# Namespace Methods

# Namespaces

Methods.Enums

Methods.Interfaces

Methods.MathObjects

Methods.Models

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# Namespace Methods.Enums

## **Enums**

<u>ConstraintType</u>

Represents the type of a constraint in a LPP.

# **Enum ConstraintType**

Namespace: Methods. Enums

Assembly: Methods.dll

Represents the type of a constraint in a LPP.

public enum ConstraintType

## **Fields**

Equal = 2

Equality constraint.

GreaterThanOrEqual = 1

Greater than or equal to constraint.

LessThanOrEqual = 0

Less than or equal to constraint.

# Namespace Methods.Interfaces

## **Interfaces**

### <u>ILinearSolver</u>

Interface that represents the essential methods for solving Linear Programming Problems (LPPs).

## Interface ILinearSolver

Namespace: Methods.Interfaces

Assembly: Methods.dll

Interface that represents the essential methods for solving Linear Programming Problems (LPPs).

public interface ILinearSolver

### **Methods**

## CalculateReducedCosts()

Calculates the reduced costs (delta values) for the current simplex tableau.

void CalculateReducedCosts()

## IsOptimal()

Determines whether the current solution is optimal.

bool IsOptimal()

#### Returns

bool♂

true if the problem has an optimal solution; otherwise, false.

### IsUnbounded()

Determines whether the LPP has a solution.

bool IsUnbounded()

### Returns

### <u>bool</u> ♂

true if the problem has no solution; otherwise, false.

## Pivot()

Finds the pivot row and column for the next step of solving.

```
void Pivot()
```

## Solve()

Performs the steps required to solve the linear programming problem.

```
void Solve()
```

# Namespace Methods.MathObjects

## Classes

### Constraint

Class that represent a constraint parts

### $\underline{Linear Programming Problem}$

Represents a LPP.

## **Class Constraint**

Namespace: Methods.MathObjects

Assembly: Methods.dll

Class that represent a constraint parts

```
public class Constraint : ICloneable
```

#### Inheritance

<u>object</u> <a>™</a> <a></a> <a>Constraint</a>

#### **Implements**

#### **Inherited Members**

 $\underline{object.Equals(object)} \ \ \ \ \ \underline{object.Equals(object, object)} \ \ \ \ \ \underline{object.MemberwiseClone()} \ \ \ \ \ \underline{object.ReferenceEquals(object, object)} \ \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \underline{object.T$ 

## **Properties**

### Coefficients

List of coefficients.

```
public List<string> Coefficients { get; set; }
```

### Property Value

<u>List</u> ♂ < <u>string</u> ♂ >

## RightHandSide

Represents the expression on the right-hand side of the constraint.

```
public string RightHandSide { get; set; }
```

## Property Value

## Type

Represents the type of constraint, such as greater than or equal, less than or equal, or equal.

```
public ConstraintType Type { get; set; }
```

Property Value

<u>ConstraintType</u>

## **Methods**

## Clone()

Creates a clone of the current object.

```
public object Clone()
```

### Returns

A new instance of the **Constraint** object.

# Class LinearProgrammingProblem

Namespace: Methods.MathObjects

Assembly: Methods.dll

Represents a LPP.

public class LinearProgrammingProblem : ICloneable

Inheritance

object ← LinearProgrammingProblem

**Implements** 

#### **Inherited Members**

 $\underline{object.Equals(object)} \ \ \ \ \ \underline{object.Equals(object, object)} \ \ \ \ \ \underline{object.MemberwiseClone()} \ \ \ \ \ \underline{object.ReferenceEquals(object, object)} \ \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \underline{object.T$ 

## **Properties**

### **ArtificialVariableCoefficients**

Coefficients for artificial variables.

```
public List<string> ArtificialVariableCoefficients { get; set; }
```

Property Value

<u>List</u> ♂ < <u>string</u> ♂ >

### Constraints

List of constraints defining the problem.

```
public required List<Constraint> Constraints { get; set; }
```

