

# ESDA 1: Distance

Class #16 | Geog 215

Introduction to Spatial Data Science

Spring 2020

*“Everything is related to everything else,  
but near things are more related than  
distant things”* - Waldo Tobler

# Quick Recap from last class

## Exploratory (Spatial) Data Analysis

Two questions to consider:

- What type of geographic variation occurs *within* my variables?
- What type of geographic variation occurs *between* my variables?

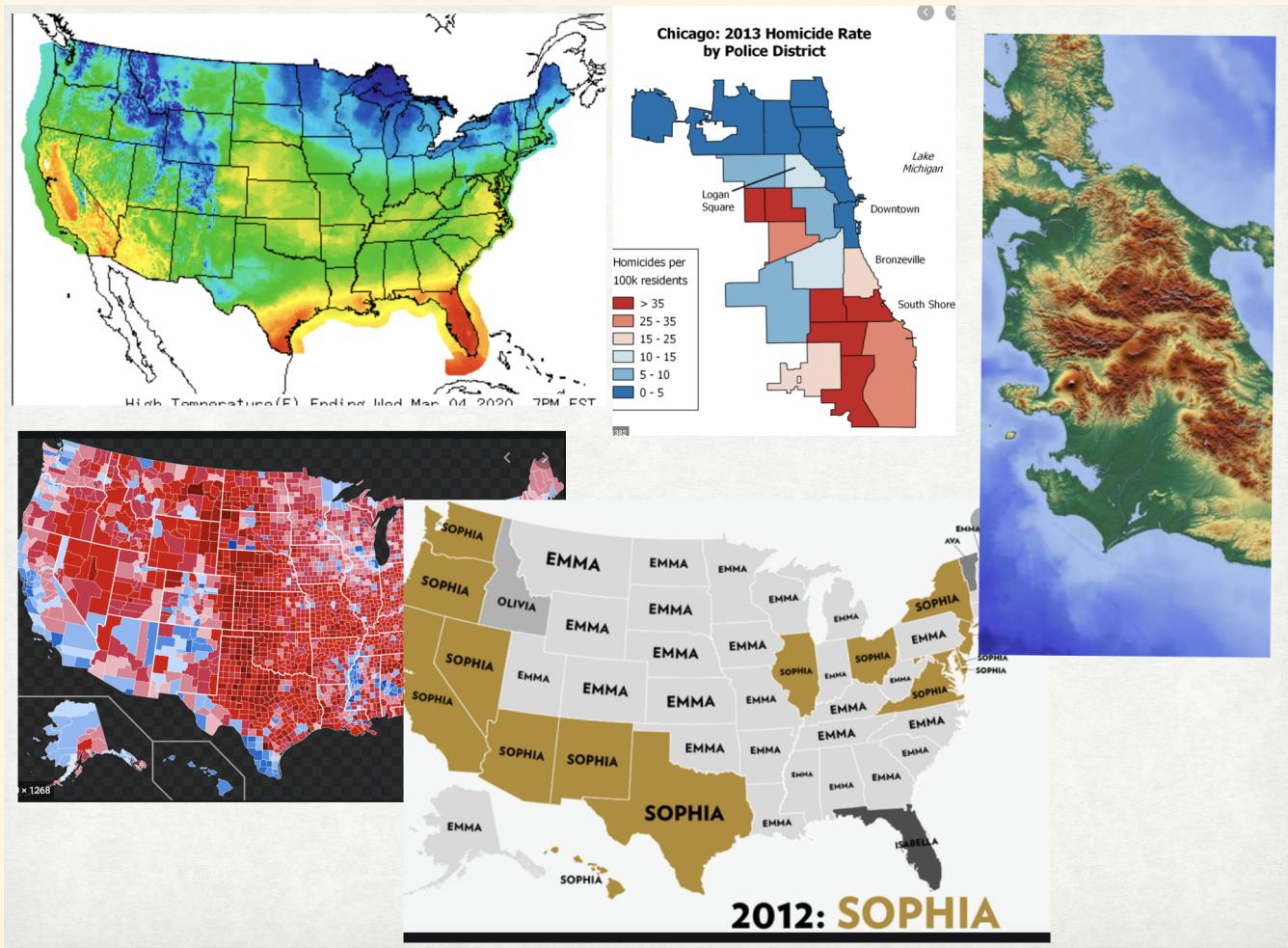
# Why do we care?

