

Recursion: Python

Stack Overflow Error in Recursive Function

A recursive function that is called with an input that requires too many iterations will cause the call stack to get too large, resulting in a stack overflow error. In these cases, it is more appropriate to use an iterative solution. A recursive solution is only suited for a problem that does not exceed a certain number of recursive calls.

For example, myfunction() below throws a stack overflow error when an input of 1000 is used.

Fibonacci Sequence

A Fibonacci sequence is a mathematical series of numbers such that each number is the sum of the two preceding numbers, starting from 0 and 1.

Call Stack Construction in While Loop

A call stack with execution contexts can be constructed using a while loop, a list to represent the call stack and a dictionary to represent the execution contexts. This is useful to mimic the role of a call stack inside a recursive function.

Binary Search Tree

In Python, a binary search tree is a recursive data structure that makes sorted lists easier to search. Binary search trees:

- Reference two children at most per tree node.
- The "left" child of the tree must contain a value lesser than its parent.
- The "right" child of the tree must contain a value greater than it's parent.

```
def myfunction(n):
    if n == 0:
        return n
    else:
        return myfunction(n-1)

myfunction(1000) #results in stack
overflow error
```

```
Fibonacci sequence: 0, 1, 1, 2, 3, 5, 8, 13, 21, ...
```

```
5

/ \

/ \

3 8

/ \ / \

2 4 7 9
```

Recursion and Nested Lists

A nested list can be traversed and flattened using a recursive function. The base case evaluates an element in the list. If it is not another list, the single element is appended to a flat list. The recursive step calls the recursive function with the nested list element as input.

Fibonacci Recursion

Computing the value of a Fibonacci number can be implemented using recursion. Given an input of index N, the recursive function has two base cases – when the index is zero or 1. The recursive function returns the sum of the index minus 1 and the index minus 2.

The Big-O runtime of the Fibonacci function is O(2^N).

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```
def flatten(mylist):
    flatlist = []
    for element in mylist:
        if type(element) == list:
            flatlist += flatten(element)
        else:
            flatlist += element
        return flatlist

print(flatten(['a', ['b', ['c', ['d']], 'e'], 'f']))
# returns ['a', 'b', 'c', 'd', 'e', 'f']
```

```
def fibonacci(n):
   if n <= 1:
     return n
   else:
     return fibonacci(n-1) + fibonacci(n-2)</pre>
```

Modeling Recursion as Call Stack

One can model recursion as a call stack with execution contexts using a while loop and a Python list. When the base case is reached, print out the call stack list in a LIFO (last in first out) manner until the call stack is empty.

Using another while loop, iterate through the call stack list. Pop the last item off the list and add it to a variable to store the accumulative result.

Print the result.

Recursion in Python

In Python, a recursive function accepts an argument and includes a condition to check whether it matches the base case. A recursive function has:

- Base Case a condition that evaluates the current input to stop the recursion from continuing.
- Recursive Step one or more calls to the recursive function to bring the input closer to the base case.

```
def countdown(value):
  call stack = []
 while value > 0 :
    call_stack.append({"input":value})
    print("Call Stack:",call_stack)
    value -= 1
  print("Base Case Reached")
 while len(call_stack) != 0:
    print("Popping {} from call
stack".format(call_stack.pop()))
    print("Call Stack:",call_stack)
countdown(4)
1.1.1
Call Stack: [{'input': 4}]
Call Stack: [{'input': 4}, {'input': 3}]
Call Stack: [{'input': 4}, {'input': 3},
{'input': 2}]
Call Stack: [{'input': 4}, {'input': 3},
{'input': 2}, {'input': 1}]
Base Case Reached
Popping {'input': 1} from call stack
Call Stack: [{'input': 4}, {'input': 3},
{'input': 2}]
Popping {'input': 2} from call stack
Call Stack: [{'input': 4}, {'input': 3}]
Popping {'input': 3} from call stack
Call Stack: [{'input': 4}]
Popping {'input': 4} from call stack
Call Stack: []
1.1.1
```