### Property Value

<u>List</u> < <u>Constraint</u> >

### **IsMaximization**

Indicates whether the problem is a maximization (true) or minimization (false).

```
public bool IsMaximization { get; init; }
```

Property Value

<u>bool</u> ♂

## ObjectiveFunctionCoefficients

Coefficients of the objective function.

```
public required List<string> ObjectiveFunctionCoefficients { get; set; }
```

Property Value

<u>List</u> ♂ < <u>string</u> ♂ >

### SlackVariableCoefficients

Coefficients for slack variables.

```
public List<string> SlackVariableCoefficients { get; set; }
```

Property Value

<u>List</u> ♂ < <u>string</u> ♂ >

### VariablesCount

Gets the total number of variables, including primary, slack, and artificial variables.

```
public int VariablesCount { get; }
```

Property Value

<u>int</u>♂

## Methods

## Clone()

Creates a copy of the linear programming problem.

```
public object Clone()
```

Returns

<u>object</u> ♂

A clone of the current  $\underline{\text{LinearProgrammingProblem}}$  object.

# Namespace Methods. Models

### Classes

#### **BranchCut**

Represents a parts of Gomory cut.

### **ExpressionValue**

Represents a text expression for the table and its actual numeric value.

#### **GomoryHistory**

Represents the current state of finding an integer solution using the Gomory cut method.

#### **SimplexHistory**

Represents the history of the simplex algorithm solving process.

#### <u>SimplexStep</u>

Represents the current state of the simplex table during pivot selection.

### **SimplexTable**

Represents a simplex tableau used during the simplex algorithm iterations.

## Class BranchCut

Namespace: Methods. Models

Assembly: Methods.dll

Represents a parts of Gomory cut.

```
public class BranchCut
```

#### Inheritance

<u>object</u> ← BranchCut

#### **Inherited Members**

<u>object.Equals(object)</u> dobject.Equals(object, object) dobject.GetHashCode() dobject.GetType() dobject.MemberwiseClone() dobject.ReferenceEquals(object, object) dobject.ToString() dob

## **Properties**

### CutExpression

List of Gomory cut values, calculated as x20 - [x20].

```
public List<Fraction> CutExpression { get; set; }
```

### Property Value

<u>List</u> < Fraction >

### FractionalElements

Dictionary containing fractional elements and their integer parts.

```
public Dictionary<string, (Fraction intPart, Fraction valueOfOriginalFraction)>
FractionalElements { get; set; }
```

<u>Dictionary</u> ♂ < <u>string</u> ♂, (Fraction <u>intPart</u> ♂, Fraction <u>valueOfOriginalFraction</u> ♂)>

### Remarks

Each entry maps a fractional variable name (e.g., y20) to a tuple, where intPart is the integer part [x20] and valueOfOriginalFraction is the original fraction value x20.

# Class ExpressionValue

Namespace: Methods. Models

Assembly: Methods.dll

Represents a text expression for the table and its actual numeric value.

public class ExpressionValue

#### Inheritance

<u>object</u> < Expression Value

#### **Inherited Members**

 $\underline{object.Equals(object)} \ \ \ \ \ \underline{object.Equals(object, object)} \ \ \ \ \ \ \underline{object.GetHashCode()} \ \ \ \ \ \underline{object.GetType()} \ \ \ \ \ \ \underline{object.MemberwiseClone()} \ \ \ \ \ \underline{object.ReferenceEquals(object, object)} \ \ \ \ \ \underline{object.ToString()} \ \ \ \ \underline{object.ToString()} \ \ \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \underline{objec$ 

### Constructors

### ExpressionValue(string, Fraction)

Represents a text expression for the table and its actual numeric value.

public ExpressionValue(string expressionText, Fraction value)

#### **Parameters**

expressionText string d

value Fraction

## **Properties**

## ExpressionText

Formatted text for the table, used in the Big M method to represent expressions like "7M - 11".

```
public string ExpressionText { get; set; }
```

