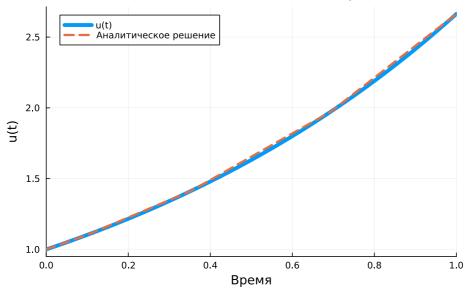
Повторение примеров

Решение обыкновенных дифференциальных уравне

Модель экспоненциального роста

```
In [1]: using DifferentialEquations
# задаём описание модели с начальными условиями:
a = 0.98
f(u,p,t) = a*u
u0 = 1.0
# задаём интервал времени:
tspan = (0.0,1.0)
# решение:
prob = ODEProblem(f,u0,tspan)
sol = solve(prob)
# подключаем необходимые пакеты:
using Plots
# строим графики:
plot(sol, linewidth=5,title="Модель экспоненциального роста", xaxis="Bpemя",yaxis="u(t)",label="u(t)")
plot!(sol.t, t->1.0*exp(a*t),lw=3,ls=:dash,label="Aналитическое решение")
```

Out[1]: Модель экспоненциального роста



```
In [2]: # задаём точность решения:
    sol = solve(prob,abstol=le-8,reltol=le-8)
    println(sol)
    # строим график:
    plot(sol, lw=2, color="black", title="Модель экспоненциального роста", xaxis="Bpemя",yaxis="u(t)",label="Числені
    plot!(sol.t, t->1.0*exp(a*t),lw=3,ls=:dash,color="red",label="Аналитическое решение")
```

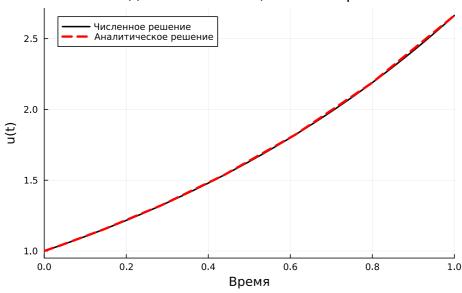
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1.7850679249179284], \; [1.7850421123301734, \; 1.7866748738768703, \; 1.820954186120135, \; 1.839183776362968, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594442, \; 1.9401594444, \; 1.9401594444, \; 1.9401594444, \; 1.9401594444, \; 1.9401594444, \; 1.9401594444, \; 1.940159444, \; 1.940159444, \; 1.940159444, \; 1.940159444, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.94015944, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9401544, \; 1.9
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92280173, 2.611167117094843, 2.6111671170948547]], [1, 1, 1, 1, 1, 1, 1, 1, 1], true, OrdinaryDiffEq.CompositeCa
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Out[2]:

Модель экспоненциального роста



Система Лоренца

```
In [3]: # задаём описание модели:
         function lorenz!(du,u,p,t)
         \sigma, \rho, \beta = p
             du[1] = \sigma^*(u[2]-u[1])
             du[2] = u[1]*(\rho-u[3]) - u[2]
         du[3] = u[1]*u[2] - \beta*u[3]
         end
         # задаём начальное условие:
         u0 = [1.0, 0.0, 0.0]
         # задаём знанчения параметров:
         p = (10, 28, 8/3)
         # задаём интервал времени:
         tspan = (0.0, 100.0)
         # решение:
         prob = ODEProblem(lorenz!,u0,tspan,p)
         sol = solve(prob)
```

```
# строим график:
plot(sol, vars=(1,2,3), lw=2, title="Аттрактор Лоренца", xaxis="x",yaxis="y", zaxis="z",legend=false)

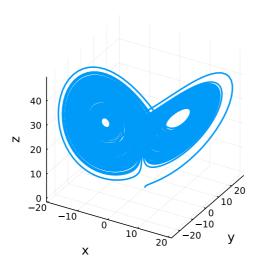
r Warning: To maintain consistency with solution indexing, keyword argument vars will be removed in a future ver sion. Please use keyword argument idxs instead.

caller = ip:0x0

@ Core :-1
```

Out[3]:

