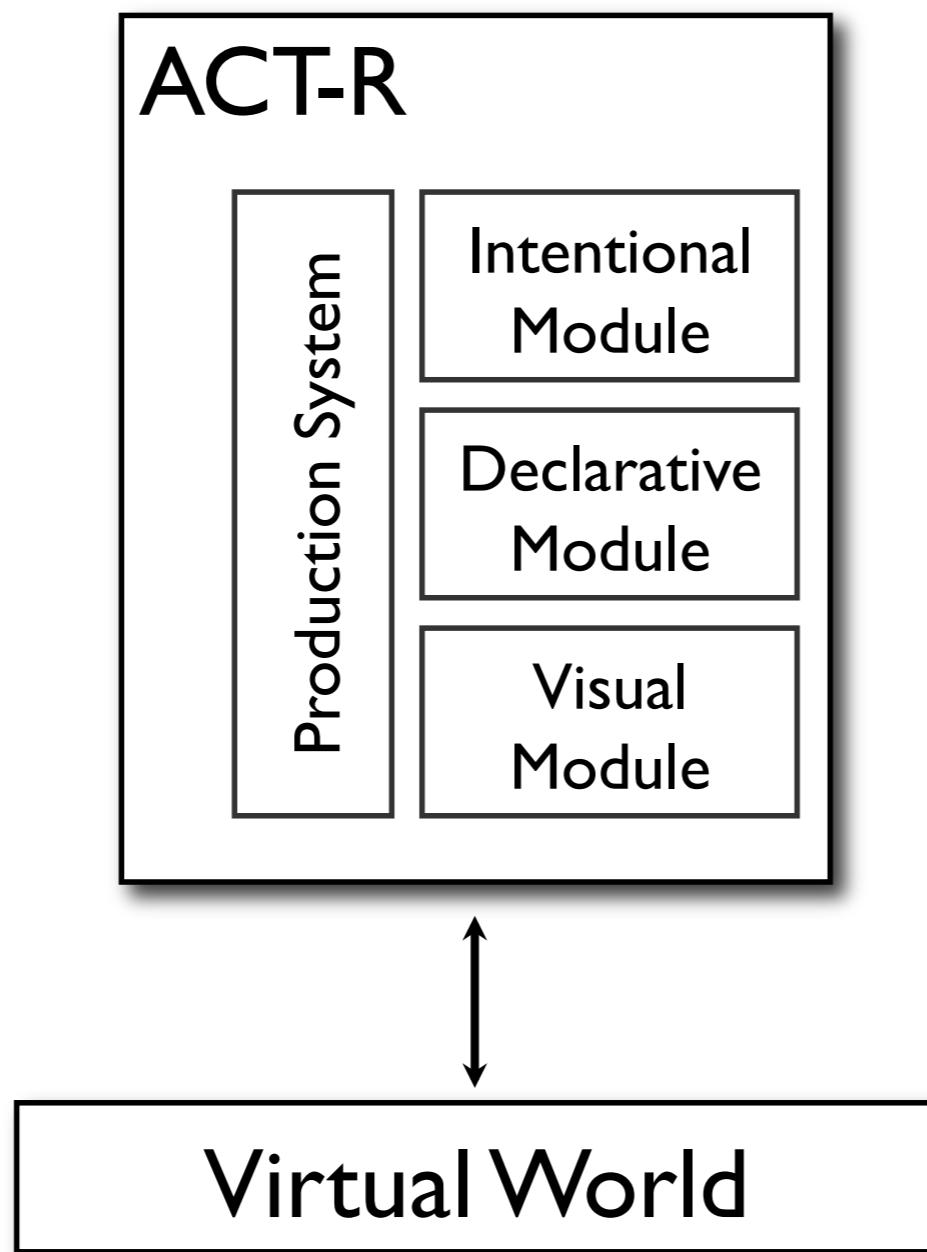
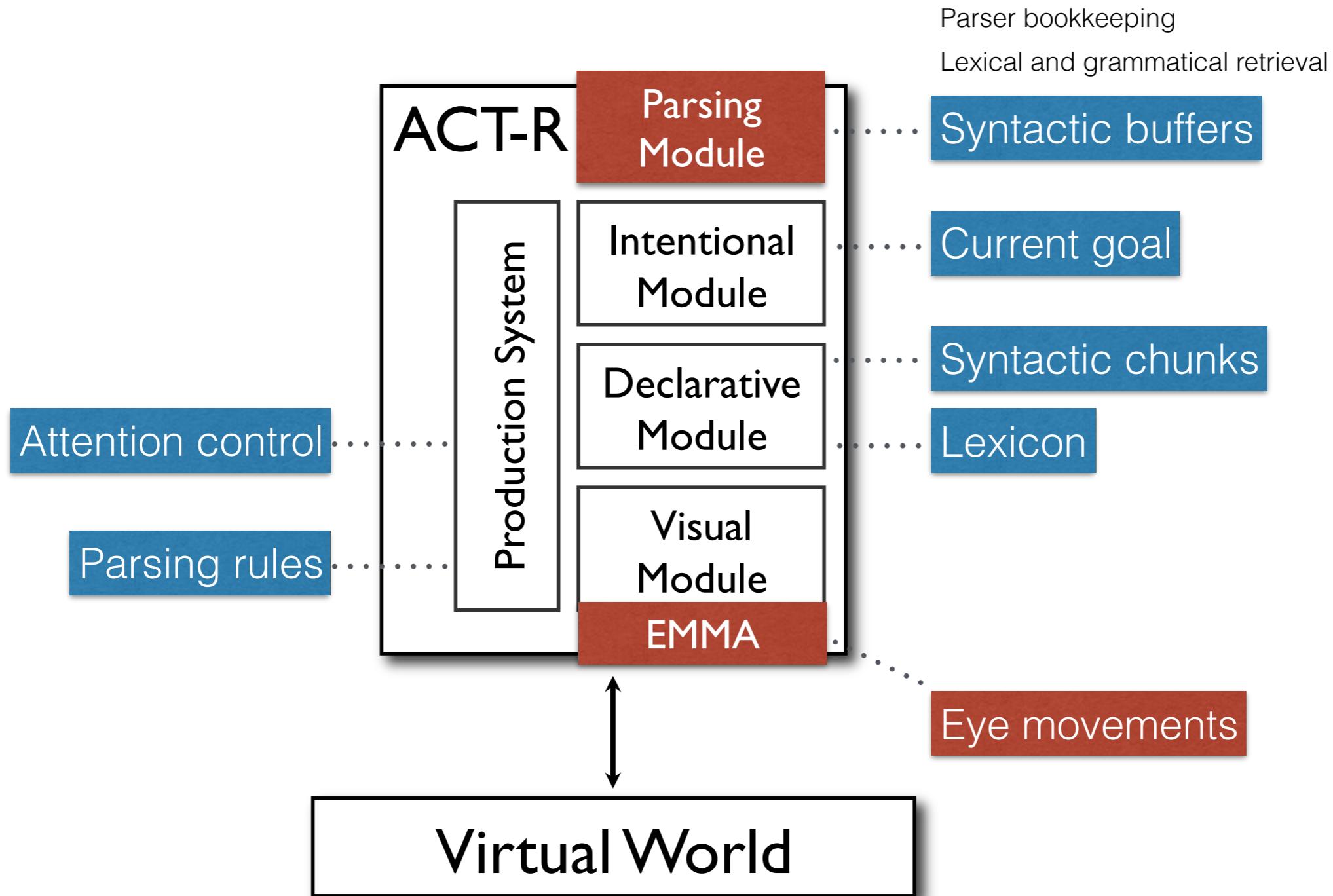


