Повторение примеров

Линейное программирование

```
In [1]: using JuMP
        using GLPK
In [2]: # Определение объекта модели с именем model:
        model = Model(GLPK.Optimizer)
Out[2]: A JuMP Model
        Feasibility problem with:
        Variables: 0
        Model mode: AUTOMATIC
        CachingOptimizer state: EMPTY_OPTIMIZER
        Solver name: GLPK
In [3]: # Определение переменных х, у и граничных условий для них:
        @variable(model, x >= 0)
        @variable(model, y >= 0)
Out[3]: y
In [4]: # Определение ограничений модели:
        @constraint(model, 6x + 8y >= 100)
        @constraint(model, 7x + 12y >= 120)
Out[4]:
                                           7x + 12y > 120
In [5]: # Определение целевой функции:
        @objective(model, Min, 12x + 20y)
Out[5]: 12x + 20y
In [6]: # Вызов функции оптимизации:
        optimize!(model)
In [7]: # Определение причины завершения работы оптимизатора:
        termination_status(model)
Out[7]: OPTIMAL::TerminationStatusCode = 1
In [8]: # Демонстрация первичных результирующих значений переменных х и у:
        @show value(x)
        @show value(y)
        # Демонстрация результата оптимизации:
        @show objective_value(model)
```

Векторизованные ограничения

```
In [9]: # Определение объекта модели с именем vector_model:
          vector_model = Model(GLPK.Optimizer)
 Out[9]: A JuMP Model
          Feasibility problem with:
          Variables: 0
          Model mode: AUTOMATIC
          CachingOptimizer state: EMPTY_OPTIMIZER
          Solver name: GLPK
In [10]: # Определение начальных данных:
          A= [ 1 1 9 5; 3 5 0 8; 2 0 6 13]
          b = [7; 3; 5]
          c = [1; 3; 5; 2]
Out[10]: 4-element Vector{Int64}:
           3
           5
           2
In [11]: # Определение вектора переменных:
          @variable(vector_model, x[1:4] >= 0)
Out[11]: 4-element Vector{VariableRef}:
           x[1]
           x[2]
           x[3]
           x[4]
In [12]: # Определение ограничений модели:
          @constraint(vector model, A * x .== b)
Out[12]: 3-element Vector{ConstraintRef{Model, MathOptInterface.ConstraintIndex{MathOptInte
          rface.ScalarAffineFunction{Float64}, MathOptInterface.EqualTo{Float64}}, ScalarSha
          pe}}:
           x[1] + x[2] + 9 x[3] + 5 x[4] == 7
           3 \times [1] + 5 \times [2] + 8 \times [4] == 3
           2 \times [1] + 6 \times [3] + 13 \times [4] == 5
In [13]: # Определение целевой функции:
          @objective(vector_model, Min, c' * x)
Out[13]: x_1 + 3x_2 + 5x_3 + 2x_4
In [14]: # Вызов функции оптимизации:
```

```
optimize!(vector_model)
In [15]: # Определение причины завершения работы оптимизатора:
         termination_status(vector_model)
Out[15]: OPTIMAL::TerminationStatusCode = 1
In [16]: # Демонстрация результата оптимизации:
         @show objective_value(vector_model)
        objective_value(vector_model) = 4.9230769230769225
Out[16]: 4.9230769230769225
         Оптимизация рациона
In [17]: category_data = JuMP.Containers.DenseAxisArray(
             [1800 2200;
             91 Inf;
             0 65;
             0 1779],
             ["calories", "protein", "fat", "sodium"],
             ["min", "max"])
Out[17]: 2-dimensional DenseAxisArray{Float64,2,...} with index sets:
             Dimension 1, ["calories", "protein", "fat", "sodium"]
             Dimension 2, ["min", "max"]
         And data, a 4×2 Matrix{Float64}:
          1800.0 2200.0
            91.0
                  Inf
             0.0
                  65.0
             0.0 1779.0
In [18]: # массив данных с наименованиями продуктов:
         foods = ["hamburger", "chicken", "hot dog", "fries", "macaroni", "pizza", "salad",
Out[18]: 9-element Vector{String}:
          "hamburger"
          "chicken"
          "hot dog"
          "fries"
          "macaroni"
          "pizza"
          "salad"
          "milk"
          "ice cream"
In [19]: # Массив стоимости продуктов:
         cost = JuMP.Containers.DenseAxisArray(
         [2.49, 2.89, 1.50, 1.89, 2.09, 1.99, 2.49, 0.89, 1.59],
```