# Tobler's First Law of Geography (TFL)

"All things are related, but nearby things are more related than distant things"

- Spatial Dependence
  - What happens at one location is dependent on what happens at another location
- Underlines almost every physical and social phenomena

# Tobler's First Law of Geography (TFL) in Action



# Tobler's First Law of Geography (TFL)

"All things are related, but nearby things are more related than distant things"

- **Spatial Dependence**
  - What happens at one location is dependent on what happens at another location
- Underlines almost every physical and social phenomena
- **If TFL weren't true**
  - **GIS would be impossible**
  - **Life would be impossible**
  - **I will be out of work... :/**

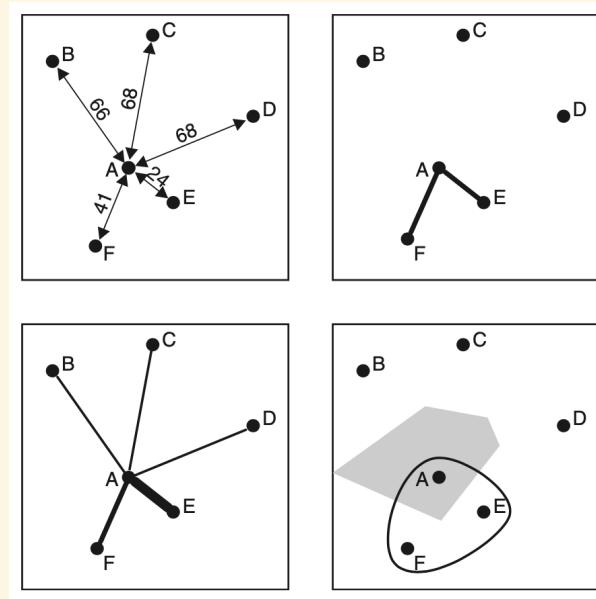
# In Exploratory Spatial Data Analysis

We try to learn about spatial dependence/trends in our data

- What is the geographic variation within my variables
  - At what spatial scale does my data look similar/dissimilar
    - eg. Till what distance from a cafo do I see similar cancer rates ?
    - eg. Where are the outliers my in my data situated?
    - Can i predict missing data?
- What is the geographic variation between my variables
  - Are 2 variables spatially correlated?
  - eg - Do places with higher bednet coverage have lower rates of malaria?  
are there any places with high coverage of bednets, but still high malaria?

# Quantifying Spatial dependence and relationships

- **Distance**
- **Adjacency**
- **Interaction**
- **Neighborhood**



# Distance

- A fundamental geographic concept
  - Affects relationships and interactions among things and places
- Physical distance
  - Separation in either space or time
  - Essential to understanding “space”
  - As an effect and/or as an outcome!

