

THERMODYNAMICS

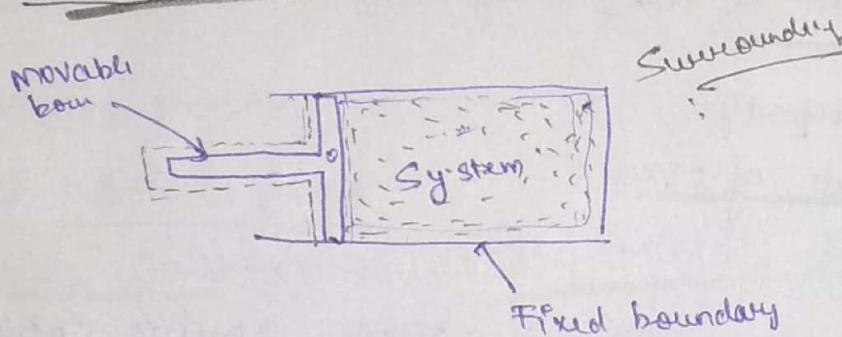
- Thermodynamics is the branch of science which deals with energy and its interaction with system and surrounding.

Energy → Ability to cause changes

System → It is a fixed mass or fixed region in space where study is focused

Surrounding → Everything the except System

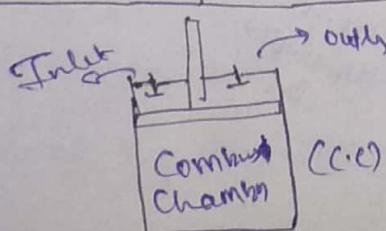
The part of the which is affected by the System is called Immediate Surrounding



Boundary → A Imaginary or Real Surface that's separates System from Surrounding

Boundary can be fixed or movable.

System	Mass	Energy	Example
1) closed System	x	✓	Piston cylinder arrangement without walls
2) Open System	✓	✓	P.C. A with valve
3) Isolated System	x	x	Universe



① Microscopic approach

In which we deals with property each and every molecule and concentration & consider of molecule

② Macroscopic approach.

We focused on system property. Instead, of particles, molecule behavior

Properties

Any characteristics which gives the information of about the system

1) Intensive property

Independent of mass eg → viscosity, Thermal con

2) Extensive property

Dependent of Mass

Note

specific enthalpy, specific volume, specific entropy, specific energy, are Intensive property.

which of the following property Intensive property.

(a) Volume → Extensive

(b) Pressure → Intensive

(c) density → Intensive

(d) Kinetic energy → Intensive

(e) Specific enthalpy → Intensive

(f) thermal conductivity → Intensive

(g) Viscosity → Intensive

(h) Refractive Index. → Intensive due to dimensions

State Variable

When we are changing the property ~~that~~ then state changes.

Any condition of the system is known as state of the system for the particular all the property will have fixed value as any changing of property of state of system changes. change of state of a system is known as process

Path Variable

The infinite state through which system passes while going from initial state to final state is called path variable or process path.

Thermodynamic process

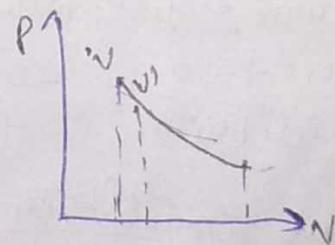
Quasi-static process

A process which occurs at very infinitely slow rate

Quasi-static process

It is represented by solid line or joined line.

In quasi-static process, each state through which system passes is an equilibrium state

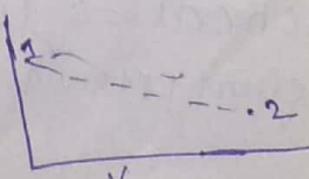


Non-

Quasi-static process

A process which is not quasi-static process

It is represented by dashed line.



Reversible and Irreversible process

When we are changing

When reversed in direction follows the same path as of the forward process and leaves no change in System and surroundings. It is called reversible

when the change in system and surroundings It is called Irreversible.

Thermodynamical equilibrium \rightarrow If the property of the system at all points become

A system is said to be in thermodynamical equilibrium if following types of equilibrium are satisfied

① Mechanical equilibrium

When all the forces are balanced.

② Chemical equilibrium

When all the chemical eqⁿ are balanced or ^{No} unbalanced chemical eqⁿ.

③ Thermal equilibrium

When two bodies are in same temp. these body are in thermal equilibrium

④ Phase equilibrium

When the phase are equal proportion or mass of per unit ~~over~~ time const.

Electrical \Rightarrow When there exist ~~an~~ uniformity of electric potential throughout the

Pure Substance

It is substance in which the chemical composition throughout the volume is same. Air, $O_2 + N_2$, brass, air, $H_2O + \text{steam}$, etc.

Pressure \rightarrow

molecular interaction

$$P_a = N/m^2$$

$$1 \text{ bar} = 10^5 N/m^2$$

$$1 \text{ psi} = 6894.75 \text{ Pa}$$

The pressure exerted by a system is defined as the force exerted normal to unit area of the boundary.

Pound/inch²

Gibb's - phase rule \rightarrow

It provides the theoretical foundation of thermodynamics

In the system there is only 1 No. of constraint

based in characterizing the chemical system and equilibrium relations of the phases present as physical condition

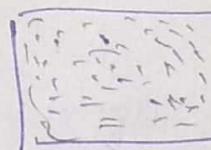
$$P + F = C + 2$$

T	\downarrow	\downarrow
No. of phases	D.O.F	No. of components

$F = \text{No. of independent intensive property required of fixed of the system}$

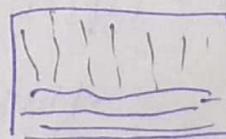
$$F = 1 + 2 + 2$$

$$\boxed{F = 3}$$



$$F = 1 + 2 - 2$$

$$\boxed{F = 1}$$



liquid water & water vapor mix

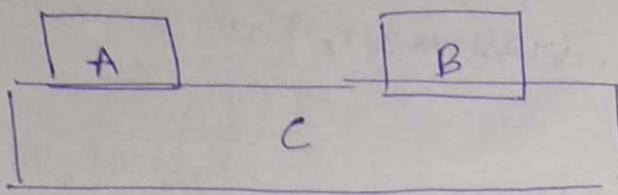
$$\boxed{L_f = \text{Latent heat} = \frac{Q}{m}}$$

The amount of heat required to change the phase of ~~one~~ 1 kg water, is called heat.

Zeroth law of thermodynamics

32°

2



$$\text{If } T_A = T_C$$

$$\text{and } T_B = T_C$$

$$\text{then } \boxed{T_A = T_B}$$

when any two bodies of different temp & B.
the attaching the body C in both they
All the system are in thermal equilibrium
between them body A = B of temp

Temp		
C	0	100
F	32	21
K	273.15	373.15

$$\boxed{\frac{C}{5} = \frac{F - 32}{9} = \frac{K - 273.15}{5}}$$

(\rightarrow the coeff of expansion of any temp normally)

How to find the eqn of temp.

$$T = ap + b \quad \textcircled{1}$$

for ice pt

$$0 = ap_i + b \quad \textcircled{2}$$

for steam pt

$$100 = ap_s + b \quad \textcircled{3}$$

$$\text{then } \textcircled{1} - \textcircled{2}$$

$$T - 0 = a(p - p_i) \quad \textcircled{4} \Rightarrow a = \frac{T}{p - p_i}$$

$$\text{then } \textcircled{1} - \textcircled{3}$$

$$-100 = a(p_i - p_s) \quad \textcircled{5}$$

Put the value of a in eqn's

$$-180 = \frac{T}{P-P_i} (P_i - P_s)$$

$$\frac{T_c}{180} = \frac{P - P_i}{P_s - P_i} \quad \text{--- (A)}$$

for degree F

$$T = aP + b \quad \text{--- (1)}$$

$$32 = aP_i + b \quad \text{--- (2)}$$

$$212 = aP_s + b \quad \text{--- (3)}$$

$$\left. \begin{array}{l} 1-2 \\ T - 32 = a(P - P_i) \quad \text{--- (4)} \\ a = \frac{T - 32}{P - P_i} \end{array} \right\} \begin{array}{l} 2-3 \\ -180 = a(P_i - P_s) \quad \text{--- (5)} \end{array}$$

then, Put the value of a in eqn (1)

$$-180 = \frac{T - 32}{P - P_i} (P_i - P_s)$$

$$\frac{T_c - 32}{180} = \frac{P - P_i}{P_s - P_i} \quad \text{--- (B)}$$

From eqn A & B

$$\frac{T_c}{180} = \frac{T_f - 32}{180}$$

$$\boxed{\frac{T_c}{5} = \frac{T_f - 32}{9}}$$

For K

$$T = ap_i + b \quad \textcircled{1}$$

$$273.15 = ap_i + b \quad \textcircled{2}$$

$$373.15 = ap_s + b \quad \textcircled{3}$$

$$T - 273.15 = a(p - p_i) \quad \left| \begin{array}{l} -100 = a(p_i - p_s) \quad \textcircled{5} \\ \textcircled{4} \end{array} \right.$$

$$a = \frac{T - 273.15}{p - p_i}$$

then put in eqn \textcircled{5}

$$-100 = \frac{T - 273.15}{p - p_i} (p_i - p_s)$$

$$\frac{-100}{T - 273.15} = \frac{p_i - p_s}{p - p_i}$$

~~$$\frac{T - 273.15}{-100} = \frac{p_s - p_i}{p - p_i}$$~~

$$\frac{T - 273.15}{100} = \frac{p - p_i}{p_s - p_i} \longrightarrow \textcircled{C}$$

then equal A = C

$$\frac{T_K - 273.15}{100} = \frac{T_c}{100}$$

$$\boxed{T_K = T_c + 273.15}$$

equal B = C

$$\frac{T_F - 32}{100} = \frac{T_K - 273.15}{100}$$

$$\boxed{\frac{T_F - 32}{9} = \frac{T_K - 273.15}{5}}$$

$$\star \quad \boxed{\frac{P - P_i}{P_s - P_i} = \frac{T - T_i}{T_s - T_i}}$$

Energy interaction :-

Internal energy (U)

~~These are all the microscopic form of energy which can't be visualised from Naked eyes. comes into the internal energy~~

Macroscopic outlook

~~Then all the outlook in Naked eyes.~~

Work

It is said to be done by the system If the sole effect on the thing is external to the system can be reduced to raise the weight. Though, weight may not be actually raised.

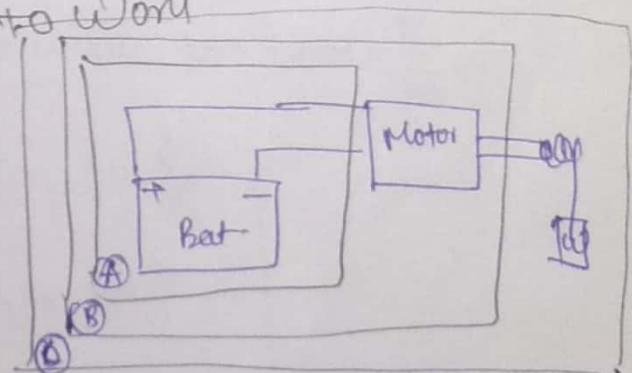
Work is a boundary phenomenon.

Work done by the system \Rightarrow Positive

work done on the system \Rightarrow Negative

Important point with respect to Work

- Work is not a property
- It is a path function
- It is a boundary phenomenon
- It is an inexact different
- It is a transient phenomenon
constant
Unstudiable



A & B \Rightarrow Work

C \Rightarrow No + work

Control System Analysis

Phase

If a quantity of matter is homogeneous or uniform throughout in physical structure and chemical composition is termed as phase

$$R = \frac{P_f - P_i}{P_i - P_0}$$

$$R = \frac{P_f}{P_i} - \frac{P_0}{P_i}$$

Pressure

Atmospheric pressure caused by the atmosphere air	Gauge Pressure measured from gauge and absolute (Brewster / Mano Methyl)	Absolute pressure measured from level of absolute zero press	Vacuum pressure of fluid to be measured is less than atm press
		Static pressure when pressure sensed by a measuring device moving with same velocity as the fluid stream	Impulse stagnation force per unit area due to the density of fluid when fluid is brought to rest gradually

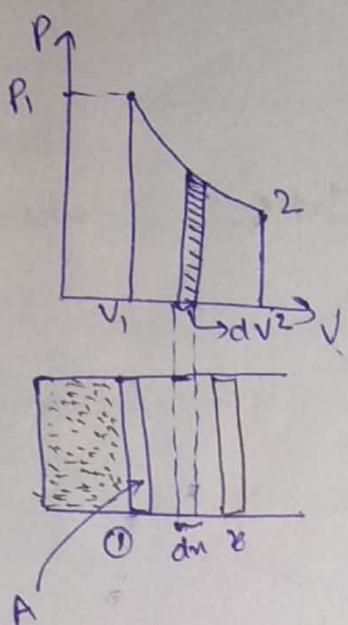
$$P_{abs} = P_{gauge} + P_{atm}$$

$$P_{abs} = P_{atm} - P_{vac}$$

- 76cm of Hg = 101.3 kN/m^2

- ~~40mm - 13.6 mm of water column = 1 mm of Hg~~

Closed System Analysis



Work = force \times displacement

Work = $P \times A \times dm$

$$\delta W = P dV$$

$$W = \int P dV$$

PdV work done, ~~Work done~~ -
displacement
Boundary Work

① Isochoric (Volume const)

② Isobaric (Pressure const)

③ Isothermal ($T=C$)

④ Adiabatic ($\Delta Q=0$)

~~Irreversible~~

⑤ Polytropic proc. ϵ

Isochoric $\boxed{TV=C} \Rightarrow \boxed{dV=0}$

then, $\boxed{W=0}$

Isobaric $\boxed{P=C}$

$$W = \int_1^2 P dV = P(V_2 - V_1)$$

Isothermal ($T=C$)

$$PV = mRT$$

$R = \text{characteristic gas const} = \frac{\bar{R}}{M}$

$$PV = C$$

$$P = \frac{C}{V} \quad \text{---} \quad ①$$

$$W = \int_1^2 \frac{C}{V} dV$$

$$W = C \ln(V_2 - V_1)$$

$$\boxed{W = C \ln \frac{V_2}{V_1}}$$

$$W = P_1 V_1 \ln \frac{V_2}{V_1}$$

$$W = P_2 V_2 \ln \frac{V_2}{V_1}$$

$$W = mRT \ln \frac{V_2}{V_1}$$

$$\boxed{W = 2.303 mRT \ln \frac{V_2}{V_1}}$$

④ Adiabatic process

$$PV^\gamma = C$$

$$P = \frac{C}{V^\gamma} \quad \gamma = 1.4$$

$$W = \int_{1}^{2} \frac{C}{V^\gamma} dV$$

γ = Adiabatic Index.

$$W = C \left[\frac{V_2^{\gamma-1}}{V_1^{\gamma-1}} \right]^2$$

$$\frac{C}{\gamma-1} [V_2^{-\gamma+1} - V_1^{-\gamma+1}]$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma = C$$

$$W = \frac{1}{\gamma-1} [P_2 V_2 - P_1 V_1]$$

$$\boxed{W = \frac{P_1 V_1 - P_2 V_2}{\gamma-1}} \text{ Joule.}$$

⑤ Polytropic process

$$PV^n = C \quad \text{where } n \text{ definite value of } n = \text{ Polytropic Index}$$

$n=0 \Rightarrow$ Iso baric

$n=\infty \Rightarrow$ Isochoric

$n=1 \Rightarrow$ Isothermal

$$n=\gamma = \frac{C_p}{C_V}$$

$$-\infty < n < +\infty$$

$$\left. \begin{array}{l} PV^{-1} = C \\ PV^2 = C \\ PV^2 = C \end{array} \right\} \text{ Polytropic}$$

$$W_{1-2} = C \int P dV = C \left(\frac{V_2^{1-n} - V_1^{1-n}}{1-n} \right)$$

$$C = P_1 V_1^n = P_2 V_2^n$$

$$W_{1-2} = \frac{P_2 V_2 V_2^{1-n} - P_1 V_1 V_1^{1-n}}{1-n} = \frac{P_1 V_1 - P_2 V_2}{n-1} \quad \text{if}$$

Process

- ① Isochoric
- ② Isobaric
- ③ Isothermal
- ④ Adiabatic
- ⑤ Polytropic

Representation

$$V=c$$

$$P=c$$

$$T=0$$

$$Q=0$$

$$PV^n=c$$

Workdone

$$W=0$$

$$W=P(V_2 - V_1)$$

$$W = 2.303 R T \ln \left(\frac{V_2}{V_1} \right)$$

$$W = \frac{P_1 V_1 - P_2 V_2}{r-1}$$

$$W = \frac{P_1 V_1 - P_2 V_2}{r-1}$$

* If the adiabatic process has to be carried out without insulation it should be carried in a very fast manner.