foods)

```
Out[19]: 1-dimensional DenseAxisArray{Float64,1,...} with index sets:
             Dimension 1, ["hamburger", "chicken", "hot dog", "fries", "macaroni", "pizza",
         "salad", "milk", "ice cream"]
         And data, a 9-element Vector{Float64}:
          2.89
          1.5
          1.89
          2.09
          1.99
          2.49
          0.89
          1.59
In [20]: food_data = JuMP.Containers.DenseAxisArray(
             [410 24 26 730;
             420 32 10 1190;
             560 20 32 1800;
             380 4 19 270;
             320 12 10 930;
             320 15 12 820;
             320 31 12 1230;
             100 8 2.5 125;
             330 8 10 180],
             foods,
             ["calories", "protein", "fat", "sodium"])
Out[20]: 2-dimensional DenseAxisArray{Float64,2,...} with index sets:
             Dimension 1, ["hamburger", "chicken", "hot dog", "fries", "macaroni", "pizza",
         "salad", "milk", "ice cream"]
             Dimension 2, ["calories", "protein", "fat", "sodium"]
         And data, a 9×4 Matrix{Float64}:
          410.0 24.0 26.0
                             730.0
          420.0 32.0 10.0 1190.0
          560.0 20.0 32.0 1800.0
          380.0 4.0 19.0 270.0
          320.0 12.0 10.0 930.0
          320.0 15.0 12.0 820.0
          320.0 31.0 12.0 1230.0
          100.0 8.0 2.5 125.0
          330.0 8.0 10.0 180.0
In [21]: # Определение объекта модели с именем model:
         model_calories = Model(GLPK.Optimizer)
Out[21]: A JuMP Model
         Feasibility problem with:
         Variables: 0
         Model mode: AUTOMATIC
         CachingOptimizer state: EMPTY_OPTIMIZER
         Solver name: GLPK
In [22]: # Определим массив:
         categories = ["calories", "protein", "fat", "sodium"]
```

```
Out[22]: 4-element Vector{String}:
                             "calories"
                             "protein"
                             "fat"
                             "sodium"
In [23]: # Определение переменных:
                         @variables(model_calories, begin
                                    category_data[c, "min"] <= nutrition[c = categories] <= category_data[c, "max"]</pre>
                                    # Сколько покупать продуктов:
                                    buy[foods] >= 0
                                    end)
Out[23]: (1-dimensional DenseAxisArray{VariableRef,1,...} with index sets:
                                     Dimension 1, ["calories", "protein", "fat", "sodium"]
                          And data, a 4-element Vector{VariableRef}:
                             nutrition[calories]
                             nutrition[protein]
                             nutrition[fat]
                             nutrition[sodium], 1-dimensional DenseAxisArray{VariableRef,1,...} with index set
                          s:
                                     Dimension 1, ["hamburger", "chicken", "hot dog", "fries", "macaroni", "pizza",
                          "salad", "milk", "ice cream"]
                          And data, a 9-element Vector{VariableRef}:
                             buy[hamburger]
                             buy[chicken]
                             buy[hot dog]
                             buy[fries]
                             buy[macaroni]
                             buy[pizza]
                             buy[salad]
                             buy[milk]
                             buy[ice cream])
In [24]: # Определение целевой функции:
                         @objective(model_calories, Min, sum(cost[f] * buy[f] for f in foods))
\texttt{Out[24]:} \quad 2.49buy_{hamburger} + 2.89buy_{chicken} + 1.5buy_{hotdog} + 1.89buy_{fries} + 2.09buy_{macaroni} + 1.99buy_{pizza} + 2.49buy_{chicken} + 1.5buy_{hotdog} + 1.89buy_{fries} + 2.09buy_{macaroni} + 1.99buy_{pizza} + 2.49buy_{macaroni} + 1.99buy_{pizza} + 2.49buy_{macaroni} + 1.99buy_{macaroni} + 1.99buy_{macaro
In [25]: # Определение ограничений модели:
                         @constraint(model_calories, [c in categories],
                          sum(food_data[f, c] * buy[f] for f in foods) == nutrition[c])
```

```
Out[25]: 1-dimensional DenseAxisArray{ConstraintRef{Model, MathOptInterface.ConstraintIndex
         {MathOptInterface.ScalarAffineFunction{Float64}, MathOptInterface.EqualTo{Float6
         4}}, ScalarShape},1,...} with index sets:
             Dimension 1, ["calories", "protein", "fat", "sodium"]
         And data, a 4-element Vector{ConstraintRef{Model, MathOptInterface.ConstraintIndex
         {MathOptInterface.ScalarAffineFunction{Float64}, MathOptInterface.EqualTo{Float6
         4}}, ScalarShape}}:
          -nutrition[calories] + 410 buy[hamburger] + 420 buy[chicken] + 560 buy[hot dog] +
         380 buy[fries] + 320 buy[macaroni] + 320 buy[pizza] + 320 buy[salad] + 100 buy[mil
         k] + 330 buy[ice cream] == 0
          -nutrition[protein] + 24 buy[hamburger] + 32 buy[chicken] + 20 buy[hot dog] + 4 b
         uy[fries] + 12 buy[macaroni] + 15 buy[pizza] + 31 buy[salad] + 8 buy[milk] + 8 buy
          [ice cream] == 0
          -nutrition[fat] + 26 buy[hamburger] + 10 buy[chicken] + 32 buy[hot dog] + 19 buy
         [fries] + 10 buy[macaroni] + 12 buy[pizza] + 12 buy[salad] + 2.5 buy[milk] + 10 bu
         y[ice cream] == 0
          -nutrition[sodium] + 730 buy[hamburger] + 1190 buy[chicken] + 1800 buy[hot dog] +
         270 buy[fries] + 930 buy[macaroni] + 820 buy[pizza] + 1230 buy[salad] + 125 buy[mi
         lk] + 180 buy[ice cream] == 0
In [26]: # Вызов функции оптимизации:
         JuMP.optimize!(model_calories)
         term status = JuMP.termination status(model calories)
Out[26]: OPTIMAL::TerminationStatusCode = 1
In [27]: hcat(buy.data, JuMP.value.(buy.data))
Out[27]: 9×2 Matrix{AffExpr}:
          buy[hamburger] 0.6045138888888888
          buy[chicken]
          buy[hot dog]
          buy[fries]
          buy[macaroni] 0
          buy[pizza]
                        0
          buy[salad]
          buy[milk]
                          6.970138888888935
          buy[ice cream] 2.59131944444441
```

