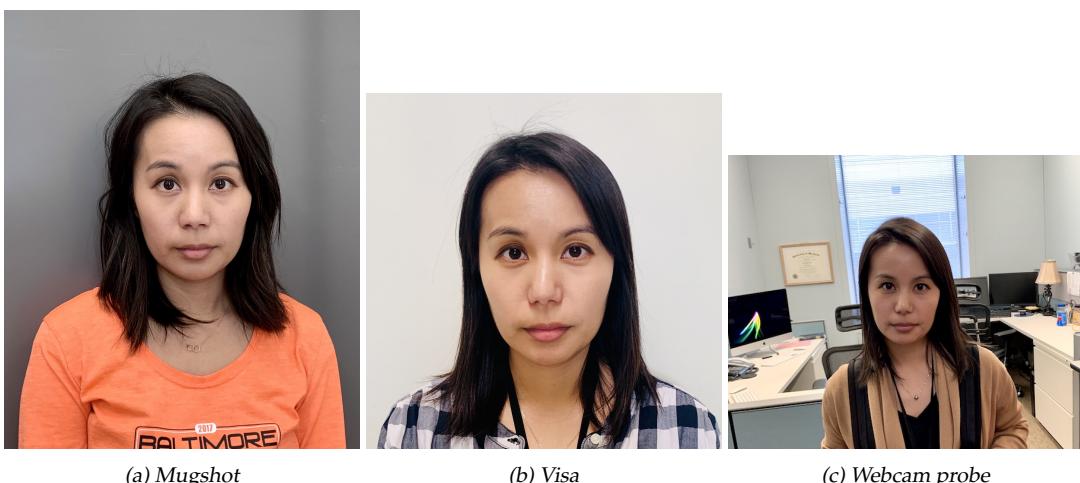


Figure 3: Samples of bona fide imagery used in this report. The subject in the photos is a NIST employee.

3 Metrics

In this section, we adopt terminology from the presentation attack detection testing standard [27] to quantify morph classification accuracy. Morph detection or attack presentation classification requires submitted algorithms to determine whether a particular image is a morph or not. Given an image, algorithms report a 1) binary decision on whether the image is a morph or not and 2) a confidence score on $[0, 1]$ representing the algorithm's certainty about whether the image is a morph.

3.1 Attack Presentation Classification Error Rate (APCER)

Using the algorithm's binary decision, APCER is defined as the proportion of morph attack samples incorrectly classified as bona fide (nonmorph) presentation. This is measured as the number of incorrectly classified morphed images, M , divided by the total number of morphed images, N_m . In the case of algorithm failure to process an image (i.e., the software

returns a non-successful return code), those failures are treated as detection of a morphed image with a confidence score of 1 and are incorporated in the calculation of APCER. Additionally, the percentage of morphs that the algorithm "failed to process" is documented as a standalone quantity in this report.

$$\text{APCER} = \frac{M}{N_m} \quad (1)$$

Note that the algorithm's binary decision is based off of some developer-defined internal threshold.

3.2 Bona Fide Presentation Classification Error Rate (BPCER)

Similarly, BPCER is defined as the proportion of bona fide (nonmorph) samples incorrectly classified as morphed samples. This is measured as the number of incorrectly classified bona fide images, B , divided by the total number of bona fide images, N_b . In the case of algorithm failure to process an image (i.e., the software returns a non-successful return code), those failures are treated as detection of a morphed image with a confidence score of 1 and are incorporated in the calculation of BPCER. Additionally, the percentage of bona fides that the algorithm "failed to process" are documented as a standalone quantity in this report.

$$\text{BPCER} = \frac{B}{N_b} \quad (2)$$

3.3 Detection Error Tradeoff (DET)

We assess detection accuracy by analyzing the confidence score returned by the algorithm. In this case, the higher the confidence value, the more likely the algorithm thinks it is a morph. A reasonable approach to the detection problem is to classify an image as either a morph or bona fide image by thresholding on its confidence value.

Given N detection scores on bona fide images, b , the BPCER is computed as the proportion above some threshold, T . Similarly, given M detection scores on morphed images, m , the APCER is computed as the proportion below some threshold, T . $H(x)$ is the unit step function [28], and $H(0)$ is taken to be 1.

$$\text{BPCER}(T) = \frac{1}{N} \sum_{i=1}^N H(b_i - T), \quad (3)$$

$$\text{APCER}(T) = 1 - \frac{1}{M} \sum_{i=1}^M H(m_i - T). \quad (4)$$

In an operational setting, BPCER can be interpreted as the rate of inconvenience for those with a legitimate, bona fide photo on a passport whose photo is being incorrectly detected as a morph. The consequence of such false detections is additional resources required to adjudicate the bona fide photo. Conversely, APCER is the rate that fraud successfully takes place when a morphed photo on a passport is incorrectly classified as a legitimate, bona fide photo (a false negative occurs).

3.3.1 BPCER vs. APCER

Operationally, it is important that morph detection technology produce very low false detection rates given the assumption that most transactions will be on legitimate, bona fide photos. Therefore, the error rate that needs to be controlled is the BPCER, the rate at which bona fide images are falsely classified as morphs. Additional amounts of resources will be required to adjudicate such errors, which drives the need to limit false detections. But given that the technology is still in its infancy and for the purposes of comparing algorithm performance, this document analyzes the trade-off between APCER and BPCER at various thresholds and reports APCER @ BPCER=0.01, which can be interpreted as "the rate that

morphed photos are being missed at the expense of inconveniencing one out of every one hundred persons holding a bona fide, legitimate photo."

4 Results

4.1 Accuracy Summary

This section provides summary accuracy information of all submitted algorithms against the various datasets that were tested against. Note that for the results in this section, all morphs were created with two subjects only and subject alpha, where known, was 0.5 for each subject (i.e., each subject contributed equally to the morph). Further analysis on morph detection results broken out by subject alpha are in Section 4.10.

4.1.1 BPCER

For each morph dataset, BPCER is evaluated using the methods described below.

- **Single-image morph detection**

- The first method, $BPCER_q$, utilizes the source images (where available) that were used to create the morphed images within each dataset. This method attempts to maintain consistent quality between the bona fides and morphs within in each dataset.
- The second method, $BPCER_m$, employs the use of a bona fide dataset consisting of approximately 1 million live-capture mugshot photos, which enables the measurement of APCER at low (operationally relevant) BPCER.
- The third method, $BPCER_v$, employs the use of a large live-capture bona fide visa dataset composed of approximately 872K images that are in very good conformance with the ISO/IEC 19794-5 Full Frontal image specifications.

- **Two-image differential morph detection**

- The first method, $BPCER_q$, utilizes the source images (where available) that were used to create the morphed images within each dataset. The probes are other portrait style images of the subjects.
- The second method, $BPCER_m$, employs the use of a bona fide dataset consisting of approximately 1 million live-capture mugshot photos. The probes are other mugshot style images of the subjects. In the future, this method will be augmented to employ the use of webcam-styled probes that better exhibit properties of real-world live-capture probes in operational settings.
- The third method, $BPCER_v$, employs the use of a large live-capture bona fide visa dataset composed of approximately 872K images that are in very good conformance with the ISO/IEC 19794-5 Full Frontal image specifications. The probes are live-capture webcam photos collected in operational settings with variations in pose, illumination, and background, which more closely mimics, for example, an eGate collection scenario.

4.1.2 Failure to Process

A failure to process occurs when the algorithm software returns a non-successful return code from the morph detection function, indicating that something went wrong while processing the image. Operationally, such failure to process events may trigger secondary processes, which may require additional resources. As such, all occurrences of failure to process by an algorithm are treated as if a morph is detected with the confidence score set to 1 and incorporated into the calculation

of both APCER and BPCER. Additionally, failure to process rates are documented independently in the accuracy tables below. For each dataset, Failure to Process (Morphs) is the proportion of morphed photos the software fails on; Failure to Process (Bona Fides)_q is the proportion of source images used as bona fides the software fails to process; and Failure to Process (Bona Fides)_m is the proportion of mugshot photos used as bona fides the software fails to process.

4.2 Single-image Morph Detection

4.2.1 Tier 1 - Low Quality Morphs

Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v * (visa)	BPCER _m * (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
ntnussl-002	Online tool from website	0.998	0.004	-	0.003	0.002	-	0.0027	0.659	0.996 ⁽¹⁾
hdalaplace-001	Online tool from website	0.839	0.376	0.003	0.177	0.004	0.0003	0.0073	0.949	0.996 ⁽²⁾
hdabsif-004	Online tool from website	0.038	0.977	0.001	0.711	0.004	0.0003	0.0082	0.978	0.996 ⁽³⁾
unibo-000	Online tool from website	0.984	0.077	0.006	0.093	0.004	0.0001	0.0045	0.982	0.996 ⁽⁴⁾
hdaprnu-004	Online tool from website	0.940	0.333	0.695	0.309	0.004	0.0003	0.0073	0.994	0.996 ⁽⁵⁾
hdalbp-006	Online tool from website	0.768	0.425	0.786	0.420	0.004	0.0004	0.0110	0.986	1.000 ⁽⁶⁾
hdalbp-005	Online tool from website	0.797	0.174	0.570	0.317	0.007	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Online tool from website	0.096	0.964	0.987	0.919	0.003	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Online tool from website	0.384	0.278	-	-	0.002	-	-	-	-

4.2.2 Tier 2 - Automated Morphs

Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v * (visa)	BPCER _m * (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Global Morph	0.798	0.012	0.006	0.093	0.000	0.0001	0.0045	0.779	0.999 ⁽¹⁾
ntnussl-002	Global Morph	1.000	0.000	-	0.003	0.000	-	0.0027	0.791	0.999 ⁽²⁾
hdalaplace-001	Global Morph	0.876	0.028	0.003	0.177	0.000	0.0003	0.0073	0.959	1.000 ⁽³⁾
hdalbp-006	Global Morph	0.462	0.106	0.786	0.420	0.000	0.0004	0.0110	0.984	1.000 ⁽⁴⁾
hdaprnu-004	Global Morph	0.984	0.039	0.695	0.309	0.000	0.0003	0.0073	0.999	1.000 ⁽⁵⁾

*APCER: This is the rate that morphs that are not detected. Lower values are better.

*BPCER: This is the rate that bona fides that were mistaken for morphs. Lower values are better.

*For each dataset, the entries are ordered by the metric in the last table column.

*Entries with “-” means results are missing either due to the algorithm not being able to process the entire dataset OR results are still currently being generated.

hdabsif-004	Global Morph	0.048	0.839	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Global Morph	0.186	0.378	0.570	0.317	0.114	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Global Morph	0.180	0.528	0.987	0.919	0.030	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Global Morph	0.199	0.386	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Local Morph	0.839	0.012	0.006	0.093	0.000	0.0001	0.0045	0.817	0.999 ⁽¹⁾
ntnussl-002	Local Morph	1.000	0.000	-	0.003	0.000	-	0.0027	0.842	0.999 ⁽²⁾
hdalaplace-001	Local Morph	0.891	0.028	0.003	0.177	0.000	0.0003	0.0073	0.967	1.000 ⁽³⁾
hdalbp-006	Local Morph	0.431	0.106	0.786	0.420	0.001	0.0004	0.0110	0.975	1.000 ⁽⁴⁾
hdaprnu-004	Local Morph	0.984	0.039	0.695	0.309	0.000	0.0003	0.0073	0.998	1.000 ⁽⁵⁾
hdabsif-004	Local Morph	0.112	0.839	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Local Morph	0.258	0.378	0.570	0.317	0.055	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Local Morph	0.138	0.528	0.987	0.919	0.063	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Local Morph	0.253	0.386	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Local Morph Colorized Average	0.836	0.012	0.006	0.093	0.000	0.0001	0.0045	0.812	0.999 ⁽¹⁾
ntnussl-002	Local Morph Colorized Average	1.000	0.000	-	0.003	0.000	-	0.0027	0.836	1.000 ⁽²⁾
hdalaplace-001	Local Morph Colorized Average	0.887	0.028	0.003	0.177	0.000	0.0003	0.0073	0.965	1.000 ⁽³⁾
hdalbp-006	Local Morph Colorized Average	0.432	0.106	0.786	0.420	0.000	0.0004	0.0110	0.978	1.000 ⁽⁴⁾
hdaprnu-004	Local Morph Colorized Average	0.981	0.039	0.695	0.309	0.000	0.0003	0.0073	0.997	1.000 ⁽⁵⁾
hdabsif-004	Local Morph Colorized Average	0.118	0.839	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Local Morph Colorized Average	0.238	0.378	0.570	0.317	0.084	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Local Morph Colorized Average	0.121	0.528	0.987	0.919	0.042	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Local Morph Colorized Average	0.251	0.386	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01

ntnussl-002	Local Morph Colorized Match	1.000	0.000	-	0.003	0.000	-	0.0027	0.888	1.000 ⁽¹⁾
unibo-000	Local Morph Colorized Match	0.947	0.012	0.006	0.093	0.000	0.0001	0.0045	0.941	1.000 ⁽²⁾
hdalbp-006	Local Morph Colorized Match	0.535	0.106	0.786	0.420	0.000	0.0004	0.0110	0.977	1.000 ⁽³⁾
hdalaplace-001	Local Morph Colorized Match	0.928	0.028	0.003	0.177	0.000	0.0003	0.0073	0.982	1.000 ⁽⁴⁾
hdaprnu-004	Local Morph Colorized Match	0.985	0.039	0.695	0.309	0.000	0.0003	0.0073	0.997	1.000 ⁽⁵⁾
hdabsif-004	Local Morph Colorized Match	0.105	0.839	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Local Morph Colorized Match	0.296	0.378	0.570	0.317	0.063	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Local Morph Colorized Match	0.285	0.528	0.987	0.919	0.051	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Local Morph Colorized Match	0.307	0.386	-	-	0.032	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Complete	0.233	0.009	0.006	0.093	0.000	0.0001	0.0045	0.213	0.970 ⁽¹⁾
ntnussl-002	Complete	1.000	0.000	-	0.003	0.000	-	0.0027	0.322	0.981 ⁽²⁾
hdalaplace-001	Complete	0.771	0.034	0.003	0.177	0.000	0.0003	0.0073	0.941	1.000 ⁽³⁾
hdalbp-006	Complete	0.267	0.094	0.786	0.420	0.000	0.0004	0.0110	0.968	1.000 ⁽⁴⁾
hdaprnu-004	Complete	0.447	0.064	0.695	0.309	0.000	0.0003	0.0073	0.992	1.000 ⁽⁵⁾
hdabsif-004	Complete	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Complete	0.168	0.275	0.570	0.317	0.106	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Complete	0.001	0.957	0.987	0.919	0.518	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Complete	0.014	0.747	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Splicing	0.335	0.009	0.006	0.093	0.000	0.0001	0.0045	0.309	0.959 ⁽¹⁾
ntnussl-002	Splicing	1.000	0.000	-	0.003	0.000	-	0.0027	0.337	0.963 ⁽²⁾
hdalaplace-001	Splicing	0.735	0.034	0.003	0.177	0.000	0.0003	0.0073	0.808	0.997 ⁽³⁾
hdaprnu-004	Splicing	0.636	0.064	0.695	0.309	0.000	0.0003	0.0073	0.831	1.000 ⁽⁴⁾
hdabsif-004	Splicing	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	0.926	1.000 ⁽⁵⁾
hdalbp-006	Splicing	0.345	0.094	0.786	0.420	0.000	0.0004	0.0110	0.973	1.000 ⁽⁶⁾
hdalbp-005	Splicing	0.225	0.275	0.570	0.317	0.103	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Splicing	0.005	0.957	0.987	0.919	0.605	0.0371	0.2877	1.000	1.000 ⁽⁸⁾