An Integrated Model of Eye Movements in Sentence Comprehension

Model Structure

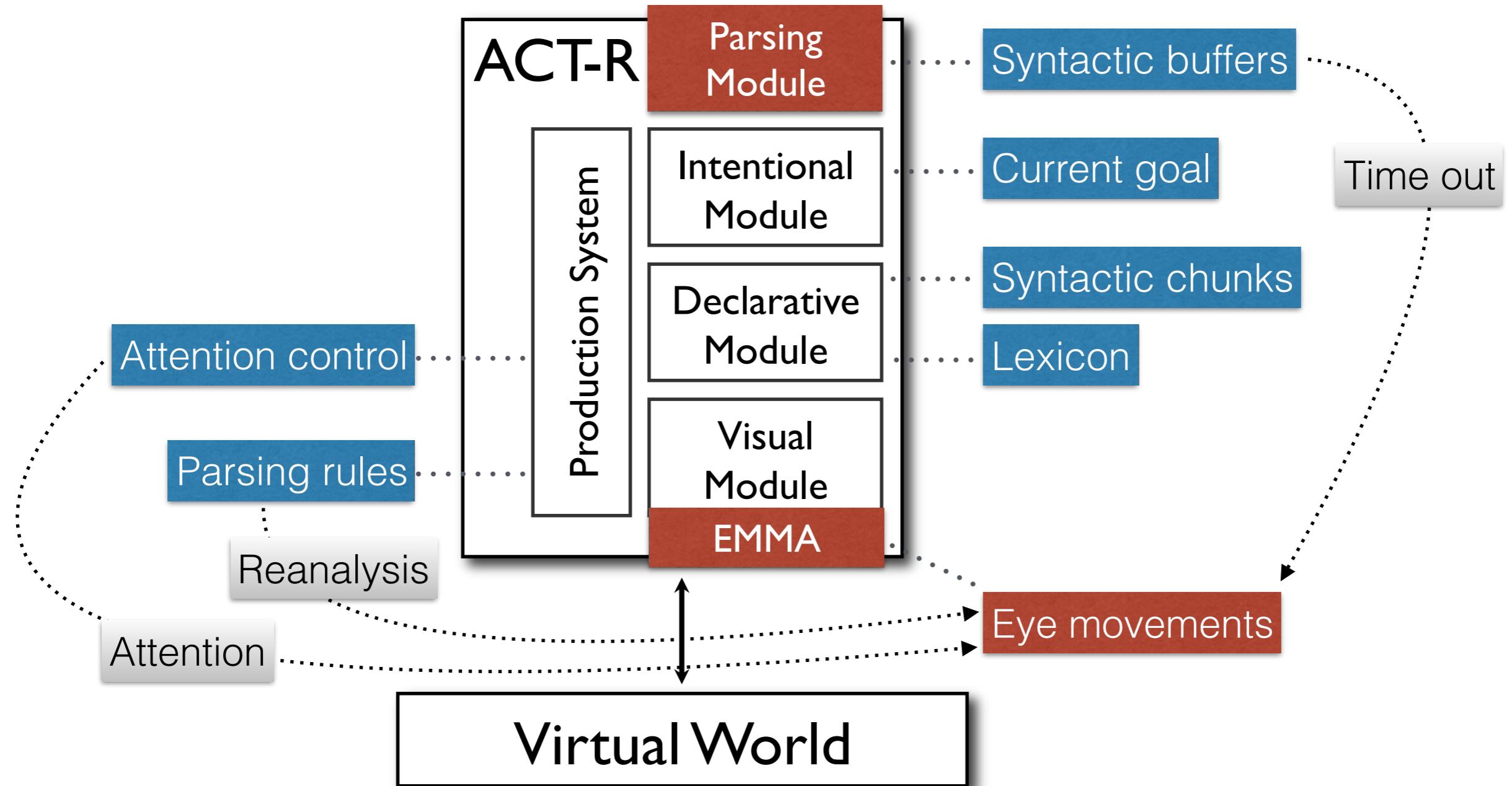


Model Structure



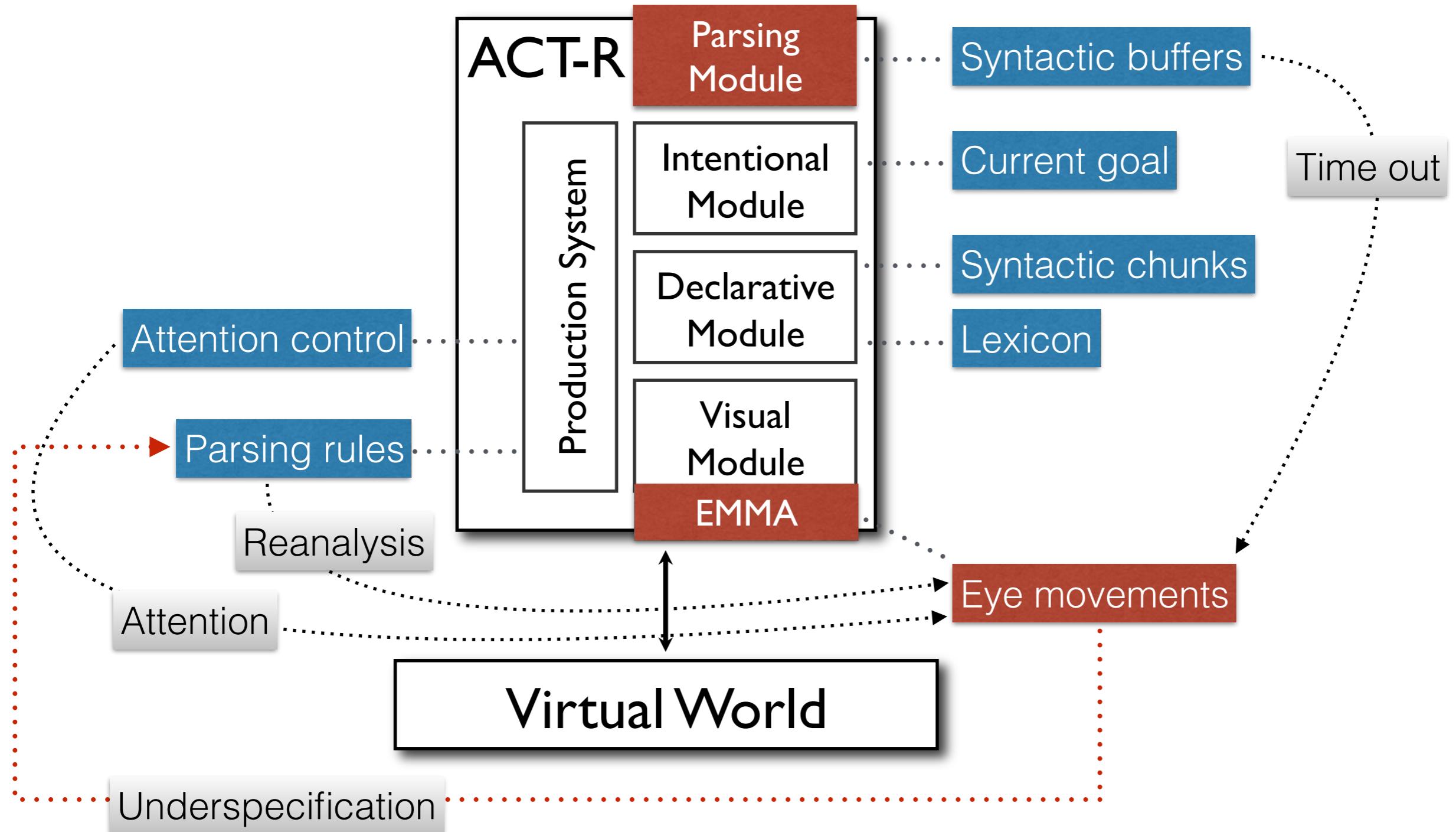
Model Structure

Eye Movement Interaction



Model Structure

Eye Movement Interaction



Contents

1. Lewis & Vasishth (2005) parser
2. Eye movement module EMMA
3. Time Out interaction
 - 3.1. Example simulation Grodner & Gibson (2005)
4. Reanalysis regressions
 - 4.1. Example simulation Staub (2010)
5. Individual differences
 - 5.1. Strategic underspecification and working memory
6. The parsing module
7. A possible extension: The articulatory loop

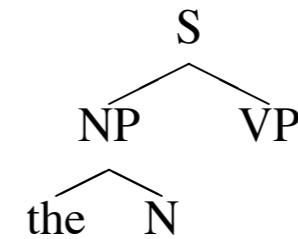
Left-Corner Parsing

$$\begin{array}{lll}
 S \rightarrow NP\ VP & Det \rightarrow a, the & NP \rightarrow Det\ N \\
 N \rightarrow man, dog & V \rightarrow ran, saw & VP \rightarrow V \\
 & & VP \rightarrow V\ NP
 \end{array}$$

INPUT: *the*

GOAL CATEGORY STACK: [S]

