2. GAMMA SOURCES

Most isotopes that are used for gamma measurements also have betas in their decay schemes. The typical decay scheme for the isotope will include a beta decay to a particular level followed by gamma emission to the ground state of the final isotope. The beta particles will usually be absorbed in the surrounding material and not enter the scintillator at all. This absorption is normally assured with aluminum absorbers. For this experiment the betas offer no real problem and so absorbers are not specified. There will be some beta absorption by the light shield over the phototube. The gammas, however, are quite penetrating and hence will pass easily through the aluminum light shield.

Generally there are two unknowns that we would like to investigate about a gamma source. One is the energy of the gammas from the source. The other is the number of gammas that leave the source per unit of time. In this experiment the student will become familiar with some of the basic NaI(Tl) measurements associated with gamma-emitting unknowns.

3. ENERGY CALIBRATION

3.1 Setup of Equipment

Set up the electronics in the arrangement shown in Fig.1. There are two parameters that ultimately determine the overall gain of the system: the high voltage that is furnished to the phototube and the gain of the linear amplifier. The gain of the photomultiplier tube is quite dependent upon its high voltage. A rule of thumb for most phototubes is that a 10% change of the high voltage will change the gain by a factor of 2. The high-voltage value depends on the phototube being used; consult your instruction manual for the phototube and select a value in the middle of its normal operating range.
(The instructor may wish to recommend a value.)

Set the indicated modules as follows:

TC948 High Voltage: See phototube instructions and set the level at about the middle of the acceptable operating range (normally about 900 V).

TC241 Linear Amplifier: Unipolar output. The gain will be adjusted during the experiment.
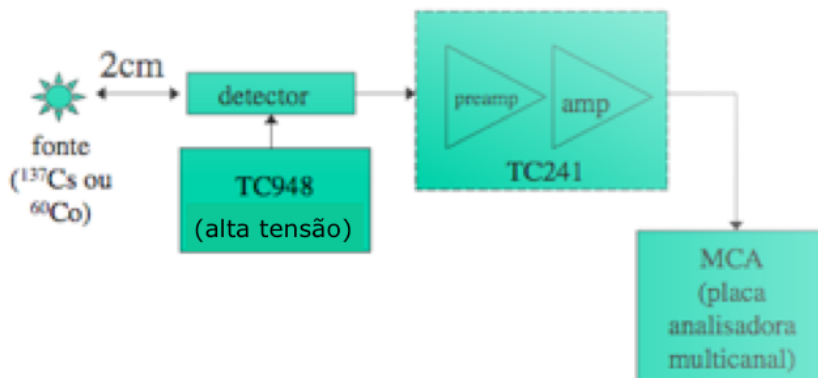Multichannel Analyzer (PC): 10-V input, 1024 channels

Fig.1. Electronic Block Diagram for Gamma-Ray Spectroscopy System with NaI(Tl) Detector.

3.3 Data Analysis - Calibration

From Table 1 make a plot of the energy of the photopeaks versus channel number. Figure 3 shows an example of the calibration plot. If other calibration sources are available, additional data points can be added to Fig. 3.
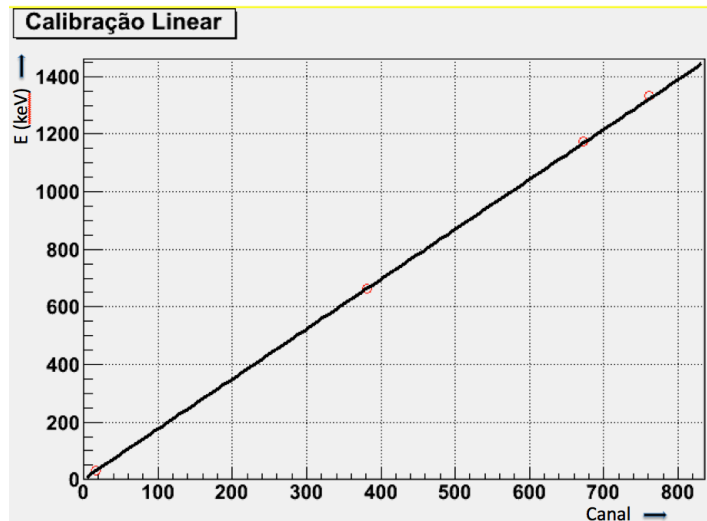

Figure 3 –Energy Calibration Curve for NaI(Tl) Detector.

(NB: If your fit programme does not take in account the errors in x-coordinate independent from y-coordinate, you need to start by performing an inverted calibration, where the values with errors are in the y-coordinate; then, from the obtained parameters, calculate the final parameters of the calibration).

4. SPECTRUM ANALYSIS OF ^{6O}Co AND ^{137}CS

4.1 Purpose

The purpose of this experiment is to explain some of the portions, other than the photopeaks, that are usually present in a pulse-height spectrum. These are the Compton edge and the backscatter peak.