ntnussl-001	Splicing	0.049	0.747	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Combined	0.250	0.009	0.006	0.093	0.000	0.0001	0.0045	0.233	0.971 ⁽¹⁾
ntnussl-002	Combined	1.000	0.000	-	0.003	0.000	-	0.0027	0.382	0.988 ⁽²⁾
hdalaplace-001	Combined	0.789	0.034	0.003	0.177	0.000	0.0003	0.0073	0.956	1.000 ⁽³⁾
hdalbp-006	Combined	0.282	0.094	0.786	0.420	0.000	0.0004	0.0110	0.973	1.000 ⁽⁴⁾
hdaprnu-004	Combined	0.501	0.064	0.695	0.309	0.000	0.0003	0.0073	0.996	1.000 ⁽⁵⁾
hdabsif-004	Combined	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Combined	0.208	0.275	0.570	0.317	0.071	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Combined	0.001	0.957	0.987	0.919	0.611	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Combined	0.014	0.747	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	UNIBO Automatic Morphed Face Generation Tool v1.0	0.000	0.641	0.006	0.093	0.000	0.0001	0.0045	0.000	0.087 ⁽¹⁾
ntnussl-002	UNIBO Automatic Morphed Face Generation Tool v1.0	1.000	0.000	-	0.003	0.000	-	0.0027	0.293	0.999 ⁽²⁾
hdalbp-006	UNIBO Automatic Morphed Face Generation Tool v1.0	0.019	0.469	0.786	0.420	0.000	0.0004	0.0110	0.684	1.000 ⁽³⁾
hdalaplace-001	UNIBO Automatic Morphed Face Generation Tool v1.0	0.447	0.031	0.003	0.177	0.000	0.0003	0.0073	0.724	1.000 ⁽⁴⁾
hdabsif-004	UNIBO Automatic Morphed Face Generation Tool v1.0	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	0.754	1.000 ⁽⁵⁾
hdaprnu-004	UNIBO Automatic Morphed Face Generation Tool v1.0	0.510	0.047	0.695	0.309	0.000	0.0003	0.0073	0.992	1.000 ⁽⁶⁾

hdalbp-005	UNIBO Automatic Morphed Face Generation Tool v1.0	0.146	0.500	0.570	0.317	0.075	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	UNIBO Automatic Morphed Face Generation Tool v1.0	0.000	0.906	0.987	0.919	0.000	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	UNIBO Automatic Morphed Face Generation Tool v1.0	0.015	0.781	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
ntnussl-002	DST	0.977	0.000	-	0.003	0.023	-	0.0027	0.906	0.977 ⁽¹⁾
unibo-000	DST	0.988	0.010	0.006	0.093	0.000	0.0001	0.0045	0.982	1.000 ⁽²⁾
hdaprnu-004	DST	0.977	0.051	0.695	0.309	0.000	0.0003	0.0073	0.994	1.000 ⁽³⁾
hdabsif-004	DST	0.035	0.916	0.001	0.711	0.000	0.0003	0.0082	1.000	1.000 ⁽⁴⁾
hdalaplace-001	DST	0.982	0.031	0.003	0.177	0.000	0.0003	0.0073	1.000	1.000 ⁽⁵⁾
hdalbp-005	DST	0.737	0.329	0.570	0.317	0.099	0.0235	0.1683	1.000	1.000 ⁽⁶⁾
hdalbp-006	DST	0.959	0.101	0.786	0.420	0.000	0.0004	0.0110	1.000	1.000 ⁽⁷⁾
hdaprnu-002	DST	0.053	0.733	0.987	0.919	0.398	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	DST	0.199	0.559	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaprnu-004	Visa-Border	0.009	0.802	0.695	0.309	0.0000	0.0003	0.0073	0.049	0.823 ⁽¹⁾
ntnussl-002	Visa-Border	1.000	-	-	0.003	0.0000	-	0.0027	0.375	0.990 ⁽²⁾
unibo-000	Visa-Border	0.536	0.013	0.006	0.093	0.0000	0.0001	0.0045	0.477	0.999 ⁽³⁾
hdalbp-006	Visa-Border	0.004	0.847	0.786	0.420	0.0000	0.0004	0.0110	0.159	1.000 ⁽⁴⁾
hdalaplace-001	Visa-Border	0.938	0.004	0.003	0.177	0.0000	0.0003	0.0073	0.994	1.000 ⁽⁵⁾
hdabsif-004	Visa-Border	1.000	0.000	0.001	0.711	0.0000	0.0003	0.0082	1.000	1.000 ⁽⁶⁾
hdalbp-005	Visa-Border	0.041	0.600	0.570	0.317	0.0304	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Visa-Border	0.000	0.992	0.987	0.919	0.0003	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Visa-Border	0.736	-	-	-	0.0001	-	-	-	-
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	UNIBO Automatic Morphed Face Generation Tool v2.0	0.002	0.641	0.006	0.093	0.000	0.0001	0.0045	0.001	0.156 ⁽¹⁾

ntnussl-002	UNIBO Automatic Morphed Face Generation Tool v2.0	1.000	0.000	-	0.003	0.000	-	0.0027	0.414	1.000 ⁽²⁾
hdalaplace-001	UNIBO Automatic Morphed Face Generation Tool v2.0	0.384	0.031	0.003	0.177	0.000	0.0003	0.0073	0.638	1.000 ⁽³⁾
hdabsif-004	UNIBO Automatic Morphed Face Generation Tool v2.0	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	0.699	1.000 ⁽⁴⁾
hdalbp-006	UNIBO Automatic Morphed Face Generation Tool v2.0	0.030	0.469	0.786	0.420	0.000	0.0004	0.0110	0.704	1.000 ⁽⁵⁾
hdaprnu-004	UNIBO Automatic Morphed Face Generation Tool v2.0	0.389	0.047	0.695	0.309	0.000	0.0003	0.0073	0.934	1.000 ⁽⁶⁾
hdalbp-005	UNIBO Automatic Morphed Face Generation Tool v2.0	0.194	0.500	0.570	0.317	0.069	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	UNIBO Automatic Morphed Face Generation Tool v2.0	0.000	0.906	0.987	0.919	0.000	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	UNIBO Automatic Morphed Face Generation Tool v2.0	0.032	0.781	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Twente	0.002	0.641	0.006	0.093	0.000	0.0001	0.0045	0.002	0.183 ⁽¹⁾
ntnussl-002	Twente	1.000	0.000	-	0.003	0.000	-	0.0027	0.304	0.998 ⁽²⁾
hdalbp-006	Twente	0.115	0.469	0.786	0.420	0.000	0.0004	0.0110	0.866	1.000 ⁽³⁾
hdabsif-004	Twente	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	0.994	1.000 ⁽⁴⁾

hdalaplace-001	Twente	0.984	0.031	0.003	0.177	0.000	0.0003	0.0073	0.997	1.000 ⁽⁵⁾
hdalbp-005	Twente	0.179	0.500	0.570	0.317	0.266	0.0235	0.1683	1.000	1.000 ⁽⁶⁾
hdaprnu-002	Twente	0.069	0.906	0.987	0.919	0.002	0.0371	0.2877	1.000	1.000 ⁽⁷⁾
hdaprnu-004	Twente	0.982	0.047	0.695	0.309	0.000	0.0003	0.0073	1.000	1.000 ⁽⁸⁾
ntnussl-001	Twente	0.027	0.781	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	MIPGAN-II	0.041	0.641	0.006	0.093	0.000	0.0001	0.0045	0.037	0.810 ⁽¹⁾
ntnussl-002	MIPGAN-II	1.000	0.000	-	0.003	0.000	-	0.0027	0.159	0.998 ⁽²⁾
hdalbp-006	MIPGAN-II	0.756	0.469	0.786	0.420	0.000	0.0004	0.0110	0.996	1.000 ⁽³⁾
hdabsif-004	MIPGAN-II	0.000	1.000	0.001	0.711	0.000	0.0003	0.0082	0.997	1.000 ⁽⁴⁾
hdalaplace-001	MIPGAN-II	0.960	0.031	0.003	0.177	0.000	0.0003	0.0073	0.998	1.000 ⁽⁵⁾
hdalbp-005	MIPGAN-II	0.299	0.500	0.570	0.317	0.000	0.0235	0.1683	1.000	1.000 ⁽⁶⁾
hdaprnu-002	MIPGAN-II	0.046	0.906	0.987	0.919	0.000	0.0371	0.2877	1.000	1.000 ⁽⁷⁾
hdaprnu-004	MIPGAN-II	0.989	0.047	0.695	0.309	0.000	0.0003	0.0073	1.000	1.000 ⁽⁸⁾
ntnussl-001	MIPGAN-II	0.068	0.781	-	-	0.000	-	-	-	-

4.2.3 Tier 3 - High Quality Morphs

Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
ntnussl-002	Manual	1.000	0.013	-	0.003	0.000	-	0.0027	0.938	0.985 ⁽¹⁾
hdabsif-004	Manual	0.195	0.545	0.001	0.711	0.000	0.0003	0.0082	0.969	1.000 ⁽²⁾
unibo-000	Manual	0.985	0.033	0.006	0.093	0.000	0.0001	0.0045	0.978	1.000 ⁽³⁾
hdalaplace-001	Manual	0.963	0.067	0.003	0.177	0.000	0.0003	0.0073	0.991	1.000 ⁽⁴⁾
hdaprnu-004	Manual	0.985	0.440	0.695	0.309	0.000	0.0003	0.0073	0.994	1.000 ⁽⁵⁾
hdalbp-006	Manual	0.867	0.480	0.786	0.420	0.000	0.0004	0.0110	0.997	1.000 ⁽⁶⁾
hdalbp-005	Manual	0.638	0.537	0.570	0.317	0.241	0.0235	0.1683	1.000	1.000 ⁽⁷⁾
hdaprnu-002	Manual	0.526	0.927	0.987	0.919	0.050	0.0371	0.2877	1.000	1.000 ⁽⁸⁾
ntnussl-001	Manual	0.712	0.166	-	-	0.000	-	-	-	-
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
unibo-000	Lincoln	0.694	-	0.006	0.093	0.000	0.0001	0.0045	0.685	0.935 ⁽¹⁾
ntnussl-002	Lincoln	1.000	-	-	0.003	0.000	-	0.0027	0.639	1.000 ⁽²⁾
hdalaplace-001	Lincoln	0.519	-	0.003	0.177	0.000	0.0003	0.0073	0.796	1.000 ⁽³⁾
hdabsif-004	Lincoln	0.000	-	0.001	0.711	0.000	0.0003	0.0082	0.981	1.000 ⁽⁴⁾
hdalbp-006	Lincoln	0.843	-	0.786	0.420	0.000	0.0004	0.0110	0.991	1.000 ⁽⁵⁾
hdalbp-005	Lincoln	0.796	-	0.570	0.317	0.000	0.0235	0.1683	1.000	1.000 ⁽⁶⁾
hdaprnu-002	Lincoln	0.056	-	0.987	0.919	0.000	0.0371	0.2877	1.000	1.000 ⁽⁷⁾
hdaprnu-004	Lincoln	0.917	-	0.695	0.309	0.000	0.0003	0.0073	1.000	1.000 ⁽⁸⁾
ntnussl-001	Lincoln	0.037	-	-	-	0.000	-	-	-	-

Algorithm	Dataset	APCER*	BPCER _q *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _q	APCER @ BPCER _q =0.1
ntnussl-001	Print + Scanned	0.016	0.547	0.00	0.02	0.180 ⁽¹⁾
unibo-000	Print + Scanned	0.492	0.062	0.00	0.02	0.328 ⁽²⁾
hdalbp-006	Print + Scanned	0.000	0.906	0.00	0.02	0.508 ⁽³⁾
ntnussl-002	Print + Scanned	0.000	0.750	0.00	0.02	0.689 ⁽⁴⁾
hdalaplace-001	Print + Scanned	0.459	0.391	0.00	0.02	0.705 ⁽⁵⁾
hdalbp-005	Print + Scanned	0.082	0.781	0.02	0.08	0.833 ⁽⁶⁾
hdabsif-004	Print + Scanned	0.000	1.000	0.00	0.02	0.951 ⁽⁷⁾
hdaprnu-002	Print + Scanned	0.000	1.000	0.00	0.06	1.000 ⁽⁸⁾
hdaprnu-004	Print + Scanned	0.328	0.875	0.00	0.02	1.000 ⁽⁹⁾

4.3 Two-image Differential Morph Detection

4.3.1 Tier 1 - Low Quality Morphs

Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdarcface-001	Online tool from website	0.001	0.417	0.303	0.382	0.008	0.0041	0.0039	0.025	1.000 ⁽¹⁾
hdadfr-002	Online tool from website	0.001	0.382	0.394	0.382	0.004	0.0871	0.0116	0.028	1.000 ⁽²⁾
hdadfr-003	Online tool from website	0.000	0.398	0.429	0.418	0.004	0.0980	0.0127	0.038	1.000 ⁽³⁾
hdabsif-004	Online tool from website	0.277	0.500	0.902	0.408	0.009	0.0870	0.0108	0.612	1.000 ⁽⁴⁾
hdalbp-006	Online tool from website	0.095	0.801	0.969	0.791	0.004	0.1006	0.0142	0.840	1.000 ⁽⁵⁾
hdawl-002	Online tool from website	0.193	0.758	0.884	0.833	0.004	0.1141	0.0165	0.901	1.000 ⁽⁶⁾
hdalaplace-001	Online tool from website	0.300	0.713	0.905	0.715	0.004	0.0870	0.0108	0.967	1.000 ⁽⁷⁾
hdawl-000	Online tool from website	0.097	0.898	0.994	0.864	0.614	0.9568	0.3556	1.000	1.000 ⁽⁸⁾

4.3.2 Tier 2 - Automated Morphs

Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdarcface-001	Global Morph	0.026	0.031	0.303	0.382	0.010	0.0041	0.0039	0.169	1.000 ⁽¹⁾
hdadfr-002	Global Morph	0.025	0.024	0.394	0.382	0.000	0.0871	0.0116	0.188	1.000 ⁽²⁾
hdadfr-003	Global Morph	0.027	0.016	0.429	0.418	0.000	0.0980	0.0127	0.204	1.000 ⁽³⁾
hdawl-002	Global Morph	0.207	0.496	0.884	0.833	0.000	0.1141	0.0165	0.927	1.000 ⁽⁴⁾
hdalbp-006	Global Morph	0.149	0.504	0.969	0.791	0.000	0.1006	0.0142	0.955	1.000 ⁽⁵⁾
hdabsif-004	Global Morph	0.558	0.165	0.902	0.408	0.000	0.0870	0.0108	0.959	1.000 ⁽⁶⁾

* APCER: This is the rate that morphs that are not detected. Lower values are better.

* BPCER: This is the rate that bona fides that were mistaken for morphs. Lower values are better.

* For each dataset, the entries are ordered by the metric in the last table column.