If an Isothermal process has to be carried out during phase change of the substance.

Slope of Isothermal and adiabatic's proc

Isothermal

$$PV=c$$

$$d(PV) = dc$$

$$VdP + PdV = 0$$

$$\boxed{\frac{dP}{dV} = -\frac{P}{V}}$$

Adiabatic

$$PV^r=c$$

$$d(PV^r) = dc$$

$$PV^{r-1}dV + V^rdP = 0$$

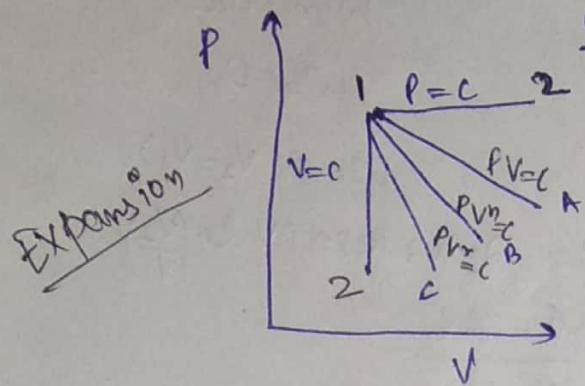
$$\frac{dP}{dV} = -\frac{rPV^{r-1}}{V^r}$$

$$= -rPV^{-\frac{1}{r}} = -\frac{rP}{V}$$

$$PV^r=c$$

$$\frac{dP}{dV} = -\frac{rPV^{r-1}}{V^r}$$

then, Adiabatic



Expansion

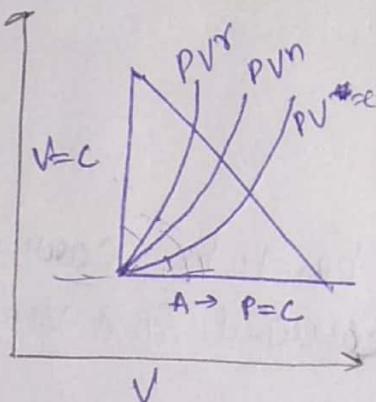
- Adiabatic is c below
- slope is more as compared to Isothermal
- Isothermal is A because $\gamma=1$ molar
- Any ~~will~~ b/w ('h').

- Adiabatic curve is more vertical than Isothermal curve,
- the slope of adiabatic curve is ' γ ' times the slope of Isothermal curve.

compression

$$(Q = -V\delta, W = +\delta V)$$

$\Rightarrow \delta V < 0$



Isothermal	Adiabatic
$\frac{dP}{dV} = \frac{-\delta P}{V}$	$\frac{dP}{dV} = -\frac{\gamma P}{V}$
isentropic com	
$\frac{dP}{dV} = \frac{\delta P}{V}$	$\frac{dP}{dV} = \frac{\gamma P}{V}$

expansion ($Q \neq V\delta, W = P\delta V$)

Ideal Gas Behaviour for Different ~~processes~~ processes

$$PV = mRT \rightarrow \text{Ideal gas}$$

R → characteristics gas eqn

① Isochoric $V = C$

$$PV = mRT$$

$$\frac{P}{T} = C$$

$$\boxed{\frac{P_1}{T_1} = \frac{P_2}{T_2}}$$

② Isothermal ($P = C$)

$$PV = mRT$$

$$\frac{V}{T} = C$$

$$\boxed{\frac{V_1}{T_1} = \frac{V_2}{T_2}}$$

③ Isothermal $PV = C$

$$PV = mRT$$

$$\boxed{P_1 V_1 = P_2 V_2}$$

④ Adiabatic process

$$PV^\gamma = C$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$\frac{P_1}{P_2} = \left(\frac{V_2}{V_1}\right)^\gamma$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^\gamma$$

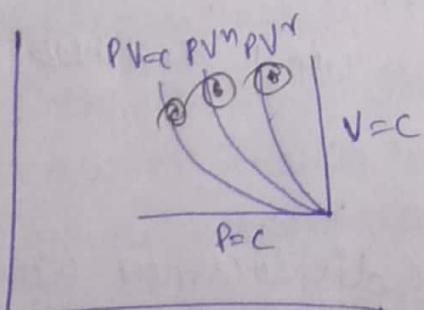
$$\frac{T_2 V_1}{T_1 V_2} = \left(\frac{V_1}{V_2}\right)^\gamma$$

By closed system
Quasi-static proc
Ideal gas

$$\frac{PV}{T} = \text{const}$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{P_2}{P_1} = \frac{T_2}{T_1} \frac{V_1}{V_2}$$



A is more vertical than it is
adiabatic

A Gas expand from initial state with $P_1 = 340 \text{ kPa}$ and $V_1 = 0.0425 \text{ m}^3$ to a final state where $P_2 = 136 \text{ kPa}$. If the pressure volume relationship during the process is $PV = C$ then determine in RT.

$$P_1 V_1^2 = P_2 V_2^2$$

$$340 \times 10^3 \times (0.0425)^2 = 136 \times 10^3 \times V_2^2$$

$$\frac{340 \times 0.0425^2}{136} = V_2^2$$

$$= 0.675 \text{ m}^3$$

$$W = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$340 \times 10^3 \times 0.0425 - 136 \times 10^3 \times 3$$

$$W = \frac{340 \times 0.0425 - 136 \times 0.675}{2-1} \text{ J}$$

$$W = 5.3108 \text{ J}$$

Q what are the other forms of work explain briefly.

Work \Rightarrow It is the sole effect external to the system
boundary has been the sole weight.

Sole effect \Rightarrow differentiate b/w work and heat

Work forms

1) Work of fluid (Mechanical work) or displacement work
It is the work when we are forcing

It is the work can be defined by when the external force can be applied at the molecule and thing's that's displaced at one place to another place is called displacement or fluid workdone.

$$F = P \cdot A$$

$$W = F \cdot dx$$

$$\delta W = P \cdot A \cdot dx$$

$$W = \int_P^V P \cdot dV$$

$$W = P(V_2 - V_1) \quad [5]$$

$$\text{During compression} = [W = -P(V_2 - V_1)] \quad [5]$$

Work done in moving an electric charge through electric field.

When the charge moving in electric field and experience a force by the electric field ~~that~~, that electric force (E) can be formed the potential difference across the charge (q) thereby called work done

~~$E = -\frac{\partial V}{\partial q}$~~

$$W = Vdq$$

It is valid only for neutrality

Paddle-wheel work or stirring work

As the weight is lowered and the paddle wheel turns there is a work transfer into the fluid system which get stirred since the volume of the system remains const.

$$\delta W = \int_m g ds = \int_T d\theta$$

Paddle wheel \Rightarrow It is a device which is converted into rotary motion into linear motion.

Shaft work \rightarrow A rotating shaft work is commonly encountered in machine elements.

Often the torque T applied to the shaft is const.

For specific const. torque, the work done during revolution is determined as follows:

$$F = \frac{T}{r}$$

$$S = 2(\pi r n)$$

$$\omega = F \cdot s$$

$$\boxed{\omega = 2\pi n T}$$

Heat

It is the form of energy transferred by virtue of temp diff.

$$\boxed{Q = mc\Delta T}$$

which is transferred

- It is the prot product
- It is the path quantity
- It is boundary phenomena
- It is transfer

Specific heat (C)

~~the amount of heat energy required to raise the temp of unit mass substance by unit degree temp. diff. measured by the 1K temp.~~

$$\boxed{C = \frac{Q}{m \Delta T}}$$

Why $C_p > C_v$

Because there is workdone of $C_p = P(V_2 - V_1)$

& In C_v workdone = 0

So, energy = microscopic + macroscopic
internal energy + work

so, the work in the C_p is more required
so heat is more required so,
 C_p is less

because C_p includes Internal energy & Workdone. Where as C_V includes only Internal energy.

At the Molecular level: At very temp.

Both C_p and C_V are increases but their ratio γ decreases.

But this gas is not applicable for Monoatomic (Inert) $1 - \frac{1}{2}$

$$\gamma = \frac{C_p}{C_V}$$

$$= \frac{C_p + N}{C_V} = 1$$

$$C_p = \frac{C_V + 1}{C_V}$$

- At the molecular level at high temp when we are breaking the bond of molecule then required more heat so, C_p and C_V are also Inert.

$$\gamma = 1.67 \text{ (monoatomic)}$$

$$\gamma = 1.4 \text{ (Diatomic)}$$

$$\gamma = 1.33 \text{ (Polyatomic)}$$

- Heat supplied by the system (+)
on the system (-)

First law of thermodynamics

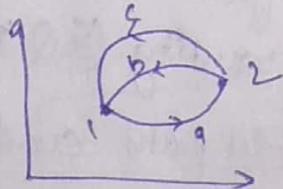
By professor (Soni)

$$E_{in} - E_{out} = E_{stored}$$

for a closed system undergoing a cycle net heat transfer is equal to net work transfer

Consequences

- ① Heat is the path function



$$1-a-2-b-1$$

$$Q_{1a2} + Q_{2b1} = w_{1a2} + w_{2b1} \rightarrow ①$$

1-a-2-c-1

$$Q_{1a2} + Q_{2c1} = W_{1a2} + W_{2c1} \rightarrow \textcircled{1}$$

$$\text{eq}_1 - \text{eq}_2$$

$$\frac{Q_{2b1} - Q_{2c1}}{W \neq 0} = W_{2b1} - W_{2c1} \rightarrow \textcircled{2}$$

$\neq 0$

↳ so, it is path function

Though, path b and c are different but the end points are same in the heat transfer in path b and c is different and hence, heat transfer depends on path and is a path function.

② Energy is a property
From eqⁿ A

$$\underbrace{Q_{2b1} - W_{2b1}}_{\text{energy}} = \underbrace{Q_{2c1} - W_{2c1}}_{\text{energy}}$$

If it is equal so, it is prop

$$\boxed{S_Q - S_W = dE}$$

Though path b and c are different and the end points are same^{but} the quantity ($S_Q + S_W$) will always be same for both the path and hence it does not depend on path and must represent a change in property.

And, that property known as energy.

- Energy is a point function
- Energy is an exact differential (dE)

$$E = M_i u_0 + M_o u_0 \\ U \quad K.E \neq P.E$$

Assumption

$\Delta K.E$ and $\Delta P.E = 0$ (For closed system)

$$dE = dU \rightarrow E = m_i u_{0,i}$$

$$S\theta - SW = dE$$

$$S\theta = dU + SW$$

$$W = W_{\text{bound}} + W_{\text{ext}}$$

$$S\theta = dU + SW_b + SW_{\text{ext}} \xrightarrow{\text{There is no other form of work.}}$$

$$S\theta = dU + PdV$$

For an Isolated system energy remains const

$$S\theta = dE + SW$$

$$dE = 0$$

$$E = \text{const}$$

(Q) PMM-I Perpetual Motion Machine of 1st Kind

According to first law of thermodynamics there can be no machine which produces work continuously without absorbing any other form of energy such

~~as~~ a device known as PMM-I

$$C_p = C_v = \cancel{2.8 + 105} \text{ J/K}$$

$$8.314$$

Heat transfer for Various processes

(a) Isochoric Process

~~del~~
$$\delta Q = dU + \delta W$$

first assume $\cancel{\delta W_b = 0}$ ~~800~~
 $\delta W_b = 0$

$$\delta Q = dU$$

$$\boxed{mC_V dT = dU}$$

Isochoric, Valid for all substances
 for Ideal gas valid for all pressures

(b) Isobasic Process

$$\delta Q = dU + \delta W$$

$$\delta Q = dU + PdV + \cancel{\delta W_b}$$

$$mC_P dT = dU + PdV$$

$$mC_P dT = dU + d(PV)$$

$$mC_P dT = d(U + PV)$$

~~For~~
$$\boxed{mC_P dT = dH}$$

$$H = \text{enthalpy} = U + PV$$

Isobasic, Valid for all substances

Ideal gas valid for all processes

③ For Isothermal process

$$\delta Q = dU + \delta W$$

for Ideal gas

$$U = f(T)$$

$$\delta Q = dT^0 + \delta W$$

$$\boxed{\delta Q = \delta W}$$

In Isothermal process the total heat supplied to the Ideal gas is converted into work and it is know not a violation of 2nd law of thermodynamics since, 2nd law is for a cycle not for a process

④ Adiabatic process

$$\delta Q = dU + \delta W$$

$$\delta Q = -\delta W$$

Polytropic
first law of open system

Heat transfer for Polytropic process



$$\delta Q = C_p - C_v = R \quad \text{--- (1)} \quad \star \star \star$$

$$\frac{C_p}{C_v} = \gamma$$

$$\boxed{C_p = \gamma C_v} \quad \text{--- (2)}$$

Putting eqn (1) in (2)

$$\gamma C_v - C_v = R$$

$$C_v(\gamma - 1) = R$$

$$\boxed{C_v = \frac{R}{\gamma - 1}}$$

and

$$\boxed{C_p = \frac{\gamma R}{\gamma - 1}}$$

$$\boxed{\delta Q = dU + \delta W}$$

$$\delta Q = m_C dT + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$= m_C (T_2 - T_1) + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$= \frac{mR}{\gamma-1} (T_2 - T_1) + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$= \frac{1}{\gamma-1} (mRT_2 - mRT_1) + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

For Ideal
gas

$$P_1 V_1 = m R T_1 \quad P_2 V_2 = m R T_2$$

$$= \frac{1}{\gamma-1} (R V_2 - R V_1) + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$\delta Q = \frac{R V_1 - R V_2}{n-1} \left[-\frac{(n-1)}{\gamma-1} + 1 \right]$$

$$\delta Q = \frac{P_1 V_1 - P_2 V_2}{n-1} \left[\frac{-n+\gamma + \gamma - \gamma}{\gamma-1} \right]$$

$$\delta Q = \frac{P_1 V_1 - P_2 V_2}{n-1} \left[\frac{\gamma - n}{\gamma - 1} \right]$$

$$\boxed{(\delta Q)_{\text{poly}} = (\delta W)_{\text{poly}} \left[\frac{\gamma - n}{\gamma - 1} \right]}$$

$$(S)_{\text{poly}} = \frac{P_1 V_1 - P_2 V_2}{n-1} \left(\frac{\gamma-n}{\gamma-1} \right)$$

$$\frac{mRT_1 - mRT_2}{\gamma-1} \left(\frac{\gamma-n}{n-1} \right)$$

$$\frac{mR}{\gamma-1} \left(\frac{\gamma-n}{n-1} \right) (T_2 - T_1)$$

$$m \underbrace{\left(-c_V \left(\frac{\gamma-n}{n-1} \right) \right)}_{\text{specific heat for polytopic process}} (T_2 - T_1)$$

$$\text{specific heat for } \underline{\text{polytopic process}} = -c_V \left(\frac{\gamma-n}{n-1} \right)$$

The specific heat of polytopic process is negative i.e., even though the heat supply temp. decreases because work done by the gas exceeds the heat supplied.