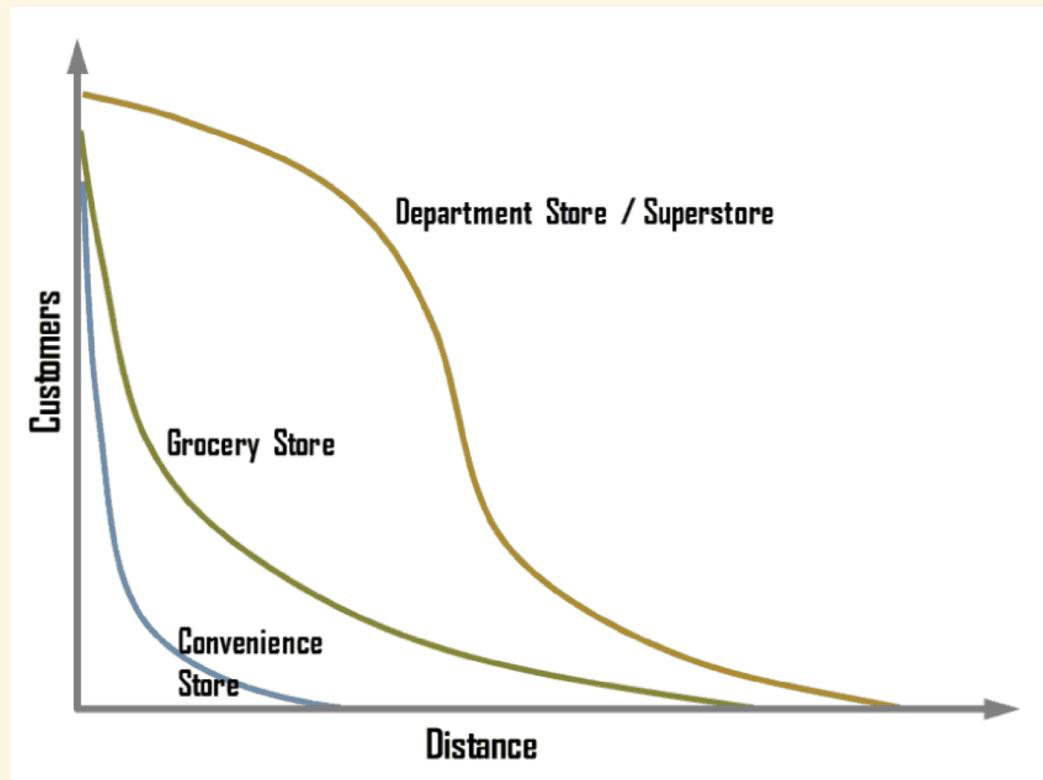
# Distance

- Social Distance
  - Connection and isolation
  - Formation of social networks
  - Are some subgroups more likely to interact or not?
  - Information dissemination

# Distance Decay

- Important concept in Geography
- Interaction (actual or potential) or relationship among phenomena decreases with increasing distance
  - Distance has “friction”

# Distance Decay



Can you think of other examples?

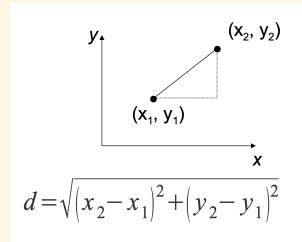
# Why Distance

Distance is a fundamental geographic concept that affects relationships and interactions among phenomena

- Sometime we want to explain it
- Sometimes we want to measure it for input to other calculations
- Sometimes we want to map it

# Euclidean Distance

- Based on **Pythagoras Theorem**
  - $a^2 + b^2 = c^2$
- Assumes:
  - A planar Earth (Project CS)
  - No differences in elevation
- Does not require a GIS
  - Simple Math Calculation
  - **Should not be used with latitude and longitude!!!**



# Euclidean Distance

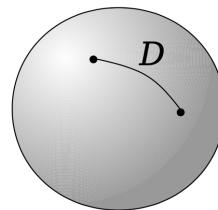
## Limitations

- Assumes flat earth
  - Especially limiting over large distances
- Assumes no slope in terrain
  - Especially limiting in mountainous terrain
- Assumes no barriers to movement
  - Barriers can include anything that's not a road (in the case of vehicular travel) or anything on the landscape that stands in the way

# Great Circle Distance

Great circle distance is the shortest distance between two points on a sphere

- Used for points stored in spherical coordinates
- Required to calculate distance in spherical coordinates, especially if points are far apart



Point 1:  $(\lambda_1, \Phi_1) \leftarrow$  longitude, latitude

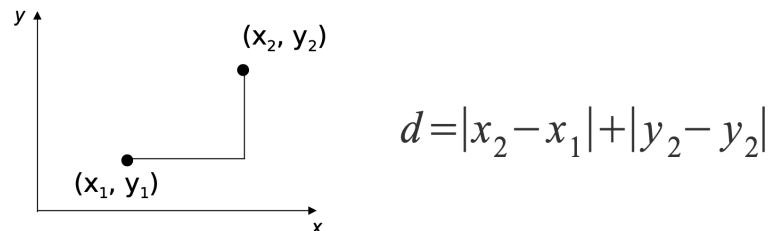
Point 2:  $(\lambda_2, \Phi_2) \leftarrow$  longitude, latitude

R: radius of the Earth  
(~6378km)

$$D = R \cdot \cos^{-1}((\sin \phi_1 \cdot \sin \phi_2) + (\cos \phi_1 \cdot \cos \phi_2 \cdot |\lambda_1 - \lambda_2|))$$

# Manhattan Distance

- One way to account for barriers is to recognize that travel can be limited to transportation routes that follow cardinal directions (N, S, E, W)
  - ##### In cities with a grid system
    - Eg. in Manhattan where most streets are at right angles