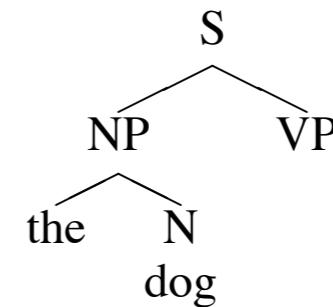
ACTIONS: If *the* is the left corner of any phrase structure rule then replace the stack content with the LHS of that rule. Repeat this left-corner rule until no further steps are possible. Wait for next input word. These actions yield the structure to the right:



INPUT: *dog*

GOAL CATEGORY STACK: [N NP VP S]

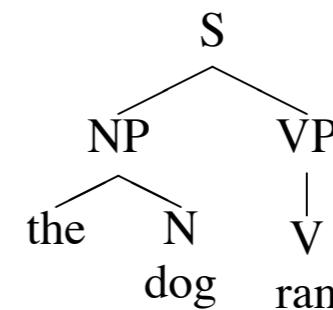
ACTIONS: Use the left-corner rule to expand *dog* to N. Since N is predicted in the incremental structure built so far (Step 1), integrate the N built up bottom-up into the tree. Since no further applications of the left-corner rule are possible, wait for the next input.



INPUT: *ran*

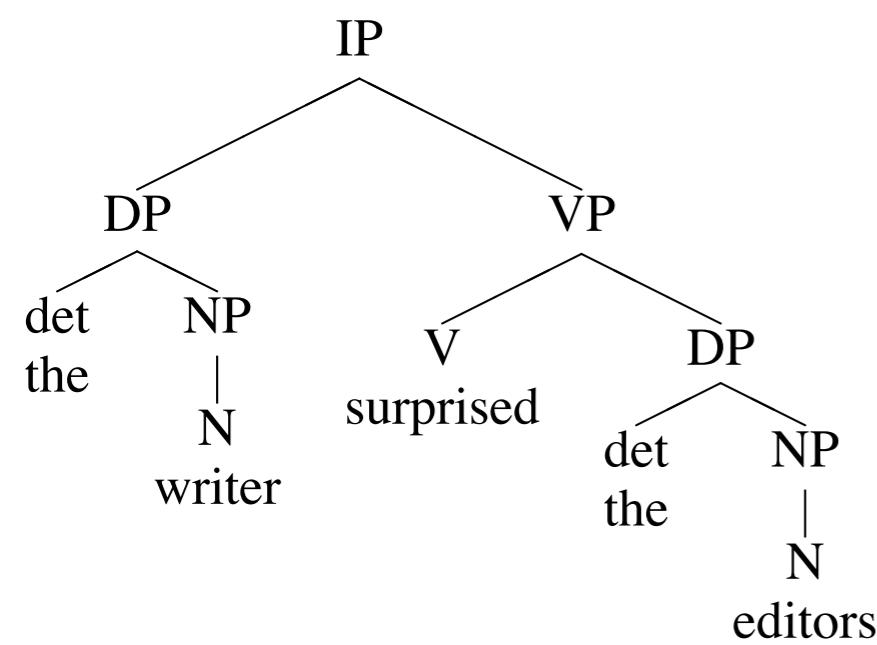
GOAL CATEGORY STACK: [VP S]

ACTIONS: Use the left-corner rule to expand *ran* to V, and apply this rule once again to expand to VP. Since a VP is predicted in the structure, integrate this with the tree.



Lewis & Vasishth (2005) Parser

The writer surprised the editors.



IP3

cat : IP
 num : sing
 spec : DP3
 comp : VP7
 tense : past
 finite : finite

DP3

cat : DP
 num : sing
 head : *the*
 comp : NP6

NP6

cat : NP
 case : nom
 num : sing
 head : *writer*

VP7

cat : VP
 num : sing-plural
 tense : past
 head : *surprised*
 comp : DP9

DP9

cat : DP
 num : plural
 head : *the*
 comp : NP14

NP14

cat : NP
 case : acc
 num : plural
 head : *editors*

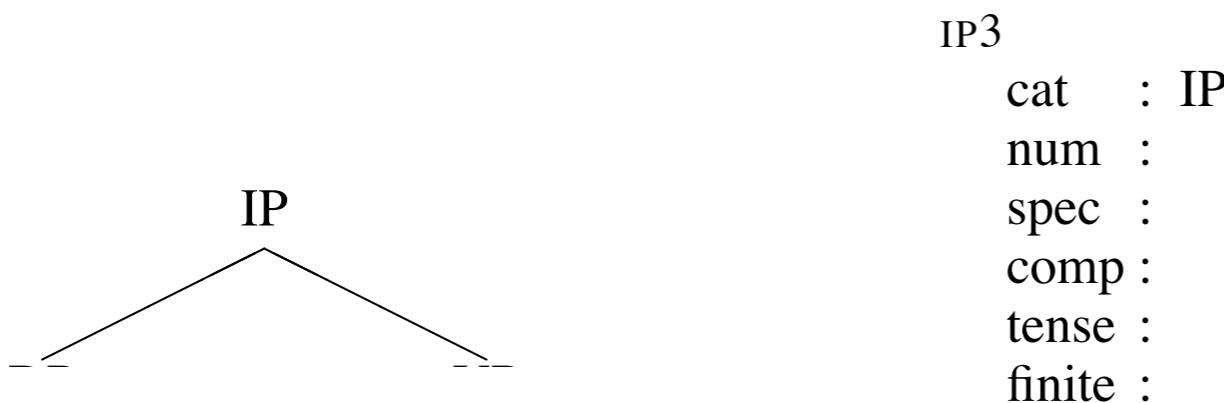
Lewis & Vasishth (2005) Parser

Goal stack

IP

DONE

The writer surprised the editors.



