

Practical - 01

R is a software for statistical analysis and data computing.

It is an effective data handling software and outcome storage is possible.

It is capable of graphical display.

R is a free software.

Q.1] solve the following.

$$4 + 6 + 8 \div 2 - 5$$

$$2^2 + |1-3| + \sqrt{15}$$

$$5^3 + 7 \times 5 \times 8 + 4615$$

$$\sqrt{4^2 + 5 \times 3 + 7/6}$$

Round off
 $46 + 7 + 9 \times 8$

code:

$$1] 4 + 6 + 8/2$$

$$[1] 14$$

$$2] 2^2 + \text{abs}(-3) + \text{sqrt}(15)$$

$$[1] 13.7082$$

$$3] 5^3 + 7 * 5 * 8 + 4615$$

$$[1] 414.2$$

$$4] \text{sqrt}(4^2 + 5 * 3 + 7/6)$$

$$[1] 5.671567$$

$$5] 46/7 + 9 * 8$$

$$[1] 78.57143$$

Q2] solve the following :

$$\textcircled{1} \quad C(2,3,5,7) * 2$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 & 6 & 10 & 14 \end{bmatrix}$$

$$\textcircled{2} \quad C(2,3,5,7) * C(2,3)$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 & 9 & 10 & 21 \end{bmatrix}$$

$$\textcircled{3} \quad C(2,3,5,7) * C(2,3,6,2)$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 & 9 & 30 & 14 \end{bmatrix}$$

$$\textcircled{4} \quad C(1,6,2,3) * C(-2,-3,-4,-1)$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} -2 & -18 & -8 & -3 \end{bmatrix}$$

$$\textcircled{5} \quad C(2,3,5,7)^2$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 & 9 & 25 & 49 \end{bmatrix}$$

$$\textcircled{6} \quad C(4,6,8,9,4,5)^2 * C(1,2,3)$$

$$\rightarrow \begin{bmatrix} 1 \\ 1 \end{bmatrix} \begin{bmatrix} 4 & 36 & 512 & 9 & 16 & 125 \end{bmatrix}$$

$$\textcircled{7} \quad C(6,2,7,5) / C(4,5)$$

Q3]

solve the following :

$$x=20, y=30, z=2$$

$$\text{find } i) x^2 + y^3 + z$$

$$ii) \sqrt{x^2 + y}$$

$$iii) x^2 + y^2$$

$$) > a = x^2 + y^3 + z$$

520

$y = \text{matrix}(\text{nrow} = 3, \text{ncol} = 3, \text{data} = \{10, 12, -5, -4, -6, 7, 9, 5\})$

y

	[,1]	[,2]	[,3]
[1,]	10	-5	7
[2,]	12	-4	9
[3,]	15	-6	5

$2^x + 3^x$

	[,1]	[,2]	[,3]
[1,]	38	-19	33
[2,]	50	-12	41
[3,]	63	-28	21

$x + y$

	[,1]	[,2]	[,3]
[1,]	14	-7	13
[2,]	19	-4	15
[3,]	24	-11	8

Q.6) Marks of statistics of computer science student

59, 20, 35, 20, 46, 45, 27, 22, 27, 58, 54, 40, 50, 35, 39

Practical-2 :

Aim: Probability distribution:

i] check whether the following are P.m.s

i)	x	$P(x)$
	0	0.1
	1	0.2
	2	-0.5
	3	0.4
	4	0.3
	5	0.5

\Rightarrow since, $P(2) = -0.5$,
be P.m.s because
 $P(x) \geq 0 \forall x$

ii)	x	1	2	3	4	5
	$P(x)$	0.2	0.2	0.3	0.2	0.2
	\therefore Prob =	(0.2, 0.2, 0.3, 0.2, 0.2)				
	\therefore sum (Prob)	1.1				
	[1] 1.1					

It cannot be P.m.s
in P.m.s, $P(x) = 1$

iii)	x	10	20	30	40	50
	$P(x)$	0.2	0.2	0.35	0.15	0.1
	\therefore Prob =	(0.2, 0.2, 0.35, 0.15, 0.1)				
	\therefore sum (Prob)	1				
	[1] 1					