*Entries with “-” in them mean results are missing either due to the algorithm not being able to process the entire dataset OR results are still currently being generated.

hdalaplace-001	Global Morph	0.242	0.606	0.905	0.715	0.000	0.0870	0.0108	0.966	1.000 ⁽⁷⁾
hdawl-000	Global Morph	0.288	0.614	0.994	0.864	0.134	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaarcface-001	Local Morph	0.016	0.031	0.303	0.382	0.010	0.0041	0.0039	0.129	1.000 ⁽¹⁾
hdadfr-002	Local Morph	0.017	0.024	0.394	0.382	0.000	0.0871	0.0116	0.136	1.000 ⁽²⁾
hdadfr-003	Local Morph	0.014	0.016	0.429	0.418	0.001	0.0980	0.0127	0.155	1.000 ⁽³⁾
hdawl-002	Local Morph	0.175	0.496	0.884	0.833	0.001	0.1141	0.0165	0.904	1.000 ⁽⁴⁾
hdabsif-004	Local Morph	0.596	0.165	0.902	0.408	0.000	0.0870	0.0108	0.958	1.000 ⁽⁵⁾
hdalaplace-001	Local Morph	0.230	0.606	0.905	0.715	0.000	0.0870	0.0108	0.960	1.000 ⁽⁶⁾
hdalbp-006	Local Morph	0.134	0.504	0.969	0.791	0.001	0.1006	0.0142	0.961	1.000 ⁽⁷⁾
hdawl-000	Local Morph	0.230	0.614	0.994	0.864	0.165	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaarcface-001	Local Morph Colorized Average	0.016	0.031	0.303	0.382	0.011	0.0041	0.0039	0.125	1.000 ⁽¹⁾
hdadfr-002	Local Morph Colorized Average	0.018	0.024	0.394	0.382	0.000	0.0871	0.0116	0.136	1.000 ⁽²⁾
hdadfr-003	Local Morph Colorized Average	0.015	0.016	0.429	0.418	0.001	0.0980	0.0127	0.155	1.000 ⁽³⁾
hdawl-002	Local Morph Colorized Average	0.182	0.496	0.884	0.833	0.001	0.1141	0.0165	0.905	1.000 ⁽⁴⁾
hdalaplace-001	Local Morph Colorized Average	0.232	0.606	0.905	0.715	0.000	0.0870	0.0108	0.955	1.000 ⁽⁵⁾
hdabsif-004	Local Morph Colorized Average	0.602	0.165	0.902	0.408	0.000	0.0870	0.0108	0.957	1.000 ⁽⁶⁾
hdalbp-006	Local Morph Colorized Average	0.134	0.504	0.969	0.791	0.000	0.1006	0.0142	0.964	1.000 ⁽⁷⁾
hdawl-000	Local Morph Colorized Average	0.257	0.614	0.994	0.864	0.147	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaarcface-001	Local Morph Colorized Match	0.016	0.031	0.303	0.382	0.010	0.0041	0.0039	0.125	1.000 ⁽¹⁾
hdadfr-002	Local Morph Colorized Match	0.021	0.024	0.394	0.382	0.000	0.0871	0.0116	0.132	1.000 ⁽²⁾

hdadfr-003	Local Morph Colorized Match	0.019	0.016	0.429	0.418	0.001	0.0980	0.0127	0.154	1.000 ⁽³⁾
hdawl-002	Local Morph Colorized Match	0.191	0.496	0.884	0.833	0.001	0.1141	0.0165	0.904	1.000 ⁽⁴⁾
hdalaplace-001	Local Morph Colorized Match	0.286	0.606	0.905	0.715	0.000	0.0870	0.0108	0.949	1.000 ⁽⁵⁾
hdabsif-004	Local Morph Colorized Match	0.616	0.165	0.902	0.408	0.000	0.0870	0.0108	0.957	1.000 ⁽⁶⁾
hdalbp-006	Local Morph Colorized Match	0.155	0.504	0.969	0.791	0.000	0.1006	0.0142	0.965	1.000 ⁽⁷⁾
hdawl-000	Local Morph Colorized Match	0.232	0.614	0.994	0.864	0.155	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaarcface-001	UNIBO Automatic Morphed Face Generation Tool v1.0	0.008	0.188	0.303	0.382	0.006	0.0041	0.0039	0.089	1.000 ⁽¹⁾
hdadfr-002	UNIBO Automatic Morphed Face Generation Tool v1.0	0.008	0.219	0.394	0.382	0.034	0.0871	0.0116	0.089	1.000 ⁽²⁾
hdadfr-003	UNIBO Automatic Morphed Face Generation Tool v1.0	0.008	0.234	0.429	0.418	0.034	0.0980	0.0127	0.103	1.000 ⁽³⁾
hdalbp-006	UNIBO Automatic Morphed Face Generation Tool v1.0	0.001	0.969	0.969	0.791	0.034	0.1006	0.0142	0.427	1.000 ⁽⁴⁾
hdabsif-004	UNIBO Automatic Morphed Face Generation Tool v1.0	0.160	0.750	0.902	0.408	0.034	0.0870	0.0108	0.577	1.000 ⁽⁵⁾

hdawl-002	UNIBO Automatic Morphed Face Generation Tool v1.0	0.063	0.938	0.884	0.833	0.034	0.1141	0.0165	0.821	1.000 ⁽⁶⁾
hdalaplace-001	UNIBO Automatic Morphed Face Generation Tool v1.0	0.294	0.734	0.905	0.715	0.034	0.0870	0.0108	0.939	1.000 ⁽⁷⁾
hdawl-000	UNIBO Automatic Morphed Face Generation Tool v1.0	0.029	0.984	0.994	0.864	0.758	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m = 0.1	APCER @ BPCER _m = 0.01
hdadfr-002	Visa-Border	0.006	0.349	0.394	0.382	0.0680	0.0871	0.0116	0.093	1.000 ⁽¹⁾
hdadfr-003	Visa-Border	0.005	0.383	0.429	0.418	0.0764	0.0980	0.0127	0.107	1.000 ⁽²⁾
hdaarcface-001	Visa-Border	0.008	0.261	0.303	0.382	0.0017	0.0041	0.0039	0.109	1.000 ⁽³⁾
hdalbp-006	Visa-Border	0.001	0.965	0.969	0.791	0.0791	0.1006	0.0142	0.208	1.000 ⁽⁴⁾
hdabsif-004	Visa-Border	0.218	0.859	0.902	0.408	0.0679	0.0870	0.0108	0.639	1.000 ⁽⁵⁾
hdawl-002	Visa-Border	0.089	0.864	0.884	0.833	0.0894	0.1141	0.0165	0.778	1.000 ⁽⁶⁾
hdalaplace-001	Visa-Border	0.038	0.913	0.905	0.715	0.0679	0.0870	0.0108	0.820	1.000 ⁽⁷⁾
hdawl-000	Visa-Border	0.005	0.993	0.994	0.864	0.9514	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER*	BPCER _q *	BPCER _v *	BPCER _m *	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m = 0.1	APCER @ BPCER _m = 0.01
hdaarcface-001	UNIBO Automatic Morphed Face Generation Tool v2.0	0.009	0.188	0.303	0.382	0.006	0.0041	0.0039	0.107	1.000 ⁽¹⁾
hdadfr-002	UNIBO Automatic Morphed Face Generation Tool v2.0	0.009	0.219	0.394	0.382	0.034	0.0871	0.0116	0.110	1.000 ⁽²⁾
hdadfr-003	UNIBO Automatic Morphed Face Generation Tool v2.0	0.010	0.234	0.429	0.418	0.034	0.0980	0.0127	0.126	1.000 ⁽³⁾

hdalbp-006	UNIBO Automatic Morphed Face Generation Tool v2.0	0.001	0.969	0.969	0.791	0.034	0.1006	0.0142	0.454	1.000 ⁽⁴⁾
hdabsif-004	UNIBO Automatic Morphed Face Generation Tool v2.0	0.146	0.750	0.902	0.408	0.034	0.0870	0.0108	0.570	1.000 ⁽⁵⁾
hdawl-002	UNIBO Automatic Morphed Face Generation Tool v2.0	0.062	0.938	0.884	0.833	0.034	0.1141	0.0165	0.814	1.000 ⁽⁶⁾
hdalaplace-001	UNIBO Automatic Morphed Face Generation Tool v2.0	0.281	0.734	0.905	0.715	0.034	0.0870	0.0108	0.924	1.000 ⁽⁷⁾
hdawl-000	UNIBO Automatic Morphed Face Generation Tool v2.0	0.030	0.984	0.994	0.864	0.758	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdadfr-002	Twente	0.007	0.219	0.394	0.382	0.034	0.0871	0.0116	0.089	1.000 ⁽¹⁾
hdaarcface-001	Twente	0.008	0.188	0.303	0.382	0.006	0.0041	0.0039	0.090	1.000 ⁽²⁾
hdadfr-003	Twente	0.008	0.234	0.429	0.418	0.034	0.0980	0.0127	0.103	1.000 ⁽³⁾
hdalbp-006	Twente	0.002	0.969	0.969	0.791	0.034	0.1006	0.0142	0.477	1.000 ⁽⁴⁾
hdabsif-004	Twente	0.255	0.750	0.902	0.408	0.034	0.0870	0.0108	0.597	1.000 ⁽⁵⁾
hdawl-002	Twente	0.067	0.938	0.884	0.833	0.034	0.1141	0.0165	0.818	1.000 ⁽⁶⁾
hdalaplace-001	Twente	0.242	0.734	0.905	0.715	0.034	0.0870	0.0108	0.890	1.000 ⁽⁷⁾
hdawl-000	Twente	0.028	0.984	0.994	0.864	0.758	0.9568	0.3556	1.000	1.000 ⁽⁸⁾
Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdaarcface-001	MIPGAN-II	0.001	0.188	0.303	0.382	0.004	0.0041	0.0039	0.031	1.000 ⁽¹⁾
hdadfr-002	MIPGAN-II	0.000	0.219	0.394	0.382	0.034	0.0871	0.0116	0.031	1.000 ⁽²⁾
hdadfr-003	MIPGAN-II	0.001	0.234	0.429	0.418	0.034	0.0980	0.0127	0.041	1.000 ⁽³⁾
hdalbp-006	MIPGAN-II	0.002	0.969	0.969	0.791	0.034	0.1006	0.0142	0.451	1.000 ⁽⁴⁾
hdabsif-004	MIPGAN-II	0.293	0.750	0.902	0.408	0.034	0.0870	0.0108	0.598	1.000 ⁽⁵⁾
hdawl-002	MIPGAN-II	0.052	0.938	0.884	0.833	0.034	0.1141	0.0165	0.791	1.000 ⁽⁶⁾
hdalaplace-001	MIPGAN-II	0.228	0.734	0.905	0.715	0.034	0.0870	0.0108	0.856	1.000 ⁽⁷⁾
hdawl-000	MIPGAN-II	0.032	0.984	0.994	0.864	0.758	0.9568	0.3556	1.000	1.000 ⁽⁸⁾

4.3.3 Tier 3 - High Quality Morphs

Algorithm	Dataset	APCER [*]	BPCER _q [*]	BPCER _v [*] (visa)	BPCER _m [*] (mugshot)	Failure to Process (Morphs)	Failure to Process (Bona Fides) _v	Failure to Process (Bona Fides) _m	APCER @ BPCER _m =0.1	APCER @ BPCER _m =0.01
hdadfr-002	Manual	0.010	0.382	0.394	0.382	0.000	0.0871	0.0116	0.091	1.000 ⁽¹⁾
hdaarcface-001	Manual	0.010	0.417	0.303	0.382	0.005	0.0041	0.0039	0.094	1.000 ⁽²⁾
hdadfr-003	Manual	0.008	0.398	0.429	0.418	0.000	0.0980	0.0127	0.106	1.000 ⁽³⁾
hdabsif-004	Manual	0.491	0.500	0.902	0.408	0.003	0.0870	0.0108	0.683	1.000 ⁽⁴⁾
hdawl-002	Manual	0.161	0.758	0.884	0.833	0.000	0.1141	0.0165	0.860	1.000 ⁽⁵⁾
hdalaplace-001	Manual	0.135	0.713	0.905	0.715	0.000	0.0870	0.0108	0.891	1.000 ⁽⁶⁾
hdalbp-006	Manual	0.143	0.801	0.969	0.791	0.000	0.1006	0.0142	0.927	1.000 ⁽⁷⁾
hdawl-000	Manual	0.036	0.898	0.994	0.864	0.649	0.9568	0.3556	1.000	1.000 ⁽⁸⁾

