



SAPIENZA
UNIVERSITÀ DI ROMA

COURSE TITLE: ADDITIVE MANUFACTURING AND PRODUCTION SYSTEMS

GUIDED BY – Prof. ALBERTO BOSCHETTO

EXERCISE 3

PART_A FLEXIBLE MANUFACTURING SYSTEMS

GROUP NAME: VALLURI

GROUP NUMBER: 10

VARUN YASHWANT RASALKAR 1921452



PART_A FLEXIBLE MANUFACTURING SYSTEMS

Demand pcs/month	Machine												
		SLM 280	Stratasys J750	Stratasys F170	DWS XPRO S	Wire Electro Discharge Machine	Manual removal job shop	Chemical bath	Ultrasonic Washer	UV oven	Sand Blasting machine	Powder coating system	Spray Coating job shop
	Machine cost	450 k€	375 k€	28 k€	95 k€	55 k€	5 k€	8 k€	12 k€	8 k€	9 k€	15 k€	4.5 k€
40	A 	21h				2.5h					15'		
29	B 				27h			1.5h		1.5h			1h
49	C 		23h				2h						
34	D 			15h			1h					0.5h	
31	E 				23h				1h	1h			
23	F 	16h				1.5h	2.5h						
33	G 		21h					4h			30'	1h	

For simplicity we convert the machine names into number in the same sequence as they appear in the table.

Steps involved,

- Dividing the products into manufacturing cells by applying KING'S algorithm.
- Add duplicate machines if necessary.
- Apply HOLLIER method to find the sequence of machines in the manufacturing cell.
- Apply Bottleneck methods to find Production Rate of Manufacturing cell, percentage Utilization of machines and Production rate of each product in the manufacturing cell.
- Apply Extended Bottleneck method to find critical number of products, mean lead time and waiting time in each manufacturing cell based on two different cases where $N < N^*$ and $N \geq N^*$.

Step 1. Apply KING'S algorithm. P and M signifies products and machines.

P/M	1	2	3	4	5	6	7	8	9	10	11	12
A	1				1					1		
B				1			1		1			1
C		1				1						
D			1			1					1	
E				1				1	1			
F	1				1	1						
G		1					1			1	1	

Taking transpose of this table and apply the row and column sorting.

M/P	A	B	C	D	E	F	G
1	1					1	
2			1				1
3				1			
4		1			1		
5	1					1	
6			1	1		1	
7		1					1
8					1		
9		1			1		
10	1						1
11				1			1
12		1					

M/P	A	B	C	D	E	F	G	Row Sorting
1	1					1		66
2			1				1	17
3				1				8
4		1			1			36
5	1					1		66
6			1	1		1		26
7		1					1	33
8					1			4
9		1			1			36
10	1						1	65
11				1			1	9
12		1						32
	2^6	2^5	2^4	2^3	2^2	2^1	2^0	
	64	32	16	8	4	2	1	

M/P	A	B	C	D	E	F	G	Row Sorting
1	1					1		66

5	1					1		66
10	1						1	65
4		1			1			36
9		1			1			36
7		1					1	33
12		1						32
6			1	1		1		26
2			1				1	17
11				1			1	9
3				1				8
8					1			4

M/P			A	B	C	D	E	F	G
1	2^11	2048	1					1	
5	2^10	1024	1					1	
10	2^9	512	1						1
4	2^8	256		1			1		
9	2^7	128		1			1		
7	2^6	64		1					1
12	2^5	32		1					
6	2^4	16			1	1		1	
2	2^3	8			1				1
11	2^2	4				1			1
3	2^1	2				1			
8	2^0	1					1		
COLOM SORTING			3584	480	24	22	385	3088	588

M/P	A	F	G	B	E	C	D
1	1	1					
5	1	1					
10	1		1				
4				1	1		
9				1	1		
7			1	1			
12				1			
6		1				1	1
2			1			1	
11			1				1
3							1
8					1		

M/P	A	F	G	B	E	C	D
-----	---	---	---	---	---	---	---

1	1	1							
5	1	1							
10*	1								
6*		1							
10			1						
2*			1						
11*			1						
4				1	1				
9				1	1				
7			1	1					
12				1					
8					1				
6						1	1		
2						1			
11							1		
3							1		

product	A	B	C	D	E	F	G
demand	40	29	49	34	31	23	33

Step 2 Apply HOLLIER method in each Manufacturing cell.