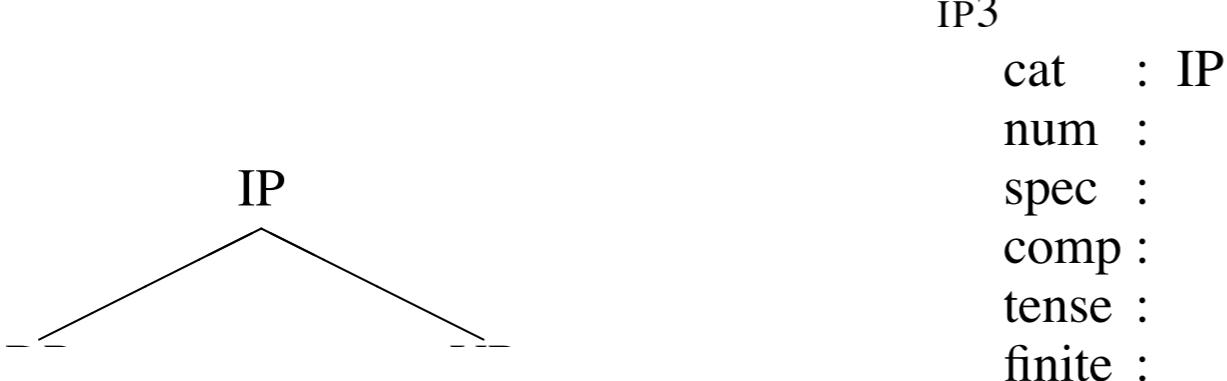
Lewis & Vasishth (2005) Parser

The writer surprised the editors.

Goal stack

IP
DONE

(P set-retrieval-cues-IP-goal-input-DET ...)



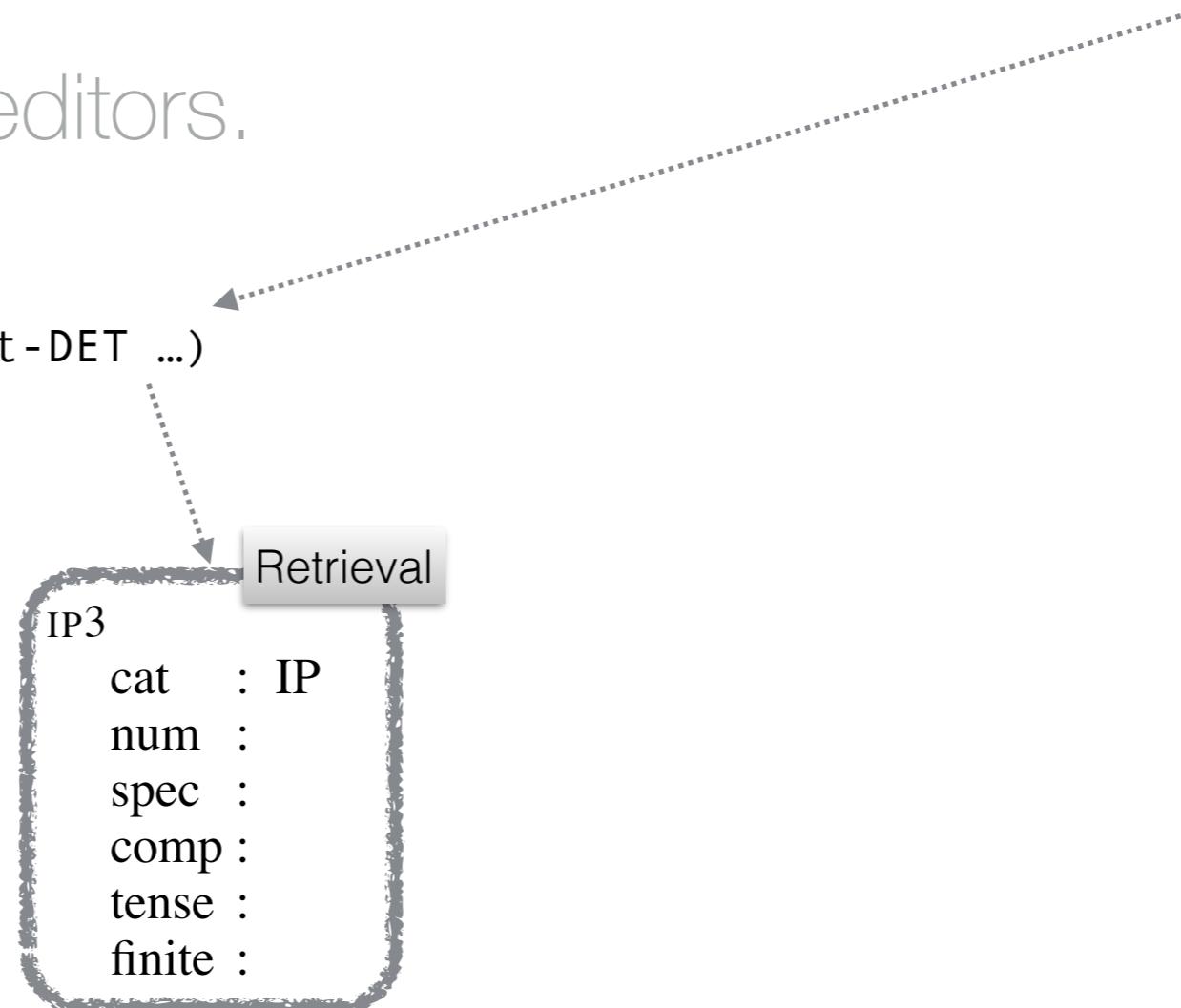
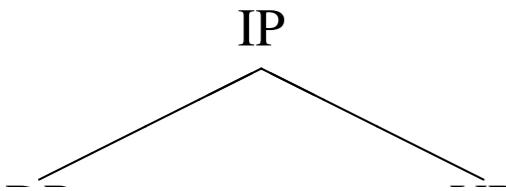
Lewis & Vasishth (2005) Parser

The writer surprised the editors.