It is a P.m.s $P(x) = 1$ and $P(x) \geq 0$

Q.23

x	1	2	3	4	5	6
P(x)	0.15	0.25	0.1	0.20	0.2	0.1

1) $P(x) = (0.15, 0.25, 0.1, 0.20, 0.2, 0.1)$
 > $P(x) =$
 > $\text{sum}(P(x))$
 > $\text{cumsum}(P(x))$
 2) $x = (1, 2, 3, 4, 5, 6)$
 > $x =$
 > $\text{plot}(x, \text{cumsum}(P(x)), "s", xlab =$
 "values", ylab "cumsum P(x)", main
 "CDF")

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$$(1) \int_0^1 f(x) dx$$

$$= \int_0^1 3x^2 dx$$

$$= \left[\frac{3x^3}{3} \right]_0^1$$

$$= [x^3]_0^1$$

$$= 1$$

sin u is integration is equal to 1,
 it is a P.d.f.

M'

1) binom (10, 100, 0.1)

2) binom (10, 12, 0.2)

3) binom (10, 12, 0.2)

4) binom (10, 12, 0.2)

5) binom (10, 12, 0.2)

6) binom (10, 12, 0.2)

7) binom (10, 12, 0.2)

8) binom (10, 12, 0.2)

9) binom (10, 12, 0.2)

10) binom (10, 12, 0.2)

Exercice 3

TOPIC: Binomial distribution

1) binom (10, 100, 0.1)

2) binom (10, 12, 0.2)

3) binom (10, 12, 0.2)

4) binom (10, 12, 0.2)

5) binom (10, 12, 0.2)

6) binom (10, 12, 0.2)

7) binom (10, 12, 0.2)

8) binom (10, 12, 0.2)

9) binom (10, 12, 0.2)

10) binom (10, 12, 0.2)

Find the probability of exactly 10 success in 100 trials, with $p = 0.1$

Suppose there are 12 m.c. each question has 5 options out of which one is correct. Find the probability of having exactly 4 correct answers. At most 4 correct answers. More than 5 correct answers.

Find the complete distribution $n = 5, p = 0.1$

$n = 12, p = 0.25$ Find the prob

i) $P(X = 5)$

ii) $P(5 < X < 7)$

520

Q1 Probability of a salesman making a sale to a customer 0.15
Find the probability of
i) no sale out of 3 customers
ii) more than 3 sale out of 10
20 customers.

Q2 A salesman has a 20% probability of making a sale out of 30 customers. What min of sales he can make with 88% probability.

Q3 X follows binomial distribution with $n=10$, $p=0.3$. Plot the pmf and cdf.

220.
 $> \text{plot}(x, \text{plot}, "n")$
 $> \text{plot}(x, \text{complot}, "c")$

$> p3 = 1 - \text{pnorm}(14, 12, 3)$
 $[1] 0.254925$
 $> cat("P(x=14) = ", p3)$

(6)
 $> \text{pnorm}(5, 12, 3)$
 $[1] 0.512180$

0.2] x follows normal distribution with $\mu=10$,
 find
 (1) $P(x \leq 7)$ 2) $P(x < x < 12)$ 3) $P(x < 12) \cup$ y generated
 (5) find k that $P(x < k) = 0.4$ 10 observations

\Rightarrow
 1) $P(x \leq 7)$
 $P1 = \text{pnorm}(7, 10, 2)$
 $> P1$

[1] 0.0668072
 2) $P(5 < x < 12)$
 $> P2 = \text{pnorm}(12, 10, 2) - \text{pnorm}(5, 10, 2)$
 $> P2$

[1] 0.8351351

3) $P(x > 12)$
 $P3 = 1 - \text{pnorm}(12, 10, 2)$
 $> P3$
 $[1] 0.1586553$

generate 10 observations

$\text{rnorm}(10, 10, 2)$
 7.324489 8.308746 8.394823 11.990873
 8.2528 10.75449 13.33875 10.266751

```

020
P(2.5 < x < 4.35)
> P3 = pnorm(3.5, 30, 10) - pnorm(2.5, 30, 10)
> P3
[1] 0.3829 249

4) pnorm(0.6, 30, 10)
[1] 32.53347

03) solution
n = 5, u = 15, s = 4
> rnorm(5, 15, 4)
[1] 16.31588
> me = median(x)
> me
[1] 15.58 400

> n = 5
> variance = (n-1) * var(x) / n
> sd = sqrt(variance)
> sd
[1] 2.32583

> cat("sample mean = ", dm)
> cat("sample median = ", me)
> cat("sample s.d = ", sd)