To prove $C_p - c_V = R$
~~For Ideal Gas~~

$$\Rightarrow \boxed{dH = dU + dPV}$$

$$mC_p dT = m(c_V dT + d(nRT))$$

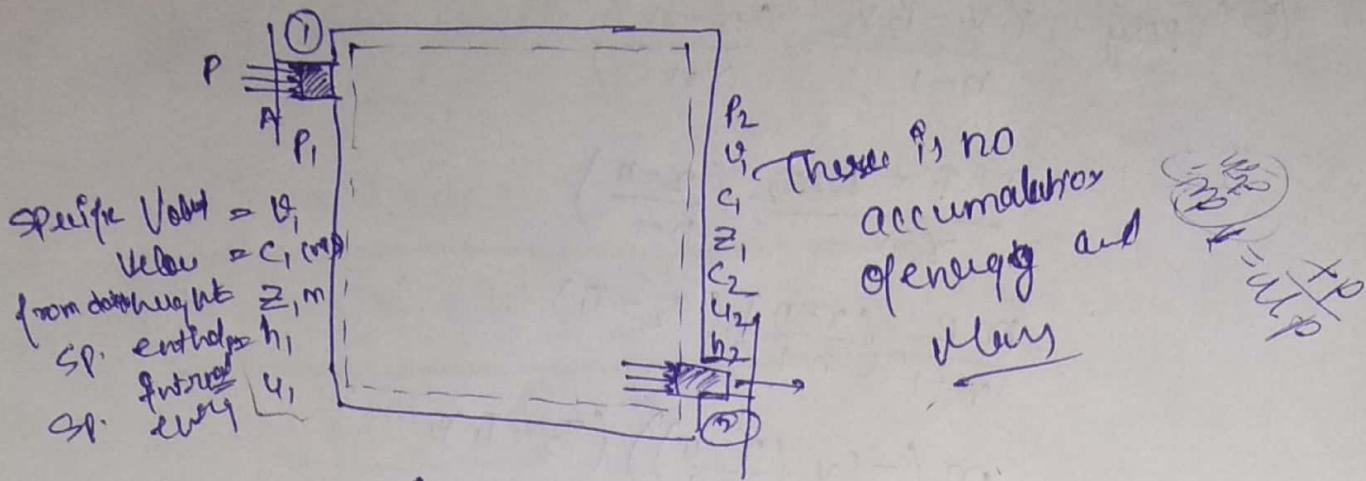
$$\cancel{mC_p dT} = \cancel{m(c_V dT)} + m(RdT)$$

$$\boxed{C_p = c_V + R}$$

Open System Analysis (Mass responsible for energy transfer)

There are two principles that flows by open system

- Conservation of mass ($M_{\text{in}} = M_{\text{out}}$)
- Conservation of energy ($E_{\text{in}} = E_{\text{out}}$)



$$\delta W = P_1 A dm$$

$$\delta W = P_1 dV$$

$$\frac{\delta W}{\delta m} = P_1 \frac{dV}{dm}$$

$$\delta W_1 = P_1 v_1$$

$$\delta W_2 = P_2 v_2$$

open system =
control volume

closed =
control mass

$$\boxed{\frac{P_1 dV}{dm} = \frac{P_2 dV}{dm}}$$

Inlet Work on $\overset{\text{control vol}}{C.V.} = -P_1 V_1$

Outlet $v \quad n \quad n = +P_2 V_2$

Steady state \rightarrow when properties do not change
with time

when properties do not change with

space is called Unif

Unsteady state - when properties ~~do not~~ change with time
and when properties do ~~not~~ change with time
Space. Non Unif

SFEE Study flow Energy equation

Study flow energy equation

$$E_{in}^{\circ} = E_{out}$$

control volume

$$\dot{m} = \rho \dot{V} \rightarrow \text{discharge}$$

$$\dot{V} = \frac{dV}{dt} \rightarrow \underline{\text{discharge}}$$

$$H_1 + \frac{C_1^2}{2} + g z_1 + \dot{q} = H_2 + \frac{C_2^2}{2} + g z_2 + w_{cv}$$

$$\dot{m}_{in} = \dot{m}_{out}$$

$$m_1(h_1 + \frac{C_1^2}{2} + g z_1 + \dot{q}) = m_2(h_2 + \frac{C_2^2}{2} + g z_2 + w_{cv})$$

$$\dot{m}_1 = \dot{m}_2$$

$$h_1 + \left(\frac{C_1^2}{2} + g z \right) + \dot{q} = h_2 + \frac{C_2^2}{2} + g z_2 + w_{cv}$$

$$\text{for } [K.E \neq P.E = 0]$$

R

$$h_1 + \dot{q} = h_2 + w_0 = \text{otherwise}$$

$$u_1 + p_1 v_1 + \dot{q} = u_2 + p_2 v_2 + w_0$$

$$\dot{q} = (u_2 - u_1) - (p_2 v_2 - p_1 v_1) + w_0$$

$$\begin{aligned} &= \Delta U + \underbrace{w_{b0} + w_0}_{\dot{w}} \\ \dot{q} &= \Delta U + \dot{w} \end{aligned}$$

$$\dot{w} = \frac{\dot{w}}{m}$$

This is the first law of thermodynamics for open system

Workdone and Q and DE for different system

- Water and its vapour in a rigid bulb

Rigid bulb $\rightarrow \text{pdV} = 0$ $W = 0$

$$Q = +Vl$$

$$\Delta E = Q - W = +Vl$$

- Water and steam circulate through various components of steam power plant

Workdone \Rightarrow Turbine Input work < Output work
 $+Vl$

Q_{in} = Heat added in the boiler > Heat rejected to cool
 $+Vl$

$$\boxed{\Delta E = 0}$$

- Hydrogen and oxygen in the form of combustible mixture within a rigid and insulated wall.

Insulated $\circlearrowleft Q = 0$

Rigid $\circlearrowleft W = 0$

$$\boxed{\Delta E = 0}$$

- In gasoline mixture

$Q \Rightarrow$ ~~heat~~ chemical Energy \rightarrow Mechanical energy
 by the mixture of air and gasoline.
 then T emp \uparrow \circlearrowleft Intensity \uparrow

$\circlearrowleft Q = -Vl$
 Intensity energy on the System $= +Vl$

$W \Rightarrow$ Work done by the System $= +Vl$

$$\Delta E = Q - W$$

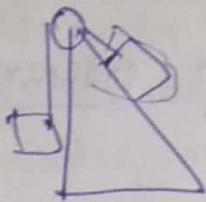
$$-Q - W = -Vl$$

Capacitor \rightarrow Work done by the system
 $\textcircled{W} \rightarrow$ Input work \leftarrow Output work
 Reservoir (Boundary) Capacity $\cancel{\text{max work}}$

$$W = +Vl$$

$Q = \text{Adiabatic System} \Rightarrow 0$

$$\Delta E = +Vl$$



Block $\rightarrow Q=0 \Rightarrow$ Block (Non Conductivity)
 $\rightarrow W = \text{Capacity} = +Vl$ due to friction
 $\Rightarrow \Delta E = -Vl$

Plane $\rightarrow Q \Rightarrow$ No heat transfer \Rightarrow
 $W = -Vl$ due to block

$$\Delta E = +Vl$$

Block & plane $\rightarrow Q=0$
 $W=0$
 $\Delta E = 0$

Fully body does not produce any work.

Thermal efficiency = $\frac{\text{Net work done}}{\text{Heat supplied}}$

$\frac{2000}{2000}$

During winter season a room measuring $5 \times 6 \times 3 \text{ m}^3$ heated electrically from initial temp. of 0°C to 20°C . The air pressure inside the room is the same as that of surroundings and is equal to 74 cm of Hg. The pressure remains const. during this process. The heat capacity of furniture and walls is 32 kJ/kg K . The sp. heat of air is 1005 J/kg K . Calculate the amount of electric energy needed for heating the room, how much air escapes through gaps, and windows during this period.

$$V = 5 \times 6 \times 3 = 90 \text{ m}^3 \quad \bar{P}_{\text{atm}} = 1.013 \times 10^5 \text{ Pa}$$

$$M_1 = \frac{PV}{RT} = \frac{0.9863 \times 10^5 \times 90}{0.287 \times (273+0)} = \frac{0.9863 \times 10^5 \times 90}{0.287 \times 273} = \frac{0.9863 \times 10^5 \times 90}{0.287 \times 273} = 1.013 \times 10^5 \text{ kg}$$

$$M_2 = \frac{0.9863 \times 10^5 \times 90}{0.287 \times 273+20} =$$

$$\text{difference} \Rightarrow M_1 - M_2 = 7.9314$$

$$Q_1 = M_1 \cdot C_p (T_2 - T_1)$$

$$M = \frac{M_1 + M_2}{2}$$

$$Q_2 = 32 \times (20 - 0) \\ = 32 \times 640$$

$$P_e = \frac{Q_1 + Q_2}{1 \text{ hour}} = 64$$

Thermodynamic process

Thermodynamic process is that process where heat or work is transferred.

transition in which a system changes from one initial state to final state

Reversible process

When the system reversed in the direct follows a same path there is no change system and surroundings is called reversible.

(a) Frictionless relative motion, electrolytes, Isothermic expansion or

Irreversible

When the reversed in the direct follows a same path there is change system and surroundings is called irreversible.

(a) Fluid flows with friction

(b) Free expansion

(c) diffusion of gas

Flow work

That work which is associated in the flow process.

then it has absent of closed system. The flow work is work required to cause the flow of fluid in any passage.

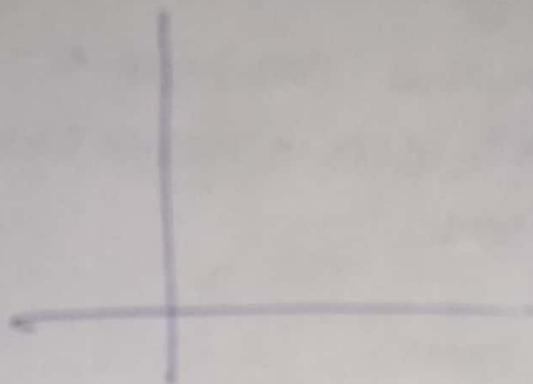
Nozzle or turbine

(V) vs (Boyle's Law) Iso chart process

$$PV^n = \text{polytropic}$$

$$\theta = \text{constant}$$

Pressure P = 1.5 bar



working for $PdV \propto \text{constant}$ pressure
Isothermal process

Application of steady flow energy equation

Conversion of unit

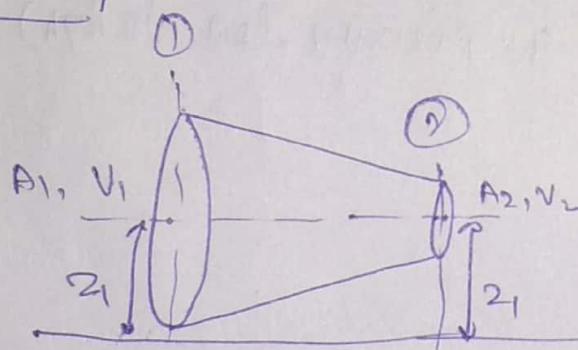
$$+ h_1 + \left(\frac{C_1^2}{2} + g z_1 \right) \times 10^3 + \dot{q} = h_2 + \left(\frac{C_2^2}{2} + g z_2 \right) \times 10^3 + \cancel{g z_2} + \dot{q}$$

$\underbrace{\text{KJ/kg}}_{\text{then it}}$

① Nozzle Velocity

Assumption

- ① Steady state
- ② Adiabatic Nozzl.
- ③ Change potential energy 0
- ④ $\underline{w_{cv} = 0}$



For brains we all uses super sonic Nozzl.

$$A_1 V_1 = A_2 V_2$$

$$\cancel{V_2} = \frac{m}{S}$$

discharge.

$$h_1 + \frac{C_1^2}{2} + g z_1 + \dot{q}^0 = h_2 + \frac{C_2^2}{2} + g z_2 + \cancel{g z_2} + \dot{q}^0$$

$$h_1 + \frac{C_1^2}{2} = h_2 + \frac{C_2^2}{2}$$

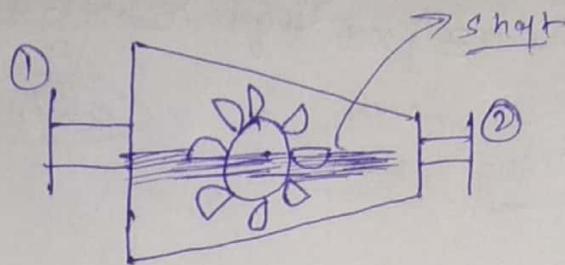
$$\boxed{C_2 = \sqrt{2(h_1 - h_2)}} \text{ m/s}$$

$C_2 \gg \gg C_1$

Turbine

Assumption

- ① Steady state
- ② Adiabatic
- ③ Kinetic energy \neq P.E = 0



$$h_1 + \frac{C_1^2}{2} + gZ_1 + q = h_2 + \frac{C_2^2}{2} + gZ_2 + \dot{W}_{cv}$$

$$\boxed{h_1 - h_2 = \dot{W}_{cv}}$$

Compressor

(Compresses the primary flow to high)

Assumption

- ① Steady state
- ② Adiabatic
- ③ Change in K.E \neq P.E = 0

$$h_1 + \frac{C_1^2}{2} + gZ_1 + q = h_2 + \frac{C_2^2}{2} + gZ_2 + \dot{W}_{cv}$$

$$\boxed{h_1 - h_2 = -\dot{W}_{cv}}$$

-ve because Work done
on the system.