Property Value

## Value

Actual numeric value of the expression.

```
public Fraction Value { get; set; }
```

Property Value

Fraction

# **Class GomoryHistory**

Namespace: Methods. Models

Assembly: Methods.dll

Represents the current state of finding an integer solution using the Gomory cut method.

```
public class GomoryHistory
```

#### Inheritance

<u>object</u> <a>del GomoryHistory</a>

#### **Inherited Members**

<u>object.Equals(object)</u> dobject.Equals(object, object) dobject.GetHashCode() dobject.GetType() dobject.MemberwiseClone() dobject.ReferenceEquals(object, object) dobject.ToString() dob

## **Properties**

### Cut

Current branch cut applied in the Gomory method.

```
public BranchCut Cut { get; set; }
```

Property Value

**BranchCut** 

### MaxFracValue

Maximum fractional part found from the optimal (non-integer) solution. The tuple contains the row index and the fractional value.

```
public (int rowIndex, Fraction value) MaxFracValue { get; set; }
```

(<u>int</u> rowIndex 7, Fraction value 7)

## Steps

List of simplex steps taken during the Gomory cut process.

```
public List<SimplexStep> Steps { get; set; }
```

Property Value

<u>List</u> ♂ < <u>SimplexStep</u> >

# **Class SimplexHistory**

Namespace: Methods. Models

Assembly: Methods.dll

Represents the history of the simplex algorithm solving process.

```
public class SimplexHistory
```

#### Inheritance

<u>object</u> 

✓ 

← SimplexHistory

#### **Inherited Members**

<u>object.Equals(object)</u> ¬ <u>object.Equals(object, object)</u> ¬ <u>object.GetHashCode()</u> ¬ <u>object.GetType()</u> ¬ <u>object.MemberwiseClone()</u> ¬ <u>object.ReferenceEquals(object, object)</u> ¬ <u>object.ToString()</u> ¬

## **Properties**

### ArtificialProblemProblem

LLP that including artificial variables.

```
public LinearProgrammingProblem? ArtificialProblemProblem { get; set; }
```

### Property Value

<u>LinearProgrammingProblem</u>

### **InitialBasis**

Initial basis variables with their values. Key — variable name; Value — RHS taken from the corresponding constraint.

```
public Dictionary<string, string> InitialBasis { get; set; }
```

### Property Value

## InitialLinearProgrammingProblem

Initial LPP before any transformations.

```
public LinearProgrammingProblem? InitialLinearProgrammingProblem { get; set; }
```

Property Value

<u>LinearProgrammingProblem</u>

## OptimalTable

Optimal simplex table.

```
public SimplexTable? OptimalTable { get; set; }
```

Property Value

<u>SimplexTable</u>

### SlackVariableProblem

LLP that including slack variables.

```
public LinearProgrammingProblem? SlackVariableProblem { get; set; }
```

Property Value

<u>LinearProgrammingProblem</u>

### Steps

List of simplex steps performed during the solving process.

```
public List<SimplexStep> Steps { get; set; }
```

Property Value

<u>List</u> ♂ < <u>SimplexStep</u> >

# Class SimplexStep

Namespace: Methods. Models

Assembly: Methods.dll

Represents the current state of the simplex table during pivot selection.

```
public class SimplexStep
```

#### Inheritance

<u>object</u> 

✓ SimplexStep

#### **Inherited Members**

## **Properties**

### PivotColumn

Index of the pivot column in the current simplex table.

```
public int PivotColumn { get; set; }
```

Property Value

<u>int</u>♂

### **PivotRow**

Index of the pivot row in the current simplex table.

```
public int PivotRow { get; set; }
```

### Property Value

## Table

Simplex tableau at the current step.

```
public required SimplexTable Table { get; set; }
```

Property Value

<u>SimplexTable</u>

# Class SimplexTable

Namespace: Methods. Models

Assembly: Methods.dll

Represents a simplex tableau used during the simplex algorithm iterations.

```
public class SimplexTable : ICloneable
```