```

Q.3) Generate 5 random no. from normal distribution and mean = 30, SD = 10. Find sample mean, median, SD and P-value. 0.66

sample x follows $N(30, 10)$

5.4] $u = 30$, $s = 10$ 1) $P(x \leq 40)$ 2) $P(x > 35)$ 3) $P(x < 25)$
 find $P(x < 25)$

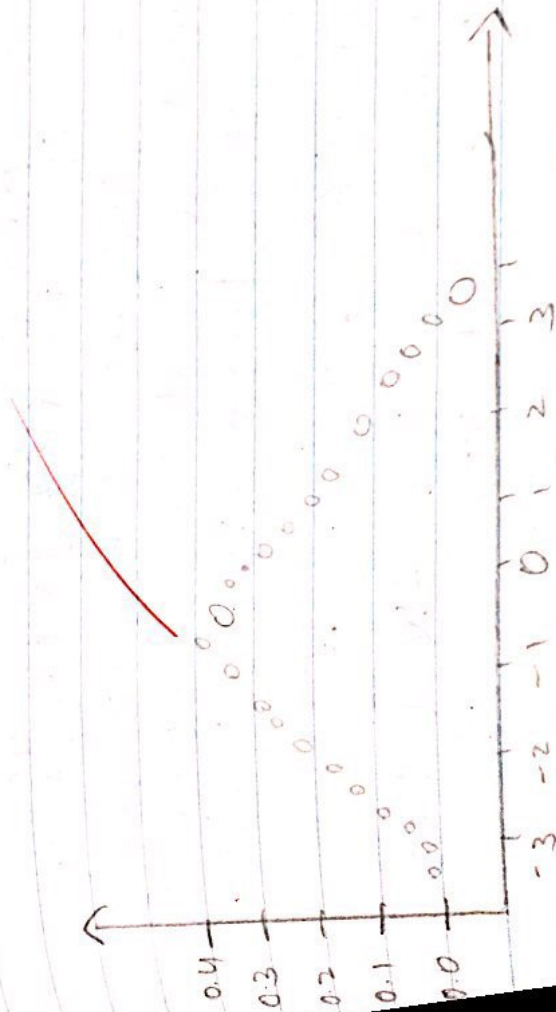
1) $P(x \leq 40)$
 $P_1 = \text{pnorm}(40, 30, 10)$
 P_1
 [1] 0.8943447
 2) $P(x > 35)$
 $P_2 = 1 - \text{pnorm}(35, 30, 10)$
 P_2
 [1] 0.3085375

sample mean = 15.58444
 sample variance = 2.332583

the standard normal graph
 $\text{plot}(\text{c}(-3:3, \text{by} = 0.1))$

$\text{dnorm}(x)$

$\text{plot}(x, y, \text{xlab} = "x \text{ values}", \text{ylab} = "Probability", \text{main} = "standard normal graph")$



x values

Practical - 05
Aim: Normal and T-test

Q1] Test the Hypothesis

$$H_0: \mu = 15$$

$$H_1: \mu \neq 15$$

Random sample of 400 size of diameter and it is calculated. The sample mean is 14 and standard deviation is 3. Hypothesis at 5% level of significance.

```
> m0 = 15, mx = 14, sd = 3, n = 400
> zcal = (mx - m0) / (sd) (sqrt(n))
> cat ("calculated value at z is =", zcal
calculated value at z is -6.66667
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
```

```
[1] 2.016796e-11
```

\therefore value of p is less than 0.05.

the Hypothesis:

$$H_0: \mu = 10$$

$$H_1: \mu \neq 10$$

A random sample of
with sample mean

size 100 is drawn
10.2 and $s.d = 2.5$.