Аттрактор Лоренца

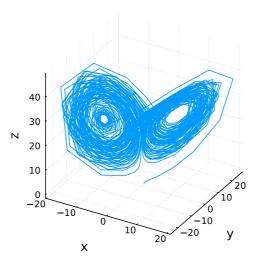


Без интерполяции

```
In [4]: # отключаем интерполяцию: plot(sol,vars=(1,2,3),denseplot=false, lw=1, title="Аттрактор Лоренца", xaxis="x",yaxis="y", zaxis="z",legend=false, lw=1, title="Aттрактор Лоренца", xaxis="x",yaxis="y", zaxis="z",legend=false, lw=1, title="Aттрактор Лоренца", xaxis="x",yaxis="y", zaxis="z",legend=false, lw=1, title="Aттрактор Лоренца", xaxis="x",yaxis="y", zaxis="z",legend=false, lw=1, title="Attraction Notes (sol, vars="y", yaxis="y", zaxis="y", zaxis="y
```

Out[4]:

Аттрактор Лоренца

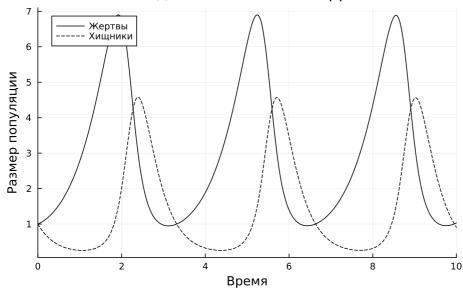


Модель Лотки-Вольтерры

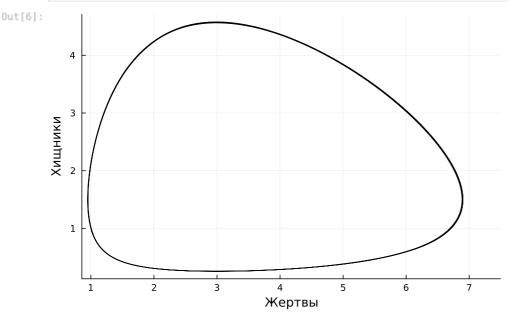
```
In [5]: using ParameterizedFunctions, DifferentialEquations, Plots;
        # задаём описание модели:
        lv! = @ode_def LotkaVolterra begin
        dx = a*x - b*x*y
        dy = -c*y + d*x*y
        end a b c d
        # задаём начальное условие:
        u0 = [1.0, 1.0]
        # задаём знанчения параметров:
        p = (1.5, 1.0, 3.0, 1.0)
        # задаём интервал времени:
        tspan = (0.0, 10.0)
        # решение:
        prob = ODEProblem(lv!,u0,tspan,p)
        sol = solve(prob)
        plot(sol, label = ["Жертвы" "Хищники"], color="black", ls=[:solid :dash], title="Модель Лотки - Вольтерры", хах
```



Модель Лотки - Вольтерры



```
In [6]: # фазовый портрет:
plot(sol,vars=(1,2), color="black", xaxis="Жертвы",yaxis="Хищники", legend=false)
```

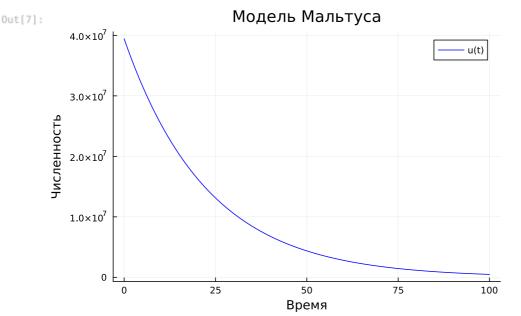


Самостоятельная работа

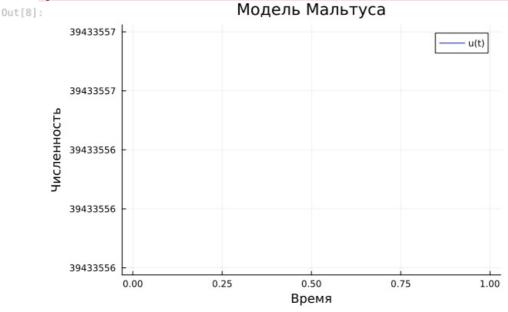
Модель Мальтуса

Модель Мальтуса --- модель роста численности изолированной популяции, где изменение роста популяции контролируется численностью уже существующей популяции, домноженной на коэффициент a, который является разницей между рождаемостью и смертностью (b-c). Коэффициенты b и c было предложено выбрать самостоятельно, и я выставлю для системы значения b=1.09 и c=1.134 (что является соответственно коэффициентами рождаемости и смертности за январьавгуст в 2022 году в Центральном федеральном округе РФ). Изначальная численность населения (39433556 человек) также взята из статистики Росстата за 2022 год (с учётом переписи населения).