4.4 DET Analyses

4.4.1 Tier 1 - Low Quality Morphs

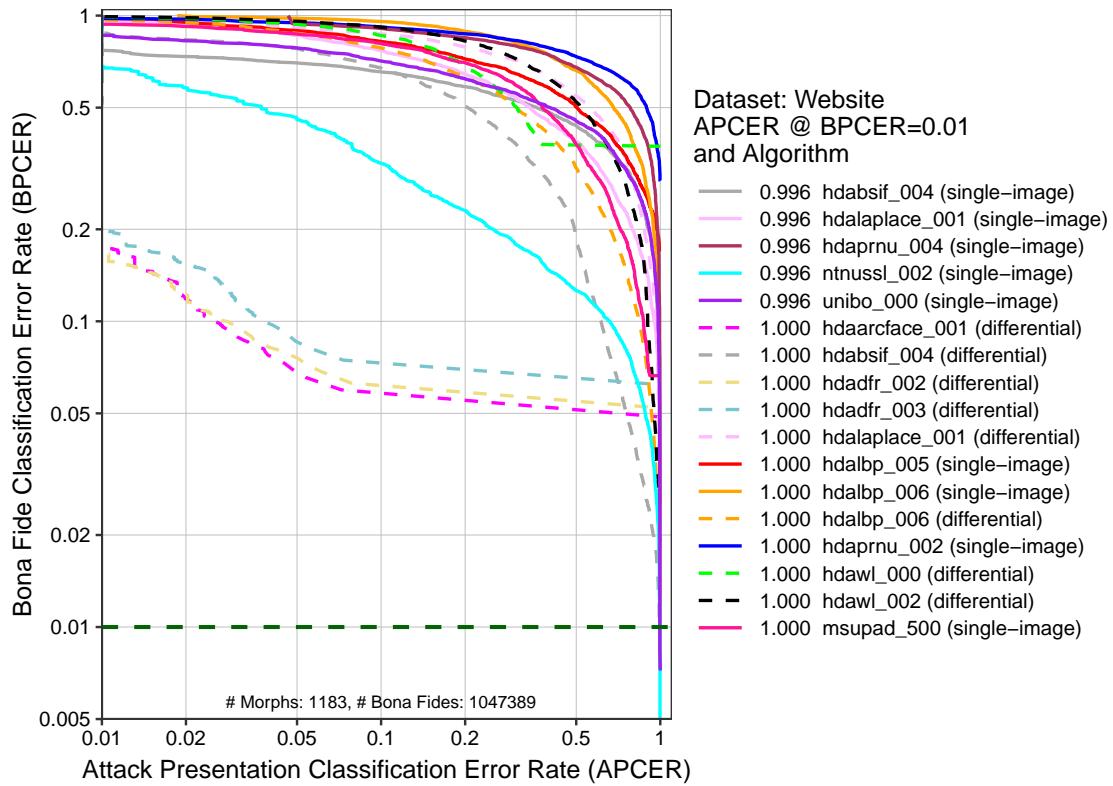


Figure 4: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

4.4.2 Tier 2 - Automated Morphs

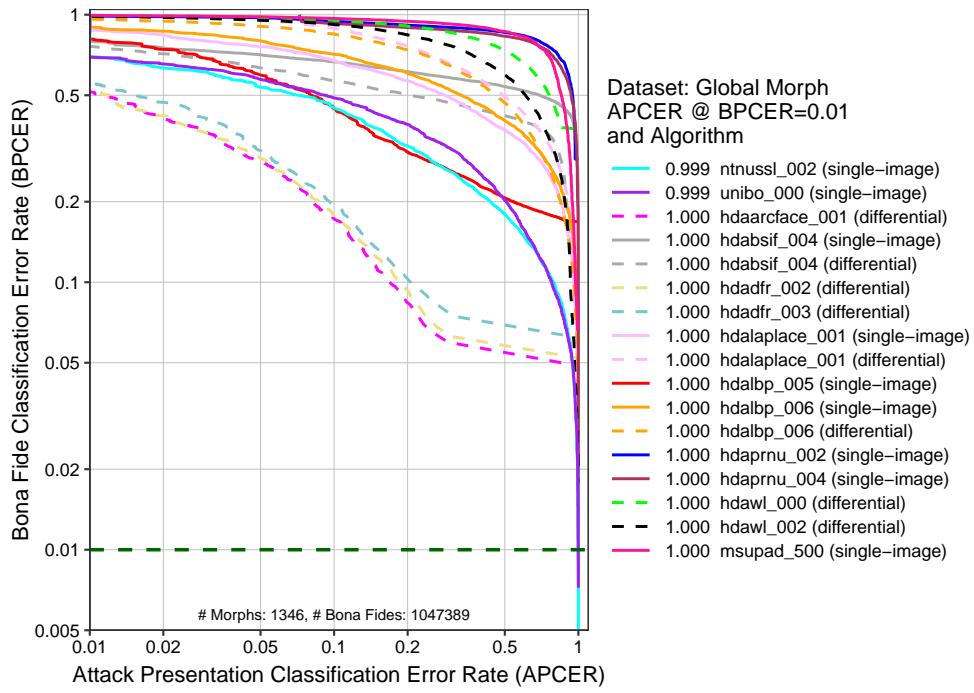


Figure 5: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

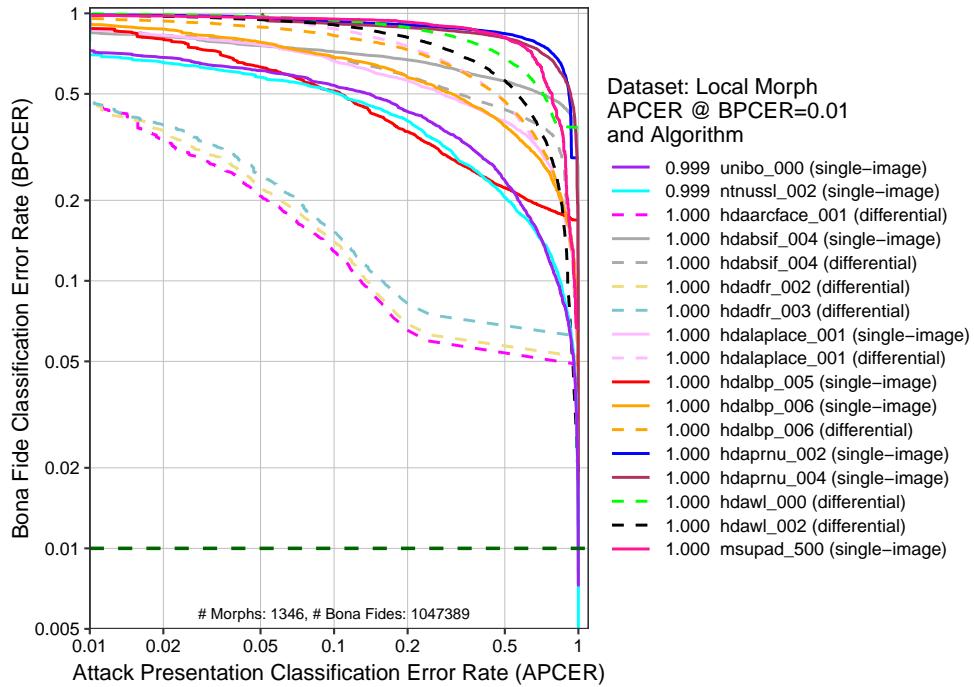


Figure 6: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

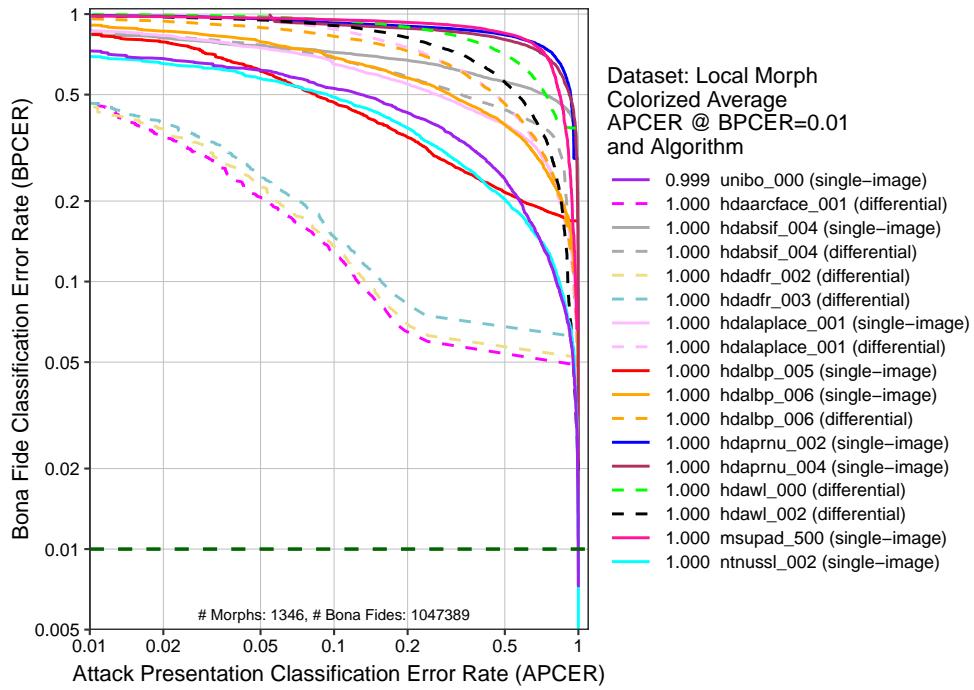


Figure 7: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

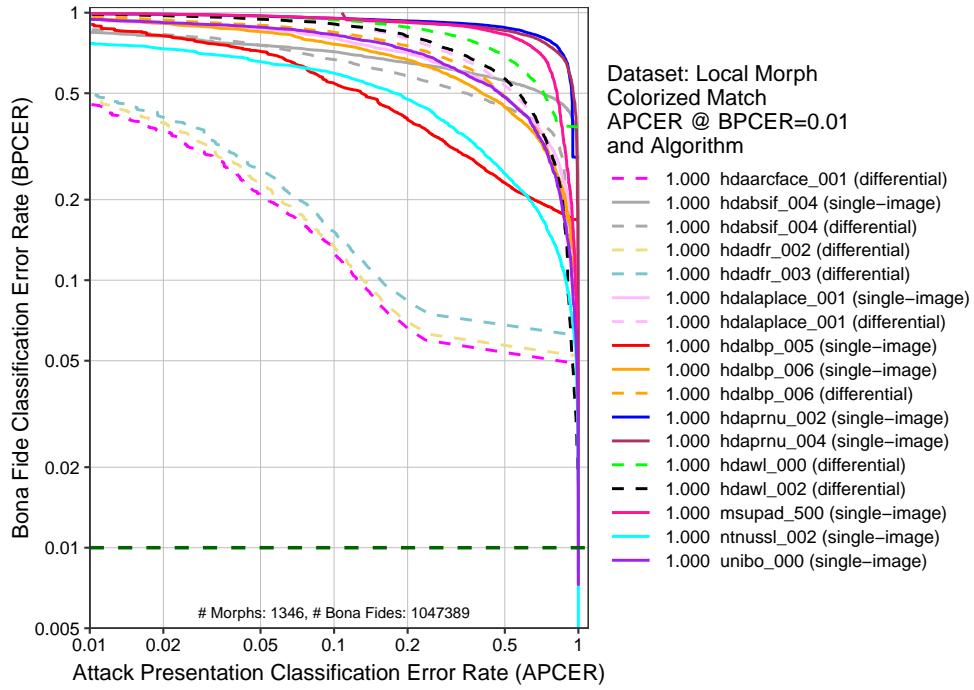


Figure 8: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

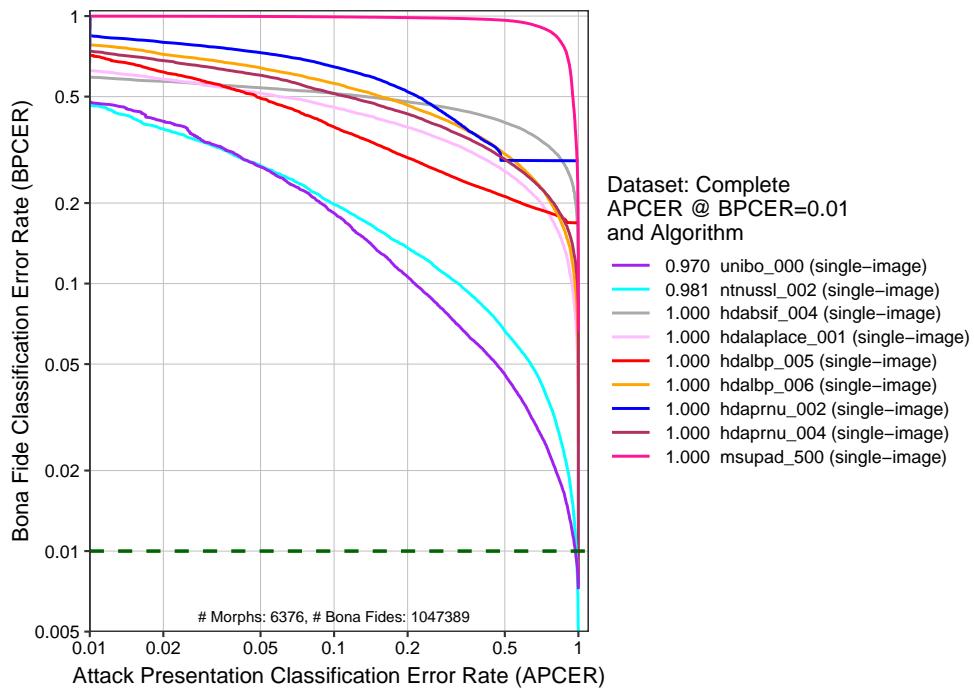


Figure 9: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

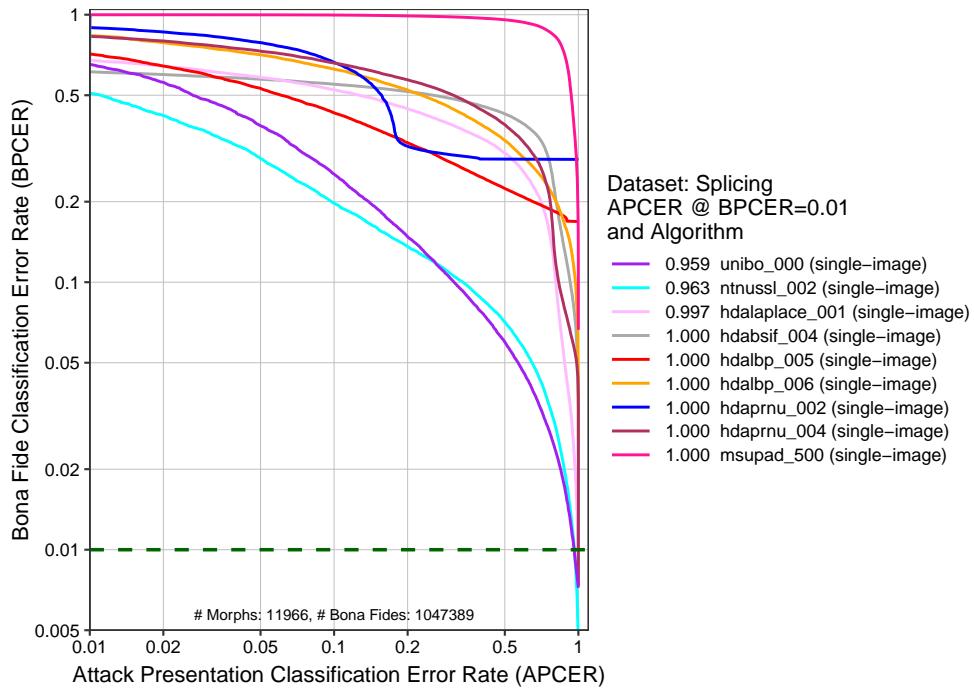


Figure 10: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

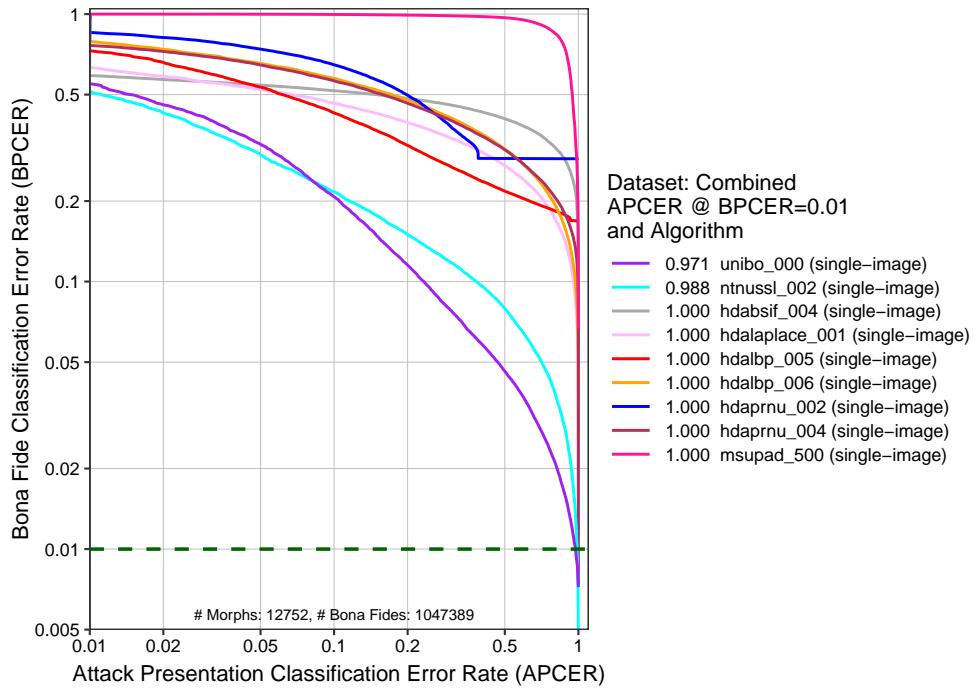


Figure 11: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

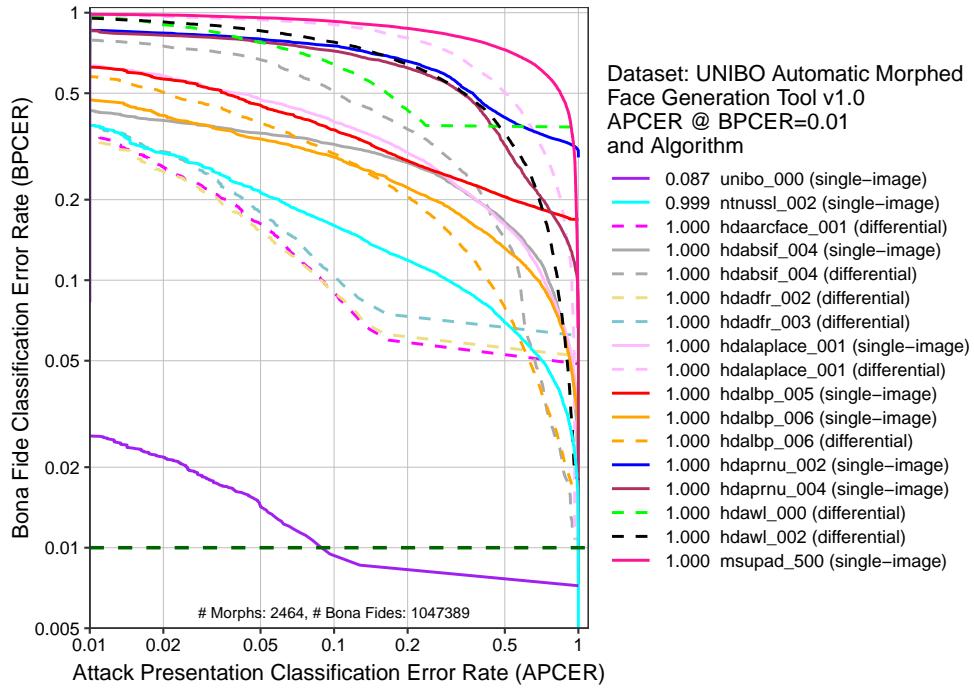


Figure 12: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

