# BACK TRACKING ALGORITHMS

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### 12.1. Rat in a Maze Problem

Statement: Consider a rat placed at **(0, 0)** in a square **matrix of order N\*N**. It has to reach the destination at **(n-1, n-1)**. Find all possible paths that the rat can take to reach from source to destination. The directions in which the rat can move are 'U'(up), 'D'(down), 'L' (left), 'R' (right).

```
class GfG{
  static boolean isSafe(int x,int y,int m[][],boolean vis[][],int n){
     if(x=-1 || y=-1 || x==n || y==n || vis[x][y] || m[x][y]==0)
       return false;
     return true;
  static void utilFun(int m[][],int n,int x,int y,ArrayList<String> res,String path,boolean
vis[][]){
     if(x==n-1 \&\& y==n-1){
       res.add(path);
       return;
     vis[x][y] = true;
     //down
     if(isSafe(x+1,y,m,vis,n)){
       path += 'D';
       utilFun(m,n,x+1,y,res,path,vis);
       path = path.substring(0,path.length()-1);
     }
     //left
     if(isSafe(x,y-1,m,vis,n)){
       path += 'L';
       utilFun(m,n,x,y-1,res,path,vis);
       path = path.substring(0,path.length()-1);
     }
     //right
     if(isSafe(x,y+1,m,vis,n)){
       path += 'R';
       utilFun(m,n,x,y+1,res,path,vis);
       path = path.substring(0,path.length()-1);
     //upper
     if(isSafe(x-1,y,m,vis,n)){
       path += 'U';
```

```
utilFun(m,n,x-1,y,res,path,vis);
    path = path.substring(0,path.length()-1);
}

vis[x][y] = false;
}
public static ArrayList<String> printPath(int[][] m, int n)
{
    ArrayList<String> res = new ArrayList<>();
    boolean vis[][] = new boolean[n][n];
    for(int i=0;i<n;i++){
        for(int j=0;j<n;j++){
        vis[i][j] = false;
        }
    }
    String path="";
    utilFun(m,n,0,0,res,path,vis);
    return res;
}</pre>
```

# 12.2. Word Boggle

Statement: Given a dictionary, a method to do lookup in dictionary and a M x N board where every cell has one character. Find all possible words that can be formed by a sequence of adjacent characters. Note that we can move to any of 8 adjacent characters, but a word should not have multiple instances of same cell.

### Example:

```
private static void findWord(char boggle[][],boolean visited[][],HashSet<String>
dic, HashSet < String > ans, int i, int j, String str){
     visited[i][j] = true;
     str += boggle[i][j];
     if(dic.contains(str)){
        ans.add(str);
     }
     //traverse all surrounded character
     for(int row=i-1;row=i+1 && row<n;row++){
        for(int col=j-1;col<=j+1 && col<m;col++){
          if(row>=0 && col>=0 && !visited[row][col]){
             findWord(boggle, visited, dic, ans, row, col, str);
          }
        }
     str = "" + str.charAt(str.length()-1);
     visited[i][j] = false;
  }
  public static void main (String[] args) {
             Scanner sc = new Scanner(System.in);
             int test = sc.nextInt();
             for(int t=0;t<test;t++){
               int len = sc.nextInt();
               HashSet<String> dic = new HashSet<>();
               for(int i=0;i<len;i++){</pre>
                  dic.add(sc.next());
               n = sc.nextInt();
               m = sc.nextInt();
               char boggle[][] = new char[n][m];
               for(int i=0;i< n;i++){
                  for(int j=0;j< m;j++){
```

```
boggle[i][j] = sc.next().charAt(0);
                  }
                }
                //processing
                HashSet<String> ans = new HashSet<>();
                boolean visited[][] = new boolean[n][m];
                String str = "";
                for(int i=0;i< n;i++){
                  for(int j=0;j< m;j++){
                     findWord(boggle, visited, dic, ans, i, j, str);
                  }
                if(ans.size()==0){
                  System.out.println(-1);
                }else{
                  Iterator iter = ans.iterator();
                  while(iter.hasNext()){
                     System.out.print(iter.next()+"");
                  }
                }
                System.out.println();
      }
}
```

# 12.3. Generate IP Addresses

Statement: Given a string S containing only digits, Your task is to complete the function **genIp()** which returns a vector containing all possible combination of valid IPv4 ip address and takes only a string S as its only argument.