#### Inheritance

<u>object</u> do ← SimplexTable

#### **Implements**

#### **Inherited Members**

<u>object.Equals(object)</u> , <u>object.Equals(object, object)</u> , <u>object.GetHashCode()</u> , <u>object.GetType()</u> , <u>object.MemberwiseClone()</u> , <u>object.ReferenceEquals(object, object)</u> , <u>object.ToString()</u>

## **Properties**

### ColumnVariables

Dictionary of column variables, where the key is the variable name (e.g., "A0"), and the value is the corresponding coefficient from the objective function.

```
public Dictionary<string, string> ColumnVariables { get; set; }
```

### Property Value

<u>Dictionary</u> ♂ < <u>string</u> ♂, <u>string</u> ♂ >

### DeltaRow

Delta row values representing the results after computing reduced costs.

```
public List<ExpressionValue> DeltaRow { get; set; }
```

### Property Value

<u>List</u> < <u>ExpressionValue</u> >

### **RowVariables**

Dictionary of row variables, where the key is the variable name (e.g., "x1"), and the value is the corresponding coefficient from the objective function.

```
public Dictionary<string, string> RowVariables { get; set; }
```

## Property Value

<u>Dictionary</u> ♂ < <u>string</u> ♂, <u>string</u> ♂ >

### **ThetaRow**

Theta row values used to identify pivot elements during the Gomory method.

```
public List<string> ThetaRow { get; set; }
```

### Property Value

<u>List</u> ♂ < <u>string</u> ♂ >

### **Values**

Numerical values of the simplex tableau.

```
public Fraction[,] Values { get; set; }
```

### Property Value

Fraction[,]

# Methods

# Clone()

Creates a clone of the current object.

```
public object Clone()
```

### Returns

### 

A new instance of the  $\underline{\text{SimplexTable}}$  object.

# Namespace Methods. Solvers

## Classes

### <u>GomorySolver</u>

Represents a solver for the Gomory Cutting Plane method.

### <u>SimplexSolver</u>

Solver for Linear Programming Problems using the Simplex method.

# Class GomorySolver

Namespace: Methods. Solvers

Assembly: Methods.dll

Represents a solver for the Gomory Cutting Plane method.

public class GomorySolver : ILinearSolver

#### Inheritance

<u>object</u> de GomorySolver

#### **Implements**

<u>ILinearSolver</u>

#### **Inherited Members**

 $\underline{object.Equals(object)} \ \ \ \ \ \underline{object.Equals(object, object)} \ \ \ \ \ \underline{object.MemberwiseClone()} \ \ \ \ \ \underline{object.ReferenceEquals(object, object)} \ \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \underline{object.T$ 

### Constructors

## GomorySolver(SimplexTable, LinearProgrammingProblem)

Represents a solver for the Gomory Cutting Plane method.

public GomorySolver(SimplexTable Table, LinearProgrammingProblem Problem)

#### **Parameters**

#### Table <u>SimplexTable</u>

The simplex table obtained after solving by the Simplex method.

Problem <u>LinearProgrammingProblem</u>

The initial linear programming problem.

## **Properties**

## GomoryHistory

History of each Gomory cut step.

```
public List<GomoryHistory> GomoryHistory { get; set; }
```

Property Value

<u>List</u> □ < <u>GomoryHistory</u> >

### **Methods**

## CalculateReducedCosts()

Calculates the reduced costs (delta values) for the current simplex tableau.

```
public void CalculateReducedCosts()
```

## IsOptimal()

Determines whether the current solution in the simplex table is optimal.

```
public bool IsOptimal()
```

### Returns

#### bool₫

true if the solution is optimal; otherwise, false.

### Remarks

A solution is optimal if all values in the first column are non-negative.

## IsUnbounded()

Determines whether the LPP has a solution. If the chosen row does not contain fractional values, no solution is found.

```
public bool IsUnbounded()
```

#### Returns

#### bool♂

true if the problem has no solution; otherwise, false.