The Compton interaction is a pure kinematic collision between a gamma photon and what might be termed a free electron in the NaI(Tl) crystal. By this process the incident gamma gives up only part of its energy to the electron. The amount given to the recoil electron depends on whether the collision is head-on or glancing. For a head-on collision the gamma imparts the maximum allowable energy for the Compton interaction. The energy of the scattered gamma can be determined by solving the energy and momentum equations for this billiard- ball collision. The solution for these equations in terms of the scattered gamma can be written as:

$$E'_\gamma = \frac{E_\gamma}{1 + \dfrac{E_\gamma}{m_ec^2}(1 - \cos\theta)} \tag{1}$$

where

      E_γ is the energy of the incident gamma in keV or MeV
      θ is the γ' scattering angle
      $m_e c^2$ is the electron rest mass (511 keV or 0.511 MeV)
      E'_γ is the energy the scattered gamma in the same units.

If θ =180° due to a head-on collision in which γ' is scattered directly back, Eq. (1) becomes:

$$E'_\gamma = \frac{E_\gamma}{1 + \dfrac{2}{0.511} E_\gamma}$$

As an example, $E'_\gamma = 0.2$ MeV for an incident gamma energy of 1 MeV. The energy of the recoil electron *(E$_e$)* for this collision would be 0.80 MeV, since:

$$E_e = E_\gamma - E'_\gamma \tag{2}$$

Hence the position of the Compton edge, which is the maximum energy that can be imparted to an electron by the Compton interaction, can be calculated by Eq. (2).

4.2 Data Analysis

Calculate the energy of the Compton edge for the 662 keV gammas from ^{137}Cs. Enter this value in Table 1. From your plot and calibration curve, does this calculation agree with your measured value? Backscattering occurs when gammas make Compton interactions in the material that surrounds the detector. Backscattered gammas from these interactions $(E_{\gamma'})$ make photoelectric interactions in the NaI(Tl) when they enter the crystal. The energy of the backscattered peak can be found by solving Eq. (2).

Solve Eq. (2) for ^{137}Cs and for the 1.33 MeV gammas from ^{60}Co. Fill in the rest of Table 1. How do your measured energies compare with the theoretical energies from Eq. (2)? If the backscatter peak is not very pronounced in your spectrum, it can be improved by accumulating a spectrum with a sheet of lead absorber placed slightly to the left of the source.

5. SPECTRUM ANALYSIS OF ^{208}Tl (or of other sufficiently high energy gamma source)

5.1 Annihilation Radiation

This process can produce peaks in the spectrum, depending on whether the annihilation, which results from pair production, occurs in the lead or in the NaI(Tl) detector. If the annihilation occurs in the lead and one of the 0.511 MeV gamma pairs interact in the detector, then an extra 0.511 MeV peak will appear in the spectrum that is being measured. It should be remembered that this process can only occur for radioactive sources that have gammas in their decay scheme greater than 1.022 MeV.

In the second case, where the incident photon annihilates in the detector, there are, in general, three peaks that can be produced. If the initial gamma has an energy Eγ, the first peak seen in the spectrum corresponds to Eγ. In this case, Eγ annihilates in the detector and both annihilation quanta interact by the photoelectric process before escaping from the detector. We have thus totally absorbed the energy of the incident gamma. A second peak will be seen at E=0.511 MeV. This peak is produced when one of the annihilation quanta is absorbed and the other escapes. In the spectra, this is called the first escape peak. The third peak of energy E= Eγ-1.022 MeV is observed when both annihilation quanta escape