# Minkowski Distance

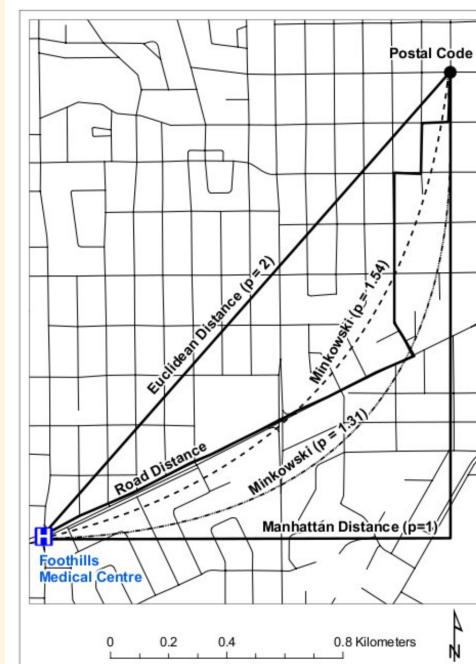
- Falls between Euclidean and Manhattan distance
- Distance of a curved arc connecting two points

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \quad \text{Euclidean}$$

$$d = |x_2 - x_1| + |y_2 - y_1| \quad \text{Manhattan}$$

$$d = \sqrt[p]{(x_2 - x_1)^p + (y_2 - y_1)^p}$$

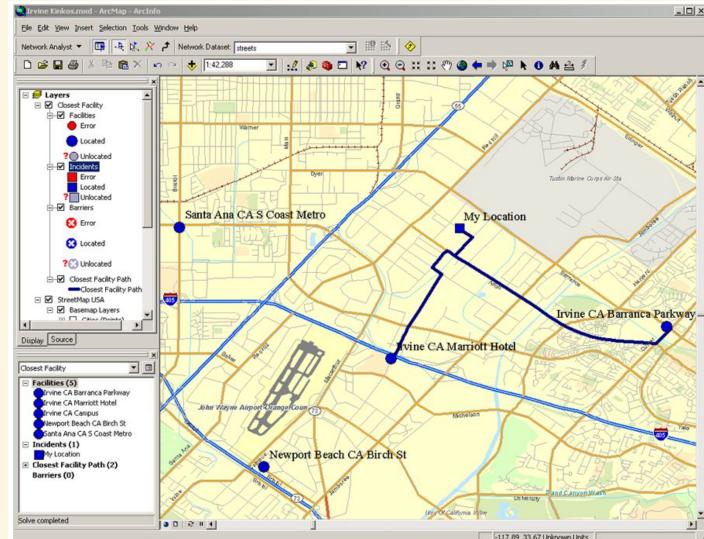
where  $1 < p < 2$



**Figure I**  
Visual illustration of road distance and distance metrics.

# Network Distance

- Restricts travel along existing arcs (lines)
  - e.g., on city streets
- Distance is the sum of the lengths of arcs that make up the route
- Available as an API from ESRI, open street maps etc. !



# Travel Time

More accurate portrayal of human movement

- Requires travel network or travel surface
  - Available as an API from ESRI
  - Can be computationally intensive
- Vehicular-based : US studies
  - Augmented using alternative travel modes
  - e.g., public transit, walking

# In what situation is Euclidean Distance Appropriate?

POLL EVERYWHERE

# Networks and Distance

In many cases, human movement is constrained to a network or network-like features

- **Point:** True “separation” among places should not be measured as straight lines, as this is not how people “overcome” distance
- **Counterpoint:** in some (many?) cases, Euclidean distances and network-based distances/times are highly correlated; hence Euclidean distances are a reasonable proxy

# Measuring Distance

Basic approaches to measuring distance among things (for comparative purposes)

- Absolute distance
  - Based upon the actual distance separating them
- Relative distance
  - Nearest feature
  - The nearest feature is considered a neighbor, or
  - Or, nearest k features
- Topology-based
- Connecting features are considered neighbors

**FINISH MIDTERM (Quiz closes indefinitely on  
Friday 11:55 pm)**

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Start thinking about project proposals

Enjoy Spring-Break

**WASH YOUR HANDS, OFTEN!**

# Distance based queries

- Distance based operations may include:
  - **Spatial query**
  - Select geographic features based on distance
    - Example, distance to health care facility
  - **Buffer**
  - Use distance to define area around a point, line, or polygon feature
  - Number of grocery stores within walking distance
  - **Identify neighbors**
  - Identify geographic features within a neighborhood
  - Whether a Cafo exists in my neighborhood