Путешествие по миру

```
In [2]: using DelimitedFiles
         using CSV
In [29]: passportdata = readdlm("data/passport-index-matrix.csv",',')
```

```
Out[29]: 200×200 Matrix{Any}:
          "Passport"
                                      "Albania" ...
                                                    "Afghanistan"
          "Afghanistan"
                                      "e-visa"
                                                   -1
           "Albania"
                                                      "visa required"
           "Algeria"
                                     "e-visa"
                                                      "visa required"
                                                      "visa required"
           "Andorra"
           "Angola"
                                      "e-visa"
                                                      "visa required"
                                                      "visa required"
           "Antigua and Barbuda"
                                    90
           "Argentina"
                                    90
                                                      "visa required"
           "Armenia"
                                                      "visa required"
                                   90
           "Australia"
                                   90
                                                      "visa required"
           "Austria"
                                   90
                                                      "visa required"
           "Azerbaijan"
                                                      "visa required"
                                    90
           "Bahamas"
                                    90
                                                      "visa required"
           "United Arab Emirates"
                                   90
                                                      "visa required"
           "United Kingdom"
                                   90
                                                      "visa required"
           "United States"
                                                      "visa required"
                                   360
                                                      "visa required"
           "Uruguay"
                                   90
           "Uzbekistan"
                                      "e-visa"
                                                      "visa required"
                                    "e-visa"
           "Vanuatu"
                                                      "visa required"
           "Vatican"
                                   90
                                                      "visa required"
           "Venezuela"
                                   90
                                                      "visa required"
           "Vietnam"
                                     "e-visa"
                                                      "visa required"
           "Yemen"
                                      "e-visa"
                                                      "visa required"
           "Zambia"
                                      "e-visa"
                                                      "visa required"
           "Zimbabwe"
                                      "e-visa"
                                                      "visa required"
In [30]: # Задаём переменные:
         cntr = passportdata[2:end,1]
         vf = (x \rightarrow typeof(x) = Int64 \mid x = "VF" \mid x = "VOA" ? 1 : 0).(passportdata[2:end])
```

```
Out[30]: 199×199 Matrix{Int64}:
                                                                 0
                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                             0 0
                                                                                                      0
                                                                                                                  0
                                                                                                                            0
                                                                                                                                      0
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                      0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                                            1
                                   1
                                                                                                                  1
                                                                                                                            0
                                                                                                                                      0
                                                                                                                                                0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                      0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        0
                                                                                                                                                                                                                                                                                            0
                                                                                                                                                                                                                                1
                                   0
                                             1
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                  0
                                                                                                                            0
                                                                                                                                      0
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                      0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                                            0
                                   1
                                                       1
                                                                 0
                                                                           1
                                                                                                                  1
                                                                                                                            0
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                            1
                                                                                                                                                                                                                                                                                            0
                                                                                     1
                                                                                              1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        0
                                                                                                                                                                                                                                                                                  0
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                                                          0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                       1
                                                                 1
                                                                           1
                                                                                              0
                                                                                                                  1
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             1
                                                                                                                                                                                                                       1
                                                                                                                                                                                                                                 1
                                   1
                                             0
                                                                                                                                                                                         0
                                                       1
                                                                 1
                                                                           1
                                                                                     1
                                                                                               0
                                                                                                         0
                                                                                                                  1
                                                                                                                             0
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                                                1
                                                                                                                                                                                                  1
                                                                                                                                                                                                             1
                                                                                                                                                                                                                       1
                                                                                                                                                                                                                                 1
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                   1
                                                                           1
                                                                                     1
                                                                                                                  0
                                                                                                                            0
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                                            0
                                   1
                                             0
                                                       1
                                                                 1
                                                                           1
                                                                                     1
                                                                                              1
                                                                                                                   1
                                                                                                                            0
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                             1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                                            0
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                                        1
                                                                 1
                                                                           1
                                                                                     1
                                                                                               1
                                                                                                         0
                                                                                                                   1
                                                                                                                             0
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                            1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        1
                                                                                                                                                                                                                                                                                            0
                                                                                                                                                                               0
                                                                                                                                                0
                                                                                                                                                                                                             0
                                   1
                                             0
                                                       1
                                                                 1
                                                                           1
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                  1
                                                                                                                                       1
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                             1
                                                                                                                                                                                                                       1
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        1
                                   1
                                                                           a
                                                                                     a
                                                                                                                            0
                                                                                                                                      1
                                                                                                                                                                               0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                                    0
                                   1
                                                                                     1
                                                                                                         0
                                                                                                                            1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                             0
                                                       1
                                                                 1
                                                                           1
                                                                                              1
                                                                                                                  1
                                                                                                                                      1
                                                                                                                                                                                                  1
                                                                                                                                                                                                            1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                                                        1
                                                                                                                                                                                                                                                                                            0
                                   1
                                                                 1
                                                                           1
                                                                                     1
                                                                                              1
                                                                                                                  1
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                           0
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                             1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                    1
                                                                           1
                                                                                                                                                                               1
                                                                                                                                                                                                             0
                                                                                                                                                                                                                                 1
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                              0
                                   1
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               1
                                                                                                                                                                                                   1
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       1
                                             0
                                                                 0
                                                                           1
                                                                                     0
                                                                                               1
                                                                                                                   0
                                                                                                                             1
                                                                                                                                       0
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             1
                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        0
                                                                                                                                                                                                                                                                                  0
                                                                                                                                                                                                                                                                                            0
                                   0
                                             0
                                                       0
                                                                 1
                                                                           1
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                                      1
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                                                              0
                                                                                                                  0
                                                                                                                            0
                                                                                                                                                0
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                                        1
                                                                                                                                                                                                                                                                                  1
                                                                                                                                                                               1
                                                                                                                                                                                         0
                                   1
                                             0
                                                       1
                                                                 1
                                                                           1
                                                                                     1
                                                                                              1
                                                                                                         0
                                                                                                                  1
                                                                                                                            0
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                                                  1
                                                                                                                                                                                                            1
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        0
                                                                                                                                                                                                                                                                                            0
                                                                                                                                                                               0
                                   1
                                             0
                                                       1
                                                                 0
                                                                           1
                                                                                     1
                                                                                               0
                                                                                                         0
                                                                                                                  1
                                                                                                                                       1
                                                                                                                                                0
                                                                                                                                                           0
                                                                                                                                                                                         0
                                                                                                                                                                                                  1
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                1
                                                                                                                                                                                                                                          1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        0
                                                                                                                            0
                                                                                                                                       0
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       0
                                             0
                                                                 0
                                                                           0
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                   0
                                                                                                                            0
                                                                                                                                       0
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                       0
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              1
                                                                                                                                                                                                                                                                        0
                                                                                                                                                                                                                                                                                  0
                                                                                                                                                                                                                                                                                            0
                                             0
                                                       0
                                                                 1
                                                                          1
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                  0
                                                                                                                            0
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                          1
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        1
                                                                                                                                                                                                                                                                                 1
                                                                                                                                                                                                                                                                                            0
                                   0
                                             0
                                                       0
                                                                 1
                                                                          0
                                                                                     0
                                                                                              0
                                                                                                         0
                                                                                                                  0
                                                                                                                            0
                                                                                                                                      1
                                                                                                                                                0
                                                                                                                                                          0
                                                                                                                                                                               0
                                                                                                                                                                                         0
                                                                                                                                                                                                  0
                                                                                                                                                                                                             0
                                                                                                                                                                                                                      1
                                                                                                                                                                                                                                                    0
                                                                                                                                                                                                                                                              0
                                                                                                                                                                                                                                                                        1
                                                                                                                                                                                                                                                                                  1
                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                          0
In [31]: # Определение объекта модели с именем model:
                               model_passports = Model(GLPK.Optimizer)
Out[31]: A JuMP Model
                                Feasibility problem with:
                                Variables: 0
                                Model mode: AUTOMATIC
                                CachingOptimizer state: EMPTY_OPTIMIZER
                                Solver name: GLPK
In [32]: # Переменные, ограничения и целевая функция:
                               @variable(model_passports, pass[1:length(cntr)], Bin)
                               @constraint(model_passports, [j=1:length(cntr)], sum( vf[i,j]*pass[i] for i in 1:le
                               @objective(model_passports, Min, sum(pass))
                              pass_1 + pass_2 + pass_3 + pass_4 + pass_5 + pass_6 + pass_7 + pass_8 + pass_9 + pass_{10} + pass_{11} + pass_{12} + pass_{13} + pass_{14} + pass_{15} + pass_{16} + pass_{17} + pass_{18} + pass_{19} + pass_{1
Out[32]:
                                +\ pass_{22} + pass_{23} + pass_{24} + pass_{25} + pass_{26} + pass_{27} + pass_{28} + pass_{29} + pass_{30} + [[\dots 139\ \mathrm{term}]]
                                +\ pass_{177}+pass_{178}+pass_{180}+pass_{180}+pass_{181}+pass_{182}+pass_{183}+pass_{184}+pass_{185}+pass_{185}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{186}+pass_{
                               + pass_{195} + pass_{196} + pass_{197} + pass_{198} + pass_{199}
In [33]:
                               # Вызов функции оптимизации:
                                JuMP.optimize!(model_passports)
                                termination_status(model_passports)
Out[33]: OPTIMAL::TerminationStatusCode = 1
In [34]: print(JuMP.objective_value(model_passports)," passports: ",join(cntr[findall(JuMP.v
```

