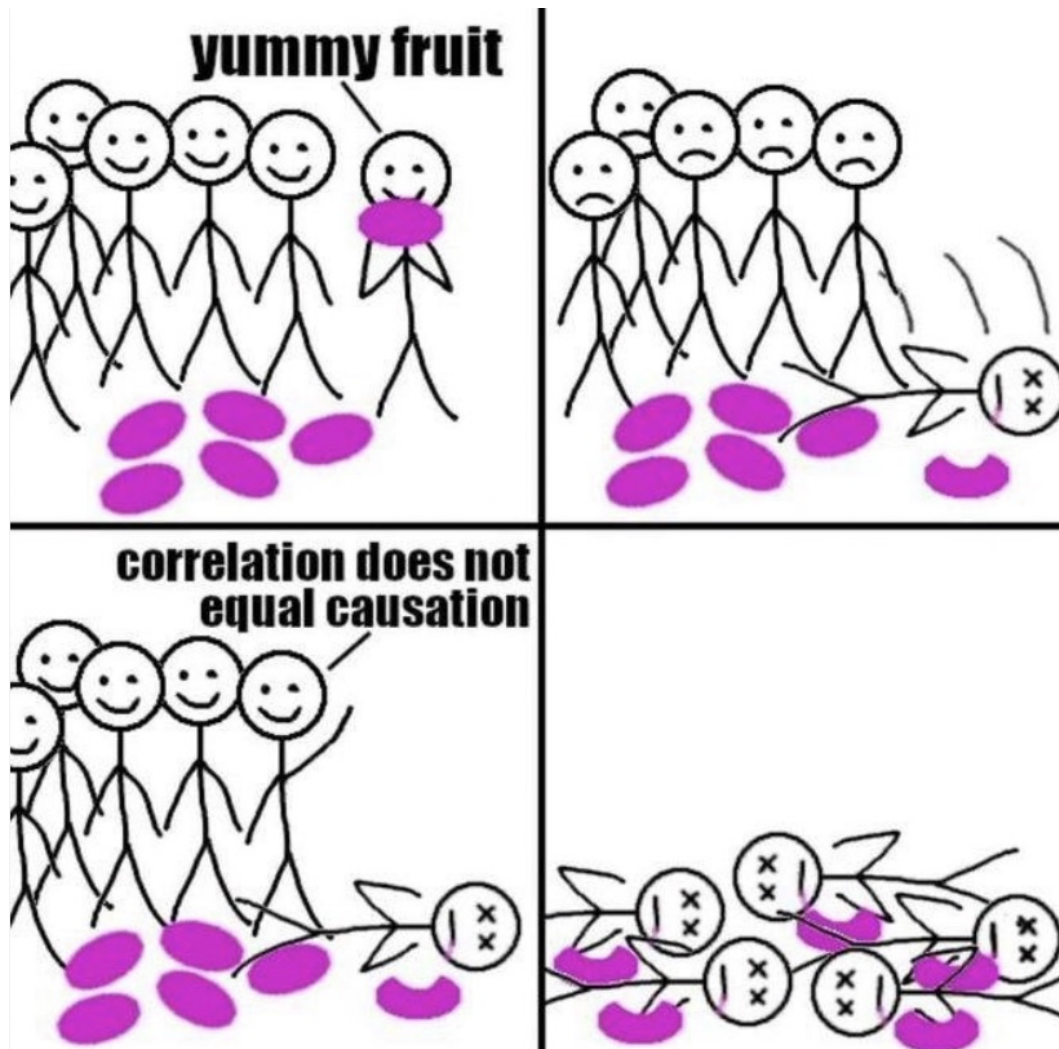


6th July 2023

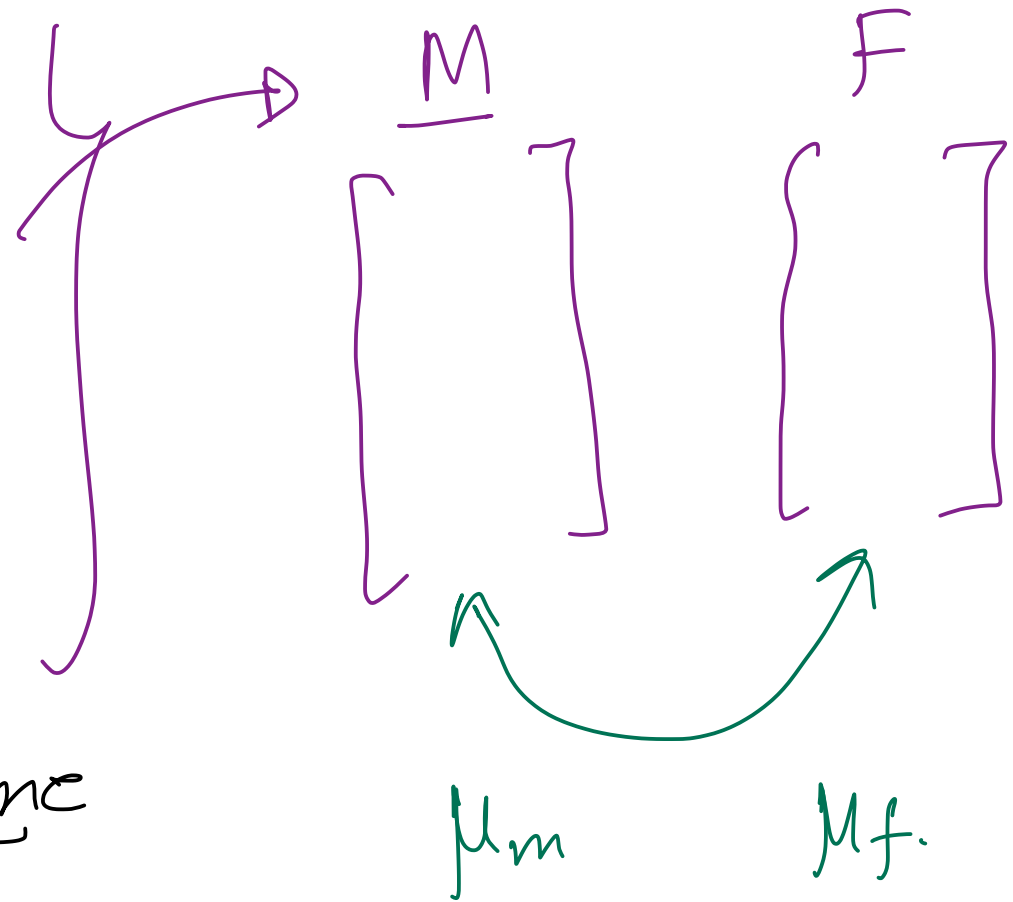
Correlations



let's start
@
9:05

① Num. v/s Cat. \rightarrow t test, z test

Gender	Income.
M	80 K
F	90 K
M	80 K
F	75 K.



②

id.

<u>Education level</u>	<u>Income</u>
1	70K
2	65K
3	59K
4	!

6

ANOVA

$\alpha = 0.05$

③ Cat vs Cat → Chi².

④ Num. w/ Numerical :

App. ID
↓
unique to
every cust.

Education

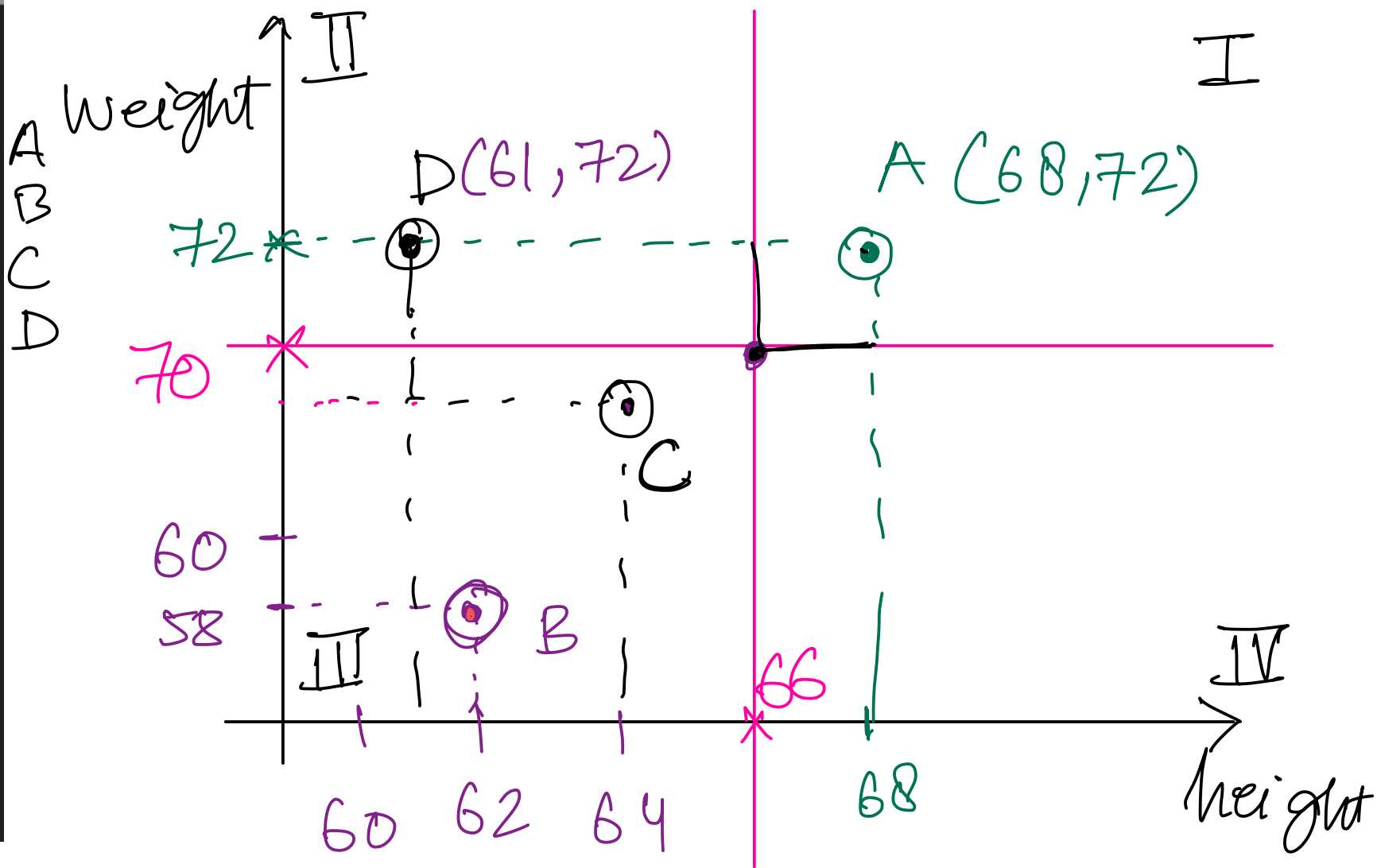
Income

Loan Amt

(Numerical) (Numerical)
var. (var.)

↓
If associated
how much?

Height (inches)	Weight (kg)	
68	72	
62	58	
64	67	
61	72	
70	79	
66	61	
61	68	
65	64	
71	80	
72	79	
$\bar{h} = 66$	$\bar{w} = 70$	



$$(68 - 66) \times (72 - 70) = (+2)(+2) = +4$$

$$(62 - 66) \times (58 - 70) = (-4)(-12) = +48$$

$$(64 - 66) \times (67 - 70) = (-2)(-3) = +6$$

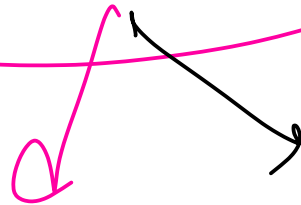
$$(61 - 66) \times (72 - 70) = (-5)(+2) = -10$$

$$(4 + 48 + 6 - 10 + \dots + 60)$$

$$(4 + 48 + 6 - 10 - - - -)$$

10

Covariance



trend

:

tve
↓

-ve

↓ y trend.

↑ y relationship
b/w var

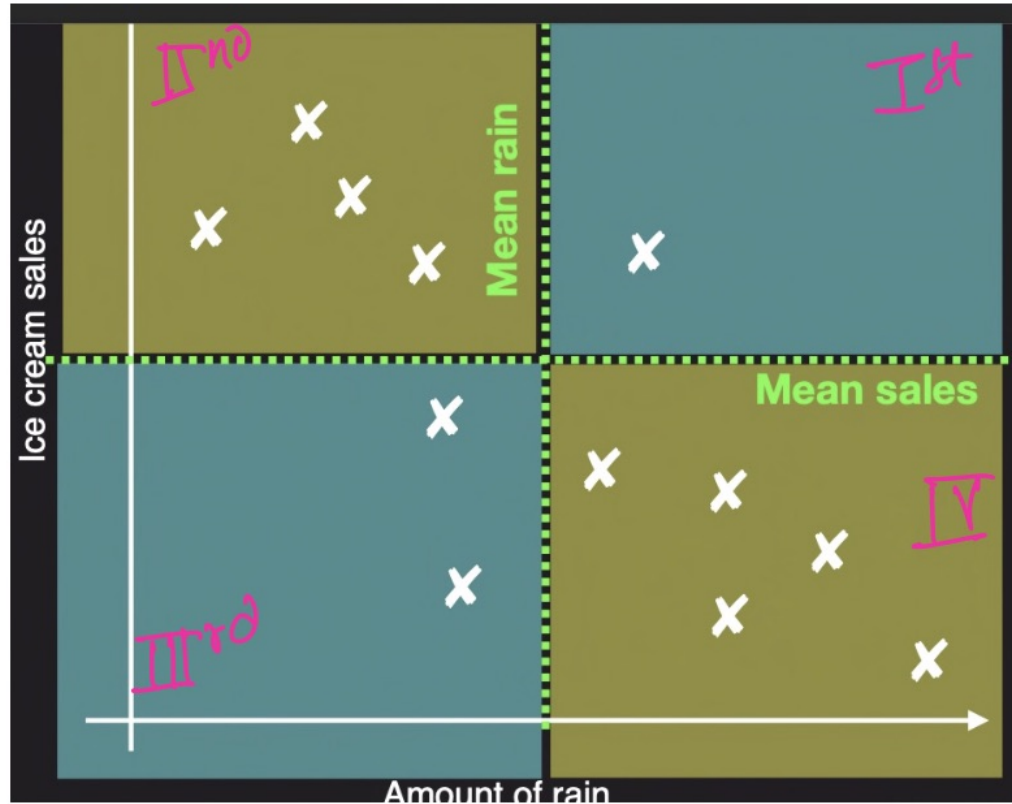
$$\text{Corr.}(x, y) = \frac{\sum_{i=1}^{10} (x_i - \bar{x}) \cdot (y_i - \bar{y})}{n}$$

$$\begin{array}{l} 1 \rightarrow (x_1, y_1) \\ 2 \rightarrow (x_2, y_2) \\ 3 \\ \vdots \\ 10 \end{array} \left. \begin{array}{l} (x_i, y_i) \\ n=10 \end{array} \right\}$$

Corr +ve

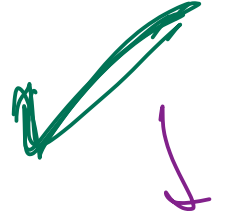
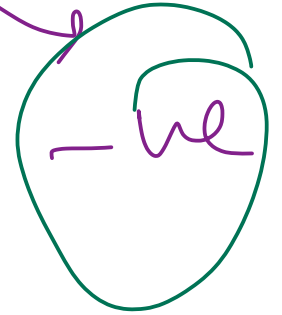
I & III
more pts

Ice cream v/s Rain :



Covariance

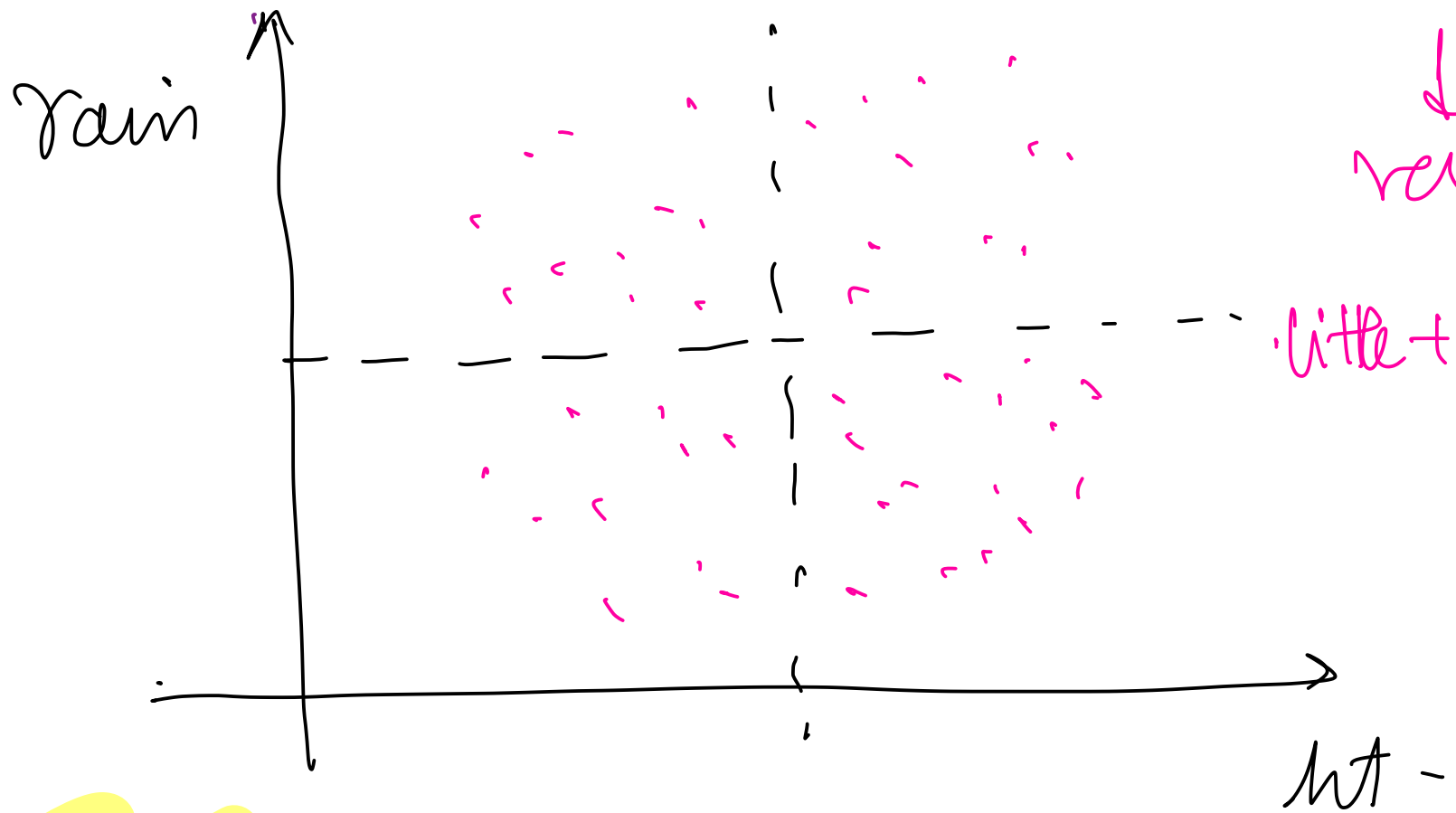
+ve



more
pts
is
in
IInd
IV

magnitude of Cov. =
$$\frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{n}$$

height v/s Amt. of Rain.



Cov. ≈ 0

↓
very low

little +ve or -ve

Covariance $\in (-\infty \text{ to } +\infty)$

↪
$$\frac{1}{n} \sum (x_i - \bar{x})(y_i - \bar{y})$$

Cov.

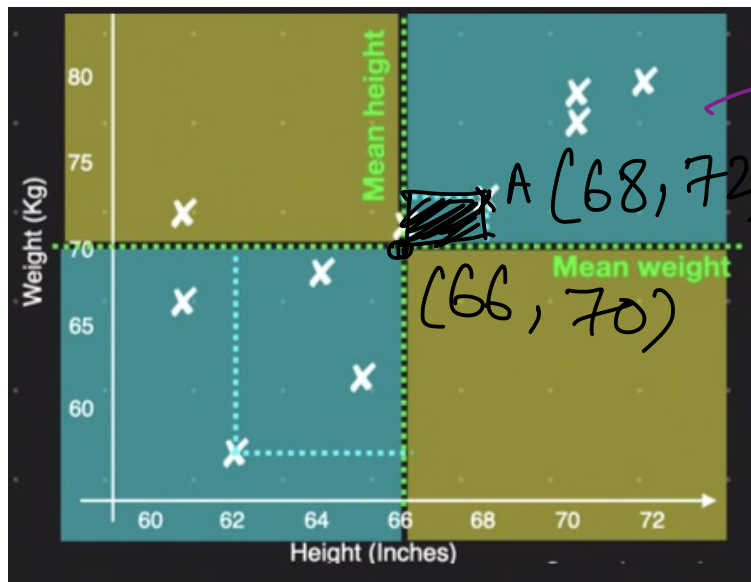


-1000 → Bhart.

-2000 → Vi bhav

Scale or units of
the variables

Not the std. qty. to quantify
linear trend.



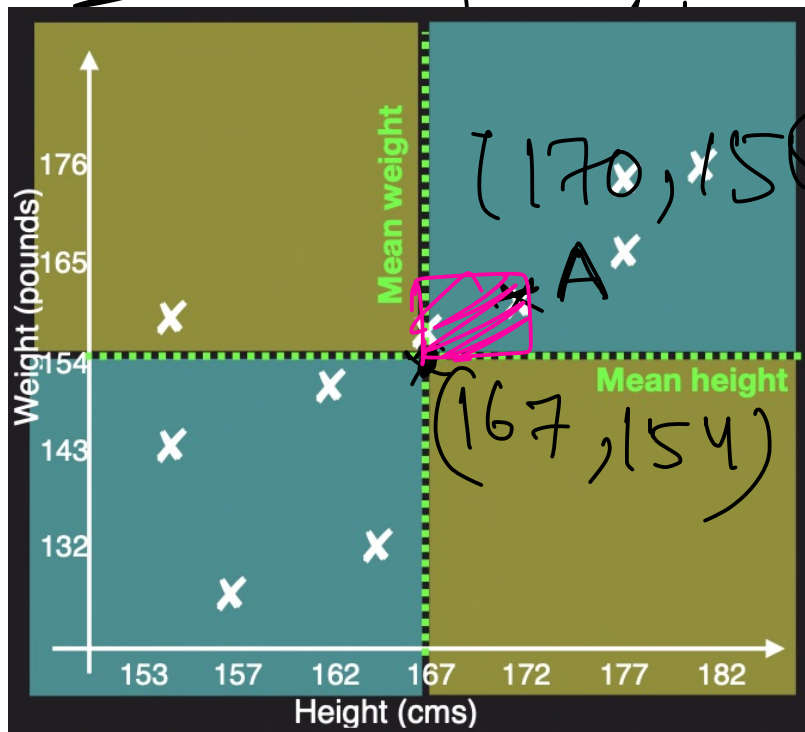
Bharat \rightarrow COV_1

$$A: (68 - 66) \cdot (72 - 70) \\ = +2 \times +2 = +4$$

Sagar \rightarrow weight \rightarrow Pounds

$\rightarrow 1 \text{ Kg} = 2.2 \text{ pounds}$

$\rightarrow 1 \text{ inch} = 2.5 \text{ cm}$



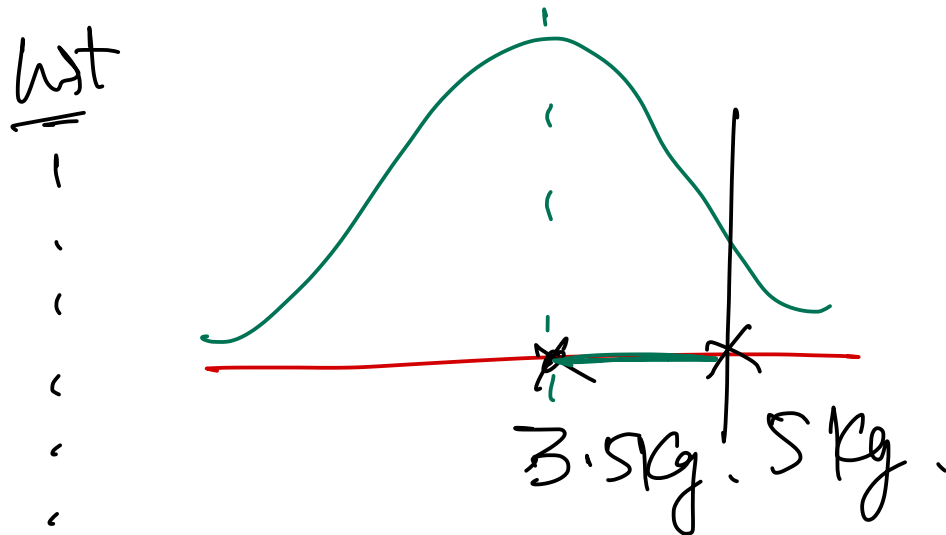
Sagar \rightarrow COV_2

$$A = (68 \times 2.5 \text{ cm}, \\ 72 \times 2.2 \text{ pounds})$$

$$A = (170 \text{ cm}, 158.4 \text{ pounds})$$

$$\begin{aligned}
 \text{Area}(A) &= (170 - 167) \times (158.4 - 154) \\
 &= 3 \times 4.4 \\
 &= 13.2
 \end{aligned}$$

* Pediatrician : (wt, ht, health)



5kg

Z score
↓
+1.1

Z score = 0

Z score = -1.2

$$Z_w = \left(\frac{w - \bar{w}}{\sigma_w} \right)$$

$$Z_w = 0$$

$$w_{child} = w_{avg.}$$

$$\downarrow$$

$$3.5$$

$$\downarrow$$

$$3.5 \text{ kg}$$

avg. wt. baby

$$Z_w = 0$$

$$Z_w \rightarrow +1.1 \rightarrow \text{over weight.}$$

$$Z_w \rightarrow -1.5 \rightarrow \text{under weight.}$$

std. qty

*

$$\text{Cov.} = \frac{1}{n} \sum (x_i - \bar{x}) (y_i - \bar{y})$$

not std. qty.

$$\frac{1}{n} \sum \frac{(x_i - \bar{x})}{\sigma_x} \cdot \frac{(y_i - \bar{y})}{\sigma_y}$$

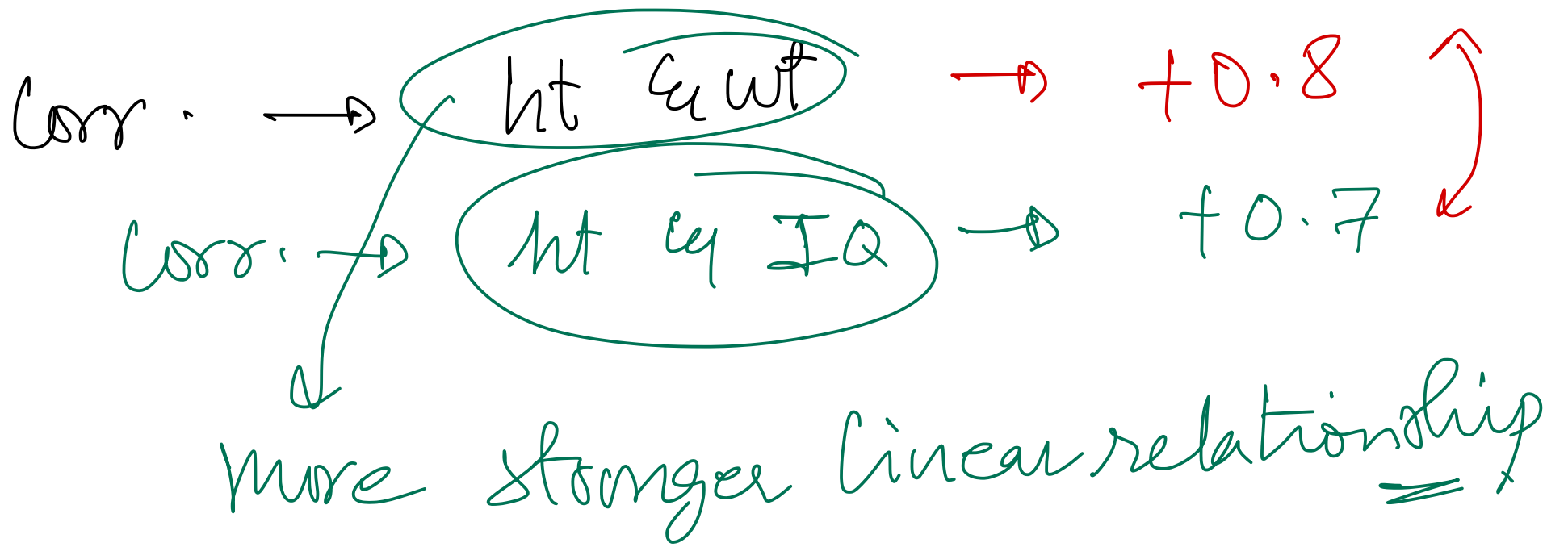
Correlation

$\rightarrow S_{xy}$

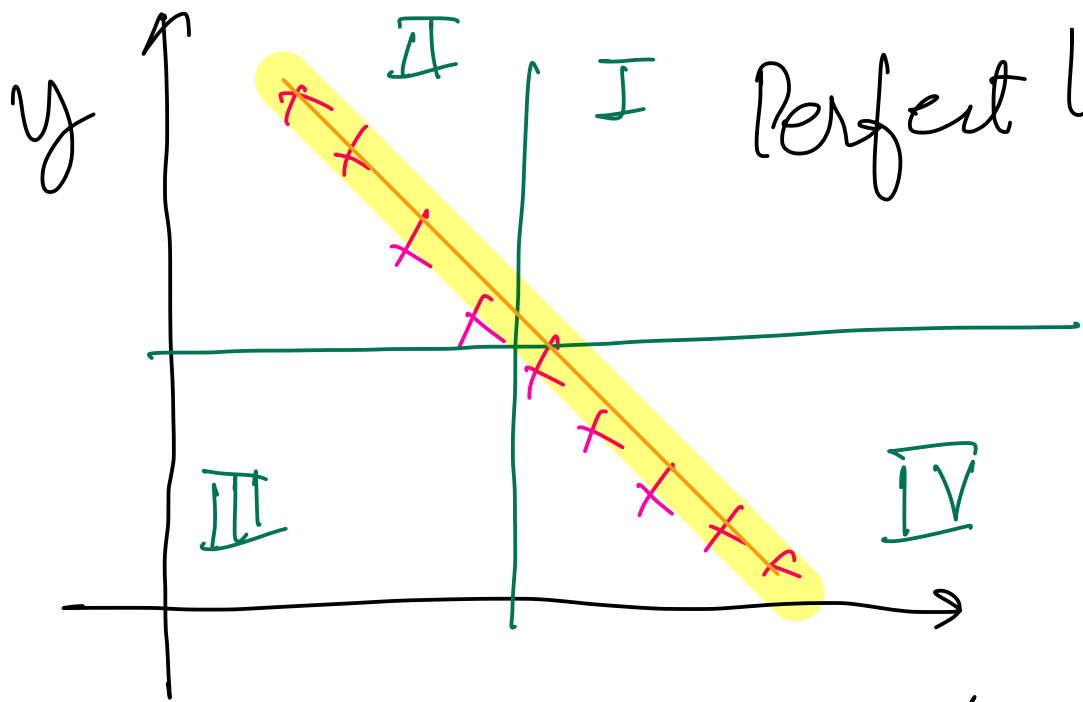
Pearson
Correlation

Cov. $\rightarrow \in (-\infty \text{ to } \infty)$

Correlation $\in (-1 \text{ to } +1)$



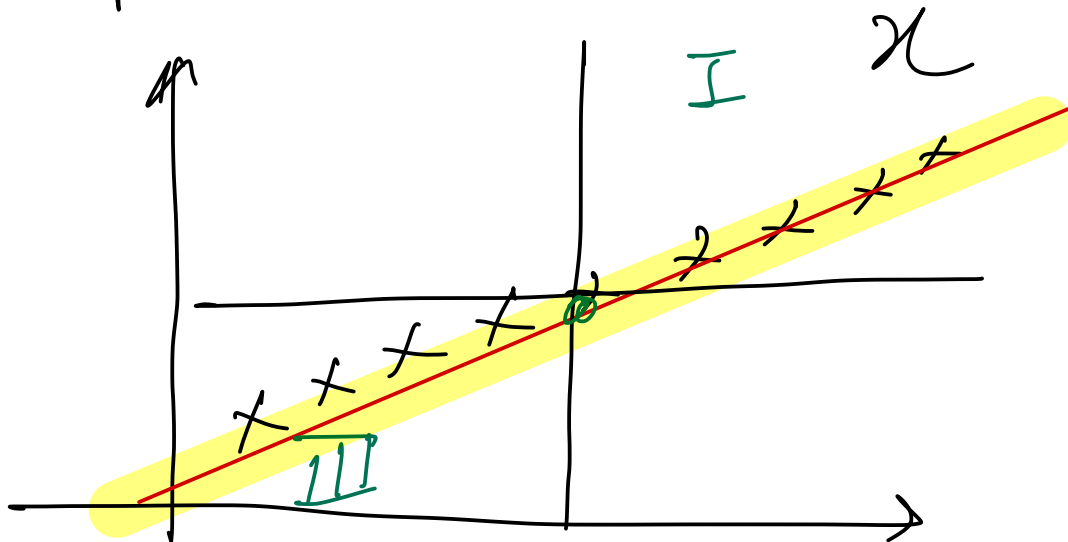
Strenght of linear relationship : Correlation



Perfect linear relationship

→ Covar → min

Corr. = -1



Covar → max

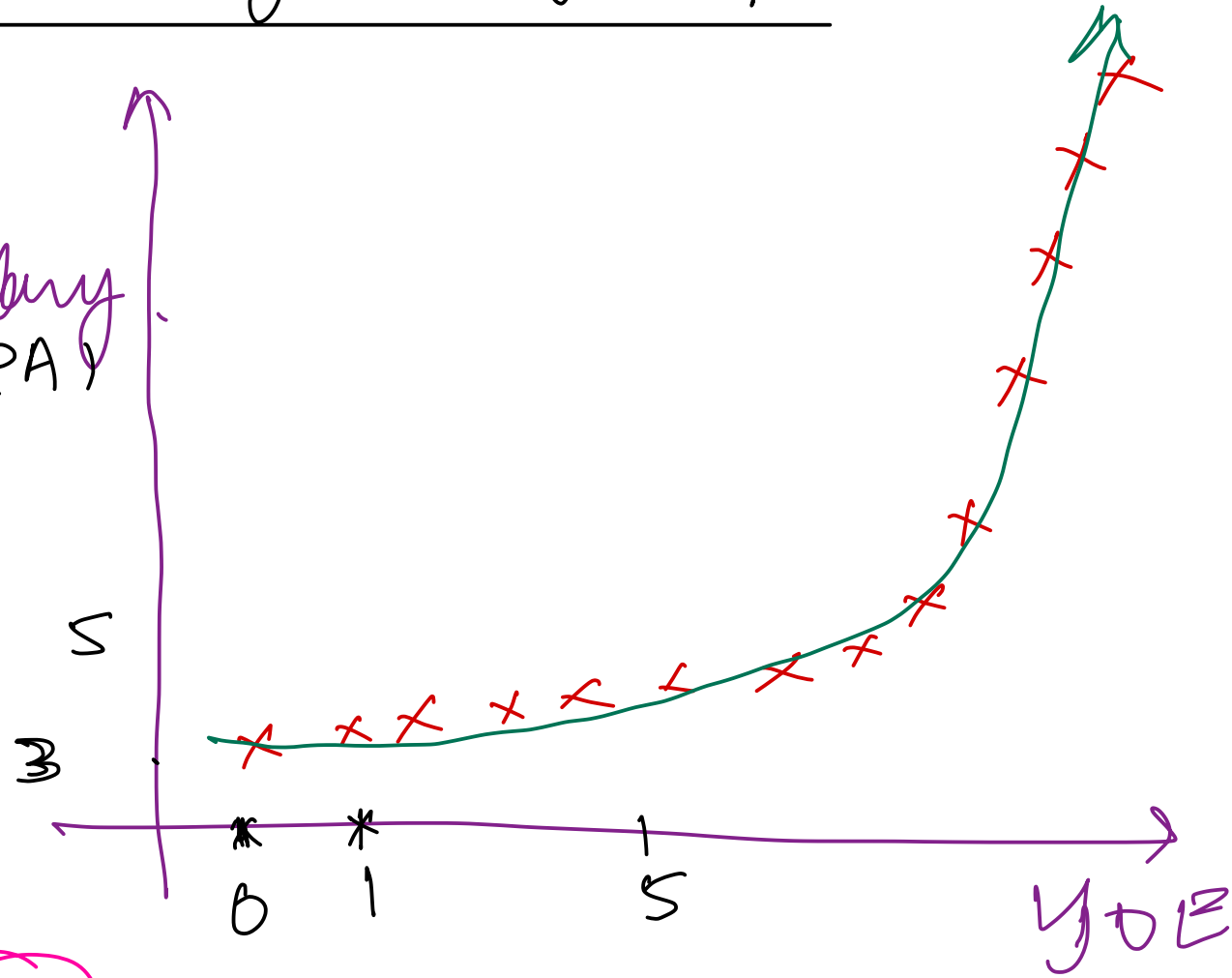
Correlation = +1

* Salary grows w/ years of Exp.:

↓
linear. → y
 → N

Salary
(LPA)

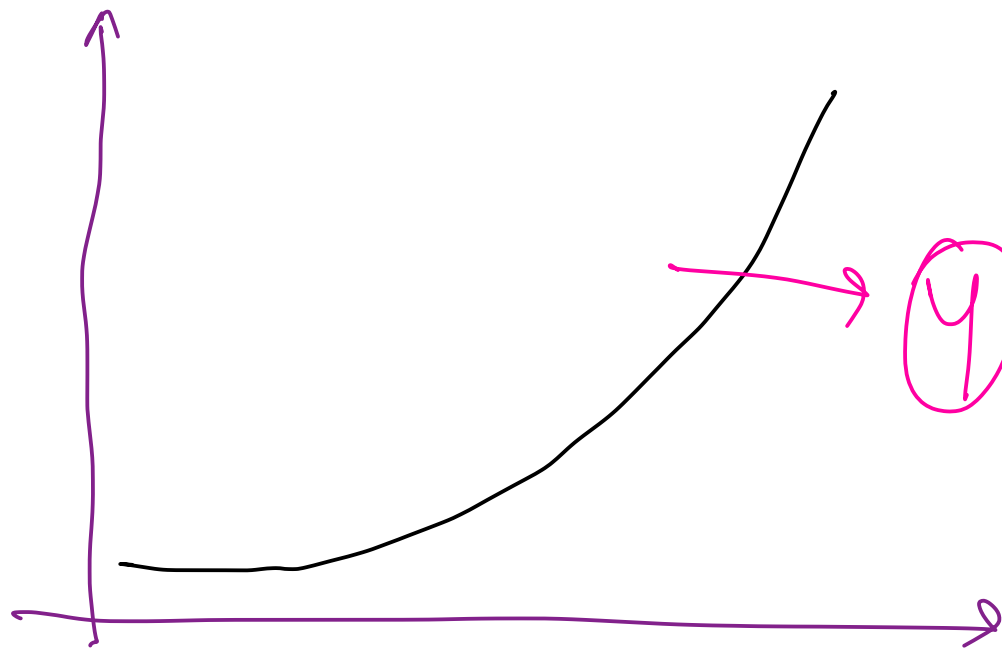
monotonically
increasing.



* Correlation → (+1) ?

→ Strength of linear relationship.

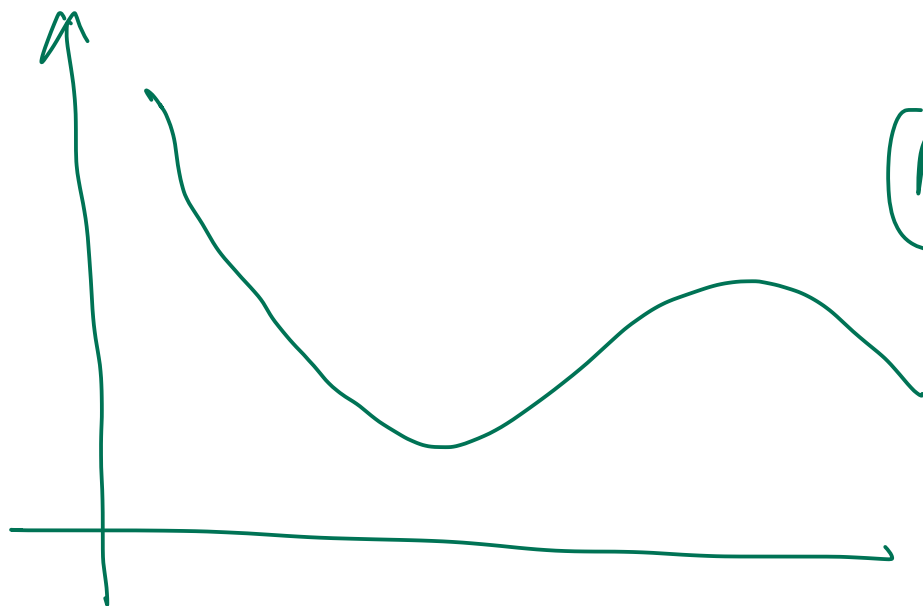
Perfectly monotonic.



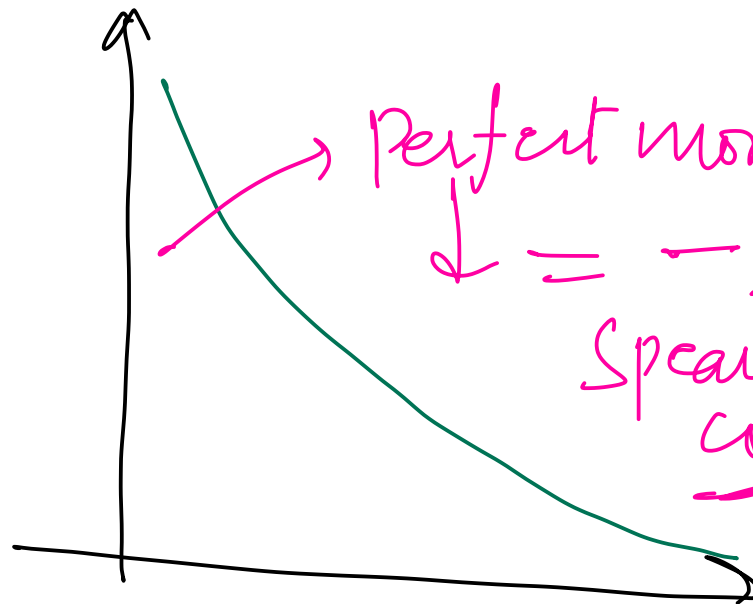
(4)

spearman corr
 $= +1$

(4)



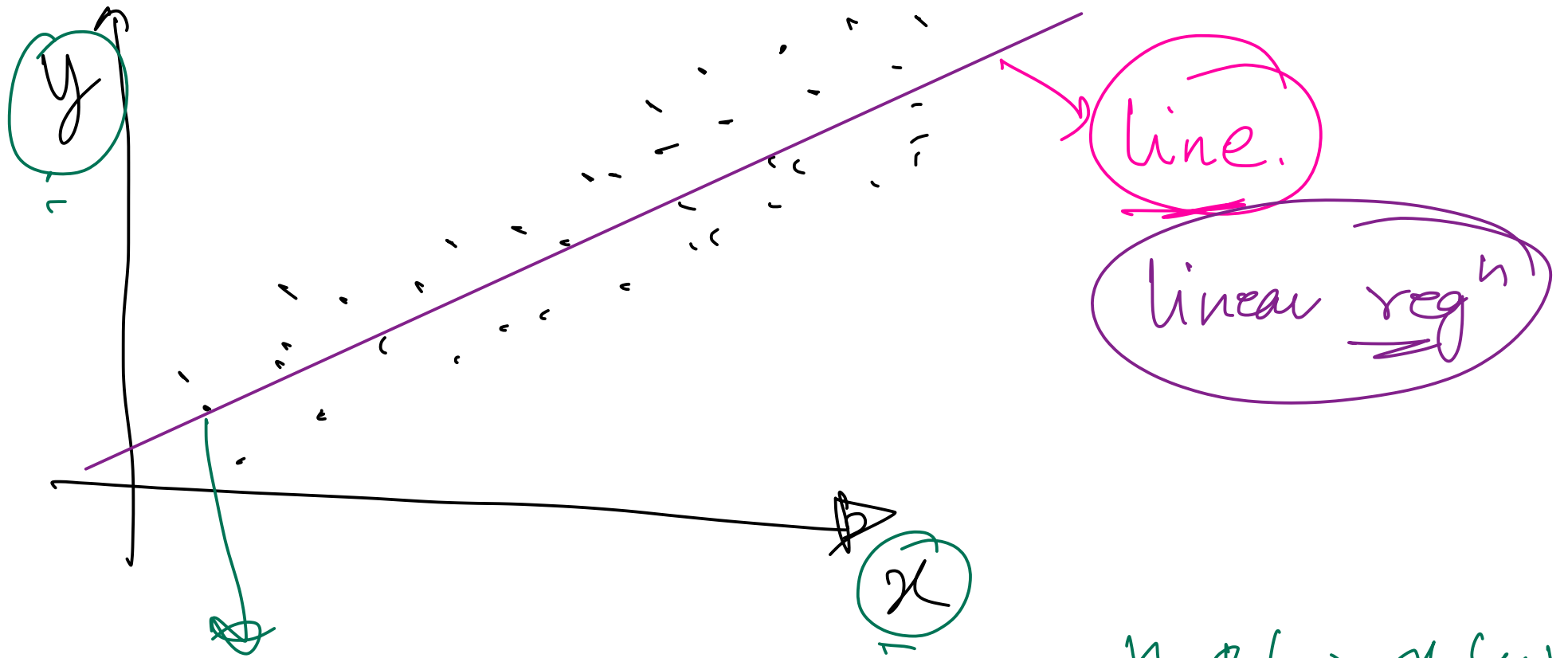
(2)