Test the hypothesis at 5% level of significance.

$$= 10, \quad \mu = 10.2, \quad s.d = 2.5, \quad n = 100$$

$$z_{cal} = (\bar{x} - \mu) / (s.d / \sqrt{n})$$

at calculated value at $z_{is} = 1.2$ (cal)
calculated value at $z_{is} = 1.777778$

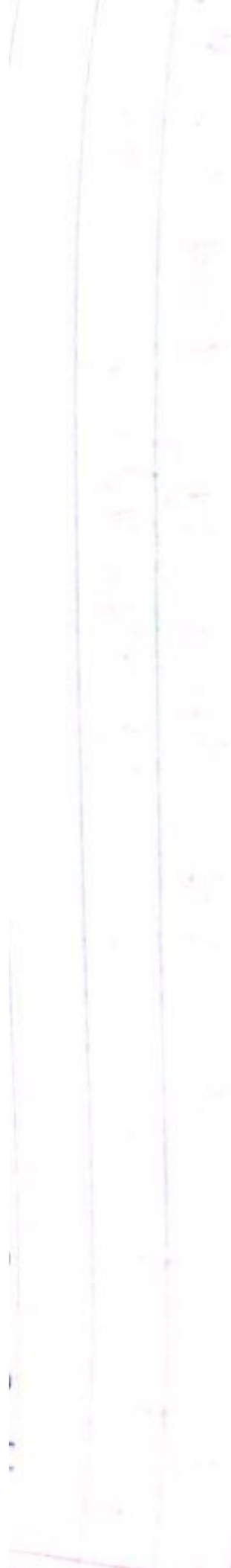
> P value

$$z_{is} = 0.075$$

value of P is

greater than 0.05

We accept H_0 . $\mu = 10$



$$(n-1) \times \text{var}(u) / n$$

$$\text{var}(u) = \frac{1}{n} \sum_{i=1}^n u_i^2 - \left(\frac{1}{n} \sum_{i=1}^n u_i \right)^2$$

$$\text{var}(u) = \frac{1}{n} \sum_{i=1}^n u_i^2 - \left(\frac{1}{n} \sum_{i=1}^n u_i \right)^2$$

$$\text{var}(u) = \frac{1}{n} \sum_{i=1}^n u_i^2 - \left(\frac{1}{n} \sum_{i=1}^n u_i \right)^2$$

$$\text{var}(u) = \frac{1}{n} \sum_{i=1}^n u_i^2 - \left(\frac{1}{n} \sum_{i=1}^n u_i \right)^2$$

$$= 12$$

$$\text{var}(u) = \frac{1}{n} \sum_{i=1}^n u_i^2 - \left(\frac{1}{n} \sum_{i=1}^n u_i \right)^2$$

$$= 12$$

$$= 12$$

$$= 12$$

$$= 12$$

$$= 12$$

2. In a random sample of 100 students, 75 use blue pens. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

- $\Rightarrow H_0: p = 0.8$ against $H_1: p \neq 0.8$
- $> p = 0.8; q = 1 - p; P = 750/1000; n = 1000$
- $> z_{cal} = (p - P) / \sqrt{pq} \times (P \times (q/n))$
- $> z_{cal}$ calculated value of $z: -3.4528102$
- $> p_{val} = 2 * (1 - P_{norm}(\text{abs}(z_{cal}))$
- $> \text{at } (1 - P_{norm}(\text{abs}(z_{cal})))$
- calculated p-value: 7.722682×10^{-5}
- \therefore p-value is less than 0.1, the value is rejected.

Two random samples of size 1000 and 2000 are drawn from two population with means 67.5 and 68. Test the hypothesis of significance.

- $H_0: \mu_1 = \mu_2$ vs $H_1: \mu_1 \neq \mu_2$
- $n_1 = 1000; n_2 = 2000; m_{x1} = 67.5; m_{x2} = 68;$
- $z_{cal} = (m_{x1} - m_{x2}) / \sqrt{(s^2/n_1 + s^2/n_2)}$
- calculated value of $z: -5.163478$
- $= 2 * (1 - P_{norm}(\text{abs}(z_{cal})))$
- calculated p-value: 1.1×10^{-7}
- p-value is less than 0.05, then reject H_0 .

Exercice 6 :

large sample test

Topic :

Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers is selected. The sample mean is calculated as 275 and S.D 30. Test the hypothesis that population mean is 250 vs not at 5% level of significance.