Goal stack

IP
DONE

(P set-retrieval-cues-IP-goal-input-DET ...)



Lewis & Vasishth (2005) Parser

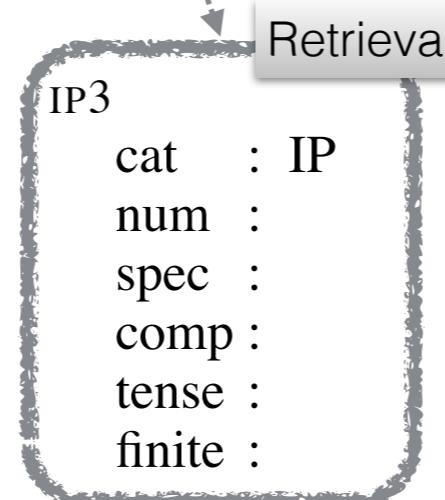
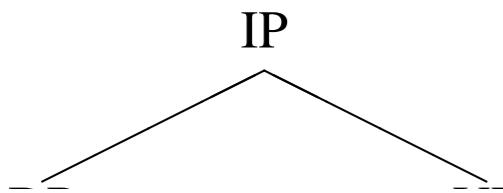
The writer surprised the editors.

Goal stack

IP
DONE

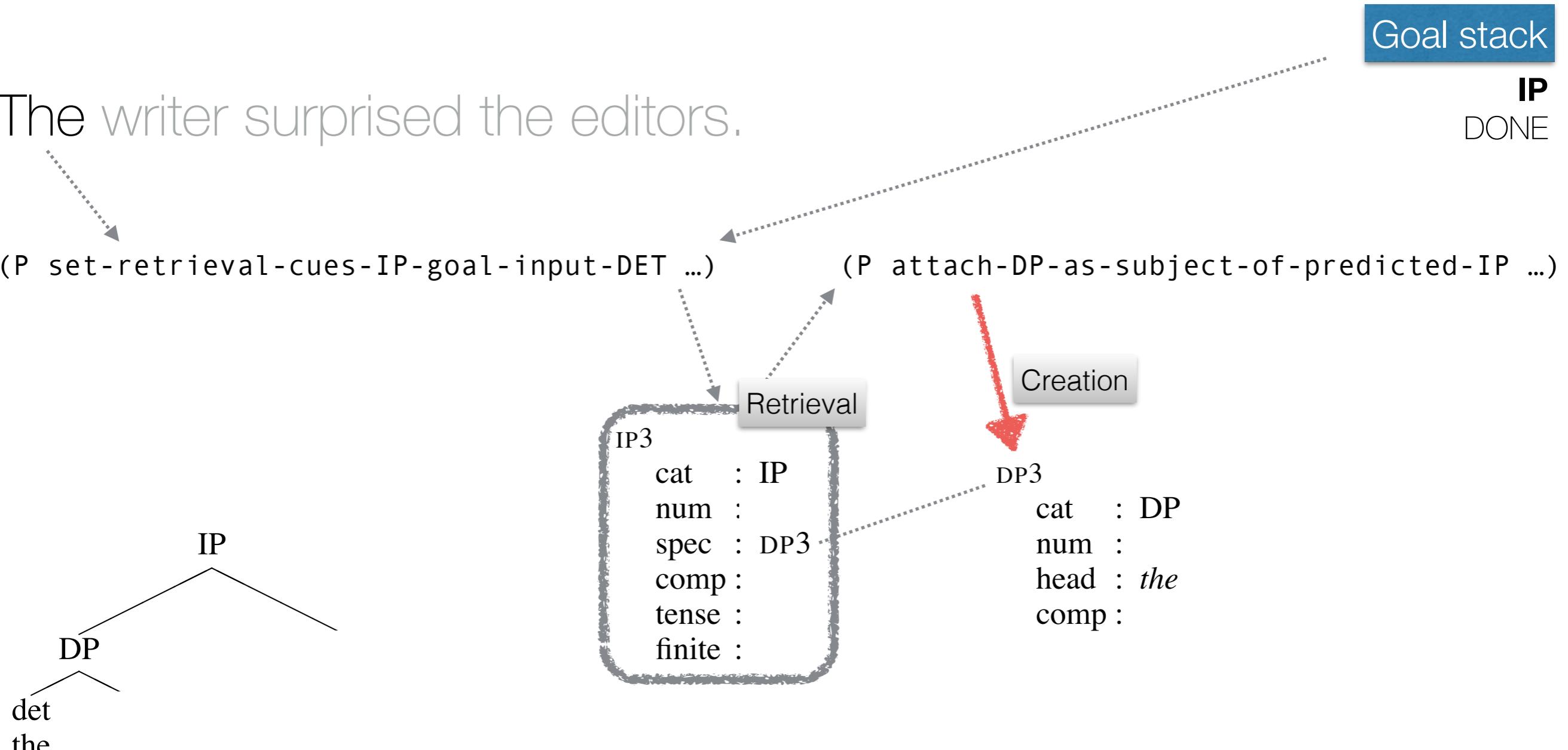
(P set-retrieval-cues-IP-goal-input-DET ...)

(P attach-DP-as-subject-of-predicted-IP ...)



