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NCERT Discrete 10.5.2 -15

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Question: For what value of n, are the nth terms of two A.Ps: 63, 65, 67,... and 3, 10, 17,... equal?

Solution:

ĺ	Parameter	Sub-question	Description	Value
ĺ	$x_i(0)$	$x_1(0)$	1^{st} term of 1^{st} A.P.	63
		$x_{2}(0)$	1^{st} term of 2^{nd} A.P.	3
ĺ	d_i	d_1	Common difference of 1 st A.P.	2
		d_2	Common difference of 2^{nd} A.P.	7

TABLE I INPUT VALUES

$$x_i(n) = x(0) u(n) + dnu(n)$$
(1)

$$X(z) = \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})^2} \quad |z| > 1$$
 (2)

$$x_1(n) = 63u(n) + 2nu(n)$$
 (3)

$$X_1(z) = \frac{63}{1 - z^{-1}} + \frac{2z^{-1}}{(1 - z^{-1})^2} \quad |z| > 1$$
 (4)

2)

$$x_2(n) = 3u(n) + 7nu(n)$$
 (5)

$$X_2(z) = \frac{3}{1 - z^{-1}} + \frac{7z^{-1}}{(1 - z^{-1})^2} \quad |z| > 1$$
 (6)

3) given,

$$x_1(n) = x_2(n)$$
 (7)

$$\therefore 63 + 2n = 7n + 3$$
 (8)

$$\implies n = 12$$
 (9)

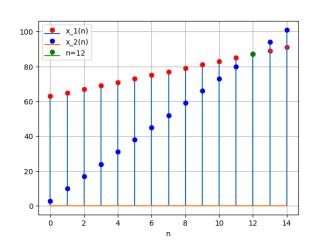


Fig. 1. Graphs of $x_1(n)$ and $x_2(n)$ and both are equal at n = 12