$H_0 : \mu = 275$ against $H_1 : \mu \neq 275$

> $\mu_x = 275$

> $\mu_0 = 250$

> $sd = 30$

> $n = 100$

> $z_{cal} = (\mu_x - \mu_0) / (sd / \sqrt{n})$

> at "calculated value of z : " , z_{cal}

calculated value of z : 8.3333

> $P_{val} = 2 * (1 - P_{norm}(\text{abs}(z_{cal}))$

> at "calculated pvalue : " , P_{val}

calculated pvalue : 0

Pvalue is less than 0.5 then the value P is accepted.

280

The study of noise level in the hospitals is claim that 1st level of noise test the some noise at hospital 1 & hospital 2

size	hospital A	hospital B
mean	61.2	69.4
sd	7.9	7.5

$H_0: \mu_1 = \mu_2$ vs $H_1: \mu_1 \neq \mu_2$

$n_1 = 34$

$n_2 = 34$

$\mu_1 = 61.2$

$\mu_2 = 69.4$

$\sigma_1 = 7.9$

$\sigma_2 = 7.5$

$z_{\alpha/2} = (x_1 - x_2) / \sqrt{\sigma_1^2/n_1 + \sigma_2^2/n_2}$

calculated value of z: 1.1625528

calculated value of z: 1.1625528

calculated value of z: 1.1625528

calculated value of z: 1.1625528

calculated value of z: 1.1625528

Practical - 7 :
Topic : small sample test

The marks of 10 students are given by
63, 65, 66, 67, 68, 69, 70, 71, 72. Test the
hypothesis that the sample comes from
operation that the sample with average 66

$\Rightarrow H_0: \mu = 66$
 $\Rightarrow \alpha$ test (63, 63, 66, 67, 68, 69, 70, 71, 72)
 $\Rightarrow t$ test (3)

on sample t-test

data :>
 $t = 68.319$, $df = 9$, $P\text{-value} = 1.558 \times 10^{-13}$
alternative hypothesis : true mean is not
equal to 0.95 percent confidence interval
5.65171 to 0.14829

sample estimates :

mean of x

67.9

$P\text{-value} = 1.558 \times 10^{-13} < 0.05$. we reject H_0

> $P\text{-value} = 1.558 \times 10^{-13}$

> if ($P\text{-value} > 0.05$) { cat ("accept H_0 ") }
else { cat ("Reject H_0 ") }

Reject H_0 .

the sales data of 6 shops before and after a special campaign will given

068

Test the hypothesis
 before : 55, 23, 31, 45, 50, 42
 after : 58, 23, 30, 55, 56, 45

H_0 - there is no significant difference between before and after the campaign

```
> x = c(33, 28, 31, 48, 50, 42)
> y = c(58, 23, 50, 55, 56, 45)
> t.test(x, y, paired = T, alternative = "greater")
```

paired t-test

data : x and y
 $t = -2.7815$, $df = 5$, $p\text{-value} = 0.0166$
 alternative hypothesis: true difference in means is greater than 0
 35 percent confidence interval

sample estimates:
 mean of difference
 -3.5

```
> pvalue = 0.0606
> if (pvalue > 0.05) [cat ("Accept H0")] else
  [cat ("Reject H0")] Accept H0.
```


2) To 5 groups of students score the following marks. Test the hypothesis that there is no significant difference between two groups.

Group 1: 18, 22, 21, 17, 20, 17, 23, 20, 22
Group 2: 16, 20, 14, 21, 20, 18, 13, 15

$\Rightarrow H_0$: There is no difference between two groups.

> x = c(18, 22, 21, 17, 20, 17, 23, 20, 22)

> y = c(16, 20, 14, 21, 20, 18, 13, 15)

> t.test(x, y)

We use two sample t-test

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no medians are applied to the

group at 10, 12, 13, 11, 14

8, 9, 12, 14, 15, 10, 9

there are no significant difference between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

there is no significant difference

between two medians.