### Pivot()

Finds the pivot row and column for the next solving step.

```
public void Pivot()
```

### Remarks

The pivot row is determined by the minimum value in column A0. Then, the theta row is calculated as  $|\Delta|$  \* xij|, and the pivot column is chosen by the minimum theta value. After that, the reduced costs are recalculated.

### Exceptions

<u>InvalidOperationException</u> 

☑

Arises if the pivot column is not found.

## Solve()

Performs the steps required to solve the LPP.

```
public void Solve()
```

### Remarks

First, checks whether the current solution contains non-integer values or is not optimal. If the solution is not optimal, calls the pivot method and repeats the check. If it is optimal, verifies whether a feasible solution exists.

Then, finds the most fractional value in the solution, constructs the Gomory cut, adds it to the simplex table, and determines the pivot element.

### Exceptions

### <u>InvalidOperationException</u> ☑

"Arises if no solution exists or the given initial values are optimal."

# Class SimplexSolver

Namespace: Methods.Solvers

Assembly: Methods.dll

Solver for Linear Programming Problems using the Simplex method.

public class SimplexSolver : ILinearSolver

#### Inheritance

#### **Implements**

<u>ILinearSolver</u>

#### **Inherited Members**

 $\underline{object.Equals(object)} \ \ \ \ \ \underline{object.Equals(object, object)} \ \ \ \ \ \underline{object.MemberwiseClone()} \ \ \ \ \ \underline{object.ReferenceEquals(object, object)} \ \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \ \underline{object.ToString()} \ \ \underline{object.T$ 

### Constructors

## SimplexSolver(LinearProgrammingProblem)

Solver for Linear Programming Problems using the Simplex method.

public SimplexSolver(LinearProgrammingProblem problem)

### **Parameters**

problem LinearProgrammingProblem

The LPP to be solved.

## **Properties**

SimplexHistory

Stores the history of the Simplex solving process.

```
public SimplexHistory SimplexHistory { get; set; }
```

Property Value

<u>SimplexHistory</u>

### **Table**

The current Simplex table used during the solution process.

```
public SimplexTable Table { get; set; }
```

Property Value

<u>SimplexTable</u>

### **Methods**

## CalculateReducedCosts()

Calculates the reduced costs (delta values) for the current simplex tableau.

```
public void CalculateReducedCosts()
```

## IsOptimal()

Determines whether the current solution in the simplex table is optimal.

```
public bool IsOptimal()
```

Returns

bool₫

true if the solution is optimal; otherwise, false.

#### Remarks

The solution is optimal if all values in the delta row are non-negative when maximizing the objective function, or all values are non-positive when minimizing.

## IsUnbounded()

Determines whether the LPP has a solution.

```
public bool IsUnbounded()
```

#### Returns

#### <u>bool</u> ☑

true if the problem has no solution; otherwise, false.

#### Remarks

Returns true if the basis still contains artificial variables even though the delta row indicates an optimal solution.

### Pivot()

Finds the pivot row and column for the next solving step.

```
public void Pivot()
```

### Remarks

The pivot column is determined by the minimum or maximum value, depending on the objective function. Then, in the pivot column, the minimum positive row value is found and selected as the pivot row. Finally, recalculates all table values accordingly.

### Exceptions

<u>InvalidOperationException</u> 

☑

Thrown if the pivot row cannot be determined (all values in the pivot column are less than or equal to 0).

## Solve()

Performs the steps required to solve the linear programming problem.

public void Solve()

### Remarks

First, if the right-hand side (RHS) of any constraint is less than 0, the constraints are converted into canonical form. Then, slack and artificial variables (if needed) are added. After that, the initial simplex table is initialized. The solver proceeds by calculating reduced costs, checking for solution existence, determining if the solution is optimal, and searching for a pivot element. Finally, artificial variables are removed if they were added.

### Exceptions

<u>InvalidOperationException</u> 

☑

Thrown if artificial variables remain in the basis after solving.