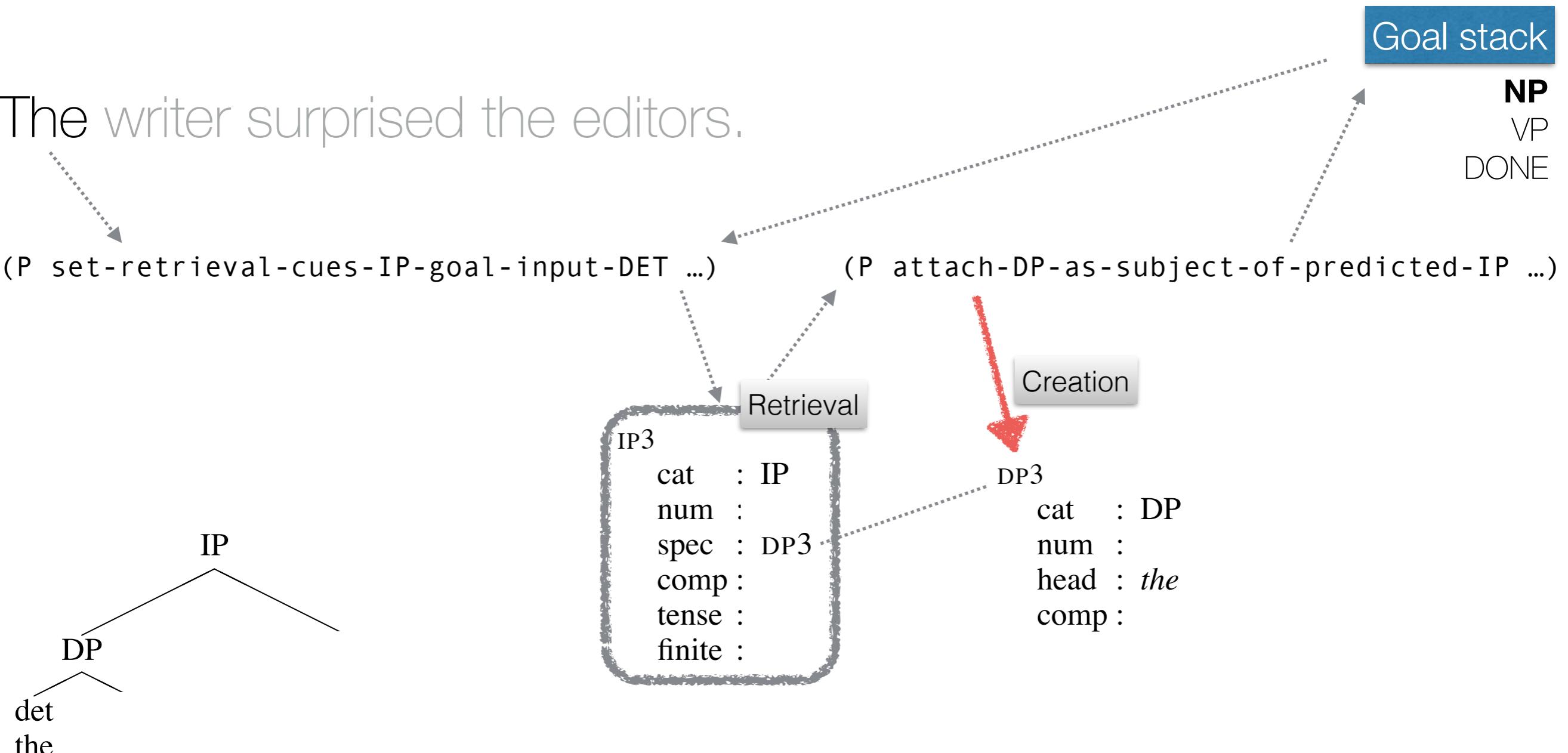
Lewis & Vasishth (2005) Parser

The writer surprised the editors.



Lewis & Vasishth (2005) Parser

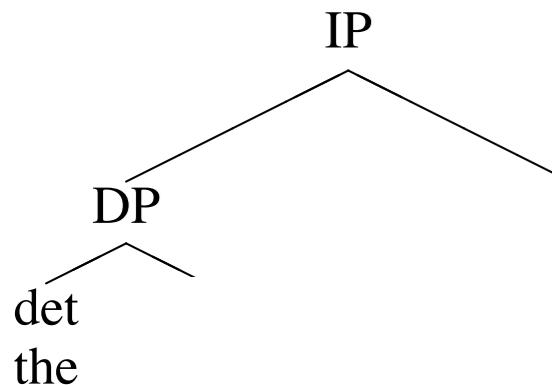
The writer surprised the editors.



```

(P set-retrieval-cues-IP-goal-input-DET
=goal>
  ISA
  state
  goal-cat
  =retrieval>
    isa
    word
    cat
==>
=lex> =retrieval
=goal>
  state
  cue1
+retrieval>
  ISA
  waiting-for-cat
  syn-obj
  wait-for-IP
)

```



```

(P attach-DP-as-subject-of-predicted-IP
=goal>
  ISA
  state
  =retrieval>
    isa
    cat
    ID
    head
    waiting-for-cat
    =lex>
      isa
      cat
      word
      number
==>
=goal>
  state
  goal-cat
  =DPb>
    isa
    cat
    ID
    head
    spec-of
    number
    waiting-for-cat
    next-goal
    =retrieval>
      spec
      waiting-for-cat
      )
      "read"
      NP-goal
      syn-obj
      DP
      =ID-DP
      =word
      =ID-RETR
      sing-plural
      wait-for-NP
      next-VP-goal
      =ID-DP
      wait-for-VP
)