34.0 passports: Afghanistan, Australia, Bahrain, Cameroon, Canada, Comoros, Congo, D enmark, Djibouti, Eritrea, Guinea-Bissau, Hong Kong, Iran, Kenya, Kuwait, Liberia, L ibya, Madagascar, Maldives, Mauritania, Morocco, Nauru, Nepal, New Zealand, North Ko rea, Palestine, Papua New Guinea, Qatar, Saudi Arabia, Singapore, Somalia, Sri Lank a, Syria, Turkmenistan

```
Портфельные инвестиции
 In [3]: using DataFrames
         using XLSX
         using Plots
         pyplot()
         using Convex
         using SCS
         using Statistics
In [36]: # Считываем данные и размещаем их во фрейм:
         T = DataFrame(XLSX.readtable("data/stock_prices.xlsx", "Sheet2"))
Out[36]: 13×3 DataFrame
         Row MSFT
                     FB
                            AAPL
              Any
                     Any
                            Any
            1 101.93 137.95 148.26
            2 102.8
                     143.8
                            152.29
            3 107.71 150.04 156.82
            4 107.17 149.01 157.76
            5 102.78 165.71 166.52
            6 105.67 167.33 170.41
            7 108.22 162.5
                            170.42
            8 110.97 161.89 172.97
```

```
In [37]: # Πος προθημε εραφμεα:
plot(T[!,:MSFT],label="Microsoft")
plot!(T[!,:AAPL],label="Apple")
plot!(T[!,:FB],label="FB")
```

9 112.53 162.28 174.97

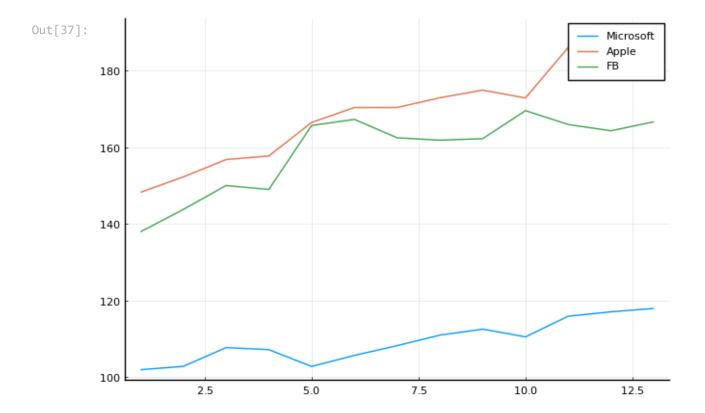
11 115.91 165.98 186.12

12 117.05 164.34 191.05

13 117.94 166.69 189.95

172.91

10 110.51 169.6



```
In [38]: # Данные о ценах на акции размещаем в матрице:
         prices_matrix = Matrix(T)
Out[38]: 13×3 Matrix{Any}:
          101.93 137.95 148.26
          102.8
                 143.8
                         152.29
          107.71 150.04 156.82
          107.17 149.01 157.76
          102.78 165.71 166.52
          105.67 167.33 170.41
          108.22 162.5
                        170.42
          110.97 161.89 172.97
          112.53 162.28 174.97
          110.51 169.6 172.91
          115.91 165.98 186.12
          117.05 164.34 191.05
          117.94 166.69 189.95
```

```
In [39]: # Вычисление матрицы доходности за период времени:
M1 = prices_matrix[1:end-1,:]
M2 = prices_matrix[2:end,:]
# Матрица доходности:
R = (M2.-M1)./M1
```

```
Out[39]: 12×3 Matrix{Float64}:
           0.00853527 0.0424067 0.027182
           0.0477626
                       0.0433936 0.0297459
          -0.00501346 -0.00686484 0.00599413
          -0.040963 0.112073 0.0555274
           0.0281183 0.00977611 0.0233606
           0.0241317 -0.0288651 5.8682e-5
           0.0254112 -0.00375385 0.014963
           0.0140579 0.00240904 0.0115627
          -0.0179508 0.0451072 -0.0117734
           0.0488644 -0.0213443 0.0763981
           0.00983522 -0.00988071 0.0264883
           0.00760359 0.0142996 -0.00575766
In [40]: # Μαπρυца рисков:
         risk matrix = cov(R)
         # Проверка положительной определённости матрицы рисков:
         isposdef(risk_matrix)
Out[40]: true
In [41]: # Доход от каждой из компаний:
         r = mean(R, dims=1)[:]
Out[41]: 3-element Vector{Float64}:
          0.012532748705136572
          0.016563036855293173
          0.02114580465503291
In [42]: # Вектор инвестиций:
         x = Variable(length(r))
Out[42]: Variable
         size: (3, 1)
         sign: real
         vexity: affine
         id: 122...222
In [43]: # Объект модели:
         problem = minimize(Convex.quadform(x,risk_matrix),[sum(x)==1;r'*x>=0.02;x.>=0])
```

```
Out[43]: minimize
         └ * (convex; positive)
             └ qol_elem (convex; positive)
                ─ norm2 (convex; positive)
                  └ ...
                └ [1.0;;]
         subject to

    ⊢ sum (affine; real)

             ☐ 3-element real variable (id: 122...222)
          - >= constraint (affine)

→ * (affine; real)

├ [0.0125327 0.016563 0.0211458]
             └─ 3-element real variable (id: 122…222)
            └ 0.02
           - >= constraint (affine)

    index (affine; real)

             └─ 3-element real variable (id: 122...222)
            <u>L</u> 0
          ->= constraint (affine)
            ├ index (affine; real)
              └─ 3-element real variable (id: 122...222)
            L 0
          └ >= constraint (affine)

    index (affine; real)

              └─ 3-element real variable (id: 122...222)
            status: `solve!` not called yet
In [44]: # Находим решение:
         solve!(problem, SCS.Optimizer)
```