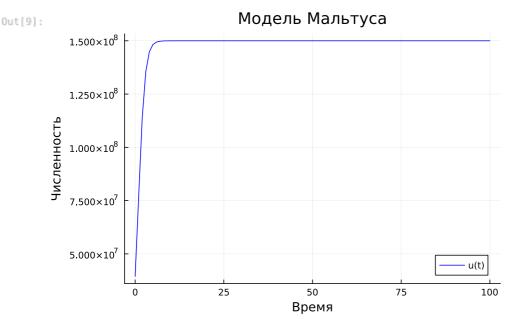
Модель Мальтуса подразумевает, что коэффициенты рождаемости и смертности не изменяются, так что если b превышает c, численность популяции будет расти (и наоборот).



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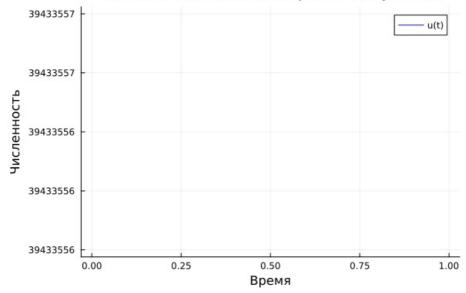


Логистическая модель роста популяции



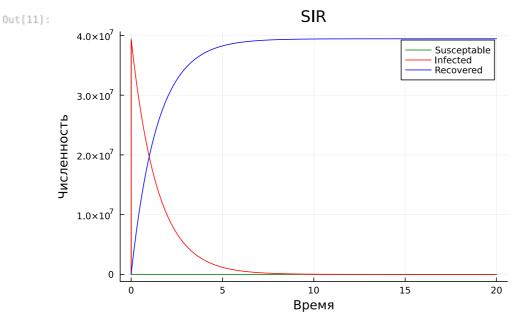
```
In [10]: anim = @animate for i in 1:length(sol.t)
             plot(sol.t[1:i], R1[1:i], title="Логистическая модель роста популяции", xaxis="Время",yaxis="Численность",la
         end
         gif(anim, "presentation//image//2.gif")
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        gif
Out[10]:
```





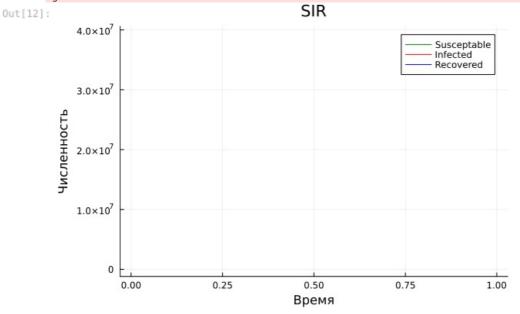
SIR

```
In [11]: function SIR!(du,u,p,t)
               du[1] = -p[1]*u[1]*u[2] # S
               du[2] = p[1]*u[2]*u[1]-p[2]*u[2] # I
               du[3] = p[2]*u[2] # R
          end
          u0 = [39433553.0, 3.0, 0.0]
          tspan = (0.0, 20.0)
          p = Float64[0.3, 0.7]
          prob = ODEProblem(SIR!,u0,tspan,p)
          sol = solve(prob,abstol=1e-6,reltol=1e-6, saveat=0.01)
          R1 = [tu[1]  for tu  in sol.u]
          R2 = [tu[2]  for tu  in sol.u]
          R3 = [tu[3] for tu in sol.u]
          plot(sol.t, R1, title="SIR", xaxis="Время",yaxis="Численность",label="Susceptable", c=:green, leg=:topright) plot!(sol.t, R2, title="SIR", label="Infected", c=:red, leg=:topright)
          plot!(sol.t, R3, label="Recovered", c=:blue, leg=:topright)
```