MANUFACTURIN CELL_1

M/P	A	F
1	1	1
5	1	1
10*	1	
6*		1

P(A)	0.634921	PART
P(F)	0.365079	MIX

product	A	F	SUM
demand	40	23	63

PART_A	OPERATIONS	L/U	1	5	10	L/U
PART_F	OPERATIONS	L/U	1	5	6	L/U

FROM	TO				
	A	1	5	10	6
	1		40		
	5			40	
	10				
	6				

FROM	TO				
	F	1	5	10	6
	1		23		
	5			23	
	10				
	6				

FROM	TO					FROM	FROM/TO
	SUM	1	5	10	6	63	infinity
	1		63			63	1
	5			40	23	0	0
	10					0	0
	6					0	0
	TO	0	63	40	23	126	
CELL_1	Option a	1	5	10	6		
	Option b	1	5	6	10		

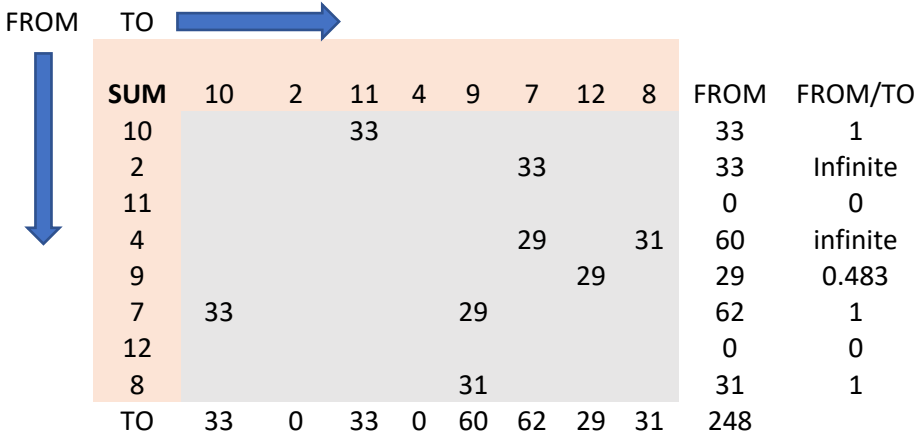
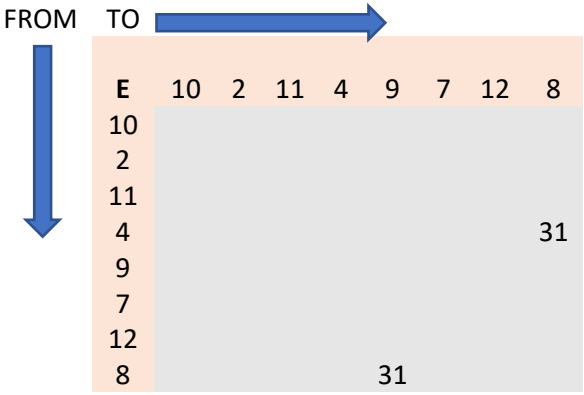
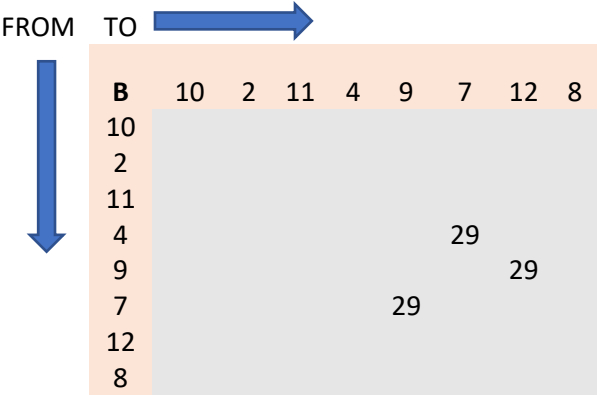
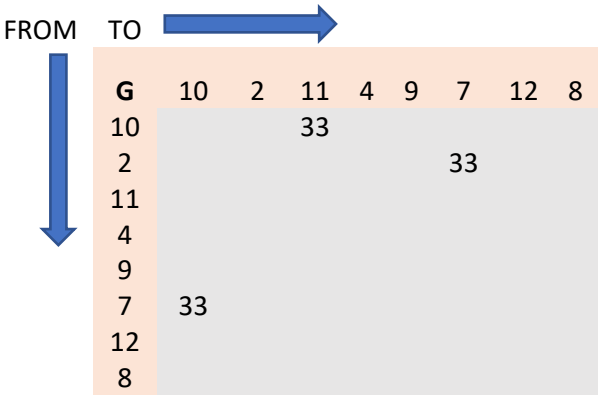
MANUFACTURING CELL_2