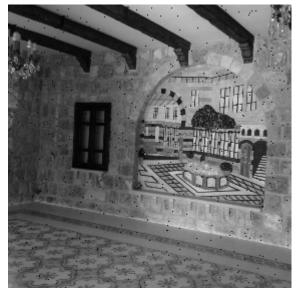
```
SCS v3.2.4 - Splitting Conic Solver
              (c) Brendan O'Donoghue, Stanford University, 2012
       ______
       problem: variables n: 6, constraints m: 14
       cones: z: primal zero / dual free vars: 2
                1: linear vars: 5
                q: soc vars: 7, qsize: 2
       settings: eps abs: 1.0e-004, eps rel: 1.0e-004, eps infeas: 1.0e-007
                alpha: 1.50, scale: 1.00e-001, adaptive_scale: 1
                max_iters: 100000, normalize: 1, rho_x: 1.00e-006
                acceleration_lookback: 10, acceleration_interval: 10
       lin-sys: sparse-direct-amd-qdldl
                nnz(A): 24, nnz(P): 0
        iter | pri res | dua res | gap | obj | scale | time (s)
            75|8.16e-005 1.46e-004 5.60e-005 5.56e-004 1.00e-001 2.48e-004
       status: solved
       timings: total: 2.50e-004s = setup: 1.25e-004s + solve: 1.25e-004s
               lin-sys: 3.27e-005s, cones: 2.31e-005s, accel: 4.50e-006s
       objective = 0.000556
In [45]: x
Out[45]: Variable
        size: (3, 1)
         sign: real
        vexity: affine
         id: 122...222
         value: [0.06922834751660403, 0.11730158220227511, 0.813469514654251]
In [46]: sum(x.value)
Out[46]: 0.9999994443731302
In [47]: r'*x.value
Out[47]: 1×1 adjoint(::Vector{Float64}) with eltype Float64:
         0.020011959361601172
In [48]: x.value .* 1000
Out[48]: 3×1 Matrix{Float64}:
          69.22834751660403
         117.30158220227511
         813.469514654251
```

Восстановление изображения

```
In [4]: using Images
In [50]: # Считывание исходного изображения:
          Kref = load("data/khiam-small.jpg")
Out[50]:
In [51]: K = copy(Kref)
         p = prod(size(K))
         missingids = rand(1:p,400)
Out[51]: 400-element Vector{Int64}:
           13926
           75313
           71284
           16985
           40139
           54158
           54979
           14764
           38463
           33118
           68673
           16737
           66617
           36699
           36677
            6733
           50628
            4083
           10212
           62751
```

```
In [52]: K[missingids] .= RGBX{N0f8}(0.0,0.0,0.0)
    K
    Gray.(K)
```

Out[52]:



In [54]: correctids = findall(Y[:].!=0)

X = Convex.Variable(size(Y))

```
In [53]: # Mampuya yβemoβ:
         Y = Float64.(Gray.(K))
Out[53]: 283×283 Matrix{Float64}:
          0.101961
                      0.0627451 0.0784314
                                            0.0941176 ...
                                                          0.509804
                                                                    0.552941
                                                                              0.666667
          0.0666667
                     0.0980392 0.0745098
                                            0.054902
                                                          0.505882
                                                                    0.584314
                                                                              0.501961
          0.0784314 0.0862745 0.0784314
                                            0.0901961
                                                          0.6
                                                                    0.701961 0.615686
          0.0862745
                     0.0666667 0.0745098
                                                          0.658824 0.705882
                                                                              0.145098
                                            0.0941176
          0.0784314
                     0.101961
                                 0.0901961
                                            0.0745098
                                                          0.713725
                                                                    0.682353 0.231373
          0.0745098
                     0.0745098 0.0784314
                                           0.0862745
                                                          0.729412 0.701961 0.168627
          0.12549
                      0.0980392 0.0862745
                                           0.0862745
                                                          0.0
                                                                    0.466667
                                                                              0.192157
          0.439216
                      0.447059
                                 0.305882
                                            0.137255
                                                          0.231373 0.184314
                                                                              0.137255
          0.458824
                      0.454902
                                 0.45098
                                            0.454902
                                                          0.196078 0.101961
                                                                              0.117647
          0.45098
                      0.466667
                                 0.458824
                                            0.45098
                                                          0.584314
                                                                    0.121569
                                                                              0.137255
          0.458824
                     0.458824
                                 0.458824
                                            0.454902
                                                          0.521569
                                                                    0.513725
                                                                              0.12549
          0.466667
                      0.45098
                                 0.458824
                                            0.47451
                                                          0.576471
                                                                    0.741176 0.117647
          0.45098
                      0.45098
                                                          0.560784
                                                                    0.67451
                                                                              0.117647
                                 0.462745
                                            0.458824
                      0.47451
                                 0.47451
                                                          0.427451 0.435294
                                                                              0.443137
          0.494118
                                            0.462745
          0.47451
                      0.482353
                                 0.470588
                                            0.470588
                                                          0.439216 0.431373
                                                                              0.431373
          0.494118
                     0.501961
                                 0.470588
                                            0.45098
                                                          0.447059
                                                                    0.447059
                                                                              0.45098
          0.470588
                      0.494118
                                 0.490196
                                            0.482353
                                                          0.431373
                                                                    0.419608
                                                                              0.419608
          0.458824
                      0.482353
                                 0.47451
                                                          0.454902
                                                                    0.435294
                                                                              0.423529
                                            0.466667
          0.443137
                      0.458824
                                 0.45098
                                            0.45098
                                                          0.309804
                                                                    0.32549
                                                                              0.34902
          0.47451
                     0.478431
                                 0.462745
                                            0.462745
                                                          0.341176
                                                                    0.345098
                                                                              0.360784
          0.482353
                      0.478431
                                 0.458824
                                            0.458824
                                                          0.423529
                                                                    0.372549
                                                                              0.321569
          0.552941
                      0.552941
                                 0.541176
                                            0.533333
                                                          0.447059
                                                                    0.411765
                                                                              0.372549
          0.552941
                      0.545098
                                 0.576471
                                            0.552941
                                                          0.435294
                                                                    0.423529
                                                                              0.407843
          0.564706
                      0.552941
                                 0.54902
                                            0.505882
                                                          0.439216
                                                                    0.431373
                                                                              0.419608
          0.568627
                      0.552941
                                 0.517647
                                            0.462745
                                                          0.439216
                                                                    0.431373
                                                                              0.427451
```

```
problem = minimize(nuclearnorm(X))
       problem.constraints += X[correctids]==Y[correctids]
Out[54]: 1-element Vector{Constraint}:
        == constraint (affine)
        ├ index (affine; real)
         └ 283×283 real variable (id: 141...996)

    79690-element Vector{Float64}

In [55]: # Находим решение:
       solve!(problem, SCS.Optimizer)
                  SCS v3.2.4 - Splitting Conic Solver
             (c) Brendan O'Donoghue, Stanford University, 2012
      ______
      problem: variables n: 240268, constraints m: 400047
      cones: z: primal zero / dual free vars: 239586
              s: psd vars: 160461, ssize: 1
      settings: eps_abs: 1.0e-004, eps_rel: 1.0e-004, eps_infeas: 1.0e-007
              alpha: 1.50, scale: 1.00e-001, adaptive_scale: 1
              max_iters: 100000, normalize: 1, rho_x: 1.00e-006
              acceleration_lookback: 10, acceleration_interval: 10
      lin-sys: sparse-direct-amd-qdldl
              nnz(A): 400330, nnz(P): 0
      _____
       iter | pri res | dua res | gap | obj | scale | time (s)
      ______
          0 | 1.50e+001 9.96e-001 8.34e+003 1.76e+002 1.00e-001 1.01e+000
         250 3.11e-004 2.58e-005 6.72e-006 4.46e+002 3.40e-001 9.48e+001
      ______
      status: solved
      timings: total: 9.48e+001s = setup: 5.96e-001s + solve: 9.42e+001s
             lin-sys: 4.95e+000s, cones: 8.73e+001s, accel: 3.16e-001s
      ______
      objective = 445.530879
In [56]: @show norm(float.(Gray.(Kref))-X.value)
       @show norm(-X.value)
       colorview(Gray, X.value)
      norm(float.(Gray.(Kref)) - X.value) = 1.2447077854577675
      norm(-(X.value)) = 124.33581441728488
```