A valid IP address must be in the form of A.B.C.D, where A, B, C, and D are numbers from 0-255. The numbers cannot be 0 prefixed unless they are 0

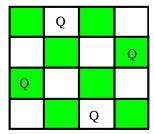
Note: Order doesn't matter.

```
For string 11211 the ip address possible are
1.1.2.11
1.1.21.1
1.12.1.1
11.2.1.1
  private boolean isValid(String str){
      String a[] = str.split("[.]");
      for(String s:a){
             int i = Integer.parseInt(s);
             if(s.length()>3 || i<0 || i>255)
                    return false;
             if(s.length()>1 && i==0)
                    return false;
             if(s.length()>1 && i!=0 && s.charAt(0)=='0')
                    return false;
       }
      return true;
  }
  public ArrayList<String> genIp(String s) {
      ArrayList<String> list = new ArrayList<>();
      if(s.length()<0 \parallel s.length()>12)
             return list;
      else{
             int size = s.length();
             String snew = s;
             for(int i=1;i<size-2;i++){ //for placing first dot
                    for(int j=i+1;j<size-1;j++){ //for placing second dot
                          for(int k=j+1; k < size; k++){ //for placing third dot
                                 snew = snew.substring(0,k)+"."+snew.substring(k);
                                 snew = snew.substring(0,j)+"."+snew.substring(j);
                                 snew = snew.substring(0,i)+"."+snew.substring(i);
                                 if(isValid(snew)){
```

```
list.add(snew);
}
snew = s;
}
}
return list;
}
```

# 12.4. N-Queen Problem

Statement: The n-queens puzzle is the problem of placing n queens on an nxn chessboard such that no two queens attack each other. Given an integer n, print all distinct solutions to the n-queens puzzle. Each solution contains distinct board configurations of the n-queens' placement, where the solutions are a permutation of [1,2,3..n] in increasing order, here the number in the *ith* place denotes that the *ith*-column queen is placed in the row with that number. For eg below figure represents a chessboard [3 1 4 2].



```
class GFG {
    static class Flag{
        int data;
        Flag(int data){
            this.data = data;
        }
    }
    static boolean isSafe(int n,int row,int col,boolean vis[][]){
        //for same row
        for(int i=col-1;i>=0;i--){
            if(vis[row][i])
```

```
return false;
  }
  //upper diagnol
  for(int i=row-1,j=col-1;i>=0 && j>=0;i--,j--){
     if(vis[i][j])
       return false;
  //lower diagnol
  for(int i=row+1,j=col-1;i<n && j>=0;i++,j--){
     if(vis[i][j])
        return false;
  }
  return true;
static void nQueen(Flag flag,int n,int col,boolean vis[][],int arr[]){
  if(col==n){
     flag.data = 1;
     System.out.print("[");
     for(int i=0;i<n;i++){
        System.out.print(arr[i]+" ");
     System.out.print("]"+" ");
     return;
  for(int i=0;i< n;i++)
     if(isSafe(n,i,col,vis)){
        arr[col] = i+1;
        vis[i][col] = true;
       nQueen(flag,n,col+1,vis,arr);
       vis[i][col] = false;
     }
  if(col = 0 \&\& flag.data = = 0){
     System.out.print(-1);
  }
}
    public static void main (String[] args) {
           Scanner sc = new Scanner(System.in);
           int test = sc.nextInt();
           for(int t=0;t< test;t++){
             int n = sc.nextInt();
             boolean vis[][] = new boolean[n][n];
```

```
int arr[] = new int[n];
Flag flag = new Flag(0);
nQueen(flag,n,0,vis,arr);
System.out.println();
}
}
}
```

### 12.5. Solve the Sudoku

Statement: Given an incomplete Sudoku configuration in terms of a 9 x 9  $\,$  2-D square matrix (mat[][]). The task to print a solved Sudoku. For simplicity you may assume that there will be only one unique solution.

### Sample Sudoku:

| 3 |   | 6 | 5 |   | 8 | 4 |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 2 |   |   |   |   |   |   |   |
|   | 8 | 7 |   |   |   |   | 3 | 1 |
|   |   | 3 |   | 1 |   |   | 8 |   |
| 9 |   |   | 8 | 6 | 3 |   |   | 5 |
|   | 5 |   |   | 9 |   | 6 |   |   |
| 1 | 3 |   |   |   |   | 2 | 5 |   |
|   |   |   |   |   |   |   | 7 | 4 |
|   |   | 5 | 2 |   | 6 | 3 |   |   |

```
class GFG {
  static boolean isSafe(int row,int col,int no,int arr[][]){
     //same row
     for(int i=0; i<9; i++){
       if(arr[row][i]==no)
          return false;
     //same column
     for(int i=0; i<9; i++){
       if(arr[i][col]==no)
          return false;
     //same cube
     int startRow = row - (row \% 3);
     int startCol = col - (col \% 3);
     for(int i=startRow;i<startRow+3;i++){
       for(int j=startCol;j<startCol+3;j++){
          if(arr[i][i]==no)
```

```
return false;
  return true;
static boolean solveSudoku(int arr[][]){
  int row = -1;
  int col = -1;
  boolean isEmpty = true;
  for(int i=0; i<9; i++){
     for(int j=0; j<9; j++){
       if(arr[i][j]==0){
          row = i;
          col = j;
          isEmpty = false;
          break;
     if(!isEmpty){
       break;
  if(isEmpty){
     return true;
  //try for 1 to 9 no.
  for(int no=1;no<=9;no++){
     if(isSafe(row,col,no,arr)){
       arr[row][col] = no;
       if(solveSudoku(arr))
          return true;
       arr[row][col] = 0;
  return false;
static void print(int arr[][]){
  for(int i=0;i<arr.length;i++){
     for(int j=0;j<arr.length;j++)
       System.out.print(arr[i][j]+" ");
}
```