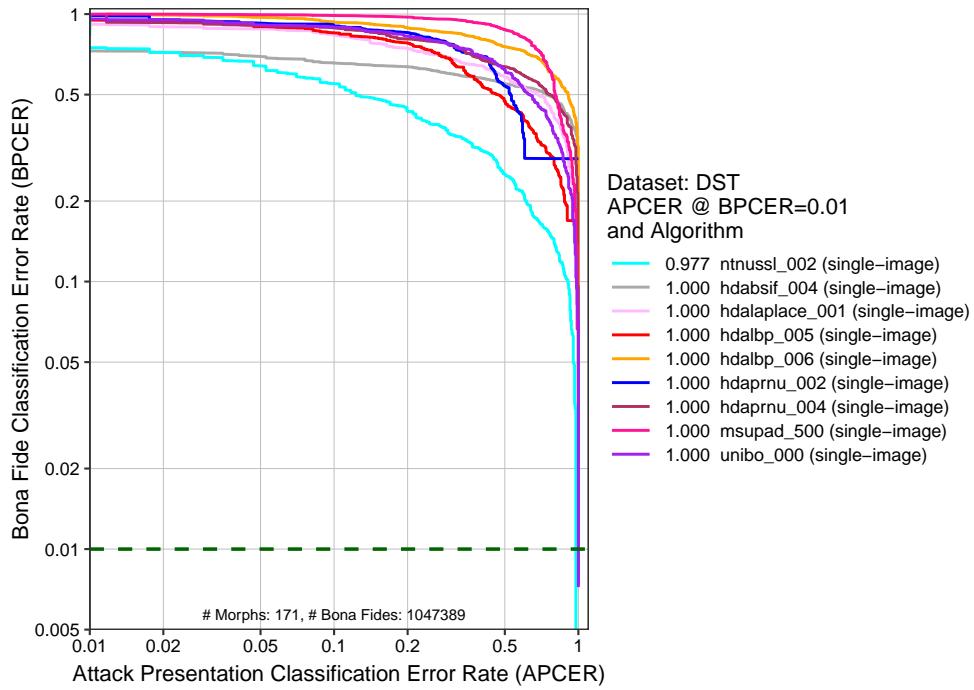


Figure 13: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

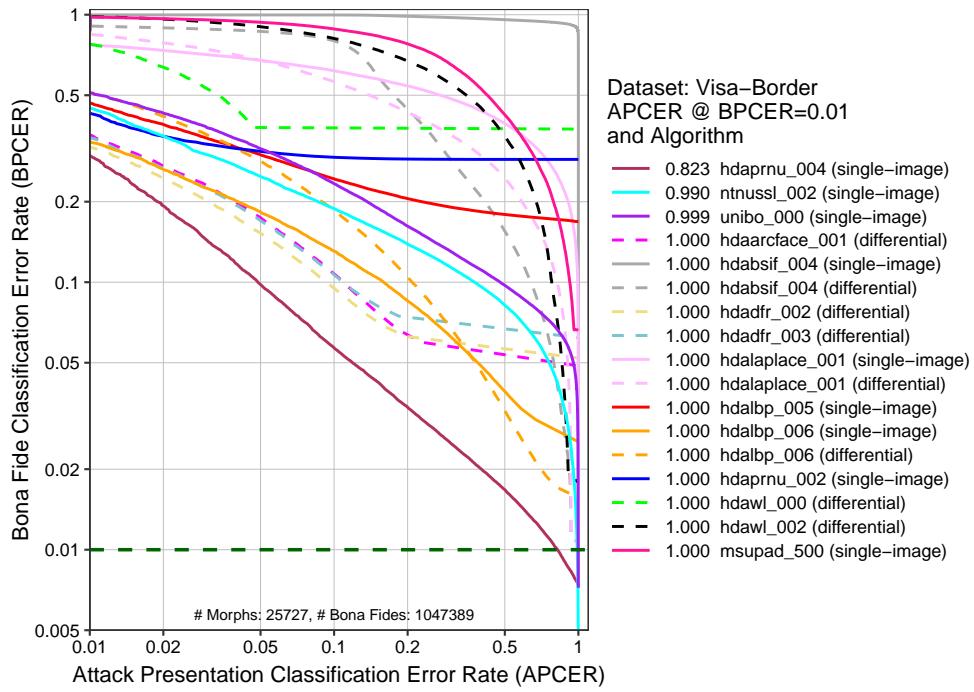


Figure 14: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

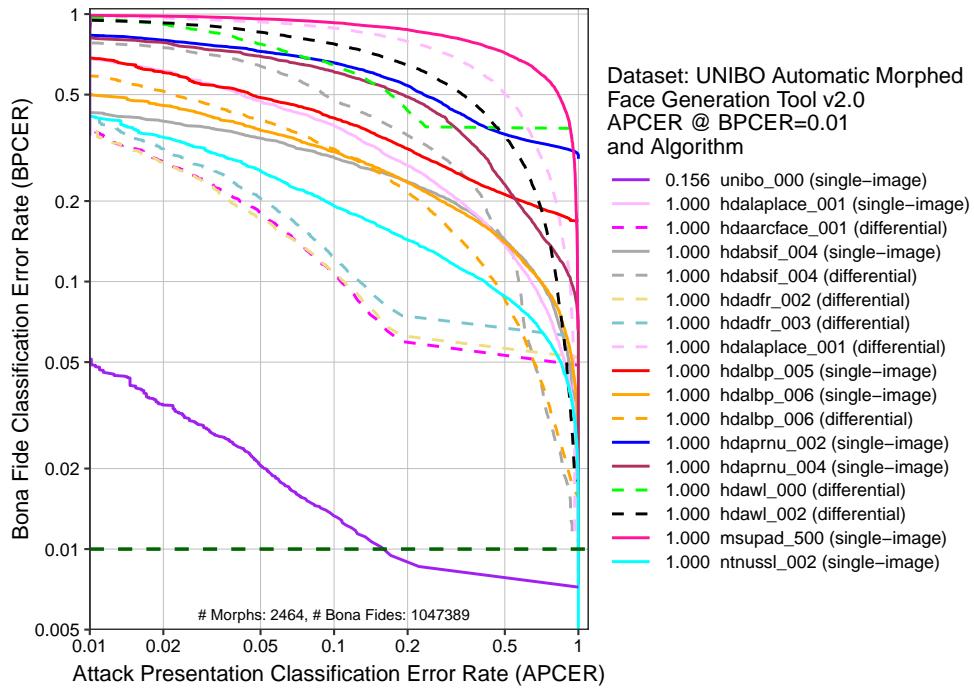


Figure 15: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

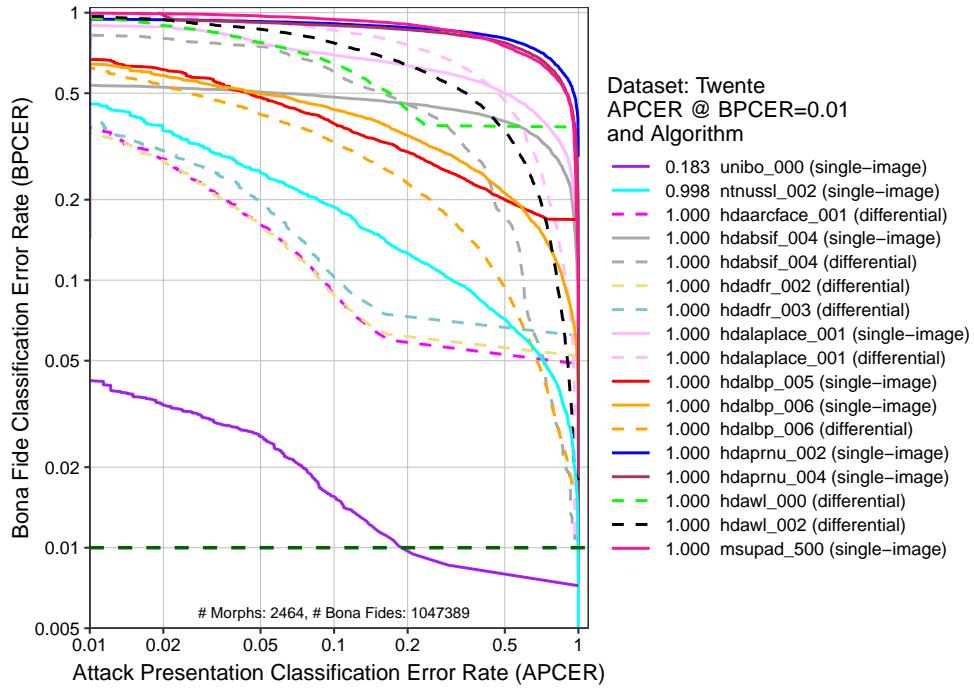


Figure 16: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

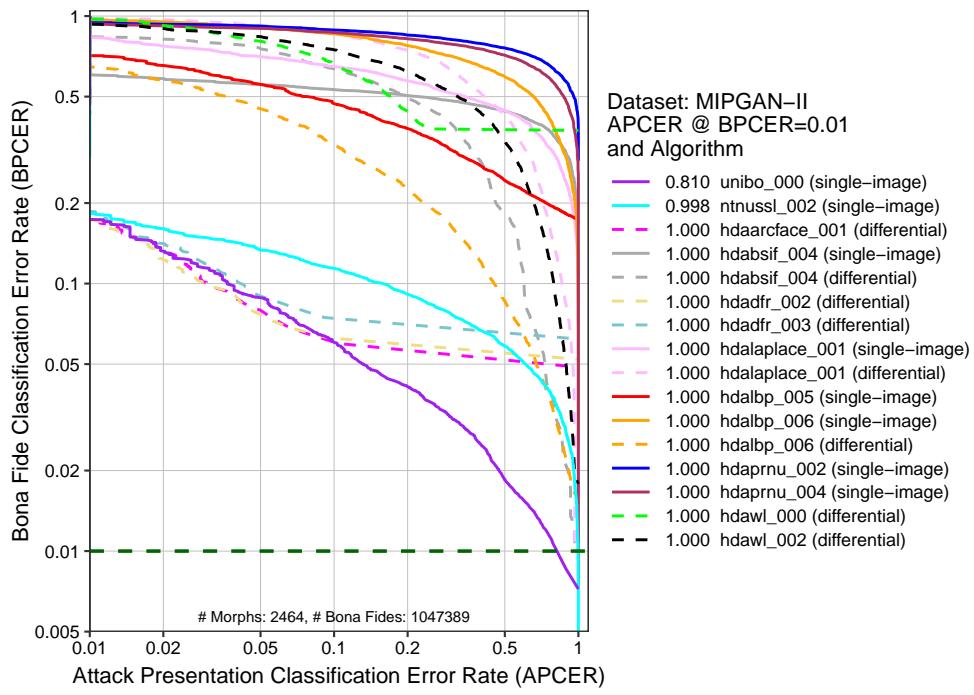


Figure 17: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

4.4.3 Tier 3 - High Quality Morphs

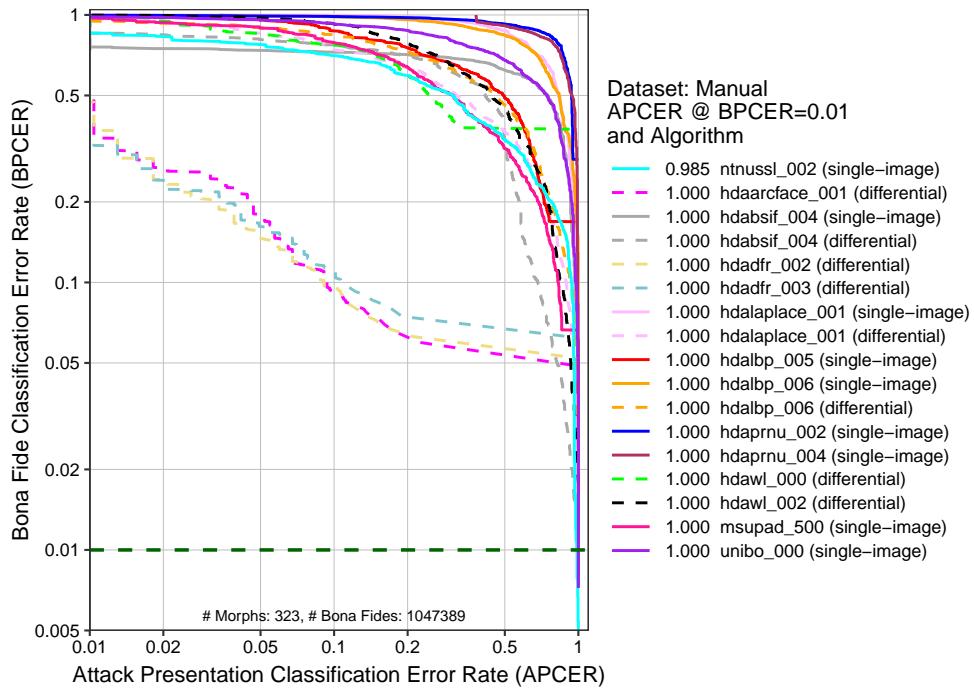


Figure 18: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

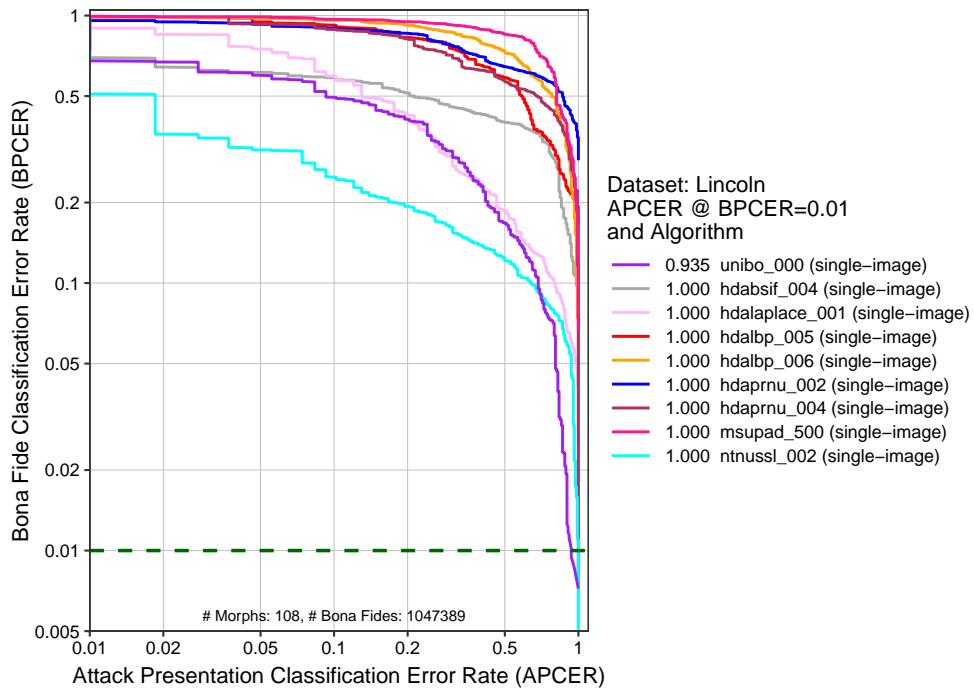


Figure 19: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

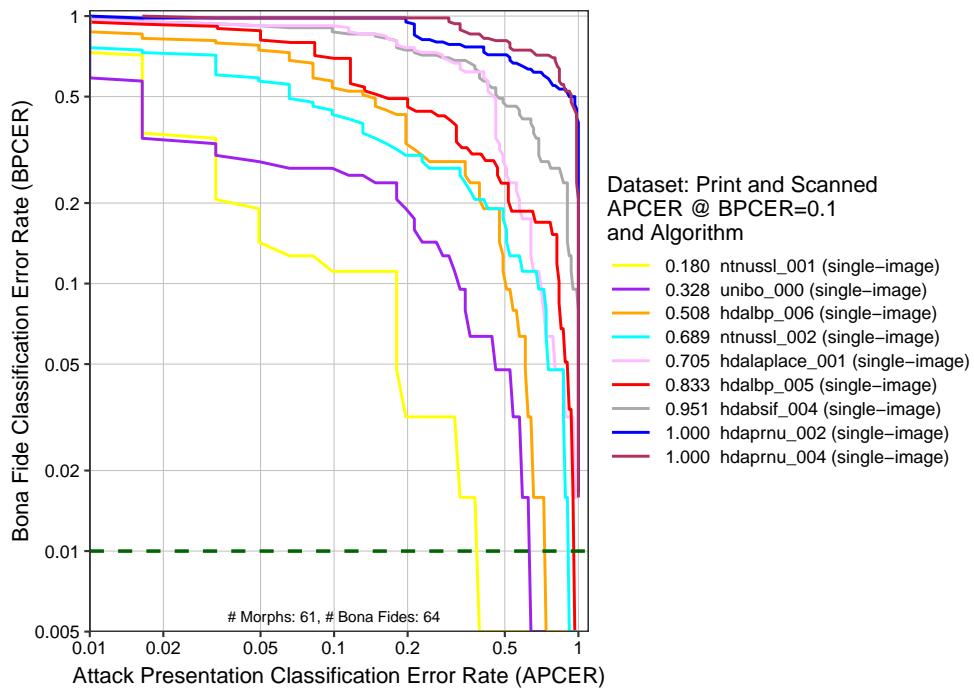


Figure 20: DET plot. This chart plots BPCER as a function of APCER. The x-axis is the rate morphs are not detected and the y-axis is the rate that bona fide images are falsely classified as morphs. The horizontal dotted dark green line represents BPCER=0.01.