Out[56]:



Самостоятельная работа

Линейное программирование

```
In [41]: model = Model(GLPK.Optimizer)
Out[41]: A JuMP Model
          Feasibility problem with:
          Variables: 0
          Model mode: AUTOMATIC
          CachingOptimizer state: EMPTY_OPTIMIZER
          Solver name: GLPK
In [42]: @variable(model, x[1:3] >= 0)
Out[42]: 3-element Vector{VariableRef}:
           x[1]
           x[2]
           x[3]
In [43]: @constraint(model, -x[1] + x[2] + 3x[3] <= -5)
         @constraint(model, x[1] + 3x[2] - 7*x[3] <= 10)
         @constraint(model, 0 \le x[1] \le 10)
Out[43]:
                                               x_1 \in [0,10]
In [44]: @objective(model, Max, x[1] + 2x[2] + 5x[3])
Out[44]: x_1 + 2x_2 + 5x_3
In [45]: optimize!(model)
```

```
In [46]: println("Оптимальное значение целевой функции: ", objective_value(model)) println("Оптимальное значение переменных: ", value.(x))

Оптимальное значение целевой функции: 19.0625
Оптимальное значение переменных: [10.0, 2.1875, 0.9375]
```

Линейное программирование. Использование массивов

```
In [160... c = [1, 2, 5]
           A = [-1 \ 1 \ 3; \ 1 \ 3 \ -7]
           b = [-5, 10]
           display(c); display(A); b
         3-element Vector{Int64}:
          1
         2×3 Matrix{Int64}:
          -1 1
           1 3 -7
Out[160... 2-element Vector{Int64}:
            -5
            10
In [161... model = Model(GLPK.Optimizer)
           @variable(model, x[1:3] >= 0)
Out[161...
           3-element Vector{VariableRef}:
            x[1]
            x[2]
            x[3]
           @constraint(model, 0 <= x[1] <= 10)</pre>
In [162...
Out[162...
                                                  x_1 \in [0, 10]
           @objective(model, Max, transpose(c)*x)
In [163...
Out[163... x_1 + 2x_2 + 5x_3
In [164...
           @constraint(model, A * x .<= b)</pre>
           2-element Vector{ConstraintRef{Model, MathOptInterface.ConstraintIndex{MathOptInte
Out[164...
           rface.ScalarAffineFunction{Float64}, MathOptInterface.LessThan{Float64}}, ScalarSh
           ape}}:
            -x[1] + x[2] + 3 x[3] <= -5
            x[1] + 3 x[2] - 7 x[3] <= 10
In [165...
          optimize!(model)
```

```
In [166... println("Оптимальное значение целевой функции: ", objective_value(model)) println("Оптимальное значение переменных: ", value.(x))

Оптимальное значение целевой функции: 19.0625
Оптимальное значение переменных: [10.0, 2.1875, 0.9375]
```

Выпуклое программирование

```
In [167... n = rand(3:5)
        m = n-rand(0:2)
        display(n); m
Out[167... 5
In [168... A = rand(m, n)
        b = rand(m)
        x = Variable(n)
        display(A); display(b); x
       5×5 Matrix{Float64}:
        0.770232 0.240449 0.77553 0.0444783
                                             0.258416
        0.035957
        0.0725477 0.237383 0.608813 0.607776
                                             0.291872
        0.679407 0.25419 0.631587 0.00426607 0.182371
        5-element Vector{Float64}:
        0.9624458021448501
        0.2624239322987302
        0.8558835816793745
        0.3059378263841269
        0.5229702845366548
Out[168... Variable
         size: (5, 1)
         sign: real
         vexity: affine
         id: 289...482
In [169...
        objective = minimize(square(norm(A * x - b, 2)), x \ge 0)
         solve!(objective, SCS.Optimizer)
```

```
SCS v3.2.4 - Splitting Conic Solver
              (c) Brendan O'Donoghue, Stanford University, 2012
       ______
       problem: variables n: 8, constraints m: 16
       cones: z: primal zero / dual free vars: 1
              1: linear vars: 6
               q: soc vars: 9, qsize: 2
       settings: eps abs: 1.0e-004, eps rel: 1.0e-004, eps infeas: 1.0e-007
               alpha: 1.50, scale: 1.00e-001, adaptive_scale: 1
               max_iters: 100000, normalize: 1, rho_x: 1.00e-006
               acceleration_lookback: 10, acceleration_interval: 10
       lin-sys: sparse-direct-amd-qdldl
               nnz(A): 36, nnz(P): 0
        iter | pri res | dua res | gap | obj | scale | time (s)
           0 | 1.71e+001 1.00e+000 1.62e+001 -8.02e+000 1.00e-001 1.26e-004
         125 1.81e-005 2.57e-006 1.57e-005 1.03e-001 1.00e-001 8.90e-003
       ______
       status: solved
       timings: total: 8.91e-003s = setup: 1.03e-004s + solve: 8.80e-003s
              lin-sys: 5.91e-005s, cones: 3.04e-005s, accel: 8.63e-003s
       ______
       objective = 0.102876
       ______
In [170...
        println("Оптимальное значение: ", objective.optval)
        println("Оптимальное решение: ", Convex.evaluate(x))
       Оптимальное значение: 0.1028679143351298
       Оптимальное решение: [2.3833981663828694е-7, 0.08100161792417866, 0.1206738628256472
       4, 0.09562982046568322, 2.4824213062123293]
```