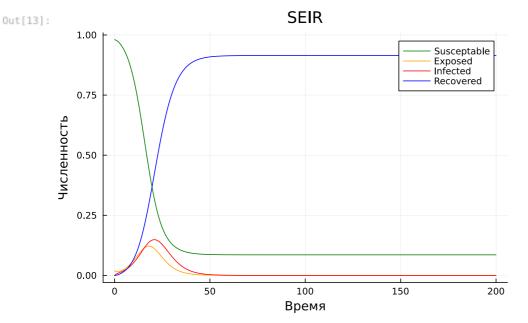
```
In [12]:
    anim = @animate for i in 1:length(sol.t)
        plot(sol.t[1:i], R1[1:i], title="SIR", xaxis="Время",yaxis="Численность",label="Susceptable", c=:green, leggent plot!(sol.t[1:i], R2[1:i], title="SIR", label="Infected", c=:red, leg=:topright)
        plot!(sol.t[1:i], R3[1:i], label="Recovered", c=:blue, leg=:topright)
    end
    gif(anim, "presentation//image//3.gif")
```

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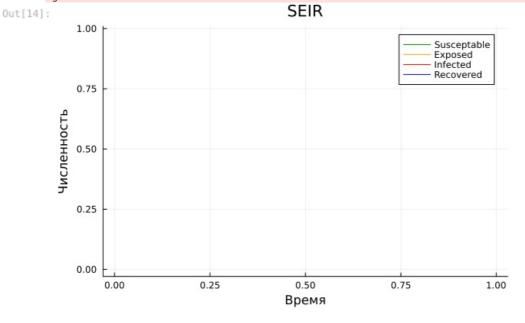
SEIR

```
In [13]: function SEIR!(du,u,p,t)
               betta, delta, gamma, N = p
               s, e, i, r = u
               du[1] = -betta / N * s * i
               du[2] = betta / N * s * i - delta * e
               du[3] = delta * e - gamma * i
               du[4] = gamma * i
          end
          u0 = [0.98, 0.02, 0.0, 0.0]
          tspan = (0.0, 200.0)
          p = Float64[0.8, 0.4, 0.3, 1.0]
          prob = ODEProblem(SEIR!,u0,tspan,p)
          sol = solve(prob,abstol=1e-6, reltol=1e-6, saveat=0.1)
          R1 = [tu[1]  for tu  in sol.u]
          R2 = [tu[2]  for tu  in sol.u]
          R3 = [tu[3]  for tu  in sol.u]
          R4 = [tu[4]  for tu  in sol.u]
          plot(sol.t, R1, title="SEIR", xaxis="Время",yaxis="Численность",label="Susceptable", c=:green, leg=:topright)
          plot!(sol.t, R2, label="Exposed", c=:orange, leg=:topright)
plot!(sol.t, R3, label="Infected", c=:red, leg=:topright)
          plot!(sol.t, R4, label="Recovered", c=:blue, leg=:topright)
```



```
In [14]:
anim = @animate for i in 1:length(sol.t)
    plot(sol.t[1:i], R1[1:i], title="SEIR", xaxis="Время",yaxis="Численность",label="Susceptable", c=:green, length plot!(sol.t[1:i], R2[1:i], label="Exposed", c=:orange, leg=:topright)
    plot!(sol.t[1:i], R3[1:i], label="Infected", c=:red, leg=:topright)
    plot!(sol.t[1:i], R4[1:i], label="Recovered", c=:blue, leg=:topright)
end
gif(anim, "presentation//image//4.gif")
```

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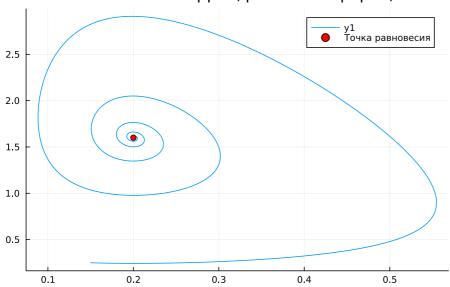
Лотки-Вольтерры

```
In [15]: using NLsolve
         # Аналитическое решение
         function find_equilibrium(a, c, d)
             function system!(du, u)
                 du[1] = a*u[1]*(1-u[1]) - u[1]*u[2]
                 du[2] = -c*u[2] + d*u[1]*u[2]
             end
             initial\_guess = [0.5, 0.5]
             result = nlsolve(system!, initial guess)
             equilibrium point = result.zero
             return equilibrium point
         # Численное решение
         function LotkiVolterry(a, c, d, x1_0, x2_0, dt, num_steps)
             x1 = x1_0
             x2 = x2_0
             results = [(x1, x2)]
```

```
for in 1:num steps
        x1_new = x1 + dt * (a * x1 * (1 - x1) - x1 * x2)
        x2 new = x2 + dt * (-c * x2 + d * x1 * x2)
        x1, x2 = x1_new, x2_new
        push!(results, (x1, x2))
    return results
end
a = 2.0
c = 1.0
d = 5.0
x1 0 = 0.15
x2^{-}0 = 0.25
dt = 0.01
num steps = 10000
results = LotkiVolterry(a, c, d, x1_0, x2_0, dt, num_steps)
R1 = [x[1] \text{ for } x \text{ in } results]
R2 = [x[2] \text{ for } x \text{ in results}]
equilibrium = find equilibrium(2,1,5)
plot(R1, R2, title="Лотки-Вольтерры (фазовый портрет)", leg=:topright)
scatter!([equilibrium[1]], [equilibrium[2]], color="red", label="Точка равновесия")
```