4.5 Impact of Image Resolution

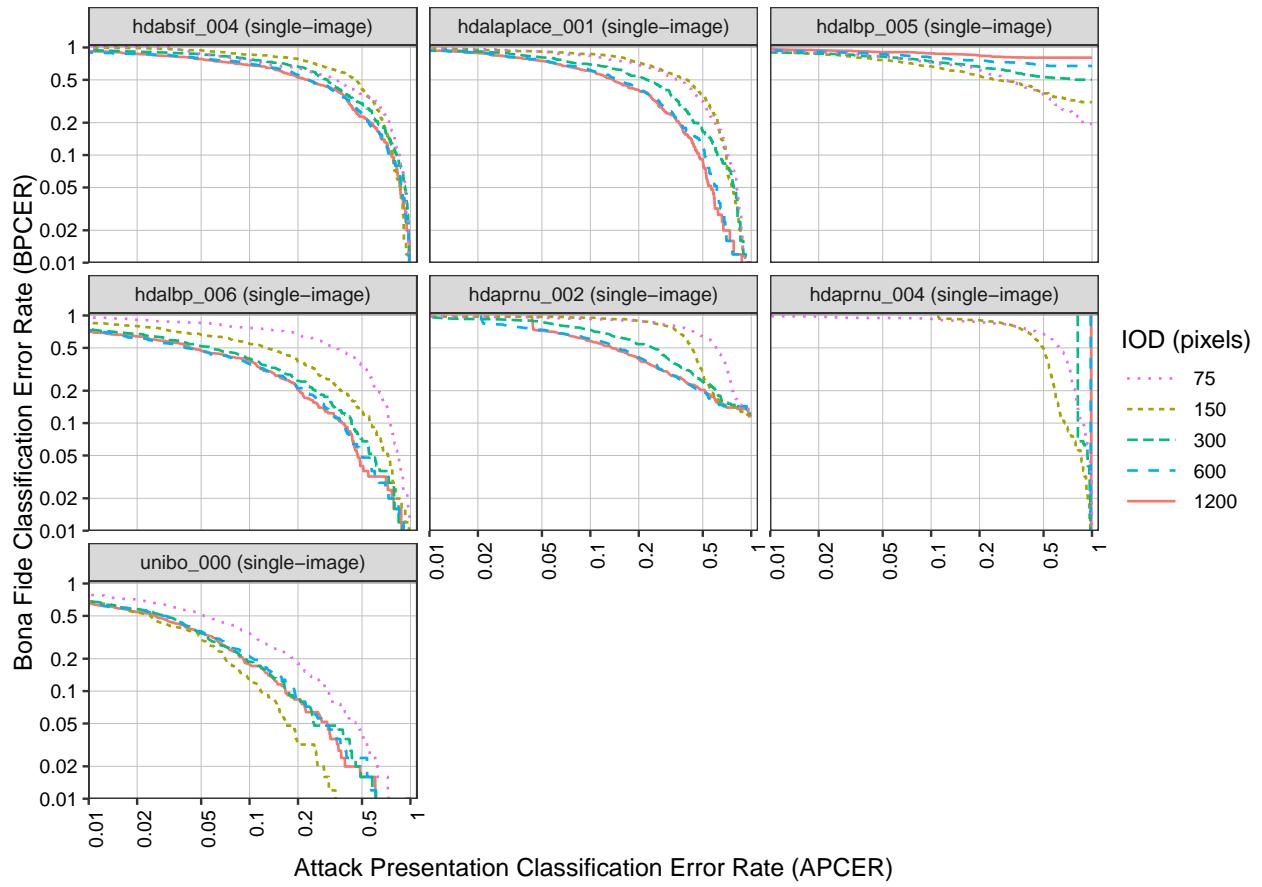


Figure 21: The DET curves show single-image morph detection error rates for different image resolutions, reported as interocular distance (IOD) or the distance between the eyes. Note that these DET curves do not show APCER and BPCER at fixed morph detection score thresholds between different image resolutions. Please refer to Figures 22 and 23 for assessments of APCER and BPCER as a function of score threshold, respectively.

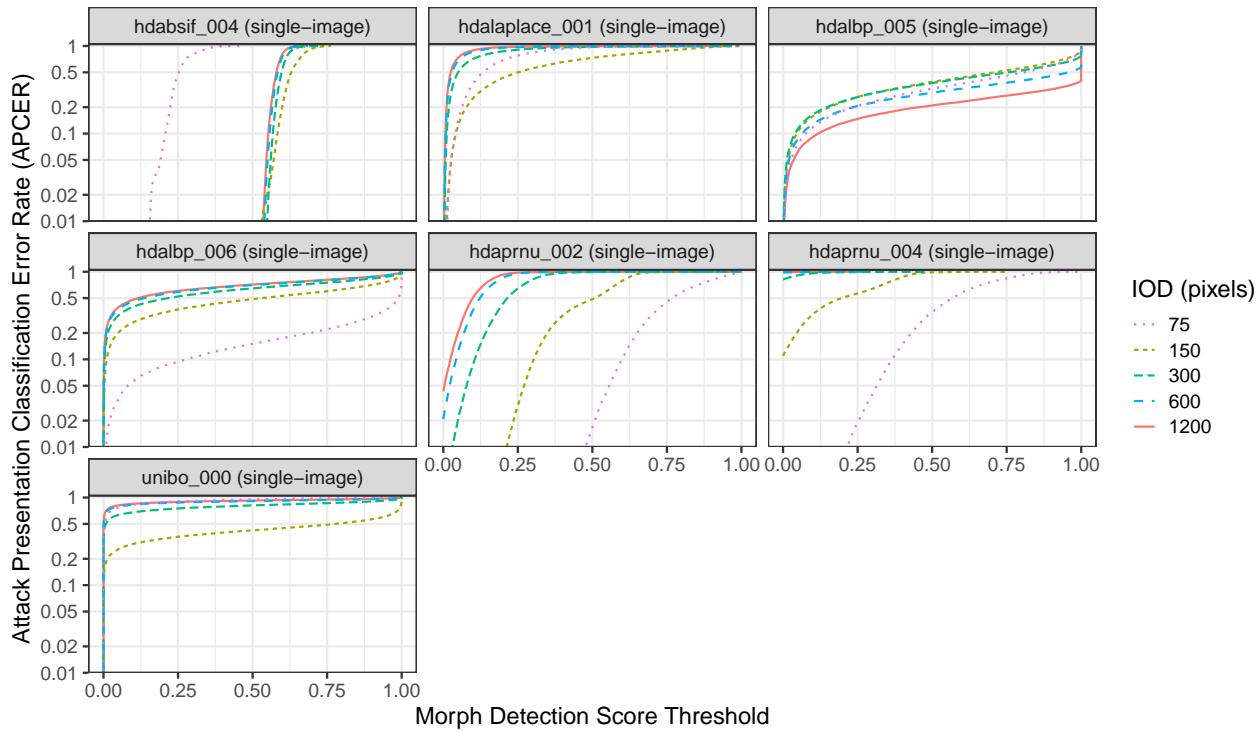


Figure 22: The curves show APCER (or morph miss rate) as a function of morph detection score threshold for different image resolutions, reported as interocular distance (IOD), the distance between the eyes.

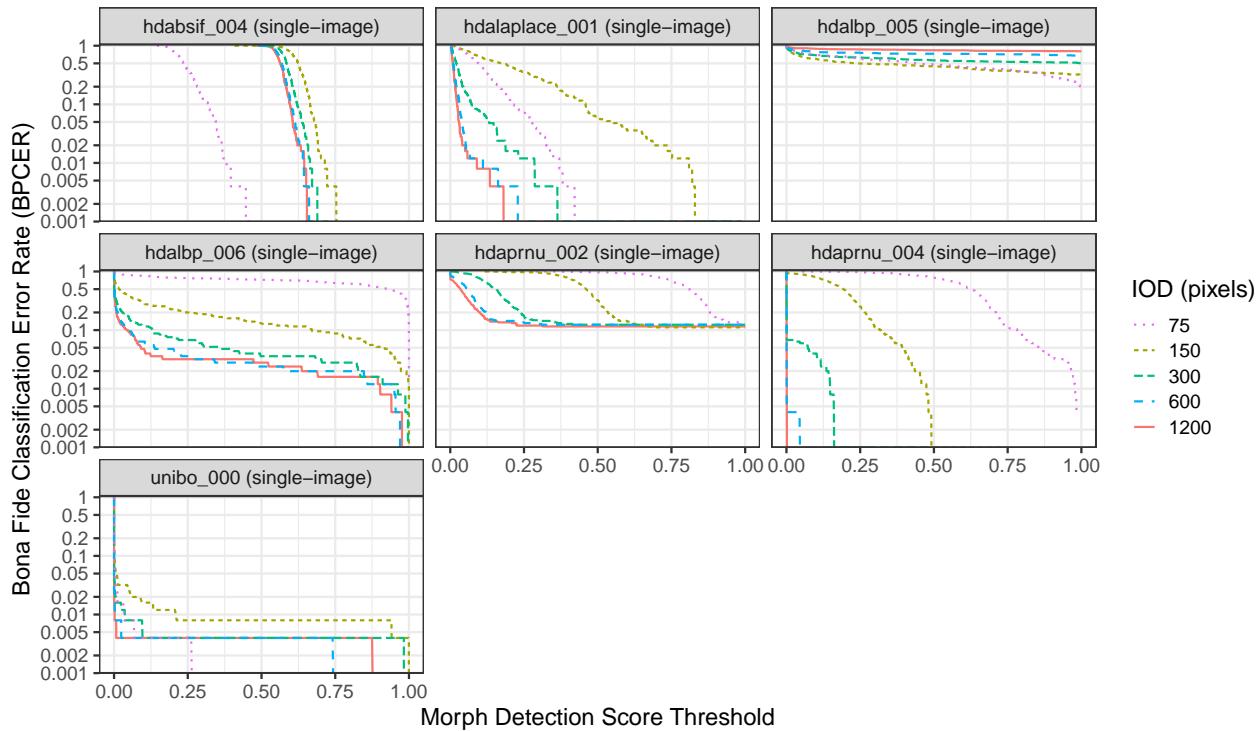


Figure 23: The curves show BPCER (or false detection rate) as a function of morph detection score threshold for different image resolutions, reported as interocular distance (IOD), the distance between the eyes.