Оптимальная рассадка по залам

```
In [85]: using Random

In [139... zals_str = collect(1:5)
    zals_data = JuMP.Containers.DenseAxisArray(
        [180 250;
        180 250;
        220 220;
        180 250;
        180 250],
        zals_str,
        ["min", "max"])
```

```
Out[139...
          2-dimensional DenseAxisArray{Int64,2,...} with index sets:
              Dimension 1, [1, 2, 3, 4, 5]
              Dimension 2, ["min", "max"]
          And data, a 5×2 Matrix{Int64}:
           180 250
           180 250
           220 220
           180 250
           180 250
In [140...
         # Переделаны обозначения, потому что не нашла способа для оптимизации
          N = 1000
          peopl = collect(1:N)
          people_pref = copy(hcat([shuffle([1, 2, 3, 10000, 10000]) for i in peopl]...))
Out[140... 5×1000 Matrix{Int64}:
           10000 10000 10000 10000 10000 ... 10000
                                                          3 10000
                                                                        3 10000
                               3 3
                                                10000 10000
                                                                        2
                                                                               3
                      1
                            3
                                                                 3
           10000
                            1
                                          2
                                                          2 10000 10000
                                                                               2
                      3
                                   1
                                                   1
               3 10000 10000
                                   2
                                          1
                                                    3 10000
                                                                 2 10000
                                                                               1
               1
                      2
                            2 10000 10000
                                                    2
                                                          1
                                                                 1
                                                                        1 10000
In [141...
         model_zal = Model(GLPK.Optimizer)
Out[141...
          A JuMP Model
          Feasibility problem with:
          Variables: 0
          Model mode: AUTOMATIC
          CachingOptimizer state: EMPTY_OPTIMIZER
          Solver name: GLPK
In [142... @variable(model_zal, answ[peopl, zals_str], Bin)
```

```
Out[142...
                                                2-dimensional DenseAxisArray{VariableRef,2,...} with index sets:
                                                                 Dimension 1, [1, 2, 3, 4, 5, 6, 7, 8, 9, 10 ... 991, 992, 993, 994, 995, 996,
                                               997, 998, 999, 1000]
                                                                 Dimension 2, [1, 2, 3, 4, 5]
                                               And data, a 1000×5 Matrix{VariableRef}:
                                                    answ[1,1]
                                                                                                                 answ[1,2]
                                                                                                                                                                               answ[1,3]
                                                                                                                                                                                                                                           answ[1,4]
                                                                                                                                                                                                                                                                                                        answ[1,5]
                                                    answ[2,1]
                                                                                                                                                                               answ[2,3]
                                                                                                                                                                                                                                           answ[2,4]
                                                                                                                                                                                                                                                                                                        answ[2,5]
                                                                                                                 answ[2,2]
                                                    answ[3,1]
                                                                                                                 answ[3,2]
                                                                                                                                                                              answ[3,3]
                                                                                                                                                                                                                                           answ[3,4]
                                                                                                                                                                                                                                                                                                        answ[3,5]
                                                                                                                 answ[4,2]
                                                                                                                                                                              answ[4,3]
                                                                                                                                                                                                                                           answ[4,4]
                                                                                                                                                                                                                                                                                                        answ[4,5]
                                                    answ[4,1]
                                                    answ[5,1]
                                                                                                                 answ[5,2]
                                                                                                                                                                              answ[5,3]
                                                                                                                                                                                                                                           answ[5,4]
                                                                                                                                                                                                                                                                                                        answ[5,5]
                                                                                                                 answ[6,2]
                                                                                                                                                                              answ[6,3]
                                                                                                                                                                                                                                           answ[6,4]
                                                                                                                                                                                                                                                                                                        answ[6,5]
                                                    answ[6,1]
                                                    answ[7,1]
                                                                                                                 answ[7,2]
                                                                                                                                                                              answ[7,3]
                                                                                                                                                                                                                                           answ[7,4]
                                                                                                                                                                                                                                                                                                        answ[7,5]
                                                    answ[8,1]
                                                                                                                 answ[8,2]
                                                                                                                                                                              answ[8,3]
                                                                                                                                                                                                                                           answ[8,4]
                                                                                                                                                                                                                                                                                                        answ[8,5]
                                                    answ[9,1]
                                                                                                                 answ[9,2]
                                                                                                                                                                              answ[9,3]
                                                                                                                                                                                                                                           answ[9,4]
                                                                                                                                                                                                                                                                                                        answ[9,5]
                                                    answ[10,1]
                                                                                                                 answ[10,2]
                                                                                                                                                                              answ[10,3]
                                                                                                                                                                                                                                           answ[10,4]
                                                                                                                                                                                                                                                                                                        answ[10,5]
                                                    answ[11,1]
                                                                                                                 answ[11,2]
                                                                                                                                                                              answ[11,3]
                                                                                                                                                                                                                                           answ[11,4]
                                                                                                                                                                                                                                                                                                        answ[11,5]
                                                    answ[12,1]
                                                                                                                 answ[12,2]
                                                                                                                                                                              answ[12,3]
                                                                                                                                                                                                                                           answ[12,4]
                                                                                                                                                                                                                                                                                                        answ[12,5]
                                                                                                                                                                                                                                                                                                        answ[13,5]
                                                                                                                                                                              answ[13,3]
                                                    answ[13,1]
                                                                                                                 answ[13,2]
                                                                                                                                                                                                                                           answ[13,4]
                                                    answ[989,1]
                                                                                                                 answ[989,2]
