

#### Group no. 4

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#### Assignment 6:

Our first dynamic programming assignment, on dynamic alignment (i.e., measuring differences between strings).

Ans...

Let  $M$  be the alignment.  $m, n$  be the position of symbols in  $X$  and  $Y$  respectively. We are considering  $\min(i, j)$  to be the minimum cost. For  $M$  at least one of the following is required to be true:

I.  $(m, n) \in M \rightarrow$

if this holds true then  $\alpha_{x_m y_n}$  is required to be paid. Along with this, align  $x_1 x_2 x_3 \dots x_{m-1}$  with  $y_1 y_2 y_3 \dots y_{n-1}$ .  
 $\min(m, n) = \alpha_{x_m y_n} + \min(m-1, n-1)$

II.  $m$ th position of  $X$  is not matched  $\rightarrow$

If this holds true, then a gap cost of  $\delta$  is paid. Along with this, align  $x_1 x_2 x_3 \dots x_{m-1}$  with  $y_1 y_2 y_3 \dots y_n$ .  
 $\min(m, n) = \delta + \min(m-1, n)$

III.  $n$ th position of  $Y$  is not matched  $\rightarrow$

If this holds true, then a gap cost of  $\delta$  is paid. Along with this, align  $x_1 x_2 x_3 \dots x_m$  with  $y_1 y_2 y_3 \dots y_{n-1}$ .  
 $\min(m, n) = \delta + \min(m, n-1)$

The minimum alignment costs can be given as:

$$\min(i, j) = \min\{\alpha_{x_m y_n} + \min(m-1, n-1), \delta + \min(m-1, n), \delta + \min(m, n-1)\}$$

Algorithm:

1. Considering Array  $M[0 \dots m, 0 \dots n]$
2. Initialising  $M[i, 0] = i \delta$  for all  $i$  and  $M[0, j] = j \delta$  for all  $j$   
...(M[i, 0] =  $i \delta$  and M[0, j] =  $j \delta$  ... we are lining  $i, j$ -letter word to  $0$ -letter word is to use  $i, j$ -gap)
3. For  $j = 1 \rightarrow n$  do
  - a. For  $i = 1 \rightarrow m$  do
    - i.  $\min(i, j) = \min\{\alpha_{x_m y_n} + \min(m-1, n-1), \delta + \min(m-1, n), \delta + \min(m, n-1)\}$
  - b. End
4. End