Limitation of first law of thermodynamics.

- ① First discuss about energy transfer only it quantity.
, doesn't discuss the grade of energy & the quality of energy.
- ② First law does not discuss about the direc'n of energy transfer.

Example of limitation of first law

$$⑥ h_1 + \frac{C_1^2}{2} + g = h_2 + \frac{C_2^2}{2} + w_{cv}$$

⑧ Axial flow comp

$$\left. \begin{array}{l} P_1 = 1 \text{ bar} \\ T_1 = 300 \text{ K} \\ C_1 = 300 \text{ m/s} \end{array} \right| \quad \left. \begin{array}{l} P_2 = 5 \text{ bar} \\ T_2 = 475.15 \\ C_2 = 100 \text{ m/s} \end{array} \right\} \quad \leftarrow \frac{T_2}{T_1} = \left(\frac{P_1}{P_2} \right)^{\frac{r}{k}}$$

$$PV = mRT$$

$$P = f R T$$

$$P_1 = f_1 R T_1$$

$$f_1 =$$

$$f_2 =$$

$$20 = f_1 A_1 V_1$$

$$h_1 + \frac{C_1^2}{2} + g z_1 + f = h_2 + \frac{C_2^2}{2} + g z_2 + w_{cv}$$

$$w_{cv} = - (h_2 - h_1) + \left(\frac{C_1^2}{2} - \frac{C_2^2}{2} \right) \times 10^{-3}$$

$$w_{cv} = - (P(T_2 - T_1) + \left(\frac{C_1^2}{2} - \frac{C_2^2}{2} \right) \times 10^{-3})$$

$$= - 1.00 \times (475.15 - 300) + \left(\frac{(800)^2 - (100)^2}{2} \right) \times 10^{-3}$$

$$= - 1.05 \times 175.15 + 0$$

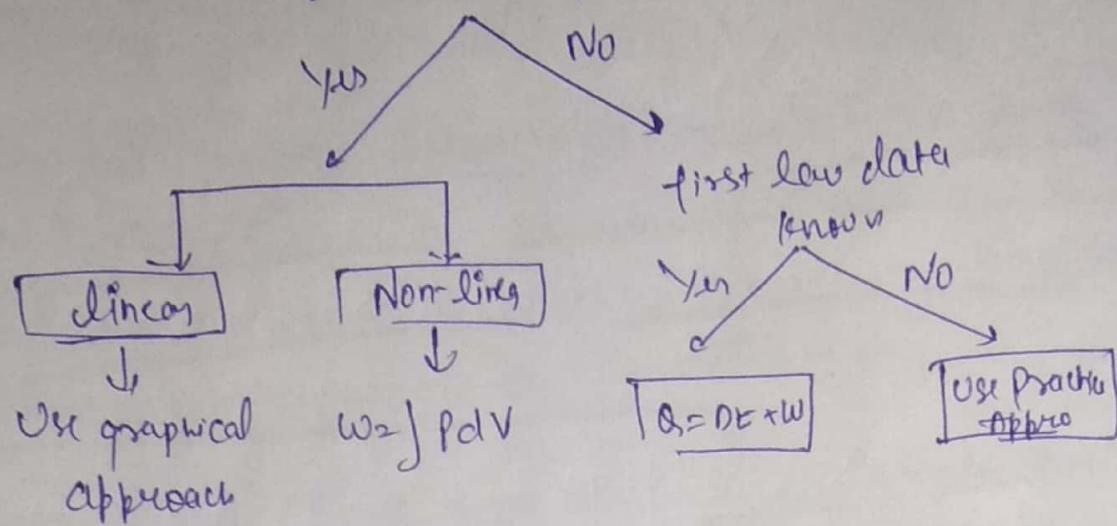
$$= - 176.020 +$$

$$= 136 \times \frac{100}{100}$$

$$20 \times 136 = \underbrace{100}_{\text{Kw}}$$

Problem solving for closed system

If $\text{P} \neq f(V)$ know



(14)

Second law of thermodynamics

Thermal energy reservoir ^(TER) → It is a large body of infinite heat capacity capable of absorbing and emitting infinite amount of heat without any considerable change in thermodynamic Co-ordinate.

Source is a TER from which we can gain an infinite amount of heat without any temp. change in source.

Sink is a TER from which we can absorb infinite amount of heat without undergoing any change in temp.

$Q_s \rightarrow$ Heat Supplied

$Q_r \rightarrow$ Heat Rejected

$Q_H \rightarrow$ Heat transfer at high Temp

$Q_L \rightarrow$ n n Low Temp

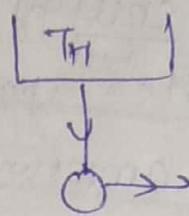
$T_H \rightarrow$ Body of Higher temp
transferring heat

$T_L \rightarrow$ n n temp of which is at lower temp.

According to second law of thermodynamics it is impossible to construct a device working on a cycle which converts low grade energy, random energy or disorganized energy (example: thermal energy, heat) into high grades (organized energy ex: work).

Statement of Kelvin or Planck

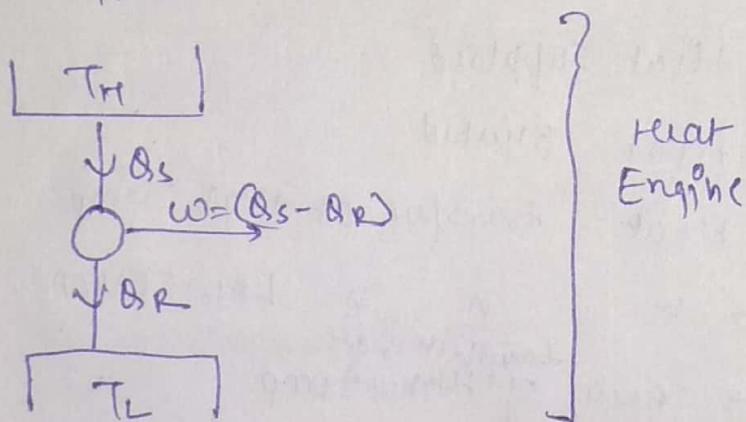
"It is impossible to develop a device working on a cycle which produces work by exchanging heat with a single reservoir."



Heat engine cycle

It is a thermodynamics cycle which produces work by the expense of heat.

According to Kelvin's principle of second law, No heat engine can have ~~any~~ an efficiency of 100%.



$$\eta = \frac{\text{Net Workdone Output}}{\text{Net Heat Input}}$$

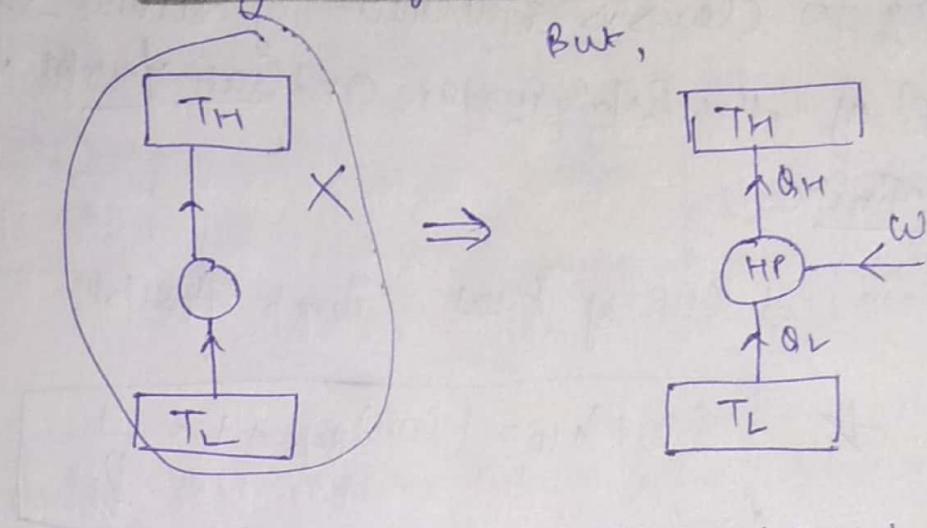
$$\eta = \frac{w}{Q_S} = \frac{Q_S - Q_R}{Q_S} = 1 - \frac{Q_R}{Q_S}$$

$$\boxed{\eta = 1 - \frac{Q_R}{Q_S}}$$

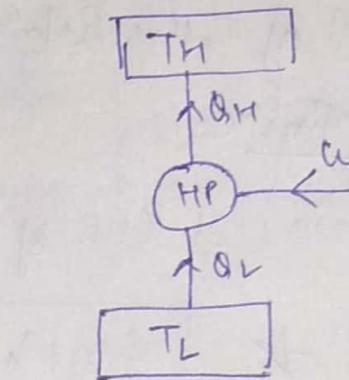
Heat engine is based on concept of Kelvin Planck statement of second law of thermodynamics as it produces work by exchanging heat with two thermal energy reservoirs.

Statement of Clausius of Second Law

It is impossible to develop a device working on a cycle which transfer heat from lower temp. to high temp. without any energy input.



But,



HP \Rightarrow Heat pump

Coefficient of performance (COP)

$$COP = \frac{\text{desired effect}}{\text{work input}}$$

$$(COP)_{\text{heat pump}} = \frac{Q_H}{w}$$

$$E_{in} = E_{out}$$

$$Q_L + w = Q_H$$

$$\boxed{w = Q_H - Q_L}$$

$$(COP)_{HP} = \frac{Q_H}{Q_H - Q_L}$$

$$(COP)_{Refrig.} = \frac{Q_L}{W_{in}}$$

$$(COP)_{Refrig.} = \frac{Q_L}{Q_H - Q_L}$$

According to Clausius statement of second law.
 The (COP) of the Refrigerator or heat pump can't
 be infinite

The relation of COP of heat pump & refri

★ $(COP)_{HP} = (COP)_{Refr} + 1 = \frac{1}{\eta_E}$

$$\frac{Q_H}{Q_H - Q_L} =$$

Refrigerator

It device which maintains the temp. of the system lower than that of surrounding.

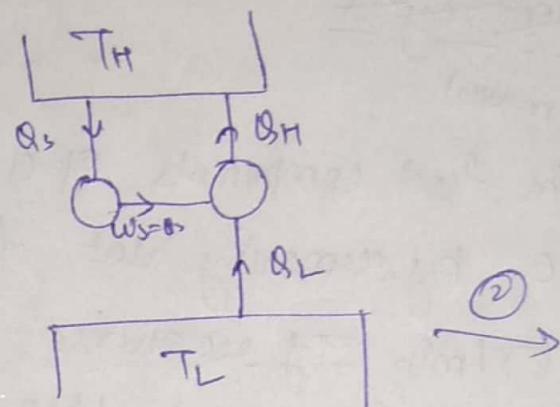
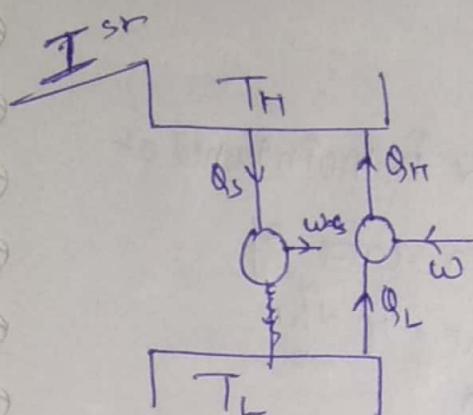
Heat Pump

It is a device which maintains the temp. of the system higher than that of surrounding.

Alo

A heat engine cycle is a thermodynamic cycle in which there is net heat transfer to the system and net work transfer from the system. The system which executes heat engine cycle is a heat engine.

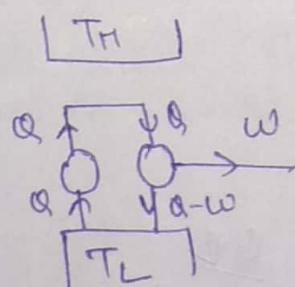
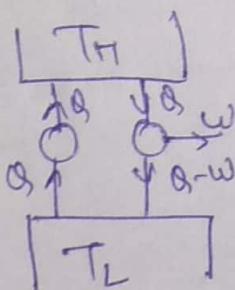
Equivalence of Kelvin Planck statement and Clausius statement of



Violet's

"Merge the device that ~~Violet's~~ Kelvin Planck statement with device Clausius statement"

As we Violet's Kelvin Planck statement + the Clausius statement gets violated automatically because after merging devices there is no need of external energy input to transfer Heat from lower temp. to higher temp.



As we ~~violate~~ violet's Clausius statement Kelvin Planck statements gets automatically violated because after merging the devices there is no need to introduce heat or

Sayler heat from source (TER).

"The violation of Kelvin plants statement leads to violation of Clausius Statement and vice-versa."

Hence, These statements are called as parallel Statement of second law of thermodynamics.

Carnot cycle

Numerical

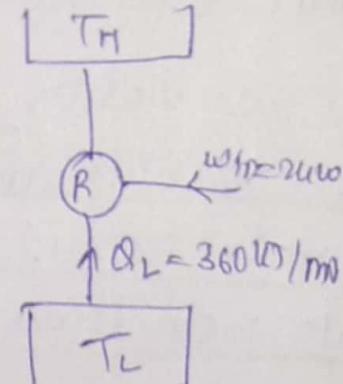
- Q The food components of a refrigerator is maintained at 4°C by removing heat from it at a rate of 360 KJ/min. If required power input to the refrigerator is 2 kW then determine
- i) COP of refrigerator
 - ii) the rate of heat rejected that flows to the refrigerator
 - (iii) \dot{Q}_H

COP

$$\dot{Q}_L = 360 \text{ KJ/min} = \frac{360}{60} = 6 \text{ KW}$$

$$\text{COP} = \frac{\dot{Q}_L}{W} = \frac{6 \text{ KW}}{2 \text{ KW}} = 3 \text{ KW}$$

$$\boxed{\text{COP} = 3}$$



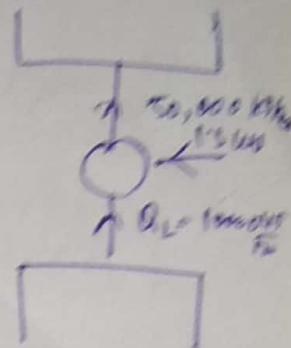
$$\text{COP} = \frac{\dot{Q}_H}{\dot{Q}_H - \dot{Q}_L}$$

$$(\dot{Q}_H - \dot{Q}_L) 3 = 6 \quad = 8 \text{ KW}$$

A commercial heat pump removes 10,000 KJ/hour of heat from the source and supplies 50,000 KJ/hour totally. Source and requires 1.5 kW of power. What is COP of Heat Pump?

$$Q_{HP} = \frac{10,000}{60 \times 60} = \frac{500}{36}$$

$$Q_L = 10,000 \text{ KJ/hour}$$



$$(COP)_{HP} = \frac{Q_L}{Q_{HP} - Q_s} = \frac{10,000}{\frac{500}{36} - 1.5} = 2$$

$$(COP)_{pu} = \frac{2}{4} + 1$$

$$\frac{10,000}{500} = 2$$

$$(COP) = \frac{10,000 \times 3600}{1.5} = 22,667$$

$$\frac{50000}{1.5} = 33,333$$

$$\begin{array}{r} 130 \\ 36) 500 \\ \underline{108} \\ 140 \\ \underline{102} \\ 102 \\ \underline{32} \\ 4 \end{array}$$

$$\text{Q}_s = \frac{150}{3600} = 2.222$$

A completely reversible heat engine operates with a source at 800 K and sink at 280 K and requires at what rate heat must be supplied to the engine in KJ/hour. for producing a power of 4 KW.

~~Note: for reversible engine efficiency is a function of temp. only~~ $(\eta = 1 - \frac{T_L}{T_H}) (1 - \frac{T_L}{T_H})$

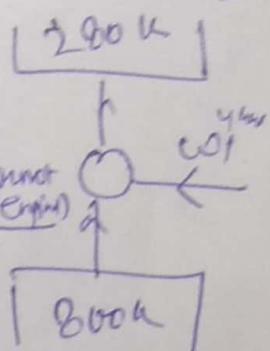
$$\eta = 1 - \frac{280}{800} = 1 - \frac{280}{800} =$$

$$\eta = 1 - \frac{280}{800} =$$

$\eta = 0.625$

$$\dot{W}_{HP} = \eta \dot{Q}_H = \eta \dot{Q}_L$$

$$\frac{\dot{Q}_H}{\dot{Q}_S} = \frac{T_L}{T_H} \Rightarrow \left[\dot{Q}_H = \dot{Q}_S \frac{T_L}{T_H} \right]$$



$$Q_S = \frac{\eta}{W}$$

$$Q_S = \frac{65}{\cancel{4}} \quad Q_{in} = \frac{4}{.65}$$

$$Q_S = \frac{4}{.65} \times 3600$$

Tu

Cannot use reversible engine
But In the daily life ~~Isentropic~~

In a ~~cannot~~ Engine the ratio of minimum to maximum temp. 0.8 If a heat pump is operated below ~~Isentropic~~
limit what is its C.O.P.

$$\textcircled{B} \quad \frac{T_{max}}{T_{min}} = \frac{T_{S_{max}}}{T_{S_{min}}} = 0.8$$

$$COP = \frac{1}{n_E}$$

$$n = 1 - \frac{T_L}{T_H} =$$

$$\approx 0.8$$

$$COP = \frac{1}{n_E} \leq$$

A reversible heat engine operating under a source temp. of 606°C and sink temp 20°C what will be the work done per KJ heat supplied to the engine.

$$\eta = 1 - \frac{T_L}{T_H}$$

$$1 - \frac{293}{879}$$

$$\frac{879 - 293}{879}$$

$$\boxed{\eta = 0.667}$$

$$\frac{T_L}{T_H} = \frac{293}{879}$$

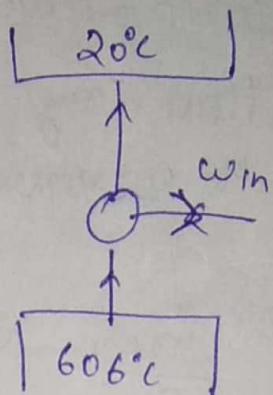
$$Q_S = \frac{W}{\eta}$$

$$Q_O =$$

$$\eta \times Q_S = W$$

$$\boxed{Q_S = 1 \text{ for per KJ}}$$

$$\boxed{W = 0.667 \text{ KJ}}$$



A refrigeration system rejects heat at a rate of 120kw and consumes 30kw . Then find the COP of refrigeration.

$$(COP)_R = \frac{1}{n} =$$

$$Q_R = 120\text{kw}$$

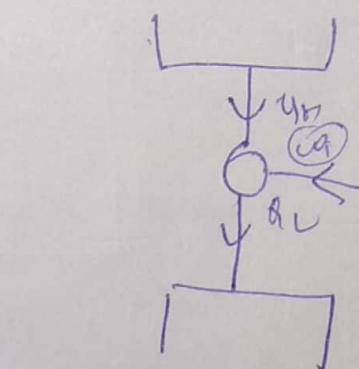
$$Q_S = 30$$

$$n = \frac{W}{Q_{in}} = \frac{120\text{kw}}{30\text{kw}}$$

$$= 1 + \frac{1}{4} = 3$$

$$1 - \frac{Q_R}{Q_S} = \frac{120}{30} - \frac{1}{4}$$

$$= 1 + \frac{1}{4} = \frac{5}{4}$$



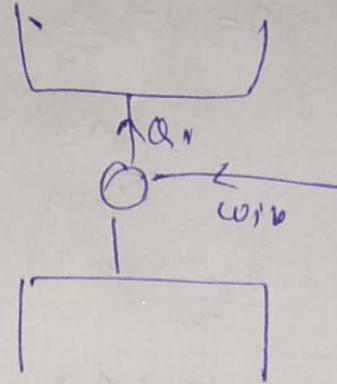
$$(COP)_R = \frac{Q_L}{Q_H - W} = \frac{30 - 30}{30} = 1$$

$$\boxed{(COP)_R = 1}$$

A refrigerator used for cooling food in a grocery store is to produce 10,000 KJ/hour^{Cooling effect} and (COP) is ref = 1.35. How many kW·Watts of power will require to operate the refrigerator.

$$\frac{10,000 \text{ KJ}}{3600} = 1\text{KJ}$$

$$= 2.7 \text{ KJ}$$



$$(COP)_1 = \frac{Q_H}{W}$$

$$= \frac{2.7}{1.35} = \underline{\underline{2.0376}}$$

Q A domestic refrigerator which follows reverse Carnot cycle set as 2°C and ^{Ambient} ambient temp is 30°C find the COP of refriger (NOTE: for a reverse Carnot cycle Q_H, Q_L , COP is a funcn of temp. only)

$$COP = \frac{T_L + T_H}{T_H} = \frac{2}{30}$$

$$\frac{30-2}{30} = \underline{\underline{0.93}}$$

$$(COP)_3 = \frac{Q_L}{Q_H - Q_L} = \frac{T_L}{T_H - T_L} = \frac{2+273}{30-2}$$

$$\frac{275}{293-275} = \frac{275}{18}$$

Reversible process is an ideal process and all natural processes are considered as irreversible processes.

All reversible processes are quasi-static but the converse is not true.

Causes of Irreversibility

a) Lack of equilibrium with system or with surroundings.

~~b) Dissipative effects.~~

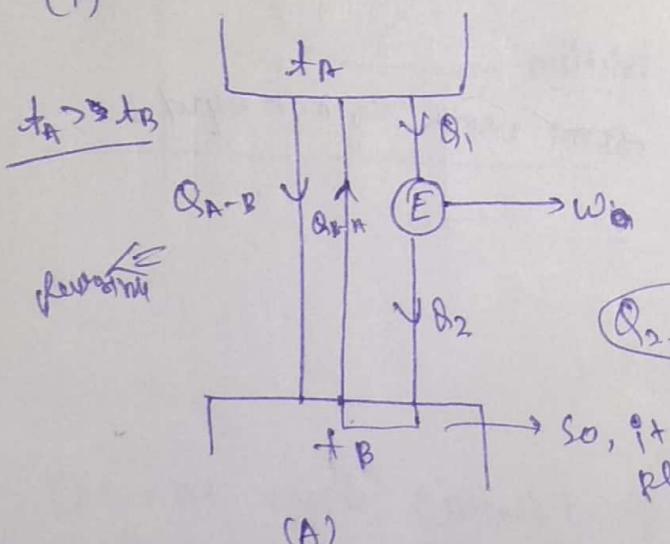
- a) i). Heat transfer through a finite temp. difference.
ii) Lack of pressure equilibrium within system
iii) Free expansion.

b) i) Friction

~~ii) Paddle wheel work~~

~~iii) Energy transfer through resistor etc.~~

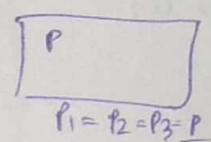
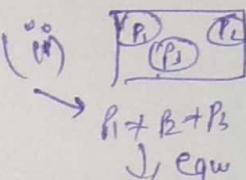
(i)



So, it violates Kelvin-Planck statement so, if Q_{A-B} is reversible

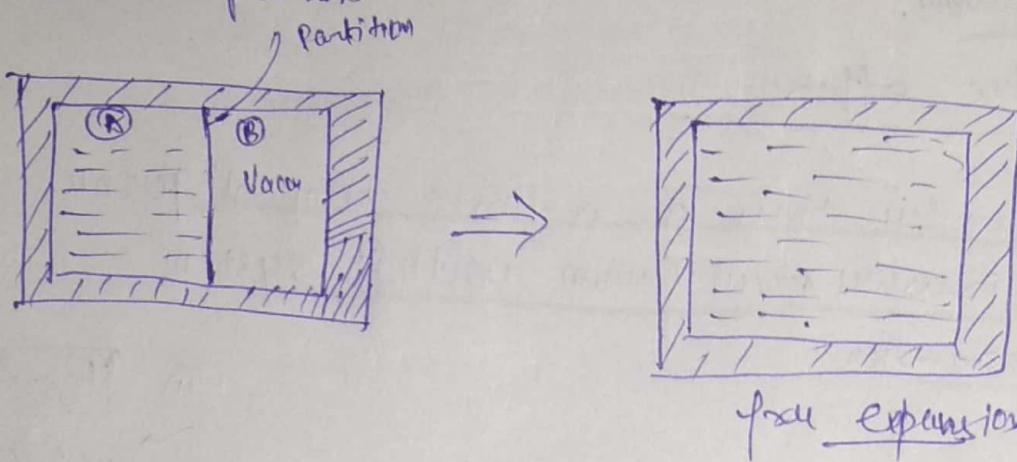
But we know,
not make it possible
it passes through
gradually
then, need to do
some work
so, it is quite an
irreversible.

Let suppose (A) as we can ^{see} figure (A) If we consider Q_{A-B} as reversible. We can consider its direction and assuming heat rejected by the engine is equals to heat transfer from $B-A$ (Q_{B-A}) that means E produces work by the

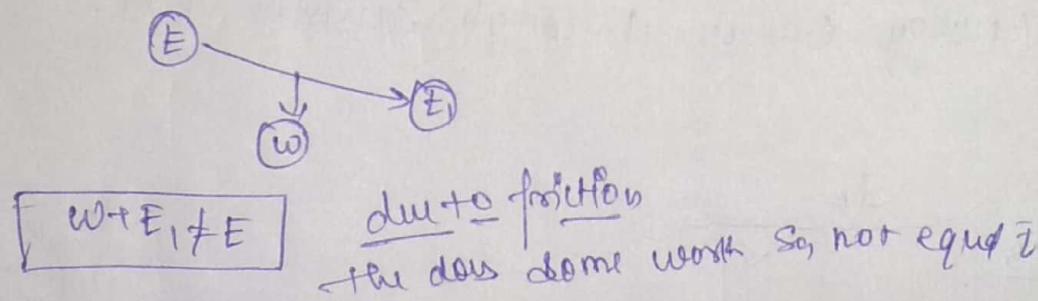


Exchanging heat with a single survivor and that is the violation of "Kelvin Planck's" statement so, we can say heat transfer through a finite temp diff is an irreversible process.

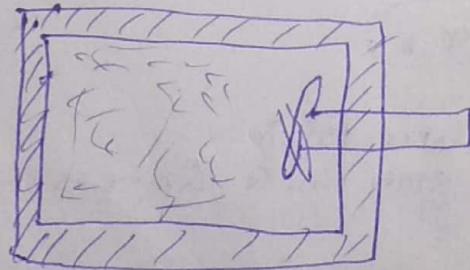
(ii) Expansion of gases against the vacuum in an insulated room is known as free expansion. It is an highly irreversible process



(ii) a)



b)



c)

Carnot cycle (Reversible cycle)

IT P.

Process 1-2

Reversible, adiabatic compression

2-3

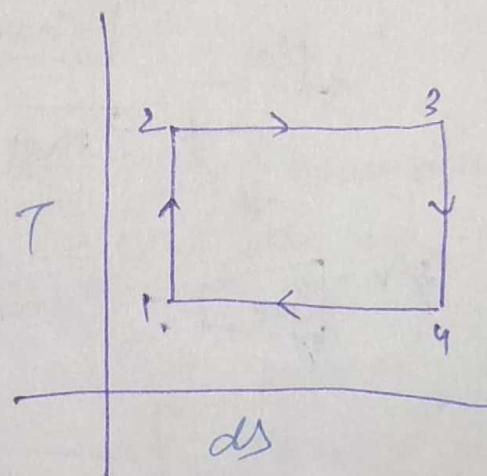
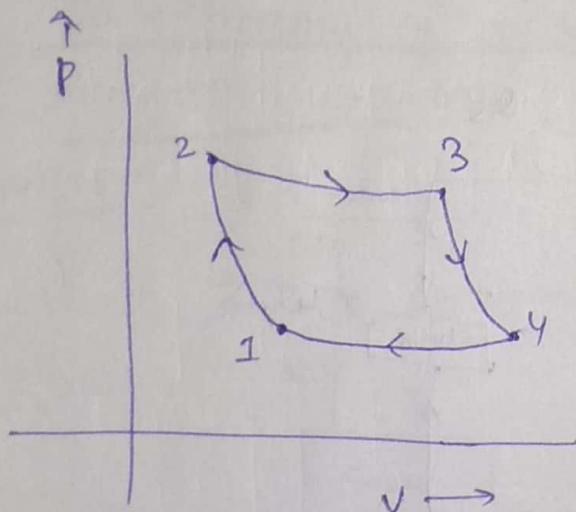
Reversible Isothermal heat addition

3-4

Reversible ~~Isothermal~~ ^{adiabatic} expansion

4-1

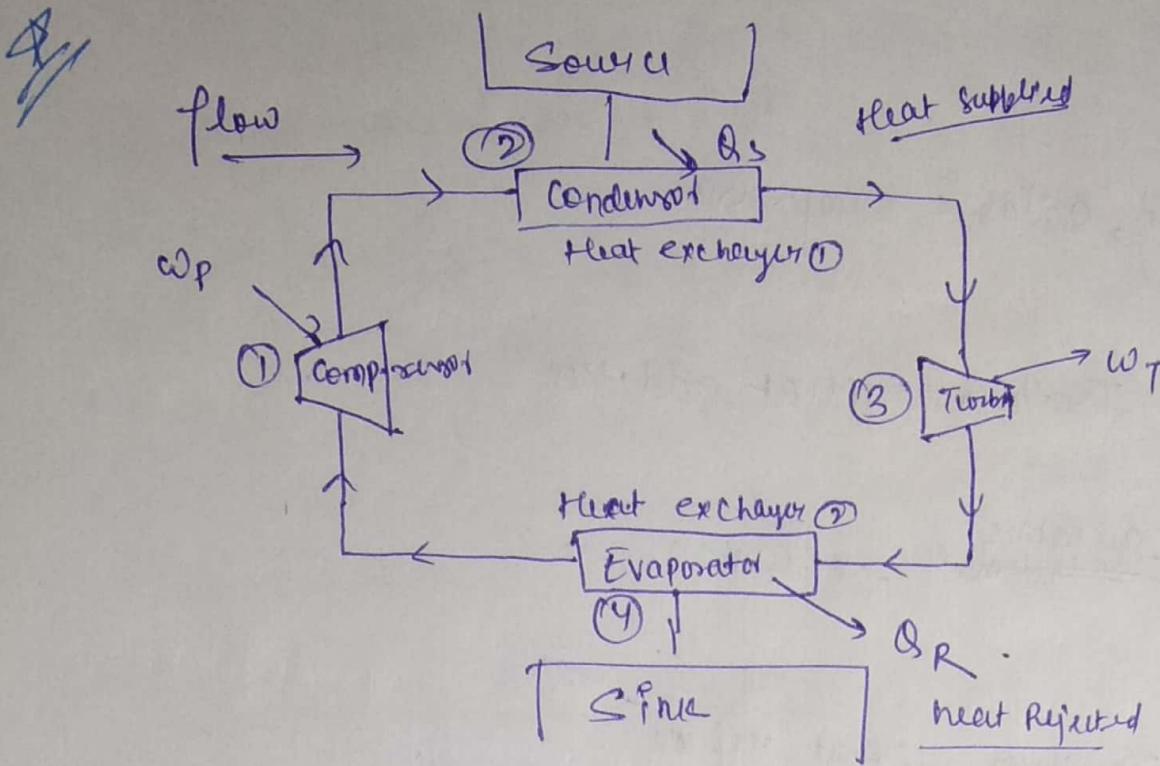
Reversible Isothermal heat rejection



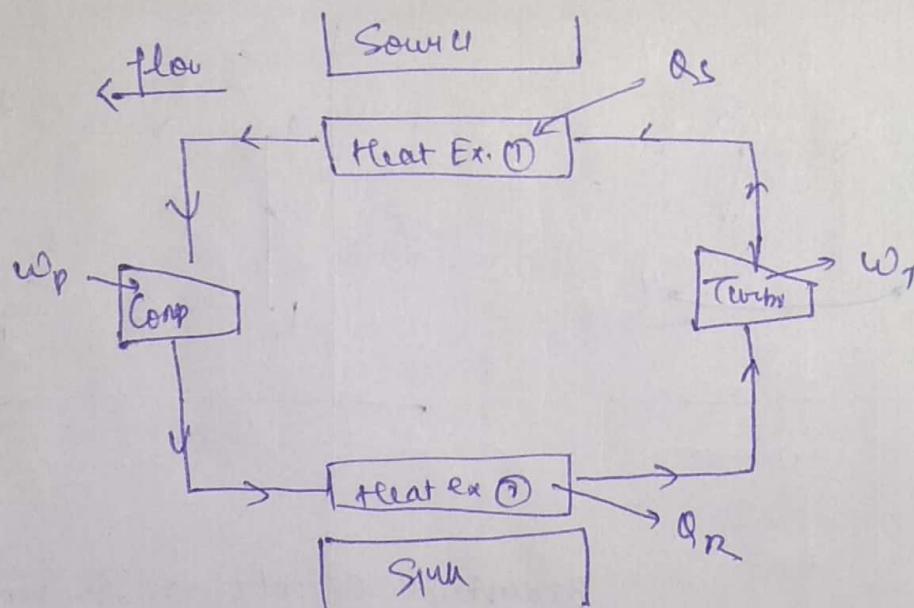
Reversible Adiabatic \Rightarrow Isentropic

Carnot cycle consist of two adiabatic two isothermal processes to realize adiabatic without insulation it must be carried out in a very fast manner and to realize Isothermal condition in single phase it must be very slow hence these combination are not possible in a cycle thus Carnot cycle is not practically feasible.

Reverse Carnot cycle



Carnot cycle



Reverse Carnot cycl.

for engine

In cyclic proce

$$(\leq Q)_{net} = (\leq w)_{net}$$

$$Q_{net} = Q_S - Q_R, \quad w_{net} = w_T - w_p$$

$$\eta = \frac{W_{net}}{Q_S}$$

For reversed Carnot cycle.

$$(\text{COP}) = \frac{D.E}{W_{net}} = \frac{D.E}{W_p - W_T}$$

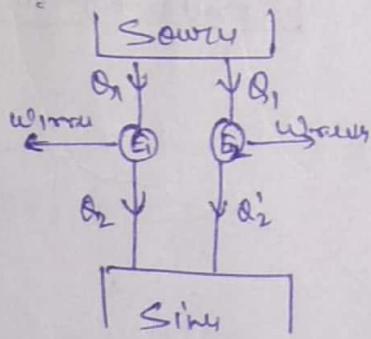
$$W_p - W_T \Rightarrow \underline{W_p \ggg W_T}$$



Carnot theorem

- 1) The efficiency of all reversible heat engines operating b/w same two reservoirs will always be the same.
- 2) The efficiency of an irreversible engine cannot exceed the efficiency of a reversible engine operating b/w the same two reservoirs.

Proof of 2)

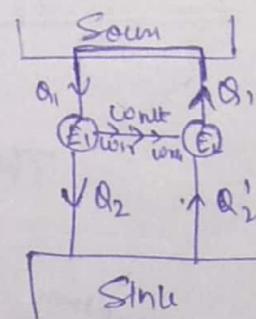


Assuming $\eta_{rev} < \eta_{irrev}$

$$\frac{W_{irrev}}{Q_1} < \frac{W_{rev}}{Q_1}$$

$$W_{irrev} > W_{rev}$$

Since, E_2 is a reversible engine
So, we can reverse it
directly.



$$W_{net} = W_{irrev} - W_{rev}$$

So, it violates the Kelvin Planck statement. because we have no need of source.

After reversing the direction of E_2 irreversible requirement can be fulfilled by reversible (Work) since $[W_{irrev} > W_{reversible}]$ and then it is net work

Output (w_{net}).

- Heat rejected by engine (E_2) is equal to the heat supplied to engine (E_1). So, we can supply heat rejected by E_2 into E_1 and thus do not require sink, and the engine is capable of producing work by exchanging heat with a single reservoir. i.e., the Violation of Kelvin's plank was statement. The assumption is wrong. Efficiency of engine is greater than η_{max} operating under same temp.

$$\boxed{\eta_{new} > \eta_{max}}$$

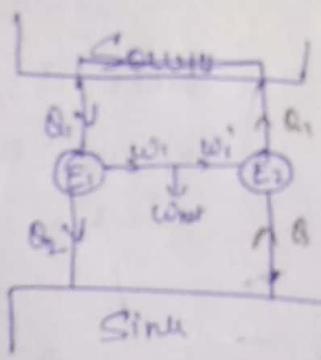
Thermodynamic Temp scale.

Proof $e(T)$

$$\eta_1 > \eta_2$$

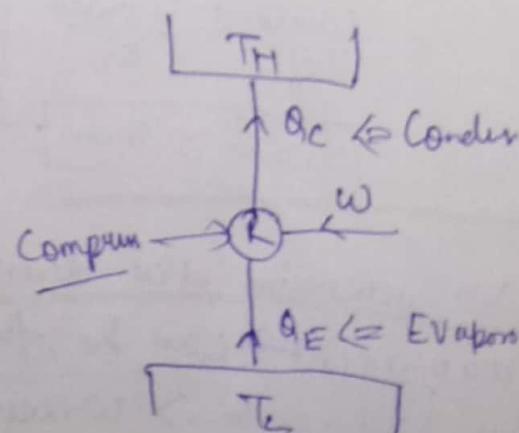
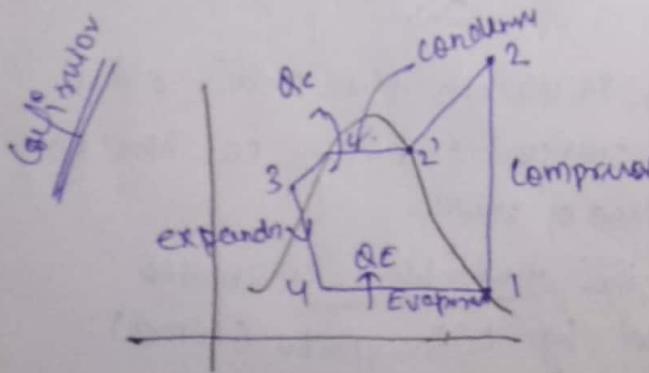
$$\frac{w_1}{Q_1} > \frac{w_2}{Q_2}$$

$$w_1 > w_2$$



$$w_{net} = w_1 - w_2$$

Then $Q_1 = Q_3 \Rightarrow$ it is violates as an plenly of



Tutorial sheet

⑧

$$\dot{Q}_S = 3000 \text{ W}$$

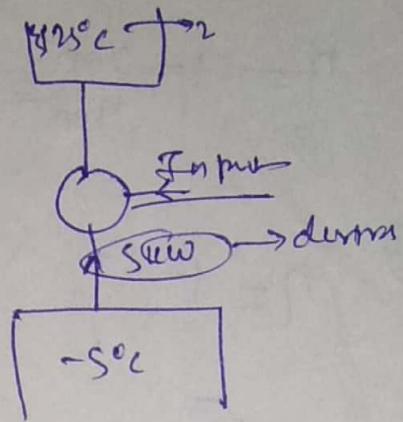
$$(COP)_{R4} = \frac{\text{desired}}{\text{Input}} = \frac{1}{\eta}$$

$$\eta = 1 - \frac{268}{298}$$

$$\eta = \frac{298 - 268}{298}$$

$$\eta = \frac{30}{298} = \frac{298}{30}$$

$$\boxed{COP = 9.9}$$



$$COP = \frac{\text{desired}}{\text{Input}}$$

$$q \cdot g = \frac{s}{w_{in}}$$

$$\cancel{q \cdot g \times 5 \text{ kW} = w_{in}}$$

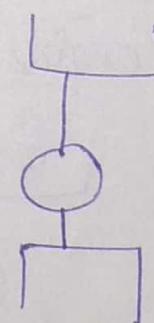
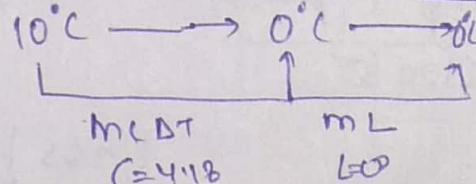
$$\boxed{49.6 \text{ kW} = w_{in}}$$

$$w_{in} = \frac{s}{q \cdot g}$$

$$\cancel{w_{in} = 0.508 \text{ kW}}$$

⑨ $(COP)_R = \frac{273}{18}$

$$= 15.1667$$



⑩ $(COP)_R = \frac{Q_E}{w_{in}}$

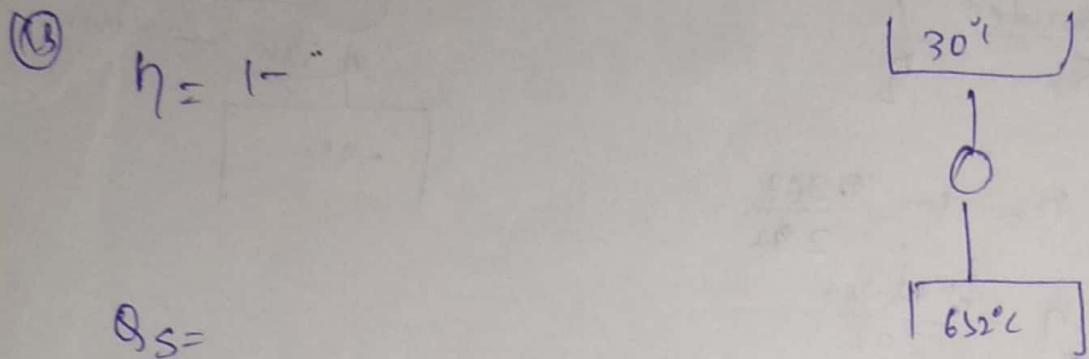
$$Q_E = mL$$

$$= \frac{1000 \times 338.5}{3600} \text{ kJ}$$

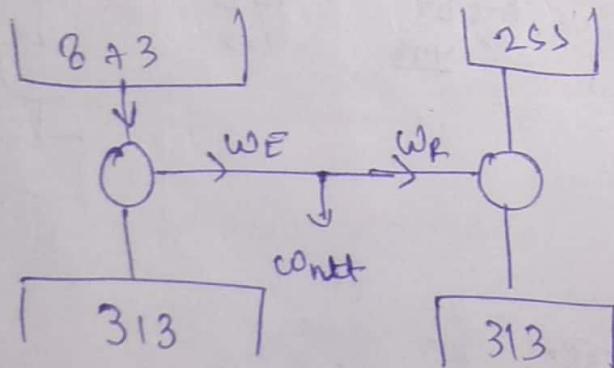
$$\boxed{Q_E = 92.6382 \text{ kJ}}$$

$$w_{in} = \frac{92.6382}{15.1667} = 6.108 \text{ kW}$$

$$\eta = 1 - \frac{200}{400} = 0.5$$



A reversible heat engine operates b/w 600°C and 40°C If the engine drives a refrigerator which operates b/w 40°C and -18°C still, there is net work output 370 kJ find out the cooling effect of the refrigerator if heat supplied to the engine 2100 kJ

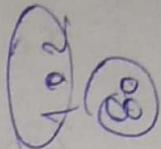


$$\eta = \frac{873 - 313}{873} = 0.642 = \frac{WE}{Q_i}$$

$$0.642 \times 2100 = WE$$

$$1348.2 = WE$$

$$\begin{aligned} w_R &= w_E - w_{out} \\ &= 1348.2 - 370 \\ &= \underline{978.2} \end{aligned}$$



$$(COP)_R = \frac{253}{313-253} = \frac{253}{50} = \underline{5.06} \quad 4.3$$

$$\frac{w_{out}}{4.3} = \frac{Q_3}{w_R}$$

$$\left(\frac{44.39 \times 928.2}{1000} = Q_3 \right) =$$

1073.