Perfectly monotonic

$\downarrow = -1$

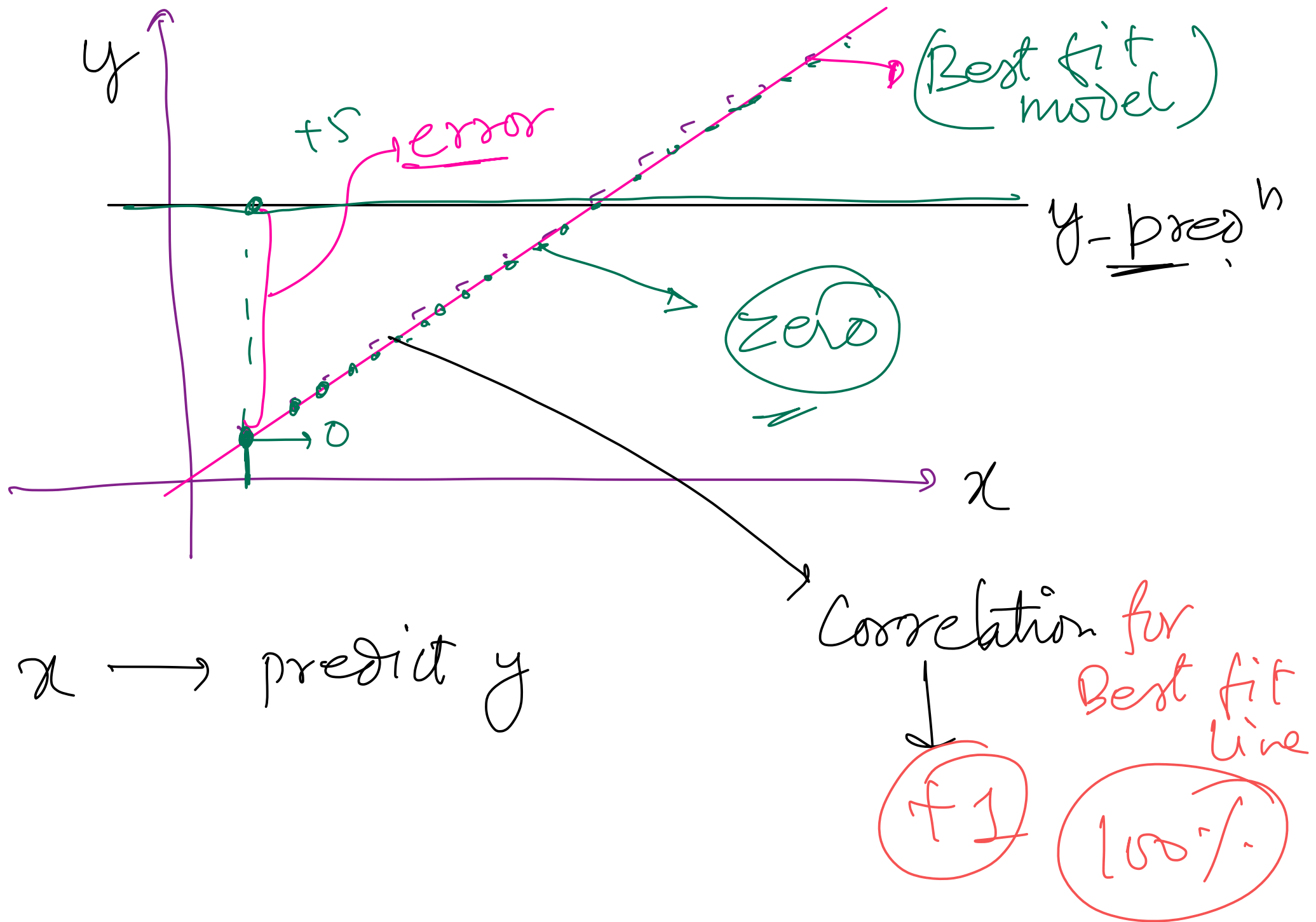
Spearman
corr



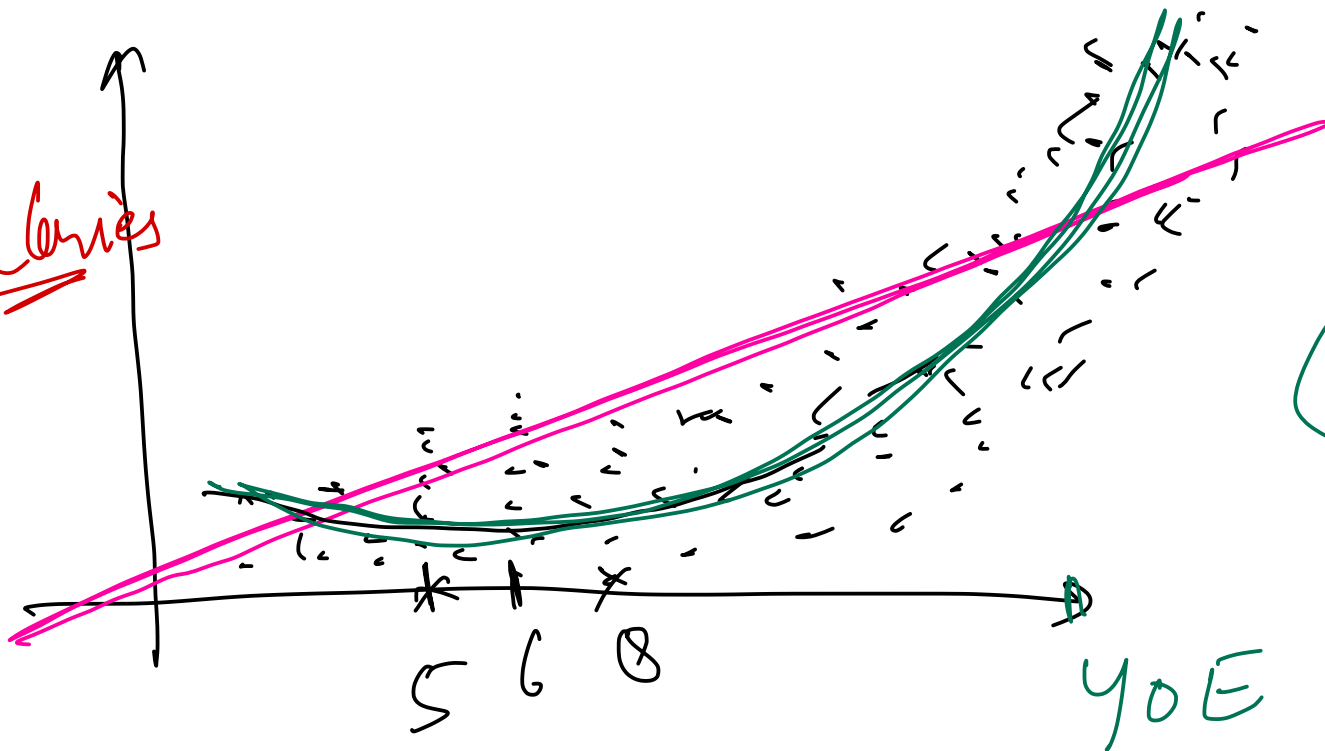
Strength of linear relpⁿ B/w x & y .

0.82

$\Rightarrow R^2$



Salaries



Naukri.com

Pearson

Spearman

New profile
(YOE)

MODEL

Expected Salary -