M/P	G	B	E
10	1		
2*	1		
11*	1		
4		1	1
9		1	1
7	1	1	
12		1	
8			1

product	demand
G	33
B	29
E	31
SUM	93

P(G)	0.35484	PART MIX
P(B)	0.31183	
P(E)	0.33333	

PART_G	OPERATIONS	L/U	2	7	10	11	L/U
PART_B	OPERATIONS	L/U	4	7	9	12	L/U
PART_E	OPERATIONS	L/U	4	8	9	L/U	



CELL_2	Option a	2	4	10	7	8	9	11	12
	Option b	4	2	7	8	10	9	12	11

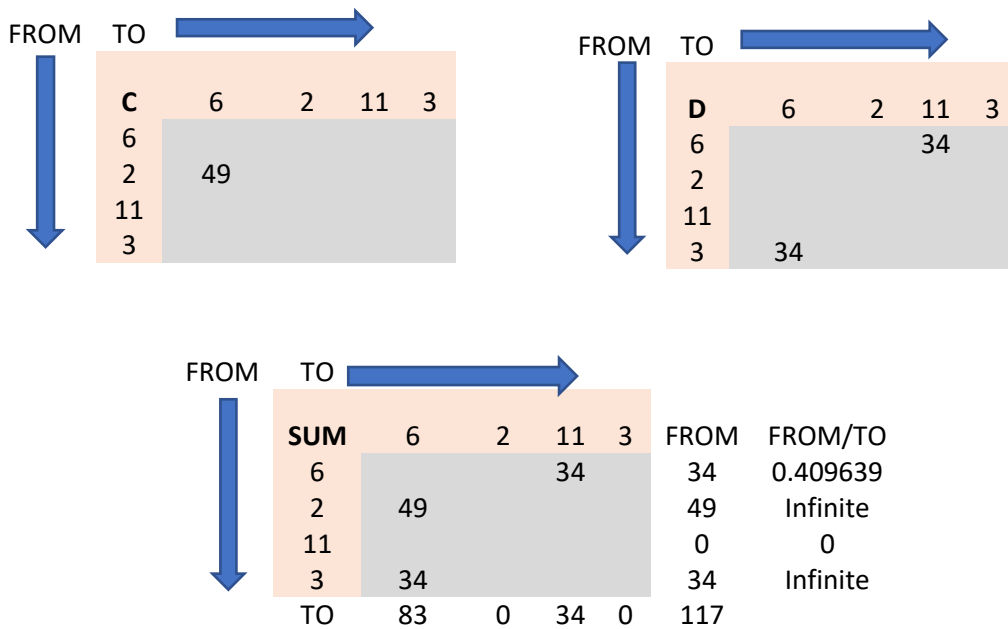
MANUFACTURING CELL_3

M/P	C	D
6	1	1
2	1	
11		1
3		1

product	demand
C	49
D	34
SUM	83

P(C)	0.590361	PART MIX
P(D)	0.409639	

PART_C	OPERATIONS	L/U	2	6	L/U	
PART_D	OPERATIONS	L/U	3	6	11	L/U



Step 3 Applying Bottleneck methods and taking some assumptions.