```
def countdown(value):
   if value <= 0:  #base case
     print("done")
   else:
     print(value)
     countdown(value-1)  #recursive case</pre>
```

Build a Binary Search Tree

To build a binary search tree as a recursive algorithm do the following:

BASE CASE:

If the list is empty, return "No Child" to show that there is no node.

RECURSIVE STEP:

- Find the middle index of the list.
- 2. Create a tree node with the value of the middle index.
- 3. Assign the tree node's left child to a recursive call with the left half of list as input.
- 4. Assign the tree node's right child to a recursive call with the right half of list as input.
- 5. Return the tree node.

Recursive Depth of Binary Search Tree

A binary search tree is a data structure that builds a sorted input list into two subtrees. The left child of the subtree contains a value that is less than the root of the tree. The right child of the subtree contains a value that is greater than the root of the tree.

A recursive function can be written to determine the depth of this tree.

Sum Digits with Recursion

Summing the digits of a number can be done recursively. For example:

```
552 = 5 + 5 + 2 = 12
```

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```
def build_bst(my_list):
  if len(my list) == 0:
    return "No Child"
  middle_index = len(my_list) // 2
  middle_value = my_list[middle_index]
  print("Middle index:
{0}".format(middle index))
  print("Middle value:
{0}".format(middle value))
 tree_node = {"data": middle_value}
 tree_node["left_child"] =
build_bst(my_list[ : middle_index])
 tree_node["right_child"] =
build_bst(my_list[middle_index + 1 : ])
  return tree_node
sorted_list = [12, 13, 14, 15, 16]
binary_search_tree =
build_bst(sorted_list)
print(binary_search_tree)
```

```
def depth(tree):
    if not tree:
        return 0
    left_depth = depth(tree["left_child"])
    right_depth = depth(tree["right_child"])
    return max(left_depth, right_depth) + 1
```

```
def sum_digits(n):
    if n <= 9:
        return n
    last_digit = n % 10
    return sum_digits(n // 10) + last_digit
sum_digits(552) #returns 12</pre>
```

Palindrome in Recursion

A palindrome is a word that can be read the same both ways - forward and backward. For example, abba is a palindrome and abc is not.

The solution to determine if a word is a palindrome can be implemented as a recursive function.

Fibonacci Iterative Function

A Fibonacci sequence is made up adding two previous numbers beginning with 0 and 1. For example:

```
0, 1, 1, 2, 3, 5, 8, 13, ...
```

A function to compute the value of an index in the Fibonacci sequence, fibonacci(index) can be written as an iterative function.

Recursive Multiplication

The multiplication of two numbers can be solved recursively as follows:

Base case: Check for any number that is equal to zero. Recursive step: Return the first number plus a recursive call of the first number and the second number minus one.

Iterative Function for Factorials

To compute the factorial of a number, multiply all the numbers sequentially from 1 to the number.

An example of an iterative function to compute a factorial

is given below.

```
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```

```
def is_palindrome(str):
   if len(str) < 2:
     return True
   if str[0] != str[-1]:
     return False
   return is_palindrome(str[1:-1])</pre>
```

```
def fibonacci(n):
    if n < 0:
        raise ValueError("Input 0 or greater
only!")
    fiblist = [0, 1]
    for i in range(2,n+1):
        fiblist.append(fiblist[i-1] +
fiblist[i-2])
    return fiblist[n]</pre>
```

```
def multiplication(num1, num2):
   if num1 == 0 or num2 == 0:
     return 0
   return num1 + multiplication(num1, num2
- 1)
```

```
def factorial(n):
    answer = 1
    while n != 0:
        answer *= n
        n -= 1
    return answer
```

Recursively Find Minimum in List

We can use recursion to find the element with the minimum value in a list, as shown in the code below.



```
def find_min(my_list):
    if len(my_list) == 0:
        return None
    if len(my_list) == 1:
        return my_list[0]
    #compare the first 2 elements
    temp = my_list[0] if my_list[0] <
my_list[1] else my_list[1]
    my_list[1] = temp
    return find_min(my_list[1:])

print(find_min([]) == None)
print(find_min([42, 17, 2, -1, 67]) == -1)</pre>
```

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