

1. 141. Write a program that finds the convex hull of a set of 2D points using the brute force approach.

Input:

- A list or array of points represented by coordinates (x, y).

Points: [(1, 1), (4, 6), (8, 1), (0, 0), (3, 3)]

Code:

```
def is_left(a, b, c):
```

```
    return (b[0] - a[0]) * (c[1] - a[1]) - (b[1] - a[1]) * (c[0] - a[0]) > 0
```

```
def is_right_or_collinear(a, b, c):
```

```
    return (b[0] - a[0]) * (c[1] - a[1]) - (b[1] - a[1]) * (c[0] - a[0]) <= 0
```

```
def convex_hull_brute_force(points):
```

```
    hull = []
```

```
    n = len(points)
```

```
    for i in range(n):
```

```
        for j in range(i + 1, n):
```

```
            a, b = points[i], points[j]
```

```
            left_side = [is_left(a, b, points[k]) for k in range(n) if k != i and k != j]
```

```
            right_or_collinear = [is_right_or_collinear(a, b, points[k]) for k in range(n) if k != i and k != j]
```

```
            if all(left_side) or all(right_or_collinear):
```

```
                if a not in hull:
```

```
                    hull.append(a)
```

```
                if b not in hull:
```

```
                    hull.append(b)
```

```
    return hull
```

```
points = [(1, 1), (4, 6), (8, 1), (0, 0), (3, 3)]
```

```
convex_hull_points = convex_hull_brute_force(points)
```

```
print("Convex Hull Points:", convex_hull_points)
```

output:

```
PS C:\Users\karth>
PS C:\Users\karth> & C:/Users/karth/AppData/Local/Programs/Python/Python312/python.exe c:/Users/karth/OneDrive/Documents/OriginLab/problems.py
Convex Hull Points: [(4, 6), (8, 1), (0, 0)]
PS C:\Users\karth>
```

Time complexity: $f(n) = O(n \log n)$