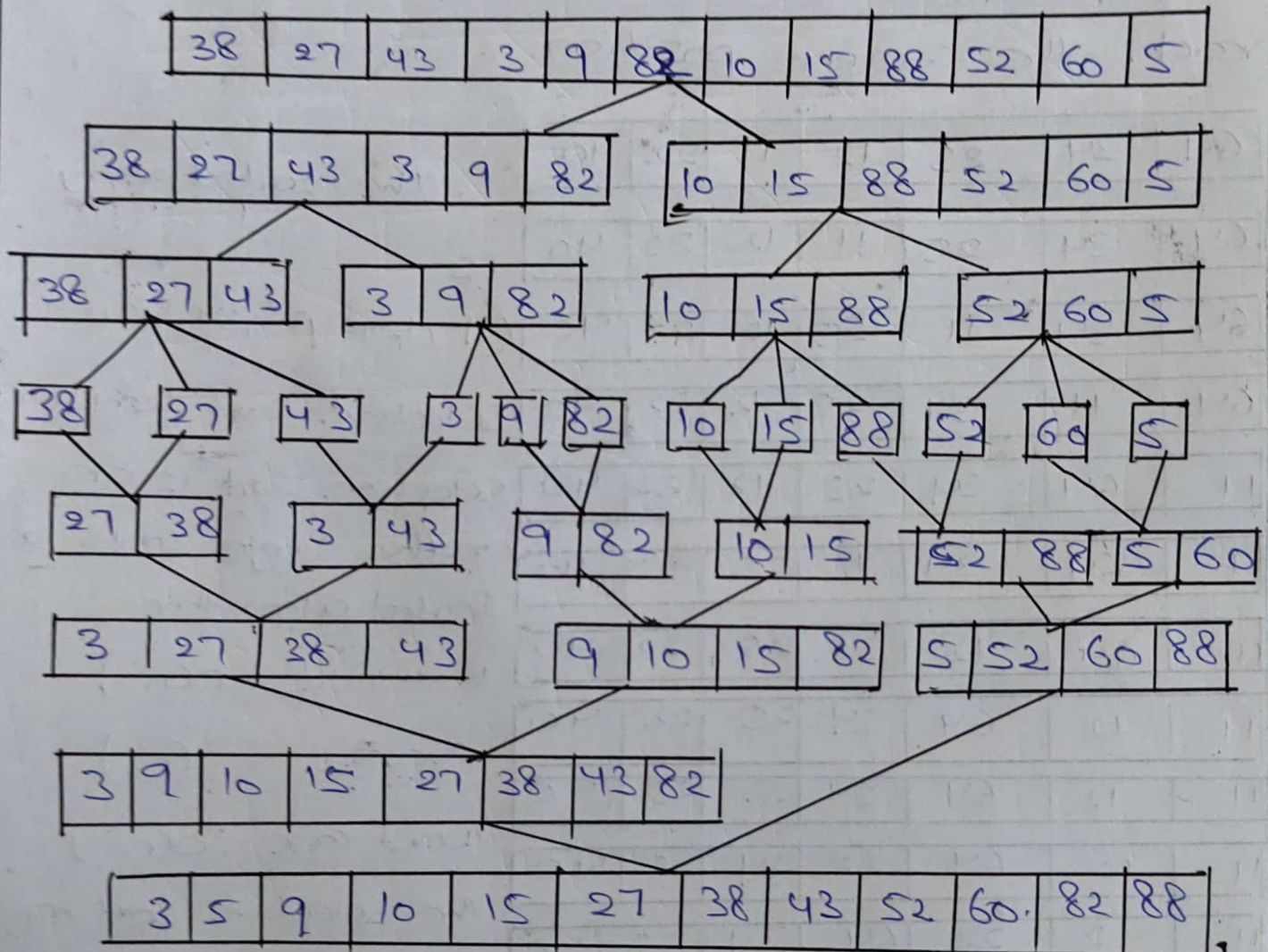


1) Sort the following elements using merge sort divide and conquer $[38, 27, 43, 3, 9, 82, 10, 15, 88, 52, 60, 5]$ using and analyze time complexity of the algorithm.

Sol given array



∴ Sorted list = $[3, 5, 9, 10, 15, 27, 38, 43, 52, 60, 82, 88]$

Time complexity:

Time complexity of merge sort is $O(n \log n)$

n is the num. of elements in the list $O(n \log n)$ increase by the input into halves $\log n$ time and n element of each time takes $O(n)$ times

2) Sort the array 64, 34, 25, 12, 11, 22, 40 using bubble sort what is the time complexity of solution sort in that best, worst, average cases.

Sol/ Given array = 64 34 25 12 22 11 40

In bubble sort we bring the smallest element in the correct position continue this each element reach the current position.