4.6 Score Distributions

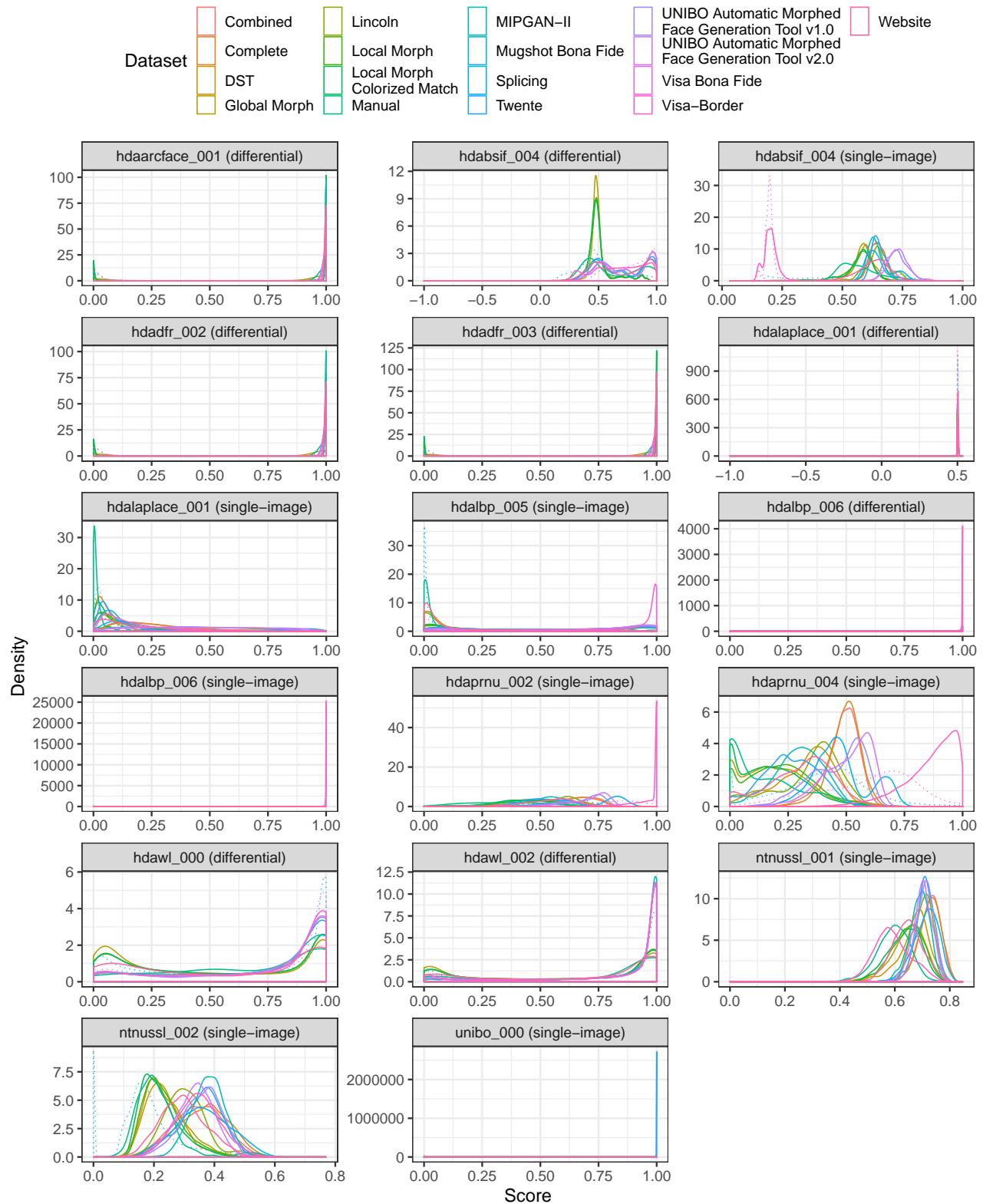


Figure 24: This figure compares the distributions of various morph + bona fide datasets. Separate distributions appear for each morph dataset (solid lines) and bona fide datasets (dotted lines).

4.7 APCER Calibration

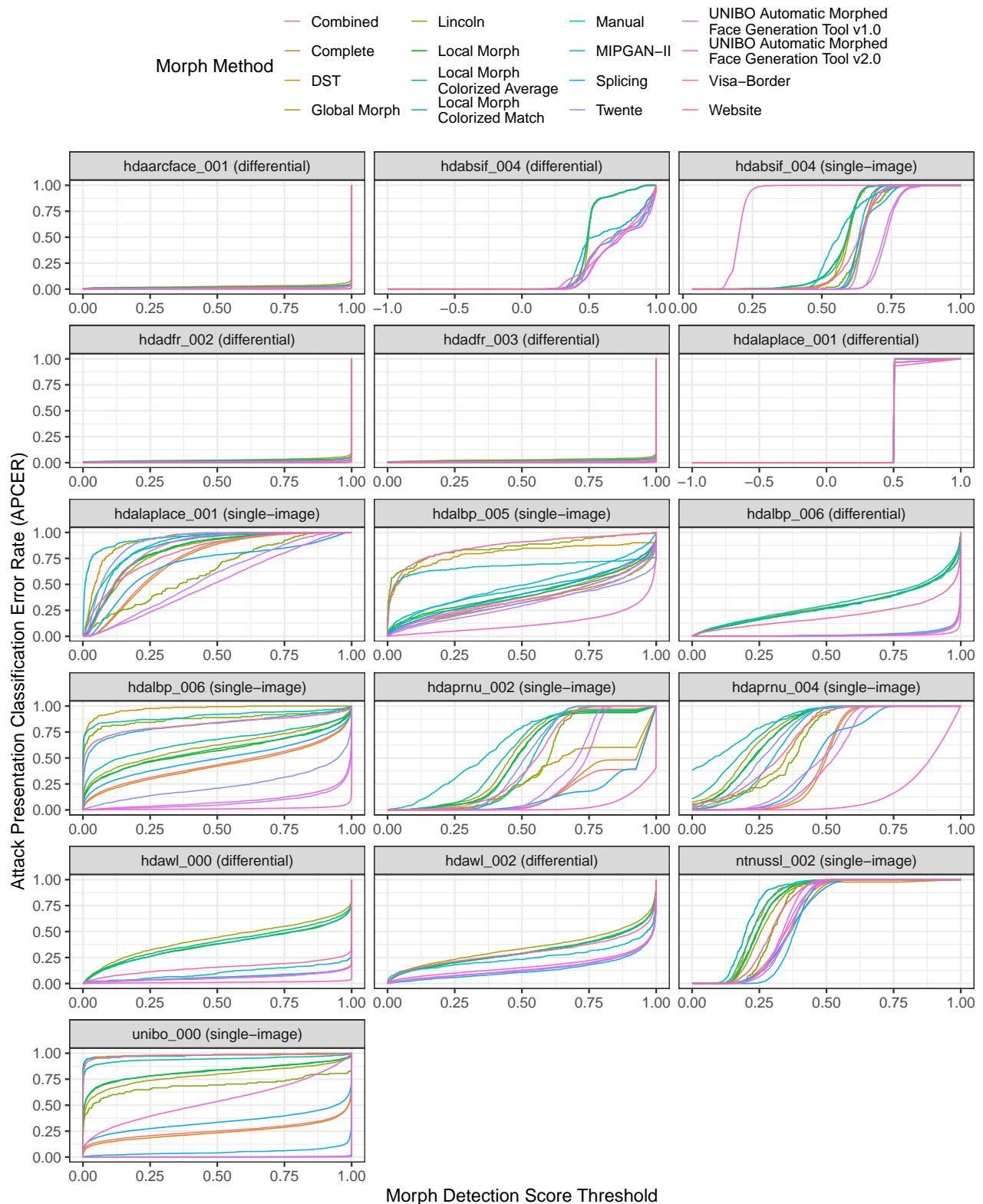


Figure 25: The APCER calibration curves show APCER (or morph miss rate) vs. morph detection score threshold. Separate curves appear for each morph dataset.

4.8 BPCER Calibration

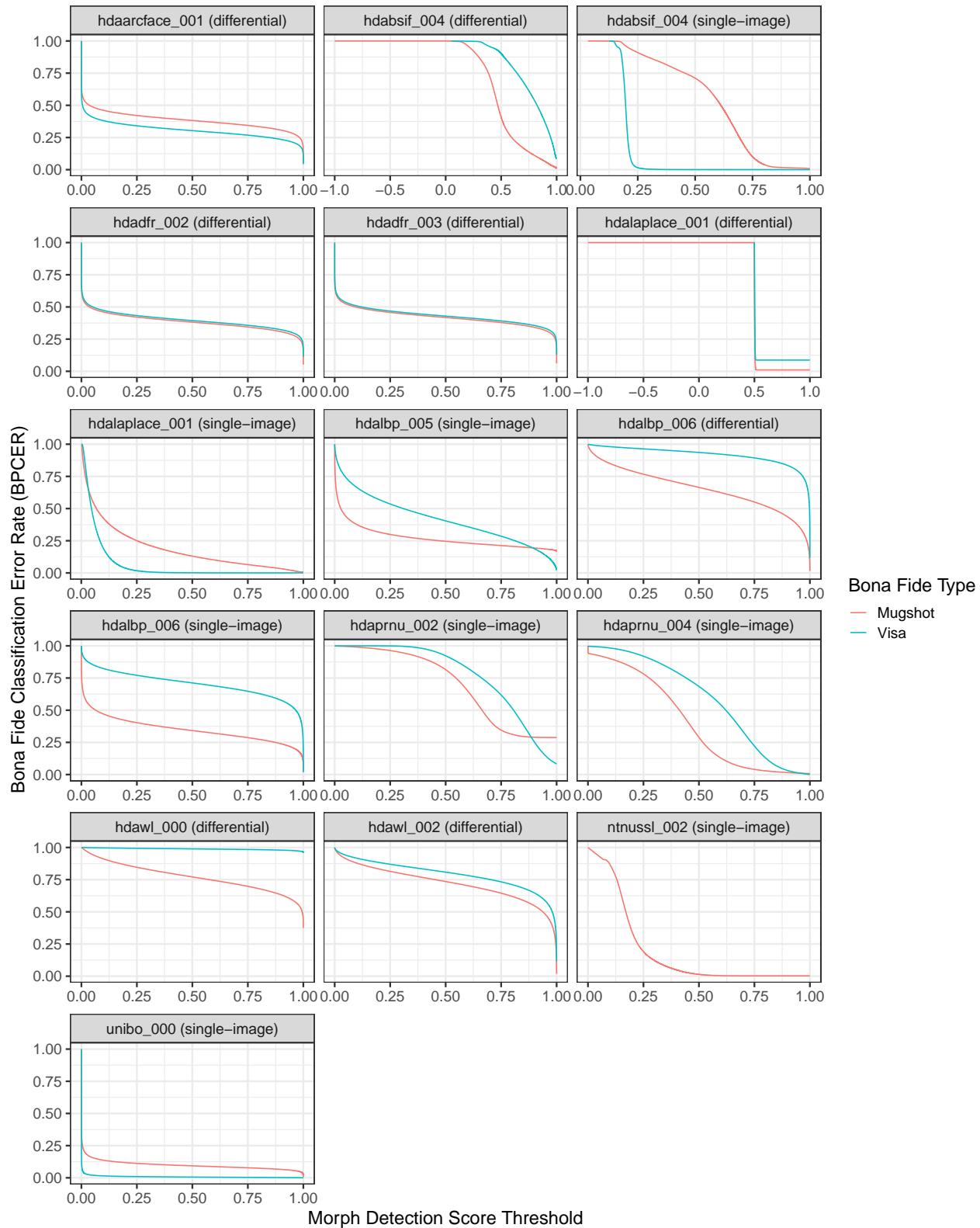


Figure 26: The BPCER calibration curves show BPCER (or false detection rate) vs. morph detection score threshold. Separate curves appear for mugshot and visa images.

4.9 Bona Fide Morph Detection Scores vs. Elapsed Time (Two-image differential)

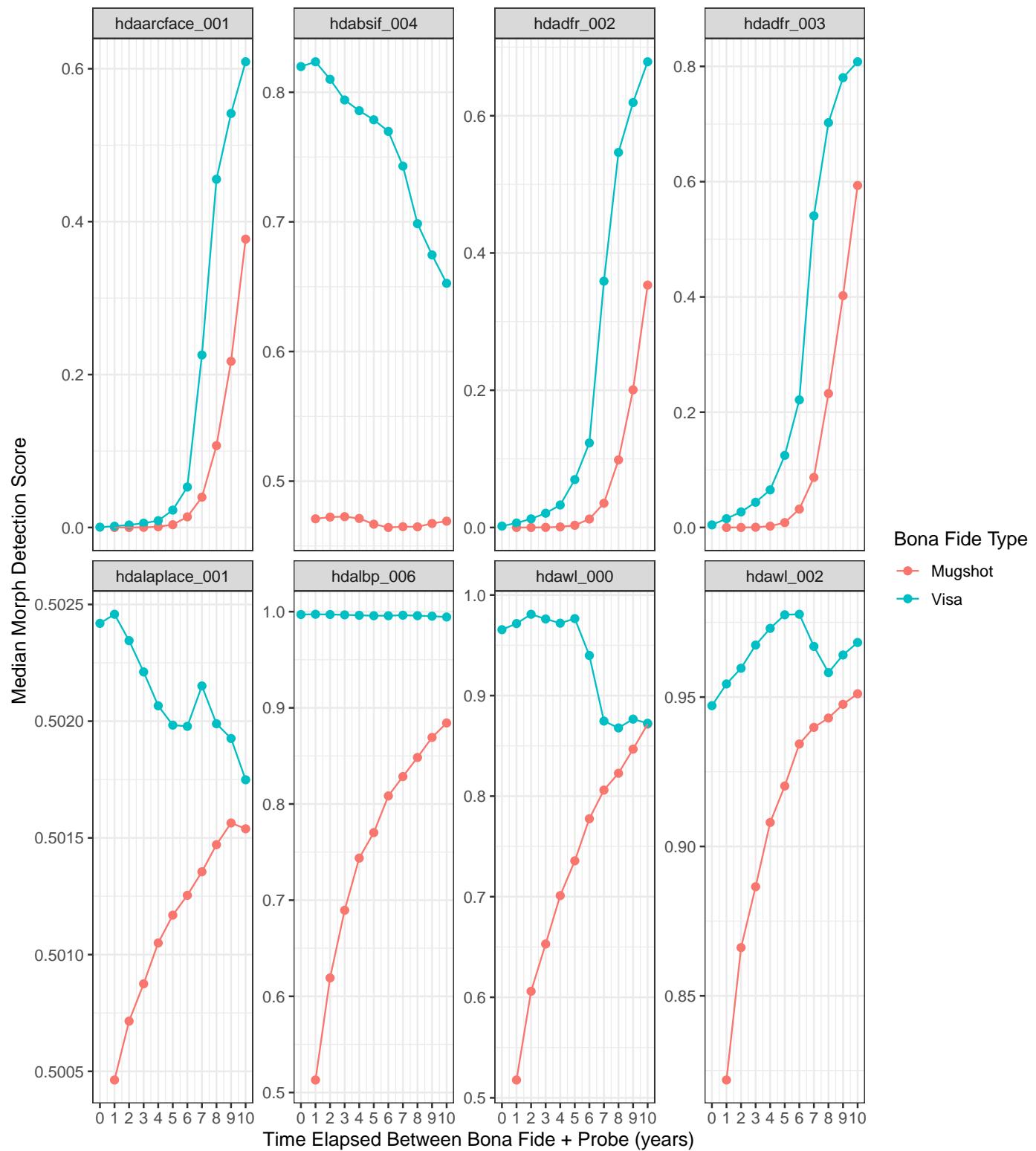


Figure 27: For the visa and mugshot datasets + probes used to evaluate differential MAD, this figure shows median morph detection score as a function of the time elapsed between the collection of the bona fide image and the live capture probe. Each plot includes scores that were successfully generated by the algorithm (i.e., results from failure to process were not used in this analysis).