Out[15]:

Лотки-Вольтерры (фазовый портрет)

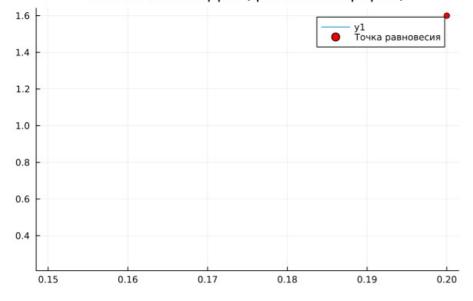


```
In [16]:
    anim = @animate for i in 1:length(R1)
        plot(R1[1:i], R2[1:i], title="Лотки-Вольтерры (фазовый портрет)", leg=:topright)
        scatter!([equilibrium[1]], [equilibrium[2]], color="red", label="Точка равновесия")
end
gif(anim, "presentation//image//5.gif")
```

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Out[16]:

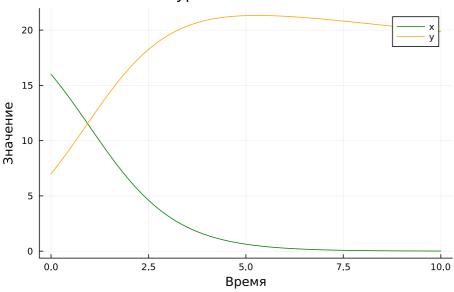
Лотки-Вольтерры (фазовый портрет)



Конкурентные отношения

Out[19]:

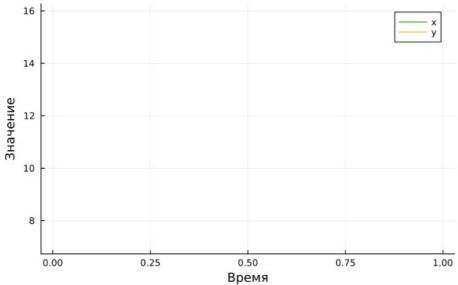
Конкурентные отношения



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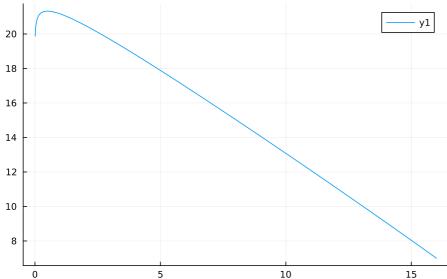
Out[20]:

Конкурентные отношения



```
In [21]: plot(R1, R2, title="Конкурентные отношения (фазовый портрет)", leg=:topright)
```

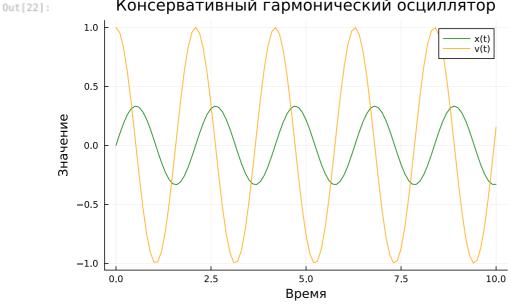
Конкурентные отношения (фазовый портрет) Out[21]:



Консервативный гармонический осциллятор

```
In [22]:
         function KGO!(du,u,p,t)
             du[1] = u[2]
             du[2] = -p[1]^2 * u[1]
         end
         u\theta = [0.0, 1.0]
         tspan = (0.0, 10.0)
         p = Float64[3.0]
         prob = ODEProblem(KGO!,u0,tspan,p)
         sol = solve(prob,abstol=1e-6, reltol=1e-6, saveat=0.1)
         R1 = [tu[1]  for tu  in sol.u]
         R2 = [tu[2]  for tu  in sol.u]
         plot(sol.t, R1, title="Консервативный гармонический осциллятор", xaxis="Время",yaxis="Значение",label="x(t)", с
         plot!(sol.t, R2, label="v(t)", c=:orange, leg=:topright)
```

Консервативный гармонический осциллятор



```
In [23]: anim = @animate for i in 1:length(R1)
             plot(sol.t[1:i], R1[1:i], title="Консервативный гармонический осциллятор", xaxis="Время",yaxis="Значение",la
             plot!(sol.t[1:i], R2[1:i], label="v(t)", c=:orange, leg=:topright)
         end
         gif(anim, "presentation//image//7.gif")
```

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Консервативный гармонический осциллятор 1.00 0.75 0.50 0.25

0.50

Время

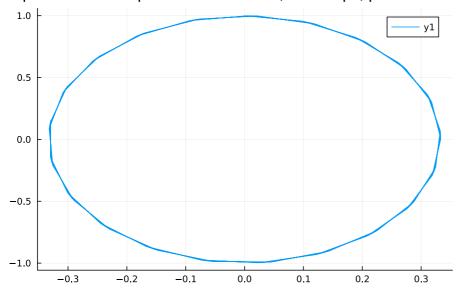
In [24]: plot(R1, R2, title="Консервативный гармонический осциллятор (фазовый портрет)", leg=:topright)

0.75

1.00

ошт[24]: Ісервативный гармонический осциллятор (фазовый по

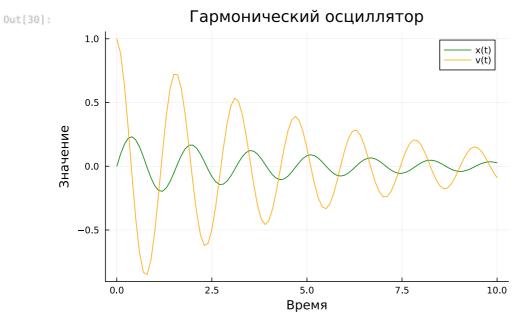
0.25



Гармонический осциллятор

0.00

```
In [30]: function GO!(du,u,p,t)
          du[1] = u[2]
          du[2] = -2.0*p[2]*u[2] - p[1]^2*u[1]
end
          u0 = [0.0, 1.0]
          tspan = (0.0,10.0)
          p = Float64[4.0, 0.2]
          prob = ODEProblem(GO!,u0,tspan,p)
          sol = solve(prob,abstol=le-6,reltol=le-6, saveat=0.1)
        R1 = [tu[1] for tu in sol.u]
        R2 = [tu[2] for tu in sol.u]
        plot(sol.t, R1, title="Гармонический осциллятор", xaxis="Время",yaxis="Значение",label="x(t)", c=:green, leg=:toplot!(sol.t, R2, label="v(t)", c=:orange, leg=:topright)
```



```
In [33]: anim = @animate for i in 1:length(R1)
    plot(sol.t[1:i], R1[1:i], title="Гармонический осциллятор", xaxis="Время",yaxis="Значение",label="x(t)", c=
    plot!(sol.t[1:i], R2[1:i], label="v(t)", c=:orange, leg=:topright)
end
gif(anim, "presentation//image//8.gif")
```

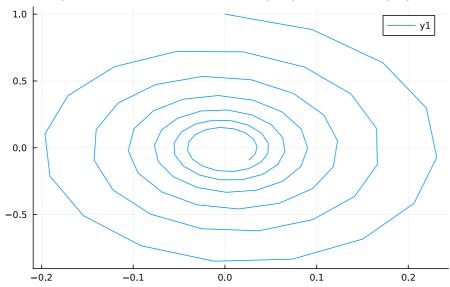
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Out[33]:


```
In [32]: plot(R1, R2, title="Гармонический осциллятор (фазовый портрет)", leg=:topright)
```

Out[32]:

Гармонический осциллятор (фазовый портрет)



Processing math: 100%