Certain values such as loading time and unloading time are not given so, it is approximated and assumed to be 4 mins and 2 mins respectively. The material handling time (T_r) is given to be 2 mins. The number of servers is 1 and so the frequency of operation becomes 1. **fijk = 1.0**

Workload of a station

$$WL_i = \sum_j \sum_k T_{cij} f_{ijk} p_j$$

Workload of the handling system

$$WL_{n+1} = n_t T_r \quad n_t = \sum_i \sum_j \sum_k f_{ijk} p_j - 1$$

Extended bottleneck method:

N	<	N*	→	case 1
N	>=	N*	→	case 2

$$MLT_1 = \sum_{i=1}^n WL_i + WL_{n+1} \quad N^* = R_p^* \left(\sum_{i=1}^n WL_i + WL_{n+1} \right)$$

Case 1 → $T_w = 0$

$$R_p = \frac{N}{MLT_1}$$

$$R_{pj} = p_j R_p$$

Case 2 → $R_{pj}^* = p_j R_p^*$

$$MLT_2 = \frac{N}{R_p^*}$$

$$T_w = MLT_2 - \left(\sum_{i=1}^n WL_i + WL_{n+1} \right)$$

T_w = waiting time & MLT = mean lead time

MANUFACTURING CELL_1

Bottleneck Method

PART	MIX P(j)	OPERATION (k)	DESCRIPTION	STATION (i)	SERVER	TIME tijk (min)
A	0.634921	1	L/U	1	1	4
		2	1	2	1	1260
		3	5	3	1	150
		4	10	4	1	15
		5	L/U	1	1	2
F	0.365079	1	L/U	1	1	4
		2	1	2	1	960
		3	5	3	1	90
		4	6	5	1	150
		5	L/U	1	1	2

Workload (min)	WL_(L/U)	6
	WL_1	1150.47619
	WL_5	128.0952381
	WL_10	9.523809524
	WL_6	54.76190476
	WL_(n+1)	8

Bottleneck is maximum of all Workloads

Bottleneck is WL_1 which means machine SLM 280

Production Rate at Bottleneck Station		
Rp	0.000869205	pc/min
Rp	0.052152318	pc/hr

production rate A	Rp*P(j)_A	0.033112583	pc/hr
production rate F	Rp*P(j)_F	0.019039735	pc/hr

in %				
Utilization	U_(L/U)	=	WL_(L/U)*Rp	0.005215232 0.521523
	U_1	=	WL_1*Rp	1 100
	U_5	=	WL_5*Rp	0.11134106 11.13411
	U_10	=	WL_10*Rp	0.008278146 0.827815
	U_6	=	WL_6*Rp	0.047599338 4.759934
	U_(n+1)	=	WL_(n+1)*Rp	0.006953642 0.695364

Extended Bottleneck Method

$$MLT_1 = \sum_{i=1}^n WL_i + WL_{n+1} \quad N^* = R_p^* \left(\sum_{i=1}^n WL_i + WL_{n+1} \right)$$

$$\begin{aligned} MLT_1 &= 1356.857143 \text{ min} \\ N^* &= 1.179387417 \end{aligned}$$

N	MLT_1 (min)	Rp (pc/min)	MLT_2 (min)	Tw (min)
1	1356.857143	0.000736997		0
2		0.000869205	2300.952381	944.0952
3		0.000869205	3451.428571	2094.571