from the detector before being absorbed. This peak is called the second escape peak. The probability of seeing the total absorption peak and the two escape peaks depends on the incident gamma energy and the size of the detector. Figure 5 shows a NaI(Tl) spectrum of ^{228}Th and its daughters. In this case Eγ is 2.615 MeV from ^{208}Tl. The single escape peak is 2.104 MeV and double escape occurs at 1.593 MeV.
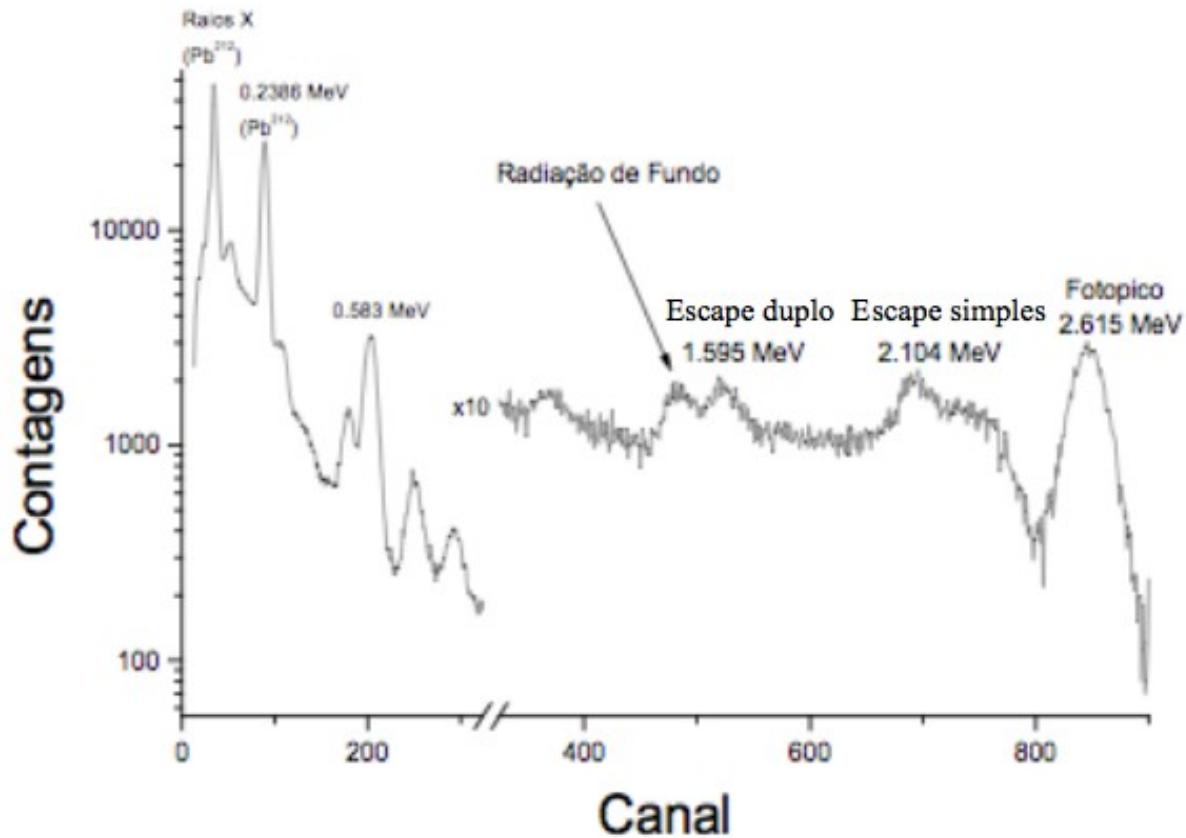

Figure 4. Gamma Ray Pulse Height Spectrum of a ^{228}Th Source. This spectrum shows the single and double escape peaks from the 2.615 MeV gammas.

6. ENERGY RESOLUTION

The resolution of a spectrometer is a measure of its ability to resolve two peaks that are fairly close together in energy. Figure 2 shows the gamma spectra relative to the ^{137}Cs and the ^{60}Co sources. The resolution of each photopeak is defined as:

$$R = \Delta E / E$$

(3)

where

        R = the resolution, usually given in percent
        ΔE = the full width of the peak at half of the maximum
        E = the centroid of the photopeak.

7. ABSORPTION OF γ*s* IN MATTER

7.1 Mass Absorption Coefficient

7.1.1 Purpose

The purpose of the experiment is to measure experimentally the mass absorption coefficient in lead for 662 keV gamma rays.

Gammas interact in matter primarily by photoelectric, Compton, or pair production interactions The total-mass absorption coefficient can be measured easily with a gamma-ray spectrometer. In this experiment we will measure the number of gammas that are removed from the photopeak by photoelectric or Compton interactions that occur in a lead absorber placed between the source and the phototube.

From Lambert's law the decrease of intensity of radiation as it passes through an absorber is given by:

$$I = I_0 \, e^{-\mu x} \qquad (4)$$

where
   I = intensity after the absorber
   I_0 = intensity before the absorber
   μ = total- mass absorption coefficient in cm^2/g
   x = density thickness in g/cm^2

The density thickness is the product of the density in g/cm3 times the thickness in cm.
The half-value layer (HVL) is defined as the density thickness of the absorbing material that will reduce the original intensity by one-half. From Eq. (4):

$$\ln I / I_0 = -\mu x \qquad (5)$$

If $I/I_0 = 0.5$ and $x =$ HVL, ln $\ln I / I_0 = -\mu x$ 0.5=-μ(HVL) and hence
$$\text{HVL} = 0.693/\mu \qquad (6)$$

In this experiment we will measure μ in lead for the 0.662MeV gammas from [137]Cs. The accepted value is 0.105 cm2/g.

7.1.2 Experimental Procedure

1. Place the ^{137}Cs source about 10 cm from the NaI(Tl) detector and accumulate the spectrum long enough for the sum under the 0.662-MeV peak (Σ_{Cs}-Σ_b) to be at least 6000 counts. Record the live time, read out the multichannel analyzer, and determine (Σ_{Cs}-Σ_b).
2. Erase the multichannel analyze and insert the first piece of lead between the source and the detector. Accumulate the spectrum for the same period of live time as in step 1 above. Read out the multichannel analyzer and determine (Σ_{Cs}-Σ_b).
3. Repeat with additional thicknesses of lead until the count-sum is less than 1000. Fill a table with the relevant data:

Table 2 Data for Mass Absorption Coefficient

Absorber	Absorber Thickness (mg/cm^2)	. . .
1	0	
2		
3		
4		
5		
6		

7.1.3 Data Analysis

Use the data from Table 2 to perform a fit in order to obtain μ. How does your value compare with the accepted value of 0.105 cm^2/g ?

(Optional) Repeat the above experiment for aluminum absorbers. The μ for aluminum is 0.074 cm^2/g.