

ASSIGNMENT - CONTEXT FREE GRAMMARS

1. Construct the derivation tree whose yield is aabbaa.
 $S \rightarrow aAS \mid a,$
 $A \rightarrow SbA \mid SS \mid ba$
2. $S \rightarrow 0B \mid 1A,$
 $A \rightarrow 0 \mid 0S \mid 1AA,$
 $B \rightarrow 1 \mid 1S \mid 0BB$
For string 00110101 find
 - left most derivation
 - right most derivation
 - derivation tree
3. Find the grammar for the following languages
 - i $L = (aaa^* + b)$
 - ii $L = \{a^n b^n : n \geq 1\}$
 - iii $L = \{a^n b^{n+1} : n \geq 2\}$
 - iv $L = ww^r : w \in \{a, b\}^*$
 - v $L = \{a^n b^m : n \leq m + 3\}$
 - vi $L = \{a^n b^m : 2n \leq m \leq 3n\}$
 - vii $L = \{a^n b^m c^k : k = |n - m|\}$
4. Show that the following grammar is ambiguous
 $S \rightarrow aSbS \mid bSaS \mid \epsilon$
5. Show that the following grammar is ambiguous
 $S \rightarrow AB \mid aaB,$
 $A \rightarrow a \mid Aa,$
 $B \rightarrow b$
6. Can the grammar for regular languages cannot be ambiguous or inherently ambiguous?

7. $E \rightarrow E + E,$

$E \rightarrow E * E,$

$E \rightarrow \text{id}$

For input: $2+3*4$ find

- left most derivation
- right most derivation
- derivation tree

8. Reduce or Remove useless productions from the following grammar

i $S \rightarrow AB,$

$A \rightarrow a,$

$B \rightarrow b,$

$B \rightarrow C,$

$E \rightarrow c$

ii $S \rightarrow AB \mid CA,$

$B \rightarrow BC \mid AB,$

$A \rightarrow a,$

$C \rightarrow aB \mid b$

iii $S \rightarrow aAa,$

$A \rightarrow Sb \mid bCC \mid DaA,$

$C \rightarrow abb \mid DD,$

$E \rightarrow aC,$

$D \rightarrow aDA$

9. Eliminate ϵ -productions, Eliminate any unit productions in the resulting grammar, Eliminate any useless symbols in the resulting grammar. Put the resulting grammar into Chomsky Normal Form

i $S \rightarrow ASB \mid \epsilon,$

$A \rightarrow aAS \mid a,$

$B \rightarrow bb \mid A \mid SbS$

⁰Don't consider comma , or full-stop . as the part of any input or terminal symbols

$$\text{ii } S \rightarrow 0A0 \mid 1B1 \mid BB,$$

$$A \rightarrow C,$$

$$B \rightarrow S \mid A,$$

$$C \rightarrow S \mid \epsilon$$

$$\text{iii } S \rightarrow AAA \mid B,$$

$$A \rightarrow aA \mid B,$$

$$B \rightarrow \epsilon$$

$$\text{iv } S \rightarrow aAa \mid bBb \mid \epsilon,$$

$$A \rightarrow C \mid a,$$

$$B \rightarrow C \mid b,$$

$$C \rightarrow CDE \mid \epsilon,$$

$$D \rightarrow B \mid A \mid ab$$

10. Convert the following grammar into Greibach Normal form

$$\text{i } S \rightarrow aSb \mid bSa \mid a \mid b$$

$$\text{ii } S \rightarrow aSb \mid ab$$

$$\text{iii } S \rightarrow ab \mid aS \mid aaS$$

$$\text{iv } S \rightarrow ABb \mid a,$$

$$A \rightarrow aaA \mid B,$$

$$B \rightarrow bAb$$