Bottleneck Method

PART	MIX P(j)	OPERATION	DESCRIPTION	STATION	SERVER	TIME tijk (min)
G	0.354839	1	L/U	1	1	4
		2	2	2	1	1260
		3	7	3	1	240
		4	10	4	1	30
		5	11	5	1	60
		6	L/U	1	1	2
B	0.311828	1	L/U	1	1	4
		2	4	2	1	1620
		3	7	3	1	90
		4	9	4	1	90
		5	12	5	1	60
		6	L/U	1	1	2
E	0.333333	1	L/U	1	1	4
		2	4	2	1	1380
		3	8	3	1	60
		4	9	4	1	60
		5	L/U	1	1	2

Workload (min)	WL_(L/U)	6
	WL_2	447.0967742
	WL_4	965.1612903
	WL_7	113.2258065
	WL_10	10.64516129
	WL_11	21.29032258
	WL_9	48.06451613
	WL_12	18.70967742
	WL_8	20
	WL_(n+1)	9.333333333

Bottleneck is maximum of all Workloads

Bottleneck is WL_4 which means machine DWS XPRO S

Production Rate at Bottleneck Station

R_p 0.001036096 pc/min
R_p 0.062165775 pc/hr

production rate G	$Rp * Pj_G$	0.022058824	pc/hr
production rate B	$Rp * Pj_B$	0.019385027	pc/hr
production rate E	$Rp * Pj_E$	0.020721925	pc/hr

in %					
Utilization	U_(L/U)	=	WL_(L/U)*Rp	0.006217	0.621657754
	U_2	=	WL_2*Rp	0.463235	46.32352941
	U_4	=	WL_4*Rp	1	100
	U_7	=	WL_7*Rp	0.117313	11.73128342
	U_10	=	WL_10*Rp	0.011029	1.102941176
	U_11	=	WL_11*Rp	0.022059	2.205882353
	U_9	=	WL_9*Rp	0.049799	4.979946524
	U_12	=	WL_12*Rp	0.019385	1.938502674
	U_8	=	WL_8*Rp	0.020722	2.072192513
	U_(n+1)	=	WL_(n+1)*Rp	0.00967	0.967023173

Extended Bottleneck Method

MLT_1 1659.52688
N* 1.71942959

N	MLT_1 (min)	Rp (pc/min)	MLT_2 (min)	Tw (min)
1	1659.52688	0.000602581		0
2		0.001036096	1930.322581	270.7957
3		0.001036096	2895.483871	1235.957

MANUFACTURIN CELL_3

Bottleneck Method

PART	MIX P(j)	OPERATION	DESCRIPTION	STATION	SERVER	TIME tijd (min)
C	0.590361	1	L/U	1	1	4
		2	2	2	1	1380
		3	6	3	1	120
		4	L/U	1	1	2
D	0.409639	1	L/U	1	1	4
		2	3	4	1	900
		3	6	3	1	60
		4	11	5	1	30
		5	L/U	1	1	2

Workload (min)	WL_(L/U)	6
	WL_2	814.6987952
	WL_6	95.42168675
	WL_11	12.28915663
	WL_3	368.6746988
	WL_(n+1)	6.819277108

Bottleneck is maximum of all Workloads

Bottleneck is WL_2 which means machine Manual Removal job shop

Production rate at bottleneck station

Rp 0.001227448 pc/min
Rp 0.07364685 pc/hr

production rate C	Rp*P(j)_C	0.043478261	pc/hr
production rate D	Rp*P(j)_D	0.030168589	pc/hr

in %				
Utilization	U_(L/U)	=	WL_(L/U)*Rp	0.007365 0.7364685
	U_2	=	WL_2*Rp	1 100
	U_6	=	WL_6*Rp	0.117125 11.71251109
	U_11	=	WL_1*Rp	0.015084 1.508429459
	U_3	=	WL_3*Rp	0.452529 45.25288376
	U_(n+1)	=	WL_(n+1)*Rp	0.00837 0.837030464

Extended Bottleneck Method

MLT_1 1303.903614
N* 1.600473233

N	MLT_1 (min)	Rp (pc/min)	MLT_2 (min)	Tw (min)
1	1303.903614	0.000766928		0
2		0.001227448	1629.39759	325.494
3		0.001227448	2444.096386	1140.193