

# NCERT Discrete 10.5.2 -15

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**Question:** For what value of  $n$ , are the  $n$ th terms of two A.Ps: 63, 65, 67,... and 3, 10, 17,... equal?

**Solution:**

Parameter	Sub-question	Description	Value
$x_i(0)$	$x_1(0)$	1 <sup>st</sup> term of 1 <sup>st</sup> A.P.	63
	$x_2(0)$	1 <sup>st</sup> term of 2 <sup>nd</sup> A.P.	3
$d_i$	$d_1$	Common difference of 1 <sup>st</sup> A.P.	2
	$d_2$	Common difference of 2 <sup>nd</sup> A.P.	7

TABLE I  
PARAMETERS USED

$$X(z) = x(0)z(z-1)^{-1} + dz(z-1)^{-2} \forall |z| > 1 \quad (1)$$

1) For the 1<sup>st</sup> A.P. let  $x_1(n)$  be  $n$ th term:

a) Finding  $x_1(n)$  for the 1<sup>st</sup> A.P:

$$x_1(0) = 63 \quad (2)$$

$$x_1(0) + d_1 = 65 \quad (3)$$

$$\Rightarrow x_1(n) = 63 + 2n \quad (4)$$

$$\therefore x_1(n) = 63u(n) + 2n \cdot u(n) \quad (5)$$

b) To find  $X_1(z)$ :

$$x_1(0) = 63 \quad (6)$$

$$d_1 = 2 \quad (7)$$

$$\therefore X_1(z) = 63z(z-1)^{-1} + 2z(z-1)^{-2} \forall |z| > 1 \quad (8)$$

2) For the 2<sup>nd</sup> A.P. let  $x_2(n)$  be  $n$ th term:

a) Finding  $x_2(n)$  for the 1<sup>st</sup> A.P:

$$x_2(0) = 3 \quad (9)$$

$$x_2(0) + d_2 = 10 \quad (10)$$

$$\Rightarrow x_2(n) = 7n + 3 \quad (11)$$

$$\therefore x_2(n) = 3u(n) + 7n \cdot u(n) \quad (12)$$

b) To find  $X_2(z)$ :

$$x_2(0) = 3 \quad (13)$$

$$d_2 = 7 \quad (14)$$

$$\therefore X_2(z) = 3z(z-1)^{-1} + 7z(z-1)^{-2} \forall |z| > 1 \quad (15)$$

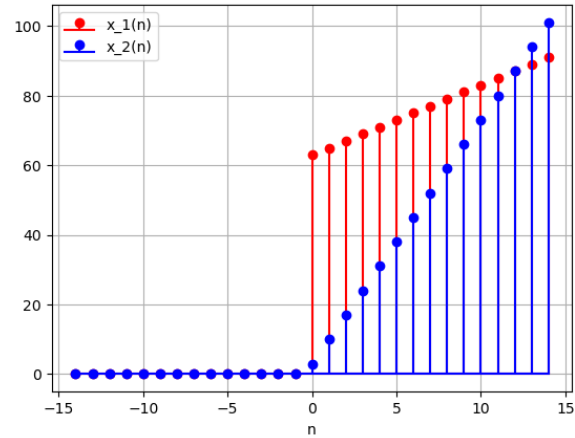


Fig. 1. Graphs of  $x_1(n)$  and  $x_2(n)$  and both are equal at  $n = 12$

given,  $x_1(n) = x_2(n)$

$$\therefore 63 + 2n = 7n + 3 \quad (16)$$

$$5n = 60 \quad (17)$$

$$\Rightarrow n = 12 \quad (18)$$

$$(19)$$

$\therefore$  13th terms of given two APs are equal.