4.10 Impact of Subject Alpha

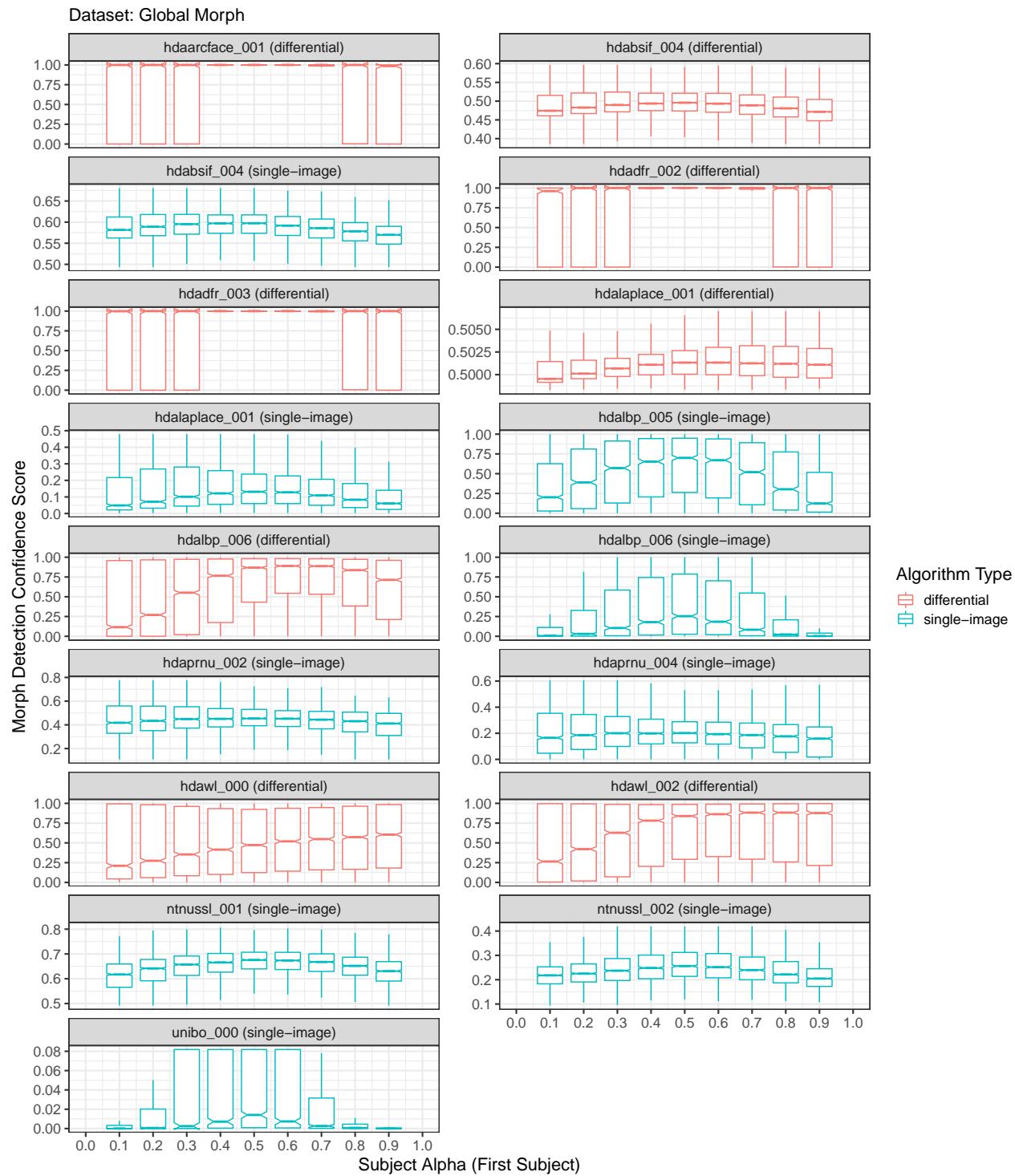


Figure 28: Boxplots plotting morph detection confidence score as a function of subject alpha (first subject in morph). Each plot includes scores that were successfully generated by the algorithm (i.e., results from failure to process were not used in this analysis).

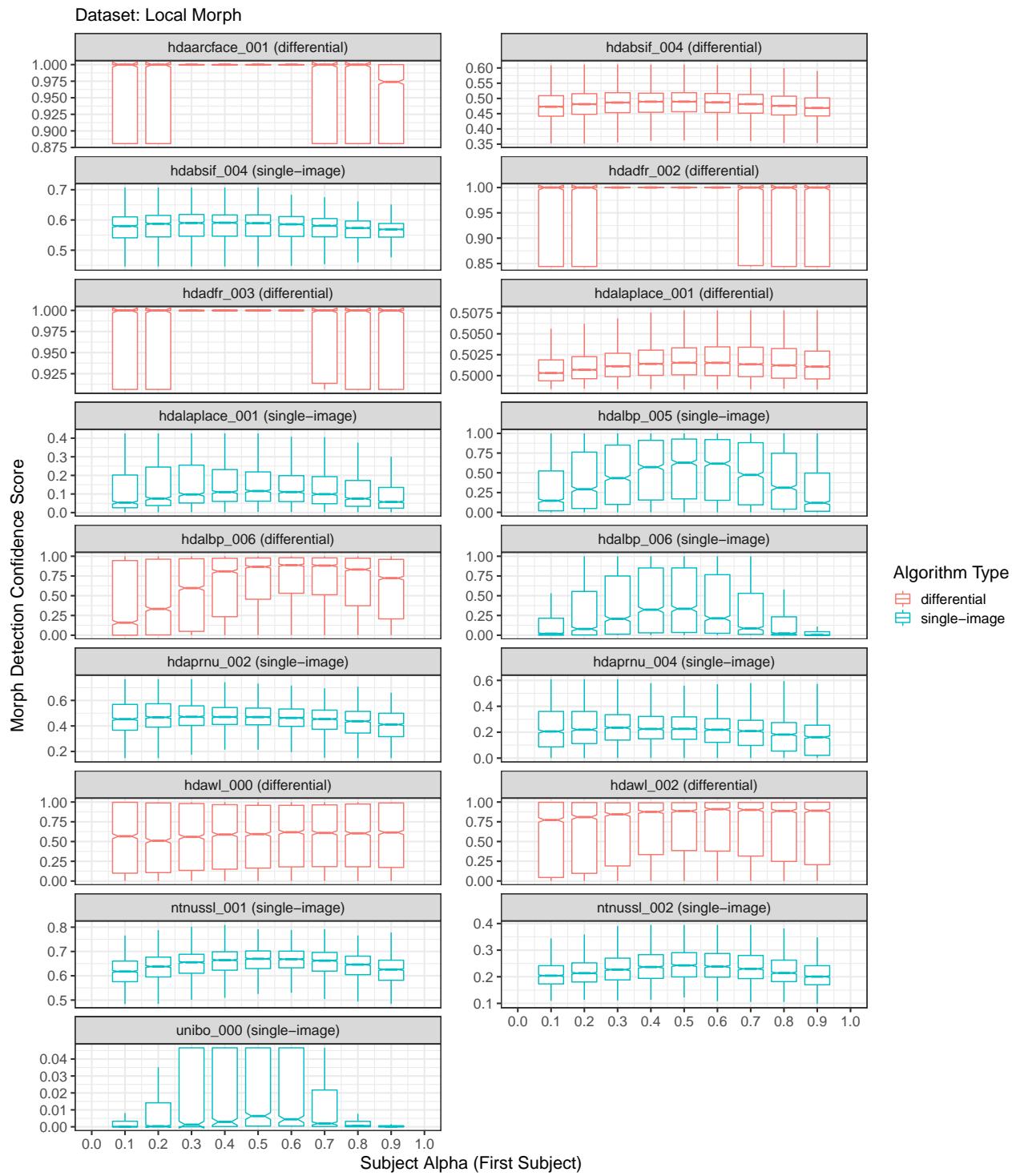


Figure 29: Boxplots plotting morph detection confidence score as a function of subject alpha (first subject in morph). Each plot includes scores that were successfully generated by the algorithm (i.e., results from failure to process were not used in this analysis).

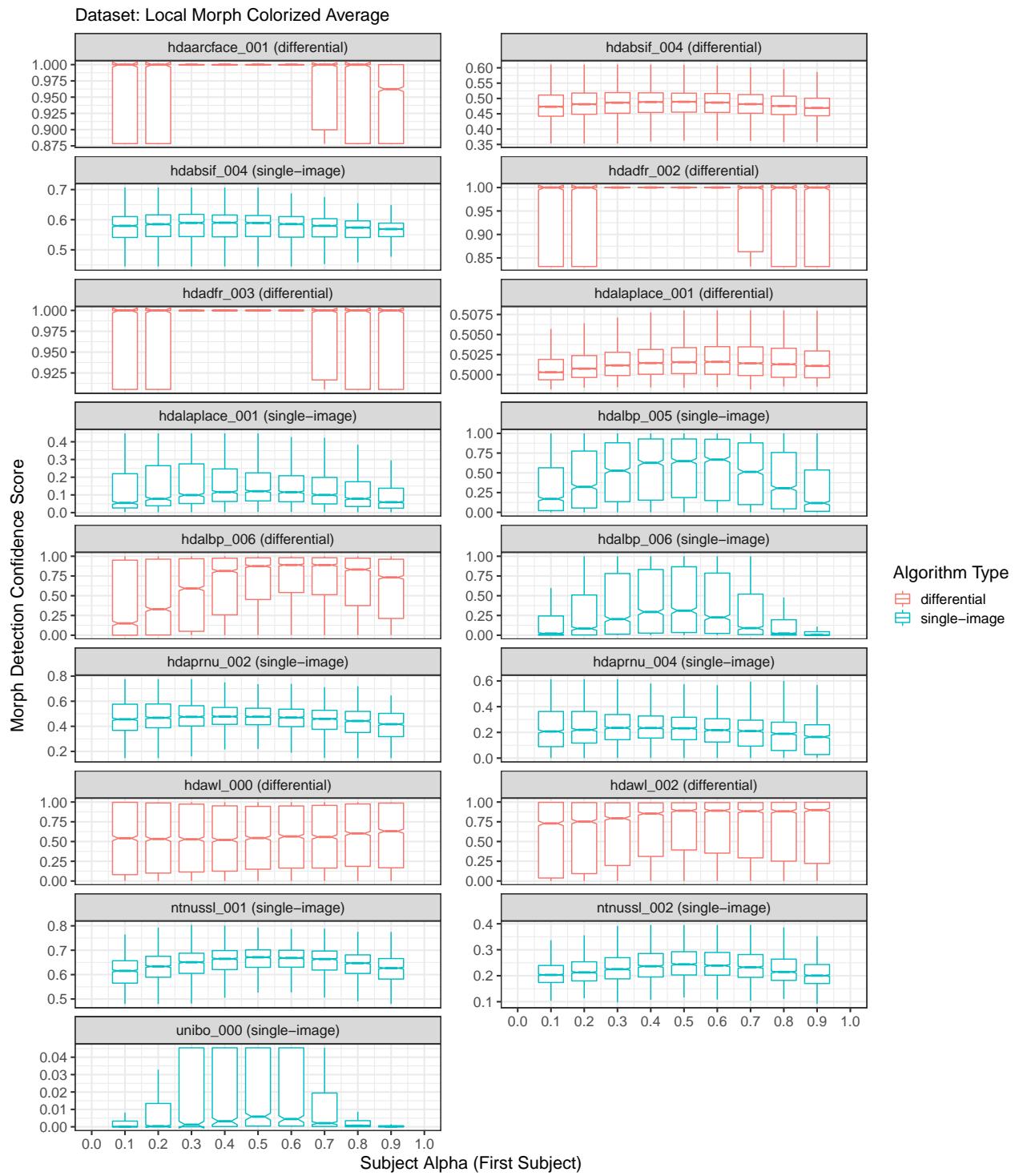


Figure 30: Boxplots plotting morph detection confidence score as a function of subject alpha (first subject in morph). Each plot includes scores that were successfully generated by the algorithm (i.e., results from failure to process were not used in this analysis).

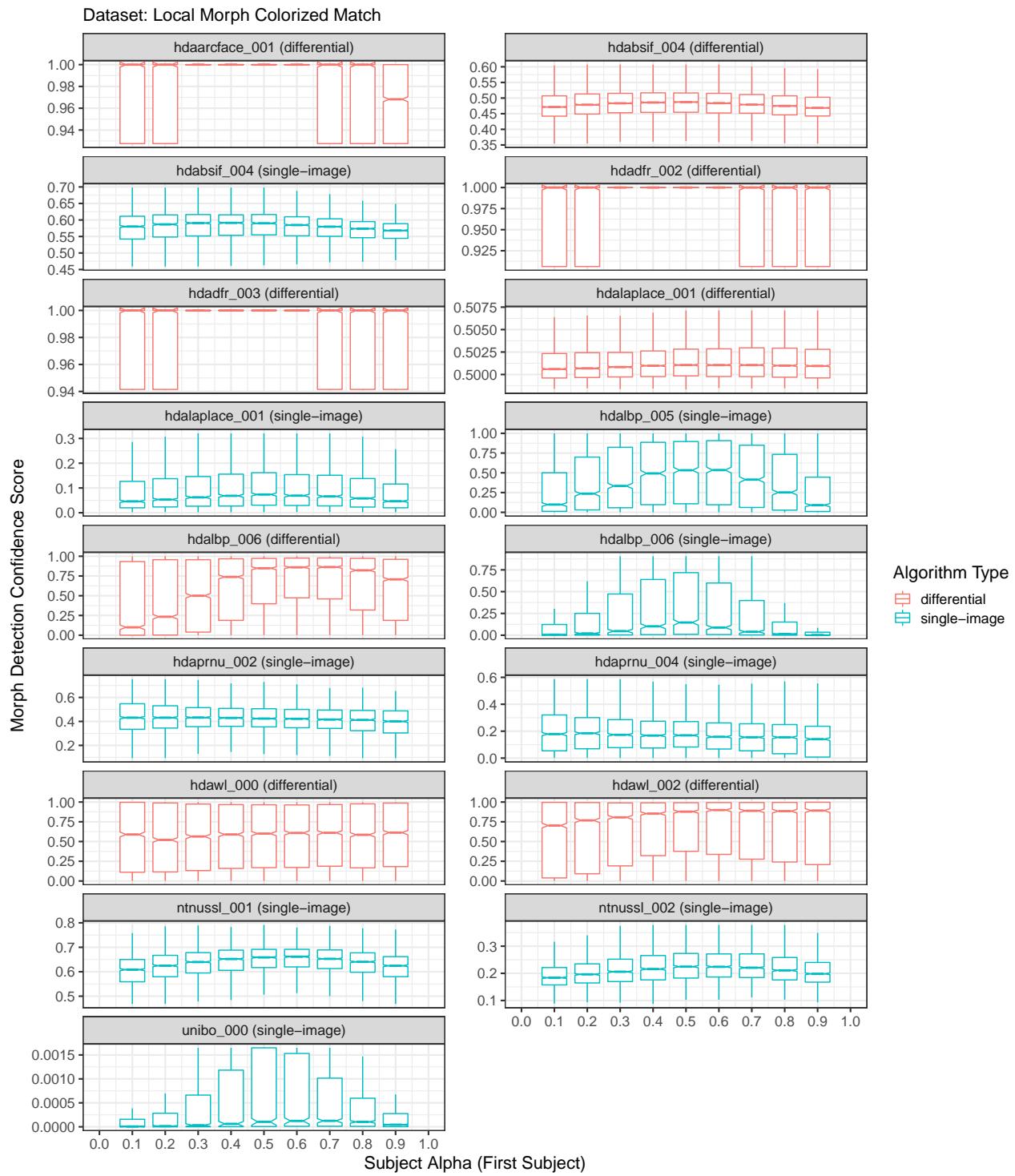


Figure 31: Boxplots plotting morph detection confidence score as a function of subject alpha (first subject in morph). Each plot includes scores that were successfully generated by the algorithm (i.e., results from failure to process were not used in this analysis).

References

- [1] Matteo Ferrara, Annalisa Franco, and Davide Maltoni. *On the Effects of Image Alterations on Face Recognition Accuracy*, pages 195–222. Springer International Publishing, Cham, 2016.
- [2] David J. Robertson, Robin S. S. Kramer, and A. Mike Burton. Fraudulent id using face morphs: Experiments on human and automatic recognition. *PLOS ONE*, 12(3):1–12, 03 2017.
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