- o (max & g, cn), g, cn) 3. prove that assertions.
- to prove the aggestion, we will derive an upper bond for ticn) + +2 cn) in terms of max 2 g, cn), g2 cn) }
 - * since +, (n) + o (g, (n), there exist c, and n, such that-

simionly, since telest to (92 lns), there exist ce and ne such that:

+2(n) < c2. 82(n) for all n > n2.

complue the portuge:

THOMBADACH

16+ uo=wax (u1, u5) . box on u> u0;

FILM = CI.g.(m) and trin) = cr.grin)

therefore, for all nano.

FILM) + +500) = C1.8100) + C5.85(0).

simplify the expression !

combine the terms on right-hand side:

E. (1) + +2 (1) < (ci+(2). max 28; (1), 82 (1) 3

concinde vid-o votations:

let c= c1+c2. We have show that.

+(cn) ++2(d) = c. max sgicul. gray for an u>no.

Big o-notation. Hence,

E, (n)+ +2(n) 60 (max 2 g, (n), 92 (n) 3).

- 2. Find the time complexity of the below rechtskence -
- A.) Identify the constants:

0=2 A=2 f(n)=1.

```
combite 108 pg
             108Pa=1085=1.
 * combase bill mith ungg.
           f(n)=1 and n'108 ba = n'=n.
 Apply the master's theorem:
 * P(n) = o(nc) where cx 109ba, then +in) = a (n'108ka).
 * F(U) = 0 (U108 pg) , then +(U)= 0 (U108 pg 108U).
 * fru) = vr (uc) where c>100 to and of (#) = Kbru) ton
 some KLI and sufficiently large n, then +(n) = o(n)
     : time complexity trul= o(U108Pc)
                               = 0(0,).
                                = a(u).
3. Show that Plu) = v2+In+E is o(v2). gi.
A) Identify the dominat term:
  * the dominat term in fin) is no since it grows
  paster than the terms a become large.
 * combane corcy tem to us:
    45 TUS
  3U = 3U5 ( for U >1)
    272Us ( ton u si).
  combaining these, we get
     n2+2n+5 < n2 + 3n2 + 5n2
     U5 + 3U + 2 5 dU5
  choose Appropriate constants:
  let c=9 and no=1. then fav all n > no
      bru) = Us + 3U+ A = dus.
```

```
| f(n) = c. n2
 it bollome that:
  E(U) = U_+ 3U+2 & O(U_).
 Thus, we have show that pun = n2 +2n+5 is oln2).
4) Prove that gen = n3+2n2+4n is 2 (n3).
4) * Identify the dominat term.
    the dominat term in gen) is n3, since it grows
  paster than the other terms as n become large.
  combine and compane terms:
    U_3 + 5U_5 + HU > U_3
  This is true because 20 +40 is always non-negative
  bon on uso.
                          of an and and
  * choose an appropriate constant:
   we can see that n2+2n2+4n > n2 for any n >0.
   Hence we can choose c=1 and no =0. There pave,
   ton on u>no:
             8(4) = 43 +542 + AU > 1.03.
   COUCITISION;
      gen) ≥ c.n3
     it bolloms that
        gen) = n2 + 2n2 + 4n + 12 (n3)
     :. 9(n) = n3 + 2n2 + HU is or (u3).
 I. Determine methor prul= Auz + IU is arus) on vot.
 4.) Those Boug (Bid o)
    * find cz and no:
```

HUS + 3U = HUS + 3US = JUS (for U = 1). so, we can choose cz=7 and no=1. Then, por all UF1: p(u) < 105 lomen comung (Bid owieda): * find c1 and no. $p(u) = \pi u_5 + 3u$ 700 + 30 = 400. so, we can choose cizy and no =1. Then, por all n =1: pro) = Huz +30 € orus). .. c1= H, c5= 4 and vo=1. manufact with the same p(u) = AU_+3U 18 B(U). and the same of the same

. c . pro of each week to the man to the other bands and and

ar and the the