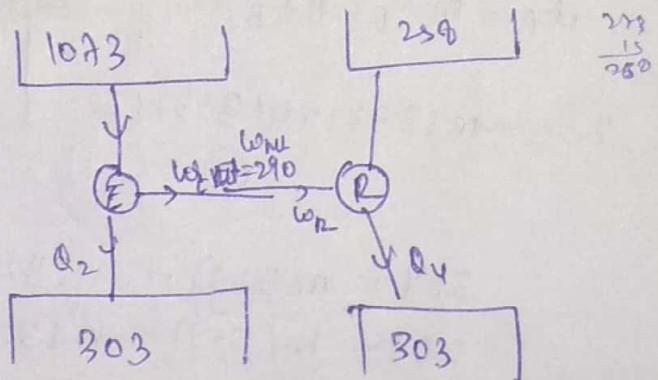
- A reversible heat engine operating b/w thermal reservoirs at 800°C and 30°C drives a refrigeration machine operating b/w -15°C and 30°C such that the heat supplied to the engine is 1900 kJ and a net work output 290 kJ determine

- (i) refrigerating effect of the refrigerator
(ii) the total amount of heat supplied to 30°C reservoir

$$\eta = \frac{1073 - 303}{1073} = \frac{770}{1073} = \underline{0.717}$$

$$\eta = 0.71 = \frac{w_E}{1900}$$

$$w_E = 0.71 \times 1900 = \underline{1363.46}$$



$$w_R = 1363.46 = \underline{1073.46}$$

$$(COP)_R = \frac{253}{45} = \underline{5.6}$$

$$17.2 = \frac{D_t}{1363.46}$$

$$\text{Set } 17.2 \times 1363.46 = D_t \quad S_A$$

$$6154.3 \quad \frac{2834.11 \times 1}{= 2818.2}$$

$$\eta = 1 - \frac{T_2}{T_1}$$

$$(Q_2 + Q_4)$$

$$\eta = 1 - \frac{Q_2}{Q_1}, \quad n_E = 1 - \frac{Q_4}{Q_2}$$

Tutorial sheetQ1

$$T = a \ln 1.83 + b$$

$$273 = a \ln 1.83 + b \Rightarrow 273 = a(0.6) + b$$

$$373 = a \ln 6.73 + b \quad \begin{array}{c} 373 = a(1.91) + b \\ - 273 = a(0.6) + b \\ \hline -100 = a(1.91 - 0.6) \end{array}$$

$$-100 = -1.31 a$$

$$\boxed{a = 76.3}$$

$$T = a \ln 2.42 + b$$

$$273 = 76.3 \times 0.6 + b$$

$$T = 76.3 \times 0.88 + 227.22 \quad 273 = 45.78 + b$$

$$T = 294.364$$

$$\boxed{T = 21.3^\circ C}$$

$$273 - 45.78 = b$$

$$\boxed{227.22 = b}$$

Q2

$$t_A = 0^\circ C = 273 \text{ K}$$

$$t_B = 373 \text{ K}$$

$$t_A = m t_B + n t_B^2 + L$$

$$273 = m(373) + n(373)^2 + L$$

①

Acc to Ques

$$t_A = 31^\circ C = 324 \text{ K}$$

$$t_B = 50^\circ C = 323 \text{ K}$$

$$324 = m(323) + n(323)^2 + L \quad \text{②}$$

$$324 = m(323) + n(323)^2 + L$$

$$273 = m(373) + n(373)^2 + L$$

$$\begin{array}{cccc} - & - & - & - \\ \hline 51 = -m(50) + n(30) \end{array} \quad \text{③}$$

$$t_A = ml$$

$$t_A =$$

③

$$O = \max_{L=0} L + O + O$$

$$100 = O + 100m + 10^n - ②$$

$S1' \neq 50^\circ C$

$$S1 = 50m + 250n \rightarrow ③$$

$$\begin{aligned} 100 &= 180m + \\ S1 \times 2 &= 50m \times 2 \end{aligned}$$

$$n = \frac{1}{2500}$$

$$m = 1.04$$

$$\begin{aligned} 10^2 &= 100m + 100n \\ 100 &= 50m + 50n \end{aligned}$$

$$2 = 5000m$$

$$m = \frac{2}{5000} = \frac{1}{2500}$$

$$d_A =$$

By the define the construction of metal.

$$1 \text{ Bar} = 10^{13} \text{ Pa}$$

④

$$P_1 V_1 = P_2 V_2$$

$$3 \times 0.18 = 0.6 \times V_2$$

$$\frac{3 \times 0.18}{0.6} = V_2^2$$

$$V_2 = \sqrt{0.9} = 0.32$$

$$\omega = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$\frac{3 \times 0.18 - 0.6 \times 0.32}{0.2-1}$$

$$\frac{-0.06 \times 10^5 \text{ N/m}^2}{24192 \times 10^9} = 29808 \text{ N/m}^2$$

$$\frac{0.6 \times 0.32}{24192 \times 10^9} = 54$$

$$\frac{0.4032}{24192 \times 10^9} = 1.67 \times 10^{-10}$$

$$\frac{0.4032}{24192 \times 10^9} = 1.67 \times 10^{-10}$$



Im draw
 $r = \frac{1}{2} m$

$$V_1 = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi (\frac{1}{2})^3$$

$P_F = 150 \text{ kPa}$

$$P_2 = 450 \text{ kPa}$$

$V_2 =$

$$P_1 V_1 = P_2 V_2$$

$$150 \times 10^3 \times \frac{4}{3}\pi (\frac{1}{2})^3 = 450 \text{ kPa} \times V_2$$

$$V \propto d^3$$

$$\frac{V_1}{V_2} \propto \frac{d_1^3}{d_2^3}$$

$P \propto d_1$

$$W = P_1 V_1 - P_2 V_2$$

$$= P(V_2 - V_1)$$

$$\frac{P_1}{P_2} = \frac{d_1^3}{d_2^3}$$

$$\frac{150}{450} = \frac{d_1}{d_2}$$

$$3 = \frac{d_1}{d_2} \cdot \frac{6^3}{d_2^2}$$

$$24 = d_2^3$$

$$d_2 = \sqrt[3]{24}$$

$$W = 150 \left(\frac{4}{3}\pi (3)^3 - \frac{4}{3}\pi \right)$$

$$150 \times \frac{4}{3}\pi \left(\left(\frac{6}{2}\right)^3 - 24 \right)$$

$$\left(\frac{6}{2} - 24 \right)$$

$$\cancel{\frac{24}{6}} \times \left(\frac{24 - 8}{24} \right)$$

$$P_1 = 150 \text{ kPa}$$

$$P_2 = 450 \text{ kPa}$$

$P \propto d^3$

$$V_1 = \left(\frac{\pi}{6}\right) \times (1)^3 = \frac{\pi}{6}$$

$$\frac{P_1}{P_2} = \frac{V_1}{V_2}$$

$$V_2 = \frac{\pi}{6} d_2^3$$

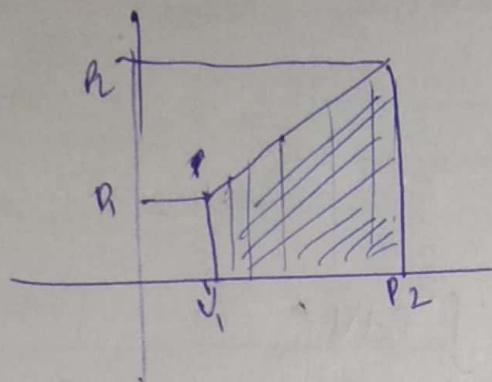
$$V \propto D^3, P \propto D^3$$

$$\boxed{P \propto V} \Rightarrow \dots$$

$$\frac{P}{V} = C$$

$$PV^{-1} = C$$

$$\omega_2 = \frac{P_1 V_1 - P_2 V_2}{n - 1}$$



$$\frac{1}{2} (150)$$

$$② \quad \omega = \int_{0.6}^V (8 - 4v) dv$$

$$150 = 8(0.6 - v) - 4(v^2 - 0.6^2)$$

$$150 = 8(V - 0.6) - \frac{4(V^2 - 0.6^2)}{2}$$

$$150 = 8V -$$

Previous Year Question 13

- ① For a closed system derive an expression for work transfer in a polytopic

According to the
Question $PV^n = C \quad \dots \text{--- } ①$

$$\text{then, } P = \frac{C}{V^n}$$

$$\text{then, Workdone} = \int_1^2 P dV$$

$$W = \int_1^2 \frac{C}{V^n} dV$$

$$= \int_1^2 CV^{-n} dV$$

$$C \left[\frac{V^{-n+1}}{-n+1} \right]_1^2$$

$$= \frac{C}{(n-1)} [V_2^{-n+1} - V_1^{-n+1}]$$

$$P_1 V_1^n = P_2 V_2^n = C$$

$$W = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

Solu.

- ② A non flow-reversible process can be written down by an eqn $P = V^2 + \frac{a}{V}$ determine the workdone if volume changes from 1 m^3 to 3 m^3

Tutorial

$$\text{Power}_{\text{ex}} = 60 \text{ W}$$

$$\text{Volume} = 86.4 \text{ m}^3$$

$$\frac{P}{F} = \frac{W}{t}$$

$$60 = \frac{W}{4 \times 60 \times 60}$$

$$6 \times 4 \times 8 \times 60 \times 60 = W$$

$$24 \times 3600 = W$$

$$\cancel{W} = 864000 = 43$$

$$864 \text{ kJ}$$

$$P = 100 \text{ kPa}$$

$$P_0 = 100 \times 10^3 \text{ Pa}$$

$$V =$$

$$\frac{P_1 V_1 - P_0 V_2}{r-1}$$

$$Q = W + \Delta E^{20}$$

$$Q = W$$

$$864 \text{ kJ} = m C_v \Delta T$$

$$\text{or } PV = mRT$$

$$m = \frac{PV}{RT}$$

$$\cancel{Q = m C_v \Delta T}$$

$$m = \frac{100 \times 10^3 \times 86.4}{0.287 \times 303}$$

$$864 \text{ kJ} = \frac{m \times 0.718 \times \Delta T}{303}$$

$$864 \text{ kJ} = \frac{98.7 \times 0.718 \times (T_2 - T_1)}{303}$$

$$\frac{864 \text{ kJ}}{98.7 \times 0.718} = T_2 - 303$$

$$\frac{864 \times 10^3}{98.7 \times 0.718} = 303 = \Delta T_2$$

$$12.19 = \Delta T$$



$$P_0 = 100 \text{ kPa}$$

$$V_0 = 20 \text{ m}^3$$

$$P = P_0 + 2(V - V_0)^2$$

$$\left. \begin{array}{l} P_1 = 100 \text{ kPa} \\ V_1 = 15 \text{ m}^3 \\ T_1 = 20^\circ \text{C} \end{array} \right| \quad \left. \begin{array}{l} P_2 = 150 \text{ kPa} \\ V_2 = 25 \text{ m}^3 \\ T_2 = ? \end{array} \right.$$

$$\frac{100 \times 15}{243} = \frac{150 \times 25}{T_2} \Rightarrow T_2 =$$

$$\frac{150 \times 25}{100 \times 15} \times 293 = \frac{25 \times 293}{10} = 733 \text{ K}$$

For Ideal Gas

$$C_p = 1.003 \text{ kJ/kgK}$$

$$C_V = 0.718 \text{ kJ/kgK}$$

$$R = 0.287 \text{ kJ/kgK}$$

24
36

273
303

$$m = \frac{100 \times 10^3 \times 86.4}{0.287 \times 303}$$

$$864 \text{ kJ} = \frac{m \times 0.718 \times \Delta T}{303}$$

$$864 \text{ kJ} = \frac{98.7 \times 0.718 \times (T_2 - T_1)}{303}$$

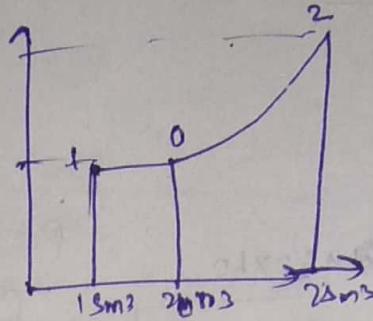
$$\frac{864 \text{ kJ}}{98.7 \times 0.718} = T_2 - 303$$

$$8.8 = \Delta T$$

$$12.19 = \Delta T$$

$$\text{Ansatz} \quad P = P_0 + 2(V - V_0)^2$$

$$w_0 =$$



$$P(V_1, V_2)$$

$$= \int_{20}^{25} P_0 + \int_{20}^{25} \left(\frac{V-20}{3}\right)^2$$

$$= P_0(25-20) + \frac{(25-20-20)^3}{3} \times \frac{28-20}{2}$$

$$\omega = \omega_{1-0} + \omega_{0-2}$$

$$\omega_{10} = 5 \times 100 = \underline{500}$$

$$P_0(100 \times 5) + \frac{(5-20)^3}{3} \times \frac{5}{2}$$

$$500 + \frac{125 \times 5}{2}$$

$$500 + \frac{625}{6}$$

$$\frac{3000 + 625}{6}$$

$$\omega_{0-2} = \int_{20}^{25} P dV$$

$$= \int_{20}^{25} P_0 + 2(V-20)^2$$

$$(100 \times (25-20)) + 2 \left(\frac{V-20}{3}\right)^3$$

$$= 100 \times 5 + 2 \left(\frac{(25-20)^2 - 20}{3}\right)^3$$

$$= 500 + \frac{2}{3} [(5^2 - 20)^3]$$

$$500 + \frac{2}{3} [25-20]^3$$

$$500 + \frac{125}{3}$$

$$\frac{1500 + 125}{3} = \frac{1625}{3} = \underline{503}$$

$$= 500 + \frac{833}{5}$$

$$= \underline{583.3}$$

$$Q + W = DE$$

$$Q + 4340 = DE$$

$$\begin{aligned} Q &= 10 \times DE \\ Q &= 4340 \times DE \\ DE &= -4340 \end{aligned}$$

(2-3)

$$42000 \leftarrow DE$$

$$\begin{aligned} \sum Q &= Q_{12} + Q_{23} + Q_{34} + Q_{41} \\ (-340 \times 200) &= Q_{41} \end{aligned}$$

Process

$$Q (\text{KJ/mm})$$

$$W (\text{KJ})$$

$$DE (KJ)$$

1-2

$$0$$

$$4340$$

$$-4320$$

2-3

$$42000$$

$$0$$

$$42000$$

3-4

$$-4200$$

$$69000$$

$$-3200$$

4-1

$$\sum Q = Q_{12} + Q_{23} + Q_{34} + Q_{41}$$

$$-340 \times 200 = 0 + 42000 + 4200 + Q_{41}$$

$$-68000 = 42000 + 4200 = Q_{41}$$

$$\rightarrow \text{Total} = Q_{41}$$

$$\sum Q = \sum W$$

$$-68000 = W_{12} + W_{23} + W_{34} + W_{41}$$

$$-68000 + 4340 - 69000 = W_{41}$$

$$-141340 = Q_{41}$$

$$(\sum E)_{\text{cycle}} = 0$$

$$E_{12} + E_{23} + E_{34} + E_{41} = 0$$

$$-4340 + 42000 - 73200 + E_{41} = 0$$

$$E_{41} = 35540$$

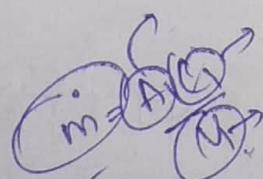
$$\text{Ratio } W_0 = \frac{-141340}{-340}$$

closed system

Note For a cyclic process area enclosed on P.V diagram is equal net work transfer.