64	34	25	12	11	22	40
----	----	----	----	----	----	----

∴ The sorted arrays

64	34	25	11	12	22	40
----	----	----	----	----	----	----

is

64	34	11	25	12	22	40
----	----	----	----	----	----	----

(11, 12, 22, 25, 34, 40, 64)

64	11	34	25	12	22	40
----	----	----	----	----	----	----

Selection sort complexity

11	64	34	25	12	22	40
----	----	----	----	----	----	----

Selection sort is an

11	64	34	12	25	22	40
----	----	----	----	----	----	----

another single confusion

11	64	12	34	25	22	40
----	----	----	----	----	----	----

Sorted algorithm

11	12	64	34	25	22	40
----	----	----	----	----	----	----

best case : $O(n^2)$

11	12	64	34	22	25	40
----	----	----	----	----	----	----

Average : $O(n^2)$

11	12	64	22	34	25	40
----	----	----	----	----	----	----

worst case : $O(n^2)$

11	12	22	64	34	25	40
----	----	----	----	----	----	----

The selection sort has

11	12	22	64	25	34	40
----	----	----	----	----	----	----

a time complexity

11	12	22	25	64	34	40
----	----	----	----	----	----	----

$O(n^2)$ it always goes

11	12	22	25	34	64	40
----	----	----	----	----	----	----

through the same no

11	12	22	25	34	40	64
----	----	----	----	----	----	----

of comparisons

3) Sort the array 64, 25, 12, 22, 11 using selection sort
 what is the time complexity of selection sort in the best, worst and average cases.

Sol/ given array :- 64, 25, 12, 22, 11

In the selection we will find the largest element in those correct position best so.

64	25	12	22	11
25	64	12	22	11
25	12	64	22	11
25	12	22	64	11
25	12	22	11	64
12	25	22	11	64
12	22	25	11	64
12	22	11	25	64
12	11	22	25	64
11	12	22	25	64

∴ The sorted list is 11, 12, 22, 25, 64

Time complexity

Selection sort Best case: $O(n^2)$

Average case: $O(n^2)$

Worst case: $O(n^2)$

The selection sort has a time complexity $O(n^2)$ it always through same $O(n^2)$ comparisons

Q) Sort the following elements using insertion sort using Brute Force Approach strategy / $[38, 27, 43, 39, 82, 10, 15, 88, 52, 60, 5]$ and analyze complexity of the algorithm.

Sol) Given array

$[38, 27, 43, 39, 82, 10, 15, 88, 52, 60, 5]$

Solve:-

38	27	43	3	9	82	10	15	88	52	60	5
27	38	43	3	9	82	10	15	88	52	60	5
27	38	43	3	9	82	10	15	88	52	60	5
3	27	38	43	9	82	10	15	88	52	60	5
3	9	27	38	43	82	10	15	88	52	60	5
3	9	27	38	43	82	10	15	88	52	60	5
3	9	10	27	38	43	82	15	88	52	60	5
3	9	10	15	27	38	43	82	88	52	60	5
3	9	10	15	27	38	43	82	88	52	60	5
3	9	10	15	27	38	43	52	82	88	60	5
3	9	10	15	27	38	43	52	60	82	88	5
3	5	9	10	27	38	43	52	60	82	8	
3	5	9	10	15	27	38	43	52	60	82	88

Time complexity: worst case: $O(n^2)$
Average case: $O(n^2)$
Best case: $O(n)$

5) Given array of $[4, -2, 5, 3, 10, -5, 2, 8, -3, 6, 7, -4, 1, 9, -1, 0, -6, 8, 11, -9]$ integers sort the following elements using insertion sort using Brute Force Approach Strategy. Analyse complexity of algorithm

Sol) Insert: $-4 =$
[4]

Insert: $-2 = [-2, 4]$

Insert: $5 = [-2, 4, 5]$

Insert: $3 = [-2, 3, 4, 5]$

Insert: $10 = [-2, 3, 4, 5, 10]$

Insert: $-5 = [-5, -2, 3, 4, 5, 10]$

Insert: $2 = [-5, -2, 2, 3, 4, 5, 10]$

Insert: $8 = [-5, -2, 2, 3, 4, 5, 8, 10]$

Insert: $-3 = [-5, -3, -2, 2, 3, 4, 5, 8, 10]$

Insert: $6 = [-5, -3, -2, 2, 3, 4, 5, 6, 8, 10]$

Insert: $7 = [-5, -3, -2, 2, 3, 4, 5, 6, 7, 8, 10]$

Insert: $-4 = [-5, -4, -3, -2, 2, 3, 4, 5, 6, 7, 8, 10]$

Insert: $1 = [-5, -4, -3, -2, 1, 2, 3, 4, 5, 6, 7, 8, 10]$

Insert: $9 = [-5, -4, -3, -2, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]$

Insert: $-1 = [-5, -4, -3, -2, -1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]$

Insert: $0 = [-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]$

Insert: $-6 = [-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]$

Insert: $-8 = [-8, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]$

Insert: $11 = [-8, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]$

Insert: $-9 = [-9, -8, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11]$

Time complexity: Best: $O(n)$, Average: $O(n^2)$, worst: $O(n^2)$