                                                                                                                                                                              answ[989,3]
                                                                                                                                                                                                                                           answ[989,4]
                                                                                                                                                                                                                                                                                                        answ[989,5]
                                                    answ[990,1]
                                                                                                                 answ[990,2]
                                                                                                                                                                              answ[990,3]
                                                                                                                                                                                                                                           answ[990,4]
                                                                                                                                                                                                                                                                                                        answ[990,5]
                                                    answ[991,1]
                                                                                                                 answ[991,2]
                                                                                                                                                                              answ[991,3]
                                                                                                                                                                                                                                           answ[991,4]
                                                                                                                                                                                                                                                                                                        answ[991,5]
                                                    answ[992,1]
                                                                                                                 answ[992,2]
                                                                                                                                                                              answ[992,3]
                                                                                                                                                                                                                                           answ[992,4]
                                                                                                                                                                                                                                                                                                        answ[992,5]
                                                    answ[993,1]
                                                                                                                 answ[993,2]
                                                                                                                                                                              answ[993,3]
                                                                                                                                                                                                                                           answ[993,4]
                                                                                                                                                                                                                                                                                                        answ[993,5]
                                                    answ[994,1]
                                                                                                                 answ[994,2]
                                                                                                                                                                              answ[994,3]
                                                                                                                                                                                                                                           answ[994,4]
                                                                                                                                                                                                                                                                                                        answ[994,5]
                                                    answ[995,1]
                                                                                                                 answ[995,2]
                                                                                                                                                                              answ[995,3]
                                                                                                                                                                                                                                           answ[995,4]
                                                                                                                                                                                                                                                                                                        answ[995,5]
                                                    answ[996,1]
                                                                                                                 answ[996,2]
                                                                                                                                                                              answ[996,3]
                                                                                                                                                                                                                                           answ[996,4]
                                                                                                                                                                                                                                                                                                        answ[996,5]
                                                    answ[997,1]
                                                                                                                 answ[997,2]
                                                                                                                                                                              answ[997,3]
                                                                                                                                                                                                                                                                                                        answ[997,5]
                                                                                                                                                                                                                                           answ[997,4]
                                                    answ[998,1]
                                                                                                                 answ[998,2]
                                                                                                                                                                              answ[998,3]
                                                                                                                                                                                                                                           answ[998,4]
                                                                                                                                                                                                                                                                                                        answ[998,5]
                                                    answ[999,1]
                                                                                                                 answ[999,2]
                                                                                                                                                                               answ[999,3]
                                                                                                                                                                                                                                            answ[999,4]
                                                                                                                                                                                                                                                                                                        answ[999,5]
                                                    answ[1000,1]
                                                                                                                 answ[1000,2]
                                                                                                                                                                              answ[1000,3]
                                                                                                                                                                                                                                           answ[1000,4]
                                                                                                                                                                                                                                                                                                        answ[1000,5]
In [143...
                                              for i in peopl
                                                               @constraint(model_zal, sum(answ[i, :]) == 1)
                                               end
                                               for i in zals_str
                                                                @constraint(model_zal, zals_data[i, "min"] <= sum(answ[:, i]) <= zals_data[i,</pre>
                                              end
                                             @objective(model_zal, Min, sum([sum([answ[t, c]*people_pref[c, t] for c in zals_str
In [146...
                                              10000answ_{1,1} + 2answ_{1,2} + 10000answ_{1,3} + 3answ_{1,4} + answ_{1,5} + 10000answ_{2,1} + answ_{2,2} + 3answ_{1,3} + 3answ_{1,4} + answ_{2,5} + 10000answ_{2,1} + answ_{2,1} + answ_{2,2} + 3answ_{2,3} + 3answ_{2,4} + answ_{2,5} + 10000answ_{2,5} + answ_{2,5} 
Out[146...
                                              +\ 2answ_{3.5} + 10000answ_{4.1} + 3answ_{4.2} + answ_{4.3} + 2answ_{4.4} + 10000answ_{4.5} + 10000answ_{5.1} + 3answ_{5.1} + 
                                               + answ_{6,4} + 10000answ_{6,5} + [[\dots 4940 \text{ terms omitted}\dots]] + 3answ_{995,1} + 10000answ_{995,2} + 2answ_{995,1}
                                               +\ 3answ_{996.4} + 2answ_{996.5} + 3answ_{997.1} + 10000answ_{997.2} + 2answ_{997.3} + 10000answ_{997.4} + answ_{997.5} + an
                                              +\ 2answ_{999,2} + 10000answ_{999,3} + 10000answ_{999,4} + answ_{999,5} + 10000answ_{1000,1} + 3answ_{1000,2} + 2answ_{1000,1} + 3answ_{1000,2} + 2answ_{1000,1} + 3answ_{1000,2} + 2answ_{1000,1} + 3answ_{1000,1} + 3answ_{1000
In [148...
                                              optimize!(model zal)
In [149...
                                              termination_status(model_zal)
                                              OPTIMAL::TerminationStatusCode = 1
Out[149...
```

```
In [153...
         ress = value.(answ)
Out[153...
          2-dimensional DenseAxisArray{Float64,2,...} with index sets:
              Dimension 1, [1, 2, 3, 4, 5, 6, 7, 8, 9, 10 ... 991, 992, 993, 994, 995, 996,
          997, 998, 999, 1000]
              Dimension 2, [1, 2, 3, 4, 5]
          And data, a 1000×5 Matrix{Float64}:
           0.0 0.0 0.0 0.0 1.0
           0.0 1.0 0.0 0.0 0.0
           0.0 0.0 1.0 0.0 0.0
           0.0 0.0 1.0 0.0 0.0
           0.0 0.0 0.0 1.0 0.0
           0.0 1.0 0.0 0.0 0.0
           1.0 0.0 0.0 0.0 0.0
           0.0 0.0 0.0 0.0 1.0
           0.0 1.0 0.0 0.0 0.0
           1.0 0.0 0.0 0.0 0.0
           0.0 0.0 0.0 0.0 1.0
           0.0 0.0 1.0 0.0 0.0
           1.0 0.0 0.0 0.0 0.0
           0.0 0.0 0.0 1.0 0.0
           0.0 1.0 0.0 0.0 0.0
           0.0 0.0 0.0 1.0 0.0
           1.0 0.0 0.0 0.0 0.0
           0.0 0.0 1.0 0.0
                             0.0
           0.0 0.0 1.0 0.0 0.0
           0.0 0.0 0.0 0.0
                             1.0
           0.0 0.0 1.0 0.0 0.0
           0.0 0.0 0.0 0.0 1.0
           0.0 0.0 0.0 0.0 1.0
           0.0 0.0 0.0 0.0 1.0
           0.0 0.0 0.0 1.0 0.0
In [157...
         zals_filling = zeros(5)
          recomendationss = zeros(N)
          for i in peopl
             for j in zals_str
                 zals_filling[j] += ress[i, j]
                 if ress[i, j] == 1
                     recomendationss[i] = j
                 end
             end
          end
In [158...
          zals_filling
Out[158...
          5-element Vector{Float64}:
           200.0
           180.0
           220.0
           198.0
           202.0
In [159...
          recomendationss
```

```
Out[159...
           1000-element Vector{Float64}:
            5.0
            2.0
            3.0
            3.0
            4.0
            2.0
            1.0
            5.0
            2.0
            1.0
            5.0
            3.0
            1.0
            4.0
            2.0
            4.0
            1.0
            3.0
            3.0
            5.0
            3.0
            5.0
            5.0
            5.0
            4.0
```

План приготовления кофе

```
5raf = 40

In [16]: objective = 400 * raf + 300 * cappuccino @objective(model, Max, objective)

Out[16]: 400raf + 300cappuccino

In [17]: optimize!(model)

In [18]: println("Paф кофе: ", round(value(raf))) println("Капучино: ", round(value(cappuccino)))
```

Раф кофе: 8.0 Капучино: 6.0 Прибыль: 5000.0

println("Прибыль: ", value(objective))

Out[15]: