# Statistical Methods for Discrete Response, Time Series, and Panel Data (W271): Group Lab 3

## U.S. traffic fatalities: 1980-2004

In this lab, you are asked to answer the question "Do changes in traffic laws affect traffic fatalities?" To do so, you will conduct the tasks specified below using the data set *driving.Rdata*, which includes 25 years of data that cover changes in various state drunk driving, seat belt, and speed limit laws.

Specifically, this data set contains data for the 48 continental U.S. states from 1980 through 2004. Various driving laws are indicated in the data set, such as the alcohol level at which drivers are considered legally intoxicated. There are also indicators for "per se" laws—where licenses can be revoked without a trial—and seat belt laws. A few economics and demographic variables are also included. The description of the each of the variables in the dataset is come with the dataste.

```
library(foreign)
library(gplots)
library(ggplot2)
library(dplyr)
library(corrplot)
library(lattice)
library(plm)
library(viridis)
library(tsibble)
library(forecast)
#library(tidyverse)
library(gridExtra)
```

#### **Exercises:**

1. (30%) Load the data. Provide a description of the basic structure of the dataset, as we have done throughout the semester. Conduct a very thorough EDA, which should include both graphical and tabular techniques, on the dataset, including both the dependent variable totfatrte and the potential explanatory variables. You need to write a detailed narrative of your observations of your EDA. Reminder: giving an "output dump" (i.e. providing a bunch of graphs and tables without description and hoping your audience will interpret them) will receive a zero in this exercise.

```
#load data
load('driving.RData')
driving.df <- data
dim(driving.df)
## [1] 1200
           56
#check for gaps in panel
table(data$state)
##
##
                 8 10 11 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29
## 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51
table(data$year)
##
## 1980 1981 1982 1983 1984 1985 1986 1987 1988 1989 1990 1991 1992 1993 1994 1995
        48
            48
                48
                    48
                        48
                            48
                                48
                                    48
                                        48
                                            48
                                                48
                                                    48
                                                        48
                                                            48
                                                                48
  1996 1997 1998 1999
                  2000 2001 2002 2003 2004
   48
        48
            48
                48
                    48
                        48
                            48
                                48
##
                                    48
```

The Dataset is panel data, that contains observations about different US states from year 1980 to 2004. There are 1200 observations in total, with 56 columns. The data has 25 observations each, one per year, from 48 continental states except state ids 2,9 and 12 (which we will later identify as Alaska, District Of Columbia and Hawaii that are not part of continental US States). All variables are observed for all states and over all time periods, hence the panel is balanced. Important variables are:

### Panel Index

year: 1980 through 2004

state: numeric id of 48 continental states, ordered alphabetically, ranging from 1 to 51.

### Dependent Variable

totfatrte: total fatalities per 100,000 population by year by state. Values range from 6.2 to 53.32

## Speed Limit Variables

sl55: 1 if speed limit == 55 for the whole year. If the law was in effect only during part of the year, it is set to fractions of 12. This applies for all indicator variables.

sl65: 1 if speed limit == 65 sl70: 1 if speed limit == 70 sl75: 1 if speed limit == 75 slnone: 1 if no speed limit sl70plus: sl70 + sl75 + slnone

## **Drinking Laws**

minage: minimum drinking age, ranges from 18 years to 21 years.

zerotol: 1 if zero tolerance law was in effect, and 0 if not. If the law was in effect only during part of the year, it is set to fractions of 12.

bac10: 1 if blood alcohol limit .10 in effect, and 0 if not. Fractions used to denote partial years, as above.

bac08: 1 if blood alcohol limit .08 in effect, and 0 if not. Fractions used to denote partial years, as above.

per se: 1 if administrative license revocation (per se law) in effect, and 0 if not. Fractions used to denote partial years, as above.

### Seatbelt Laws

sbprim: 1 if primary seatbelt law was in effect, 0 otherswise. There are no fractions in this variable. sbsecon: 1 if secondary seatbelt law was in effect, 0 otherswise. There are no fractions in this variable.

seatbelt: 0 if none, =1 if primary, =2 if secondary. There are no fractions in this variable.

## Age iimit Laws

gdl: 1 if graduated drivers license law was in effect, and 0 if not. Fractions used to denote partial years, similar to speed limit.

## Demographic variables

statepop: state population by year by state. Values range from 453,401 to 35,894,000 vehicmiles: vehicle miles traveled, billions. Values range from 3.7027 to 329.6 unem: unemployment rate, percent. Values range from 3.2 to 18 perc14\_24: percent population aged 14 through 24. Values range from 11.7 to 20.3

### Year Dummy

Dummy variables d80 - d04 indicating years

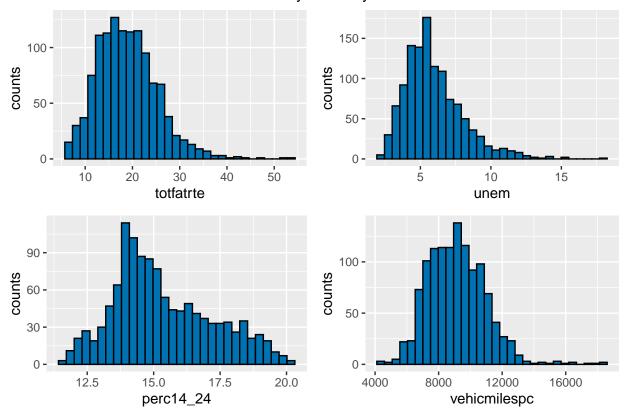
It will be useful to add more context around the state information, in addition to the state id. Since we know the id is alphabetical, we get the aphabetical list of US states with two letter abbreviated code, and match with the state variable in fatality data.

```
#get state name
us.states = read.csv("usstates.csv", header = TRUE, sep = ",", dec = ".")
data.with.name <- merge(data, us.states, by=c("state", "state"))</pre>
```

To start EDA, we perform univariate analyses of important variables fatality rate, unemployment, % of younger population, and vehiclemilespc to examine the distribution.

```
totfatrte.hist <- ggplot(driving.df, aes(x = totfatrte)) + geom_histogram(bins = 30, fill="#unem.hist <- ggplot(driving.df, aes(x = unem)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = perc14_24)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x = vehicmilespc)) + geom_histogram(bins = 30, fill="#0072B2", comperc14_24.hist <- ggplot(driving.df, aes(x =
```

# Univariate Analysis of key Variables



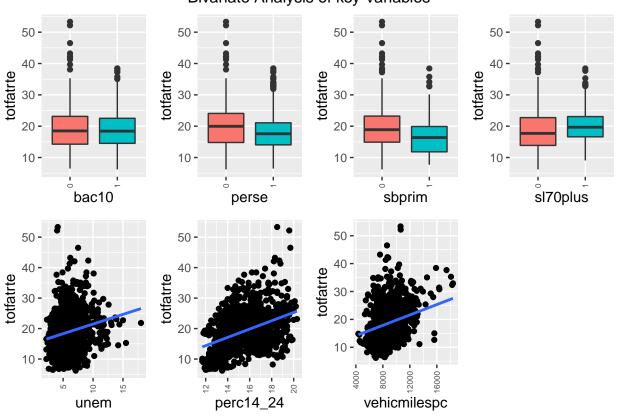
The distribution looks approximately normal with some tail for totfatrte, unem, and vehiclemilespc. It looks normal with higher slope at the top and lower slope at the bottom for perc14-24.

Next, we examine the bivaraite relationship between some of the important explanatory variables and fatality rate.

```
totfatrte.unem.scatter <- ggplot(driving.df, aes(unem, totfatrte)) +
  geom_point() +
  geom_smooth(method = "lm", formula = y ~ x, se = FALSE) + theme(axis.text.x = element_text(a)
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
totfatrte.perc14_24.scatter <- ggplot(driving.df, aes(perc14_24, totfatrte)) +
  geom_point() +
  geom_smooth(method = "lm", formula = y ~ x, se = FALSE) + theme(axis.text.x = element_text(axis.text.x)
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
totfatrte.vehicmilespc.scatter <- ggplot(driving.df, aes(vehicmilespc, totfatrte)) +
  geom_point() +
  geom_smooth(method = "lm", formula = y ~ x, se = FALSE) + theme(axis.text.x = element_text(a)
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
# grid.arrange(
    totfatrte.unem.scatter, totfatrte.perc14_24.scatter, totfatrte.vehicmilespc.scatter,
    ncol = 2, nrow = 2,
    top="Bivariate Analysis of key Variables")
```

```
driving.df.mutate <- driving.df %>%
 mutate(bac08 = ifelse(bac08 > 0.5,1,0)) \%
 mutate(bac10 = ifelse(bac10 > 0.5,1,0)) \%%
 mutate(perse = ifelse(perse > 0.5,1,0)) %>%
 mutate(s170plus = ifelse(s170plus > 0.5,1,0)) \%
 mutate(gdl = ifelse(gdl > 0.5,1,0))
totfatrte.bac10.box \leftarrow ggplot(driving.df.mutate, aes(x = factor(bac10), y = totfatrte)) +
  geom_boxplot(aes(fill = factor(bac10))) + xlab("bac10") + theme(axis.text.x = element_text(axis.text))
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
totfatrte.perse.box \leftarrow ggplot(driving.df.mutate, aes(x = factor(perse), y = totfatrte)) +
  geom_boxplot(aes(fill = factor(perse))) + xlab("perse") + theme(axis.text.x = element_text(axis.text))
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
totfatrte.sbprim.box \leftarrow ggplot(driving.df.mutate, aes(x = factor(sbprim), y = totfatrte)) +
  geom_boxplot(aes(fill = factor(sbprim)))+ xlab("sbprim") + theme(axis.text.x = element_text())
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
totfatrte.sl70plus.box \leftarrow ggplot(driving.df.mutate, aes(x = factor(sl70plus), y = totfatrte))
  geom_boxplot(aes(fill = factor(s170plus)))+ xlab("s170plus") + theme(axis.text.x = element_text.x
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
grid.arrange( totfatrte.bac10.box, totfatrte.perse.box, totfatrte.sbprim.box, totfatrte.sl70pl
  ncol = 4, nrow = 2,
  top="Bivariate Analysis of key Variables")
```

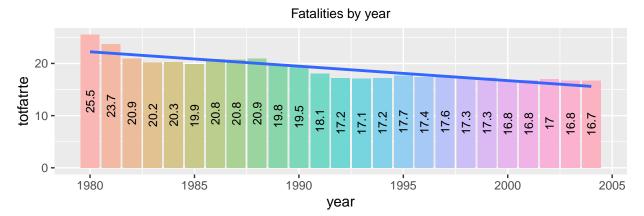
# Bivariate Analysis of key Variables



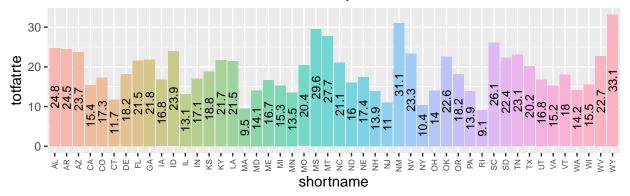
Then, determine both the common and individual driving behaviors of US States across time, we'll analyze the aggregate of traffic laws in US across time and across states. Then we'll focus on the fatality progression of top and bottom ranked US states across years. We'll also evaluate how the fatality pattern is different between years 1980 and 2004.

Below we analyze the fatality rate change by year and overall change by state.

```
#fatality change by year
traffic.yearly.aggr <- data %>%
                                  group_by(year) %>% summarise_at(vars(totfatrte, nghtfatrte,
#fatality change by state
traffic.state.perc.aggr <- data.with.name %>%
  group_by(shortname) %>%
  summarise_at(vars(totfatrte,nghtfatrte,wkndfatrte), funs(mean))
year.plot <- ggplot(traffic.yearly.aggr, aes(year, totfatrte)) +</pre>
  geom_bar(aes(fill = factor(year)), position = "dodge", stat="identity") + ggtitle("Fatalities
  #geom_abline(intercept, slope, linetype, color, size) +
  geom_smooth(method = "lm", formula = y ~ x, se = FALSE) + geom_text(data = traffic.yearly.ag
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
state.plot <- ggplot(traffic.state.perc.aggr, aes(shortname, totfatrte)) +</pre>
  geom_bar(aes(fill = factor(shortname)), position = "dodge", stat="identity") + ggtitle("Fata
  scale_fill_hue(c=45,l=80) + theme(plot.title = element_text(size = 8, hjust = 0.5)) +
  theme(axis.text.x = element_text(angle = 90, size = 6, vjust = 0.5, hjust=1)) +
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none") +
conditional_plot = function(data, plotvar, condvar, title) {
 g <- ggplot(data, aes(as.factor(condvar), plotvar, color = as.factor(condvar)))</pre>
 g + geom_boxplot() + geom_jitter(width = 0.2) + ggtitle(title) + theme(axis.text.x = element
}
# yIndex by year (Heterogeineity across year)
cplot.1 <- conditional plot(data.with.name, data.with.name$totfatrte, data.with.name$year, "To
# yIndex by country (Heterogeineity across countries)
cplot.2 <- conditional_plot(data.with.name, data.with.name$totfatrte, data.with.name$name, "To
grid.arrange(year.plot, state.plot, nrow = 2, ncol = 1)
```



# Fatalities by state

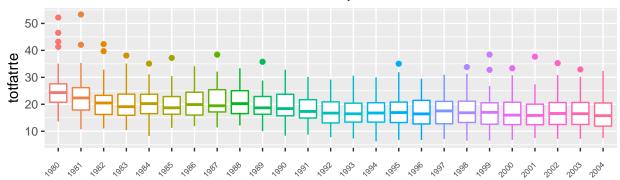


```
cplot.1 <- data.with.name %>%
    ggplot(aes(x = factor(year), y = totfatrte,color = as.factor(year))) +
    geom_boxplot() + ggtitle("Totalfatrte by Year") + theme(axis.text.x = element_text(angle = 4)

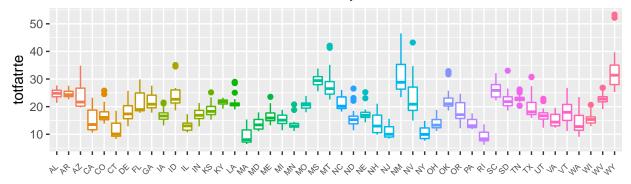
cplot.2 <- data.with.name %>%
    ggplot(aes(x = factor(shortname), y = totfatrte,color = as.factor(name))) +
    geom_boxplot() + ggtitle("Totalfatrte by State") + theme(axis.text.x = element_text(angle = 4)

grid.arrange(cplot.1, cplot.2, nrow = 2, ncol = 1)
```





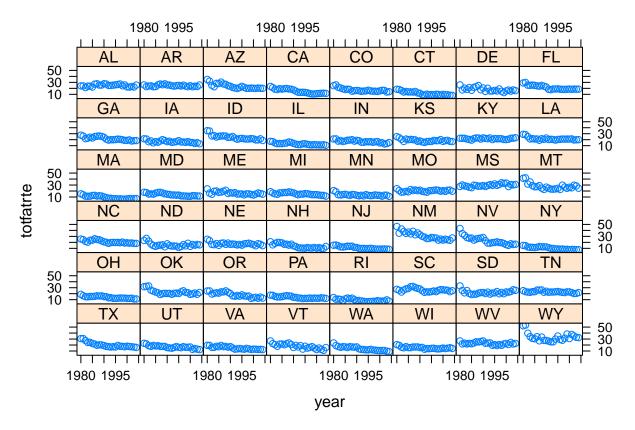
## Totalfatrte by State



We can see that the fatality rate is largely decreasing from 1980 to 2004. The fatality rates range from ~9 to ~34. Wyoming, New Mexico, Mississippi, Montana, and South Carolina are the states with highest fatality rates while New York, New Jersey and Rhode Island are the states with lowest fatality rates. The pattern shows that the states with more rural roads have higher fatality rates - the geography and road conditions are thus important omitted variables in the dataset. In addition, the fatality split by cause (drunk driving, speeding) by state by year could be an important predictor. Another omitted variable could be the a measure of compliance to the traffic laws - speed limit, seat belt - at the state level. #TODO add about heterogeneity in year (not much) and state (there is)

Next we analyze how the fatality rates varied over the years, in individual states.

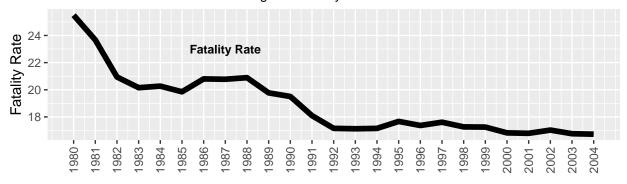
xyplot(totfatrte ~ year | shortname, data=data.with.name, as.table=T)

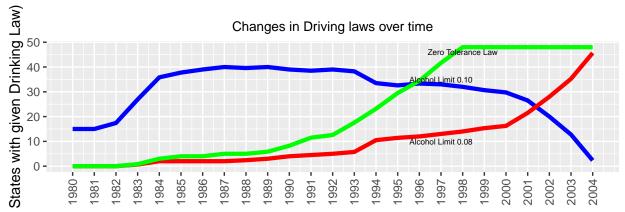


The above xyplot confirms that most of the States shows an overall decrease in the traffic fatality rate, except states like *Mississippi*. One interesting point is that the traffic fatality rate is not dependent on the state area or population - the top 2 states with size and population, Texas and California, are not amoing the top states in traffic fatality rate.

Below, we explore the prevalence of traffic laws over the years. We hypothesize that the fatality rate is influeced the most by drinking and overspeeding and proceed to examine the applicable laws.

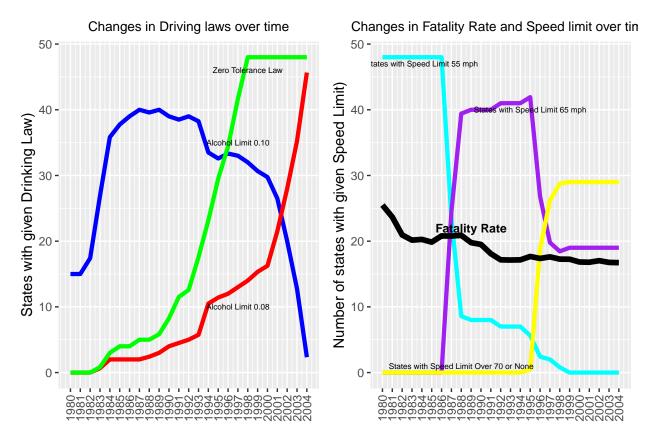
## Changes in Fatality Rate Over Time





```
sl.df <- data %>% group_by(year) %>%
summarise(sl55 = sum(sl55), sl65 = sum(sl65),sl70plus = sum(sl70plus), totfatrte = mean(totfat:
sl.plot <- ggplot(sl.df, aes(x = year)) +
geom_line(aes(y = sl55, color='sl55'), size = 1.5, group = 1) +</pre>
```

```
geom_line(aes(y = sl65, color='sl65'), size = 1.5, group = 1) +
  geom_line(aes(y = s170plus, color='s170plus'), size = 1.5, group = 1) +
  geom_line(aes(y=totfatrte, color='totfatrte'), size = 2, group = 1) +
  scale_x_continuous(breaks = seq(min(sl.df$year), max(sl.df$year), 1)) + theme(axis.text.x = 6
      values = c(
            s155 = "cyan",
            s165 = "purple",
           s170plus="yellow",
           totfatrte="black")) + labs(title = "Changes in Fatality Rate and Speed limit over t
y = "Number of states with given Speed Limit)",
x = "") +
  annotate("text", x = 1989, y = 22, label = "Fatality Rate", size = 3, fontface = "bold") +
  annotate("text", x = 1984, y = 47, label = "States with Speed Limit 55 mph", size = 2) +
   annotate("text", x = 1995, y = 40, label = "States with Speed Limit 65 mph", size = 2) +
   annotate("text", x = 1988, y = 1, label = "States with Speed Limit Over 70 or None", size =
  theme(plot.title = element_text(size = 10, hjust = 0.5)) + theme(legend.position = "none")
grid.arrange(bac.plot, sl.plot, nrow = 1, ncol = 2)
```



Over the years, more states are adopting stricter alcohol limits. In 2004, over 45 states have a stricter bac limit of 0.08, compared to 0 in 1980. Similarly, all states have adopted the zero tolerance law in 2004 compared to 0 states in 1980. This is consistent with the decrease in fatality rates over time that observed before. Regarding speed limit, states had lower speed limit in 1980

- however, the speed limits were more relaxed in the later years as can be seen by the increase in the number of states with speed limit 70 or above, as seen in the above graph.

```
\#TODO add bac8 + 10, sbprime, per se, gdl.
```

Vehicle Miles shows an increase over years while % of youngest population and unemployment rate reduced ever so sightly.

Thus we see that some of the traffic and demographic variables show similar patterns as fatality rate and could be important predictors for the fatality rate.

Lets proceed to examine the individual behavior in the panel. First, we'll examine how the traffic fatality rates changed over years for the first 3 States from the top and bottom of the fatality rate.

```
#fatality change by state
traffic.state.aggr <- data.with.name %>%
    group_by(shortname) %>%
    summarise_at(vars(totfat, nghtfat,wkndfat), funs(sum))

top.3.fatalities <- traffic.state.perc.aggr %>%
        filter(rank(desc(totfatrte))<=3) %>% arrange(desc(totfatrte))

bottom.3.fatalities <- traffic.state.perc.aggr %>%
        filter(rank((totfatrte))<=3) %>% arrange((totfatrte))

cbind(top.3.fatalities[,1:2],bottom.3.fatalities[,1:2])
```

```
##
     shortname totfatrte shortname totfatrte
## 1
                 33.1408
                                        9.0900
            WY
                                 RΙ
## 2
                 31.0608
            NM
                                 MA
                                        9.4512
## 3
            MS
                 29.5548
                                       10.4380
                                 NY
```

```
data.top.filtered <- data.with.name %>% filter(shortname %in% c("WY"))
data.bottom.filtered <- data.with.name %>% filter(shortname %in% c("RI"))

#data.with.name %>% filter(shortname %in% c("MS", "NM", "WY", "MA", "NY", "RI") & year == '2004') %
#data.with.name %>% filter(year == '2004') %>% dplyr::select(year,name,totfatrte) %>% arrange(
data.merged <- union(data.top.filtered,data.bottom.filtered)</pre>
```

The top 3 are Wyoming, New Mexico and Mississippi. The bottom 3 are Rhode Island, New York and Massachussets. To put this in context, in 2004, in Wyoming, the probability of dying in a motor vehicle accident is nearly 5 times as high as in Rhode Island, the state with the lowest death rate. Below, we see the average fatality rate for each state across years.

```
df.transformed <- data.merged %>%
  mutate(
    perse = case_when(
    perse >= 0.5 ~ 1,
```

```
TRUE ~ 0
),
bacat = case_when(
  bac10+bac08 >= 0.5 ~ 1,
  TRUE ~ 0
)
)

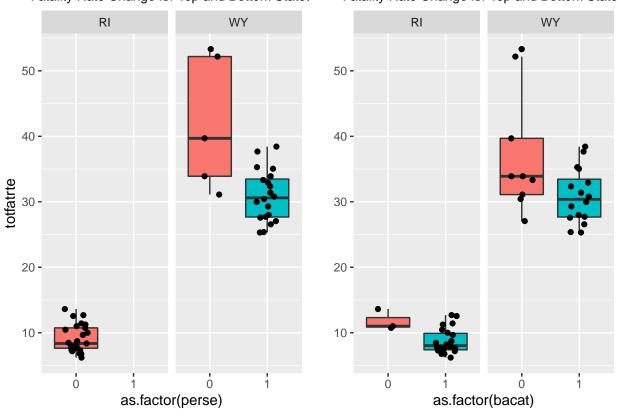
g.1 <- ggplot(df.transformed, aes(as.factor(perse), totfatrte)) + geom_boxplot(aes(fill = factor))

g.2 <- ggplot(df.transformed, aes(as.factor(bacat), totfatrte)) + geom_boxplot(aes(fill = factor))

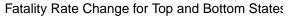
grid.arrange(g.1, g.2, nrow = 1, ncol = 2)</pre>
```

## Fatality Rate Change for Top and Bottom States

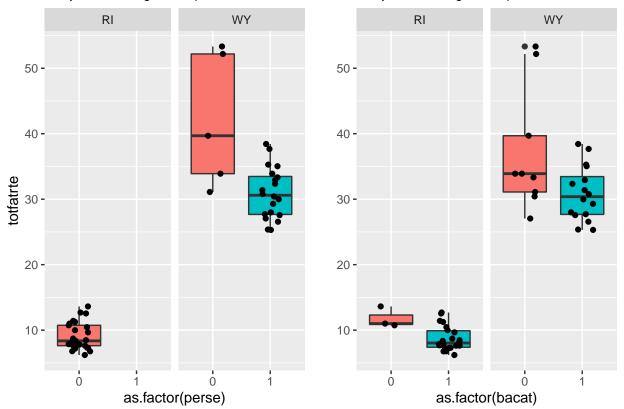
## Fatality Rate Change for Top and Bottom States



```
g.1 <- ggplot(df.transformed, aes(as.factor(perse), totfatrte)) + geom_boxplot(aes(fill = factor)
g.2 <- ggplot(df.transformed, aes(as.factor(bacat), totfatrte)) + geom_boxplot(aes(fill = factor)
grid.arrange(g.1, g.2, nrow = 1, ncol = 2)</pre>
```



## Fatality Rate Change for Top and Bottom States



```
df.80.04 <- data.with.name %>% filter(year %in% c('1980','2004')) %>% dplyr::select(year,shorts)
ggplot(df.80.04, aes(shortname, totfatrte, group = year, colour = as.factor(year))) +
   geom_line(aes(y=totfatrte), size = 2) + ggtitle("Growth Curve by Year") + theme(axis.text.x)
```

# Growth Curve by Year



The plotmeans graph shows there is heterogeneity across states, but very little heterogeneity across years. #TODO: The above graphs collectively provide the below information. Some of them are different ways of representing the same info, we need to pick and choose.

We can see that New Mexico and Wyoming has high variance in the data, with NM consistently reducing the traffic fatality rate over years. However, WY reduced the fatality rate from 80's to mid 90's and had a gradual increase after. The bottom 3 states have very low variance across years.

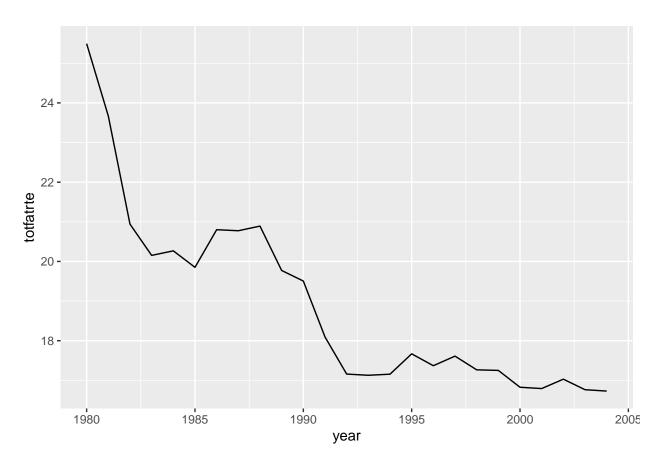
2. (15%) How is the our dependent variable of interest totfatrte defined? What is the average of this variable in each of the years in the time period covered in this dataset? Estimate a linear regression model of totfatrte on a set of dummy variables for the years 1981 through 2004. What does this model explain? Describe what you find in this model. Did driving become safer over this period? Please provide a detailed explanation.

totfatrte defines the total fatalities per 100,000 population.

```
yearlyavg <- aggregate(totfatrte~year, driving.df, mean)
# Printing the yearly average for total fatality rate
yearlyavg</pre>
```

```
## year totfatrte
## 1 1980 25.49458
```

```
## 2 1981 23.67021
## 3 1982 20.94250
## 4 1983 20.15292
## 5 1984 20.26750
## 6 1985 19.85146
## 7
     1986 20.80042
## 8
     1987 20.77479
## 9 1988 20.89167
## 10 1989 19.77229
## 11 1990 19.50521
## 12 1991
          18.09479
## 13 1992 17.15792
## 14 1993 17.12771
## 15 1994 17.15521
## 16 1995 17.66854
## 17 1996 17.36938
## 18 1997
          17.61062
## 19 1998 17.26542
## 20 1999 17.25042
## 21 2000 16.82562
## 22 2001
          16.79271
## 23 2002 17.02958
## 24 2003 16.76354
## 25 2004 16.72896
# Plotting the yearly total fatality rate
ggplot(yearlyavg) +
 geom_line(
   mapping = aes(x = year, y = totfatrte)
)
```



```
##
## Call:
\#\# lm(formula = totfatrte \sim d81 + d82 + d83 + d84 + d85 + d86 +
       d87 + d88 + d89 + d90 + d91 + d92 + d93 + d94 + d95 + d96 +
       d97 + d98 + d99 + d00 + d01 + d02 + d03 + d04, data = driving.df)
##
##
## Residuals:
        Min
                  1Q
                       Median
                                     ЗQ
                                             Max
## -12.9302 -4.3468
                     -0.7305
                                3.7488 29.6498
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                            0.8671
## (Intercept) 25.4946
                                     29.401 < 2e-16 ***
## d81
                -1.8244
                            1.2263
                                    -1.488 0.137094
## d82
                -4.5521
                            1.2263
                                    -3.712 0.000215 ***
                                    -4.356 1.44e-05 ***
## d83
                -5.3417
                            1.2263
## d84
                            1.2263 -4.263 2.18e-05 ***
                -5.2271
```

```
-4.602 4.64e-06 ***
## d85
                -5.6431
                             1.2263
## d86
                -4.6942
                             1.2263
                                     -3.828 0.000136 ***
                                     -3.849 0.000125 ***
## d87
                -4.7198
                             1.2263
                                     -3.754 0.000183 ***
## d88
                -4.6029
                             1.2263
## d89
                -5.7223
                             1.2263
                                     -4.666 3.42e-06 ***
## d90
                -5.9894
                             1.2263
                                     -4.884 1.18e-06 ***
## d91
                -7.3998
                             1.2263
                                     -6.034 2.14e-09 ***
## d92
                -8.3367
                             1.2263
                                     -6.798 1.68e-11 ***
## d93
                -8.3669
                             1.2263
                                     -6.823 1.43e-11 ***
## d94
                -8.3394
                             1.2263
                                     -6.800 1.66e-11 ***
## d95
                -7.8260
                                     -6.382 2.51e-10 ***
                             1.2263
## d96
                -8.1252
                             1.2263
                                     -6.626 5.25e-11 ***
                                     -6.429 1.86e-10 ***
## d97
                -7.8840
                             1.2263
## d98
                -8.2292
                             1.2263
                                     -6.711 3.01e-11 ***
## d99
                -8.2442
                             1.2263
                                     -6.723 2.77e-11 ***
                                     -7.069 2.67e-12 ***
## d00
                -8.6690
                             1.2263
## d01
                -8.7019
                             1.2263
                                     -7.096 2.21e-12 ***
                                     -6.903 8.32e-12 ***
## d02
                -8.4650
                             1.2263
                                     -7.120 1.88e-12 ***
## d03
                -8.7310
                             1.2263
                             1.2263
                                     -7.148 1.54e-12 ***
## d04
                -8.7656
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.008 on 1175 degrees of freedom
## Multiple R-squared: 0.1276, Adjusted R-squared: 0.1098
## F-statistic: 7.164 on 24 and 1175 DF, p-value: < 2.2e-16
```

3. (15%) Expand your model in Exercise 2 by adding variables bac08, bac10, perse, sbprim, sbsecon, sl70plus, gdl, perc14\_24, unem, vehicmilespc, and perhaps transformations of some or all of these variables. Please explain carefully your rationale, which should be based on your EDA, behind any transformation you made. If no transformation is made, explain why transformation is not needed. How are the variables bac8 and bac10 defined? Interpret the coefficients on bac8 and bac10. Do per se laws have a negative effect on the fatality rate? What about having a primary seat belt law? (Note that if a law was enacted sometime within a year the fraction of the year is recorded in place of the zero-one indicator.)

 $\#\# lm(formula = totfatrte \sim d81 + d82 + d83 + d84 + d85 + d86 +$ 

d87 + d88 + d89 + d90 + d91 + d92 + d93 + d94 + d95 + d96 +

 $d97 + d98 + d99 + d00 + d01 + d02 + d03 + d04 + bac08 + bac10 + perse + sbprim + sbsecon + sl70plus + gdl + perc14_24 + unem +$ 

##

##

##

```
##
       vehicmilespc, data = driving.df)
##
## Residuals:
##
       Min
                                    3Q
                  1Q
                       Median
                                            Max
## -14.9160 -2.7384
                     -0.2778
                                2.2859
                                        21.4203
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                           2.476e+00 -1.097 0.272847
## (Intercept)
               -2.716e+00
                -2.175e+00
## d81
                           8.276e-01
                                      -2.629 0.008686 **
## d82
                           8.534e-01 -7.729 2.33e-14 ***
                -6.596e+00
## d83
                -7.397e+00
                           8.690e-01
                                      -8.512 < 2e-16 ***
## d84
                -5.850e+00
                           8.763e-01
                                      -6.676 3.79e-11 ***
## d85
                -6.483e+00
                          8.948e-01
                                      -7.245 7.82e-13 ***
## d86
                -5.853e+00
                           9.307e-01
                                      -6.289 4.52e-10 ***
## d87
                -6.367e+00 9.670e-01 -6.585 6.87e-11 ***
## d88
                -6.592e+00
                           1.014e+00
                                      -6.502 1.17e-10 ***
## d89
                                      -7.667 3.68e-14 ***
                -8.071e+00
                          1.053e+00
                          1.077e+00 -8.319 2.46e-16 ***
## d90
                -8.959e+00
## d91
                -1.107e+01 1.101e+00 -10.052
                                               < 2e-16 ***
## d92
                -1.288e+01
                           1.123e+00 -11.473
                                               < 2e-16 ***
## d93
                -1.273e+01 1.136e+00 -11.204
                                               < 2e-16 ***
## d94
                -1.236e+01 1.157e+00 -10.685
                                               < 2e-16 ***
## d95
                -1.195e+01 1.184e+00 -10.098
                                              < 2e-16 ***
## d96
                -1.388e+01 1.223e+00 -11.343 < 2e-16 ***
## d97
                -1.426e+01 1.250e+00 -11.408 < 2e-16 ***
## d98
                -1.504e+01 1.265e+00 -11.886 < 2e-16 ***
## d99
                -1.509e+01 1.284e+00 -11.750 < 2e-16 ***
## d00
                -1.544e+01 1.305e+00 -11.831
                                               < 2e-16 ***
## d01
                -1.618e+01 1.334e+00 -12.131
                                               < 2e-16 ***
                -1.672e+01 1.348e+00 -12.406
## d02
                                              < 2e-16 ***
## d03
                -1.702e+01 1.359e+00 -12.521
                                               < 2e-16 ***
## d04
                -1.671e+01 1.387e+00 -12.049
                                              < 2e-16 ***
                                      -4.648 3.73e-06 ***
## bac08
                -2.498e+00 5.375e-01
                -1.418e+00 3.963e-01
## bac10
                                      -3.577 0.000362 ***
## perse
                -6.201e-01
                           2.982e-01
                                      -2.079 0.037791 *
## sbprim
                -7.533e-02 4.908e-01
                                      -0.153 0.878032
                6.728e-02 4.293e-01
## sbsecon
                                        0.157 0.875492
## s170plus
                 3.348e+00 4.452e-01
                                        7.521 1.09e-13 ***
                -4.269e-01 5.269e-01
                                      -0.810 0.417978
## gdl
                 1.416e-01
## perc14_24
                           1.227e-01
                                        1.154 0.248675
                 7.571e-01
                           7.791e-02
                                        9.718 < 2e-16 ***
## unem
                                      30.804 < 2e-16 ***
## vehicmilespc 2.925e-03
                           9.497e-05
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.046 on 1165 degrees of freedom
## Multiple R-squared: 0.6078, Adjusted R-squared: 0.5963
```

```
## F-statistic: 53.1 on 34 and 1165 DF, p-value: < 2.2e-16
```

bac10 is defined as the blood alcohol limit of .10 bac08 is defined as the blood alcohol limit of .08

Both the variables bac08 and bac10 have the negative coefficients of -2.498 and -1.418 respectively. They are statistically significant and it implies that they have a strong negative correlation to the total fatality rate. If we come up with a stricter law and decrease the blood alcohol limit to .10 then the fatalities rate decreases more.

Yes. perse variable has a statistically significant negative correlation with the total fatality rate. The coefficient value is -0.6201 which implies a small change in the rate.

## **TODO** write up about primary seatbelt law

4. (15%) Reestimate the model from *Exercise 3* using a fixed effects (at the state level) model. How do the coefficients on *bac08*, *bac10*, *perse*, *and sbprim* compare with the pooled OLS estimates? Which set of estimates do you think is more reliable? What assumptions are needed in each of these models? Are these assumptions reasonable in the current context?

```
pnldata <- pdata.frame(driving.df, c("state", "year"))</pre>
model.fe <- plm(totfatrte ~ d81+d82+d83+d84+d85+d86+d87+d88+d89+
                      d90+d91+d92+d93+d94+d95+d96+d97+d98+d99+
                      d00+d01+d02+d03+d04 + bac08 + bac10 + perse + sbprim + sbsecon + s170plu
summary(model.fe)
## Oneway (individual) effect Within Model
##
## Call:
## plm(formula = totfatrte ~ d81 + d82 + d83 + d84 + d85 + d86 +
       d87 + d88 + d89 + d90 + d91 + d92 + d93 + d94 + d95 + d96 +
##
       d97 + d98 + d99 + d00 + d01 + d02 + d03 + d04 + bac08 + bac10 +
##
       perse + sbprim + sbsecon + sl70plus + gdl + perc14_24 + unem +
##
##
       vehicmilespc, data = pnldata, model = "within")
##
## Balanced Panel: n = 48, T = 25, N = 1200
##
## Residuals:
##
         Min.
                 1st Qu.
                              Median
                                        3rd Qu.
                                                      Max.
## -8.4273592 -1.0258600 -0.0029547 0.9572345 14.8109310
##
## Coefficients:
##
                   Estimate Std. Error t-value Pr(>|t|)
## d81
                -1.51107133   0.41321486   -3.6569   0.0002672 ***
## d82
                -3.02549578   0.44243119   -6.8383   1.316e-11 ***
## d83
                -3.50360069 0.45657705 -7.6736 3.628e-14 ***
                -4.25936110 0.46494255 -9.1610 < 2.2e-16 ***
## d84
## d85
                -4.72679311 0.48547032 -9.7365 < 2.2e-16 ***
```

```
-3.66118539 0.51769787 -7.0721 2.686e-12 ***
## d86
## d87
             -4.76712131   0.60155650   -7.9246   5.501e-15 ***
## d88
             -6.12997263 0.64019069 -9.5752 < 2.2e-16 ***
## d89
## d90
             -6.22973766 0.66485076 -9.3701 < 2.2e-16 ***
             -6.91714040 0.68195432 -10.1431 < 2.2e-16 ***
## d91
## d92
             -7.77417239 0.70288580 -11.0604 < 2.2e-16 ***
## d93
             -8.09410864 0.71594741 -11.3055 < 2.2e-16 ***
## d94
             -8.50421668 0.73410866 -11.5844 < 2.2e-16 ***
## d95
             -8.25540198 0.75623634 -10.9164 < 2.2e-16 ***
## d96
             -8.60661913 0.79594975 -10.8130 < 2.2e-16 ***
## d97
             -8.70781739  0.81975686  -10.6224 < 2.2e-16 ***
             ## d98
## d99
             -9.47489124  0.84399083  -11.2263  < 2.2e-16 ***
## d00
             -9.99185979  0.85606370  -11.6719 < 2.2e-16 ***
             -9.63121721  0.87255395  -11.0380 < 2.2e-16 ***
## d01
## d02
             ## d03
             -9.33936116  0.91107045  -10.2510 < 2.2e-16 ***
## d04
             -1.43722116  0.39421213  -3.6458  0.0002788 ***
## bac08
## bac10
             -1.15161719  0.23398721  -4.9217  9.867e-07 ***
## perse
             -1.22739974   0.34271485   -3.5814   0.0003564 ***
## sbprim
## sbsecon
             -0.34970784 0.25217091 -1.3868 0.1657826
## s170plus
             ## gdl
             -0.41177619 0.29257391 -1.4074 0.1595790
## perc14_24
              0.18712169  0.09509969  1.9676  0.0493567 *
## unem
             -0.57183997  0.06057851  -9.4397 < 2.2e-16 ***
## vehicmilespc 0.00094005 0.00011104 8.4656 < 2.2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:
                        12134
## Residual Sum of Squares: 4535.3
## R-Squared:
                0.62624
## Adj. R-Squared: 0.59916
## F-statistic: 55.0943 on 34 and 1118 DF, p-value: < 2.22e-16
```

5. (10%) Would you perfer to use a random effects model instead of the fixed effects model you built in *Exercise* 4? Please explain.

## Oneway (individual) effect Random Effect Model

```
(Swamy-Arora's transformation)
##
##
## Call:
## plm(formula = totfatrte \sim d81 + d82 + d83 + d84 + d85 + d86 +
##
       d87 + d88 + d89 + d90 + d91 + d92 + d93 + d94 + d95 + d96 +
       d97 + d98 + d99 + d00 + d01 + d02 + d03 + d04 + bac08 + bac10 +
##
##
       perse + sbprim + sbsecon + sl70plus + gdl + perc14 24 + unem +
##
       vehicmilespc, data = pnldata, model = "random")
## Balanced Panel: n = 48, T = 25, N = 1200
##
## Effects:
##
                   var std.dev share
## idiosyncratic 4.057
                         2.014 0.328
## individual
                 8.294
                         2.880 0.672
## theta: 0.8615
##
## Residuals:
##
       Min. 1st Qu.
                       Median 3rd Qu.
                                           Max.
## -8.25582 -1.15221 -0.15787 0.93086 16.45691
##
## Coefficients:
##
                   Estimate Std. Error z-value Pr(>|z|)
                                          8.1801 2.835e-16 ***
## (Intercept)
                 1.7149e+01 2.0964e+00
## d81
                -1.5489e+00 4.2830e-01 -3.6164 0.0002988 ***
## d82
                -3.2433e+00 4.5772e-01 -7.0858 1.383e-12 ***
## d83
                -3.7447e+00 4.7212e-01 -7.9318 2.161e-15 ***
## d84
                -4.3729e+00 4.8064e-01 -9.0981 < 2.2e-16 ***
## d85
                -4.8609e+00 5.0136e-01 -9.6954 < 2.2e-16 ***
## d86
                -3.8295e+00 5.3416e-01 -7.1693 7.539e-13 ***
## d87
                -4.5014e+00 5.7213e-01 -7.8678 3.610e-15 ***
## d88
                -4.9819e+00 6.1887e-01 -8.0500 8.279e-16 ***
## d89
                -6.3713e+00 6.5797e-01 -9.6833 < 2.2e-16 ***
## d90
                -6.5357e+00 6.8279e-01 -9.5720 < 2.2e-16 ***
## d91
                -7.3027e+00 7.0030e-01 -10.4279 < 2.2e-16 ***
## d92
                -8.2390e+00 7.2126e-01 -11.4230 < 2.2e-16 ***
## d93
                -8.5418e+00 7.3449e-01 -11.6296 < 2.2e-16 ***
## d94
                -8.9183e+00 7.5297e-01 -11.8442 < 2.2e-16 ***
                -8.6769e+00 7.7541e-01 -11.1902 < 2.2e-16 ***
## d95
## d96
                -9.0969e+00 8.1573e-01 -11.1518 < 2.2e-16 ***
                -9.2203e+00 8.3984e-01 -10.9786 < 2.2e-16 ***
## d97
                -9.8922e+00 8.5380e-01 -11.5860 < 2.2e-16 ***
## d98
## d99
                -1.0032e+01 8.6426e-01 -11.6071 < 2.2e-16 ***
## d00
                -1.0549e+01 8.7667e-01 -12.0330 < 2.2e-16 ***
## d01
                -1.0274e+01 8.9336e-01 -11.5000 < 2.2e-16 ***
## d02
                -9.6376e+00 9.0278e-01 -10.6755 < 2.2e-16 ***
## d03
                -9.6828e+00 9.1090e-01 -10.6300 < 2.2e-16 ***
## d04
                -1.0054e+01 9.3254e-01 -10.7816 < 2.2e-16 ***
```

```
## bac08
                -1.5693e+00 4.0384e-01 -3.8860 0.0001019 ***
## bac10
                -1.1380e+00 2.7604e-01
                                        -4.1227 3.744e-05 ***
                -1.0933e+00 2.3885e-01
                                        -4.5772 4.712e-06 ***
## perse
                                        -3.3465 0.0008184 ***
## sbprim
                -1.1761e+00 3.5144e-01
## sbsecon
                -3.4758e-01 2.6024e-01
                                        -1.3356 0.1816862
## s170plus
                2.9969e-02 2.7772e-01
                                         0.1079 0.9140655
## gdl
                -3.8524e-01 3.0249e-01
                                        -1.2736 0.2028095
                                         2.0259 0.0427722 *
## perc14_24
                 1.9695e-01 9.7213e-02
                -4.9238e-01 6.1839e-02 -7.9622 1.690e-15 ***
## unem
## vehicmilespc 1.1744e-03
                            1.0983e-04 10.6933 < 2.2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:
                            12834
## Residual Sum of Squares: 5078.6
## R-Squared:
                   0.60429
## Adj. R-Squared: 0.59274
## Chisq: 1779.05 on 34 DF, p-value: < 2.22e-16
```

#### phtest(model.fe, model.re)

```
##
## Hausman Test
##
## data: totfatrte ~ d81 + d82 + d83 + d84 + d85 + d86 + d87 + d88 + d89 + ...
## chisq = 148.69, df = 34, p-value = 2.727e-16
## alternative hypothesis: one model is inconsistent
```

Fixed effect model should be used

6. (10%) Suppose that *vehicmilespc*, the number of miles driven per capita, increases by 1,000. Using the FE estimates, what is the estimated effect on *totfatrte*? Please interpret the estimate.

The coefficient for the *vehicmilespc* variable is 0.00094005 using the FE estimates and it is highly statistically significant. In other words, There will be an increase of 0.94 fatalities per 100k for an increase of 1000 vehicle miles driven per capita.

7. (5%) If there is serial correlation or heteroskedasticity in the idiosyncratic errors of the model, what would be the consequences on the estimators and their standard errors?

There is no serial correlation in the idiosyncratic errors of our model as shown in the p-value below. However if there is Serial correlation then it will not affect the unbiasedness or consistency of OLS estimators, but it does affect their efficiency. With positive serial correlation, the OLS estimates of the standard errors will be smaller than the true standard errors. This will lead to the conclusion that the parameter estimates are more precise than they really are. There will be a tendency to reject the null hypothesis when it should not be rejected.

# pbgtest(model.fe)

```
##
## Breusch-Godfrey/Wooldridge test for serial correlation in panel models
##
## data: totfatrte ~ d81 + d82 + d83 + d84 + d85 + d86 + d87 + d88 + d89 + d90 + d91 + d90
## chisq = 340.4, df = 25, p-value < 2.2e-16
## alternative hypothesis: serial correlation in idiosyncratic errors</pre>
```