Practical 8:
Topic: large and small sample t_{α}

$H_0: \mu = 55$ against $H_1: \mu \neq 55$

$$\begin{aligned} &> \text{max} = 55 \\ &> \text{mo} = 52 \\ &> n = 100 \end{aligned}$$

$$\begin{aligned} &> \text{sd} = 7 \\ &> \text{calc} = (\text{max} - \text{mo}) / (\text{sd} / \sqrt{n}) \end{aligned}$$

$$> 2 \text{ calc}$$

$$\{1\} \text{ u2e5714}$$

$$> \text{pval} = 2 * \text{ci} - \text{pnorm}(\text{abs}(\text{calc}))$$

$$\{1\} - 1.82153e - 05 \quad (\text{pval is rejected})$$

$H_0: \mu = 0.5$ against $H_1: \mu \neq 0.5$

$$> P = 350/200$$

$$> P = 0.5$$

$$> n = 200$$

$$> q = 1 - P$$

$$> 2 \text{ calc} = (\text{P} - P) / \sqrt{P * (1 - P)}$$

$$> 2 \text{ calc}$$

$$\{1\} 0$$

$$> \text{pval} = 2 * \text{ci} - \text{pnorm}(\text{abs}(\text{calc}))$$

$$> \text{pval}$$

$$\{1\} 1$$

(Pval is accepted)

$\alpha = 0.05$
 $H_0: \mu = 66$ (no problem)
 $H_1: \mu \neq 66$ (problem)
 against $H_1: \mu \neq 66$

$\alpha = 0.05$
 $H_0: \mu = 66$
 $H_1: \mu \neq 66$
 and sample $t = -108.1$

data: x
 $t = 47.1$
 alternative hypothesis the mean is
 equal to 66 percent confidence
 interval 66 ± 4.9
 61.1 to 70.9

sample mean at 2
 68.42 is rejected
 $H_0: \mu = 66$
 $H_1: \mu \neq 66$

data: x
 $t = 47.1$
 alternative hypothesis the mean is
 equal to 66 percent confidence
 interval 66 ± 4.9
 61.1 to 70.9

Buschall - 09

Aim: chi-square tests and PIV. V. R.
 will use the following data, test whether the
 calculation of the name and child are independent
 or not

condition of name
 child condition clean 70 dirty 50

daily clean 80 20
 dirty 35 45

Test the hypothesis that vaccine and disease
 are independent or not } vaccine
 Affected not affected

disease Affected 70 46
 not affected 35 37

perform a ANOVA test the following
data observations.

Type

50, 52

A

53, 55, 53

B

60, 58, 57, 56

52, 54, 54, 55

: practical 10 :

Aim : non-parametric test

Following all the amount of
 a nephrology industry in 20 days
 to test the hypothesis that the population
 median is 21.5 at 5% level of
 significance

data - 17, 15, 20, 20, 10, 10, 22, 25, 27, 9,
 20, 17, 6, 24, 14, 15, 23, 24, 26

: Population median is 21.5.

$n = \text{length}(data)$
 $\mu = 21.5$

$p = \text{length}(data) - \text{sum}(data > \mu)$
 $= \text{length}(data) - \text{sum}(data < \mu)$

$V = \text{sum}(data > \mu)$
 $V = \text{pbinom}(-sp, n, 0.5)$

V
 0.4113015

The following are values of sample
 test the hypothesis that population
 median is 60 against the alternative
 is more than against the alternative
 ing
 data: 63, 65, 60, 61, 89, 51, 68, 62, 63, 64,
 69, 72, 69, 48, 66, 72, 62, 08, 137, 69

Population median = 60, H_1 : Population
 median > 60
 $C = C(\text{data})$
 will use test (α) alter = 'greater'

at $\alpha = 0.05$, $P\text{-value} = 0.0220$
 $= 145$, hypothesis: \rightarrow up location
 alternative greater than 60
 value < 0.05 (rejected)

of alternative is less: alter = 'less'
 alternative is not equal
 alter = 'two sided'

of alter the alternative is greater;
 alter = 'greater'
 WRT test the population median
 or less than 12
 7, 24, 25, 20, 21, 32, 28, 12, 25, 26
 median is 12, H_1 : Population


```

> x = c(weight before)
> y = c(weight after)
> d = x - y
> wilcox.test(d, alter = "two.sided",
              mu = 0)

```

wilcox on signed rank test with continuity correction

data: d
 $V = 4.5$, $P\text{-value} = 0.4981$
 alternative hypothesis: true location is not equal to 0

$P\text{-value} > 0.05$ (accepted).

$\frac{M}{5.20}$