For closed system $\dot{Q}_{\text{in}} + \dot{W}_{\text{out}} + \dot{E} = 0$

C.R.



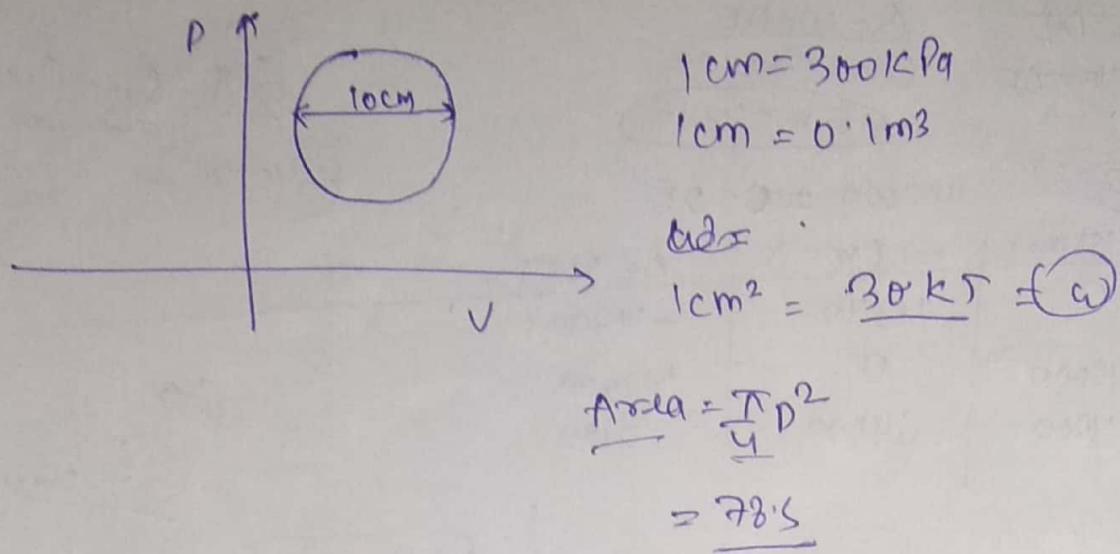
$$\begin{aligned} \dot{Q}_1 &= m(h_2 - h_1) \\ \dot{V}_1 &= \dot{V}_2 \\ \dot{P}_1 &= \dot{P}_2 \\ \dot{T}_1 &= \dot{T}_2 \end{aligned}$$

$$\dot{Q} = \int \dot{V} dh$$

$$\dot{Q} = m(h_2 - h_1)$$

$$\dot{W} = - (h_2 - h_1)$$

(8)



$$1 \text{ cm} = 300 \text{ kPa}$$

$$1 \text{ cm} = 0.1 \text{ m}^3$$

$$\omega = \dots$$

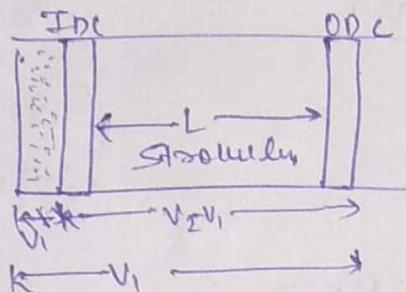
$$1 \text{ cm}^2 = 30 \text{ kT} \text{ if } \omega$$

$$A = 0.12 \text{ m}^2$$

$$P_1 = 1.5 \text{ MPa}$$

$$P_2 = 0.15 \text{ MPa}$$

$$(V_2 - V_1) = \frac{A \omega \Delta P}{\rho g} \times L$$



$$A \omega \Delta P = \frac{1}{2} (P_1 + P_2) (V_2 - V_1)$$

$$= \frac{1}{2} (1.5 + 0.15) \times 10^6 (0.12) \times 0.30$$

$$= \frac{1}{2} (1.65) \times 0.12 \times 10^6$$

(10)

$$P = \frac{S}{V} + 1.5$$

$$\int W = \int_{0.05}^{0.03} P dV$$

$$= \frac{S}{V} + 1.5 V$$

~~$$(\rightarrow S \cdot 0.05 + 1.5 \cdot 0.05^2 - (\rightarrow S \cdot 0.03 + 1.5 \cdot 0.03^2))$$~~

$$W = S \log V + 1.5 V^2$$

$$S \log \frac{0.03}{0.05} + 1.5 [(0.03)^2 - (0.05)^2]$$

$$- S \times 0.48 + 0.75 [0.0025 - \frac{0.0225}{0.0025}]$$

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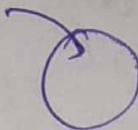
$$- S \times 1.10 + 0.75 [1.5 \times 0.01]$$

$$= - S \cdot 5.4 + 1.5 \times 0.1 = - S \cdot 5.4 + 0.15 = \underline{5.25}$$

$$-5.64 \times 10^5 \text{ bar m}^3$$

$$\frac{-5.64 \times 10^5}{10^3}$$

$$= -564.3 \times 10^2 = \underline{564.3 \text{ kJ}}$$



$$\underline{Q = -45 \text{ kJ}}$$

$$-45 + 564.3 = \Delta U$$

$$\boxed{519.3 \text{ kJ} = \Delta U}$$

$$\Delta H = \Delta U + n(PV)$$

$$\Delta H = 519.3 + \Delta R_{\text{ext}} V_2 - P_2 V_1$$

$$P_1 = \frac{S}{V_{0.05}} + 1.3 \quad P_2 = \frac{S}{0.15} + 1.3$$

$$\underline{101.5 \times 10^2} = 333 + 1.3 = \underline{34.8 \times 10^2}$$

$$\Delta H = \cancel{\Delta U} + 519.3 + \cancel{(34.8 \times 0.15)^2} + 101.5 \times 0.05 \times 10^2$$

$$= (5.22 - 0.507)$$

$$+ 4.71$$

$$519.3 + 4.71$$

$$= \underline{524.45}$$

$$(11) \quad C_p = 1.3 + \frac{T_2}{T_1 + T_2}$$

$$\underline{dT} = \int_{T_1 = 20^\circ\text{C}}^{T_2 = 260^\circ\text{C}} C_p dT$$

$$\underline{dQ} = \int_{T_F = 20^\circ\text{C}}^{T_B = 260^\circ\text{C}} C_p dT$$

$$Q = \underline{\Delta U + W}$$

(12)

$$V = 0.2 \text{ m}^3$$

$$P_1 = 4 \text{ kPa}$$

$$P_2 = 1.02$$

$$T = 130^\circ\text{C}$$

$$\gamma = \frac{CP}{CV} = \frac{1}{0.314}$$

~~Ans~~

$$P_1 V_1^{\gamma} = P_2 V_2^{\gamma}$$

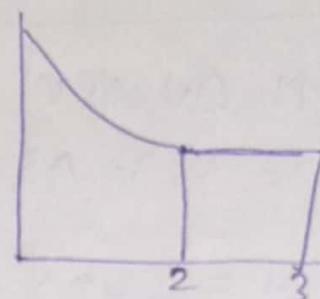
$$4 \times 10^{-2}^{1.4} = 1.02 V_2^{1.4}$$

$$\frac{4}{1.02} (0.2)^{1.4} = V_2^{1.4}$$

$$3.92 \times 0.16 = V_2^{1.4}$$

$$V_2 = 1.4 \sqrt{3}$$

$$\frac{P_2}{V_2}$$



$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{1-\gamma}{\gamma}}$$

$$T_2 = T_1 \left(\frac{P_2}{P_1} \right)^{\frac{1-\gamma}{\gamma}}$$

$$(T_2 = 272.32 \text{ K})$$

$$m = \frac{P_1 V_1}{RT_1}$$

$$h_3 - h_1 = m(C_p(T_3 - T_2))$$

$$72.5 = 0.644 \times 1 \times (272.32 - 272.32)$$

$$(T_3 = 326.79 \text{ K})$$

$$\frac{V_2}{T_2} = \frac{V_3}{T_3}$$

$$V_3 = 0.733 \text{ m}^3$$

$$w_{1-2} = \frac{P_1 V_1 - P_2 V_2}{\gamma-1} =$$

$$w_{23} = P_2 (V_3 - V_2) = 1.02 \times 10^3 (\sim)$$

$$w = 83454$$

for poly tropic process

$$W_{1 \rightarrow 2} = \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$85454 = \frac{4 \times 10^5 \times 0.53 - 1.02 \times 10^5 \times 0.93}{n-1}$$

$$n-1 = \frac{4 \times 10^5 \times 0.53 - 1.02 \times 10^5 \times 0.93}{85454}$$

$$n = 1 + \frac{4 \times 10^5 \times 0.53 - 1.02 \times 10^5 \times 0.93}{85454}$$

$$\boxed{PV = mRT}$$
$$V_F = \frac{mR\bar{T}}{P}$$

$$\boxed{R = \frac{8.314}{30}}$$

$$(13) \quad PV^{1.3}$$

$$P_1 V_1^{1.3} = P_2 V_2^{1.3}$$

~~isobar~~

$$P_1 V_1^{1.3} = P_2 V_2^{1.3}$$

$$\boxed{V_2^{1.3} = \frac{P_1 V_1^{1.3}}{P_2}}$$

$$\boxed{T_2 = T_1 \left(\frac{V_1}{V_2} \right)^{1.3}}$$

$$C_P = C_V = R$$

$$C_P = R = C_V$$

$$\boxed{1.33 - \cancel{R} = C_V}$$

$$\boxed{\frac{C_P}{C_V} = \gamma}$$

$$DQ = n \bar{q} + w$$

~~DQ~~

$$\boxed{(DQ)_{poly} = SW \times \left(\frac{\gamma - 1}{\gamma - 1} \right)}$$

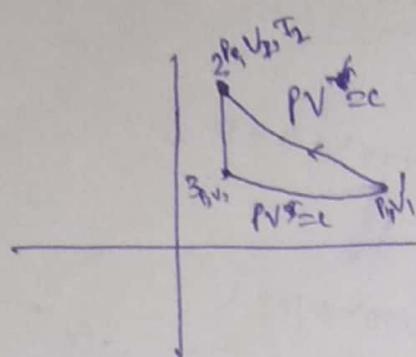
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Q14

$$V_1 = 0.1 \text{ m}^3$$

$$T_1 = 300 \text{ K}$$

$$P_1 = 1 \text{ bar}$$



$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$\frac{P_1 V_1^\gamma}{P_2^\gamma} = V_2^\gamma$$

$$1 \times (0.1)^{1.4} = V_2$$

$$\boxed{V_2 = 0.023 \text{ m}^3}$$

$$R = \text{constant} \rightarrow \frac{P}{RgT}$$

$$\gamma = \frac{C_P}{C_V} = \frac{14.3}{102} =$$

$$\frac{C_P - C_V}{C_V} = R$$

$$14.3 - 102$$

$$\boxed{4.1 = R}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1} \right)^{\frac{1}{\gamma-1}}$$

$$\boxed{T_2 = 543.43 \text{ K}}$$

$$\frac{102 \times 10^3}{4.1 \times 300} = m$$

$$\frac{10^2 \times 10^3}{0.102 \times 300} = m$$

$$\frac{10^5}{0.102 \times 300} = m$$

$$\boxed{m = 0.1161 \text{ kg}}$$

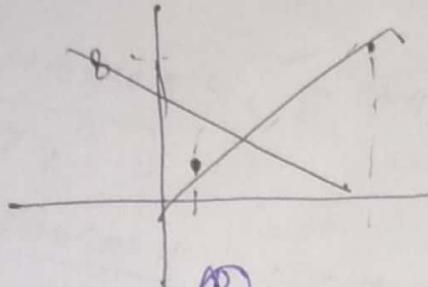
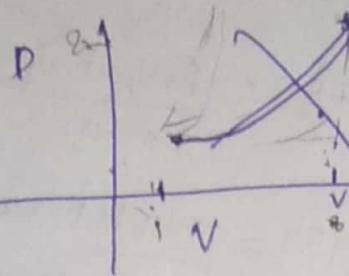
Ans:

$$w_{1-2} = \frac{P_1 V_1 - P_2 V_2}{\gamma-1}$$

$$w_{2-3} = 0$$

$$w_{3-1} = P_1 V_1 \ln \left(\frac{V_3}{V_1} \right)$$

$$w = \frac{P_1 V_1 - P_2 V_2}{\gamma-1} + P_1 V_1 \ln \left(\frac{V_3}{V_1} \right)$$



$$\frac{102}{14.3} = \frac{102}{102}$$

$$W = \frac{100 \times 0.1 - 800 \times 0.23}{1.4 - 1} + 0.1 \times 0.23 \times \ln\left(\frac{0.01^3}{0.23}\right)$$

$$= \frac{-21 + 14.85}{-6.31}$$

$$P_3 V_3 = P_1 V_1$$

$$\boxed{P_3 = \frac{P_1 V_1}{V_3}} \Rightarrow 4.73 \text{ bar.}$$

$V_3 = V_2$

$$= \frac{1 \times 0.1}{0.023}$$

$$\text{or } \frac{P_3}{T_3} = P$$

$$C_p \cdot C_v = R$$

~~Cp~~

$$\begin{aligned} \Delta H &= m v dT \\ &= 0.1161 \times 0.718 \times (T_3 - T_2) \\ &= 0.1161 \times 0.718 \times (43 - 300) \\ \text{on } &= 0.1161 \times 0.718 \times 243 \end{aligned}$$

$$C_p = \frac{0.005}{0.287}$$

~~(0.287)~~

~~0.718~~

By cyclic process

$$\boxed{\sum Q = \sum W} \Rightarrow 5.43 \text{ kJ}$$

⑥ $T_1 = 300$

$$T_2 = 1030 \text{ K}$$

$$T_2 = T_3 = 1050 \text{ K}$$

$$W_{\text{ext}} = W_2 + W_{23} + W_{31}$$

$$P_2 V_2 \ln\left(\frac{V_3}{V_2}\right) + P_1 (V_2 - V_3)$$

$$P_3 V_3 \ln\left(\frac{V_1}{V_3}\right) + P_1 (V_3 - V_1)$$

$$m P_1 V_1 \ln\left(\frac{V_1}{V_2}\right) + P_1 (V_1 - V_2)$$