```

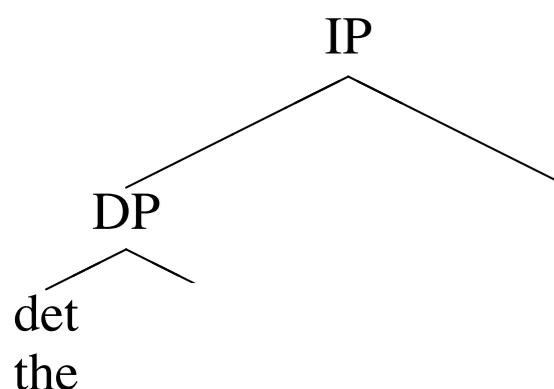
```

(P set-retrieval-cues-IP-goal-input-DET
=goal>
  ISA
  state
  goal-cat
  =retrieval>
    isa
    word
    cat
  ==>
  =lex> =retrieval
  =goal>
    state
    cue1
  +retrieval>
    ISA
    waiting-for-cat
  )

```

comprehend-sentence
"read"
IP-goal |.....
lexical-entry
=word
DET

syn-obj
wait-for-IP



Goal stack

```

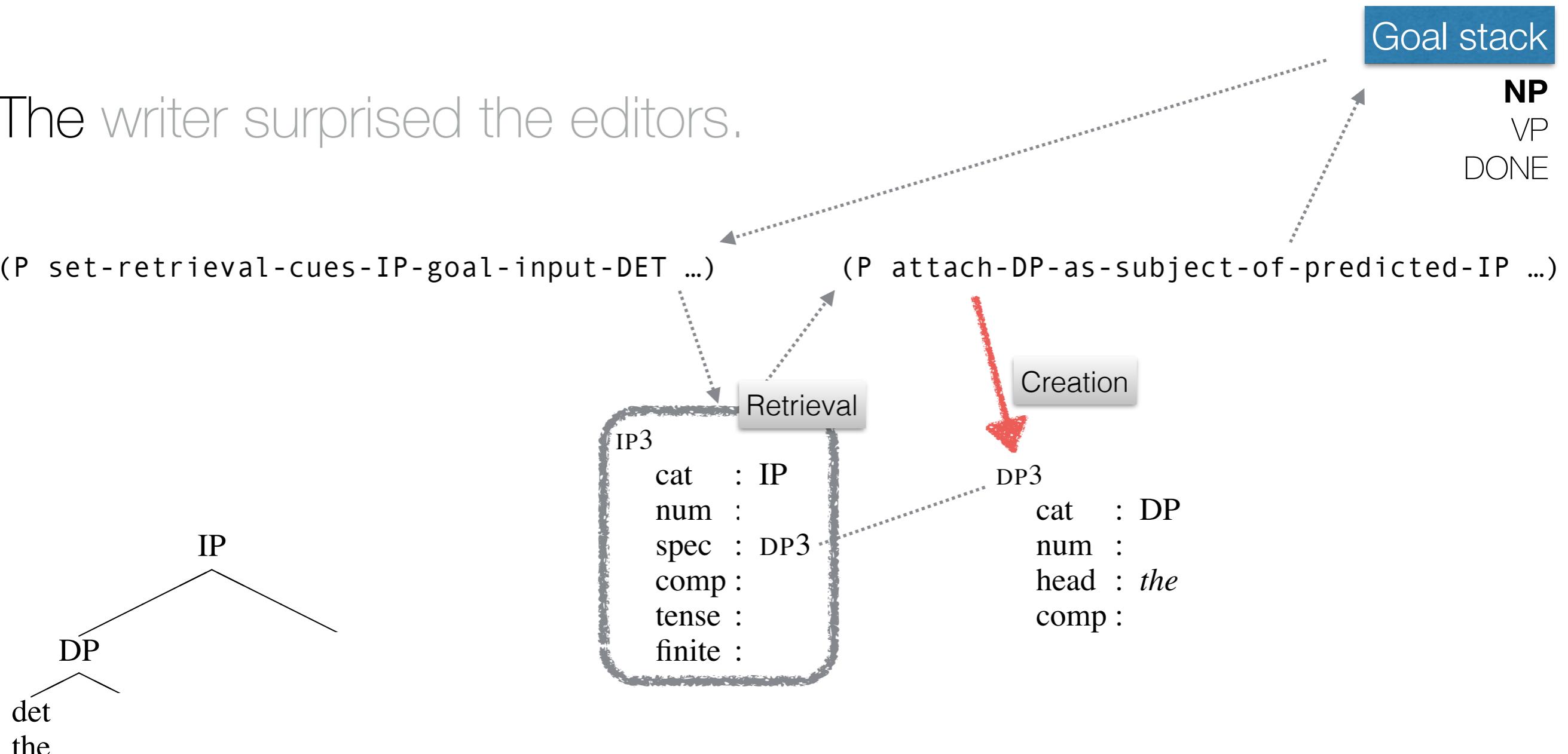
(P attach-DP-as-subject-of-predicted-IP
=goal>
  ISA
  state
  =retrieval>
    isa
    cat
    ID
    head
    waiting-for-cat
    =lex>
      isa
      cat
      word
      number
    ==>
    =goal>
      state
      "read"
      NP-goal
    +DPb>
      isa
      cat
      ID
      head
      spec-of
      number
      waiting-for-cat
      next-goal
      =retrieval>
        spec
        waiting-for-cat
      )

```

comprehend-sentence
"wm-retrieval"
syn-obj
IP
=ID-RETR
nil
wait-for-IP
lexical-entry
DET
=word
sing-plural-lex
"read"
NP-goal
syn-obj
DP
=ID-DP
=word
=ID-RETR
sing-plural
wait-for-NP
next-VP-goal
=ID-DP
wait-for-VP

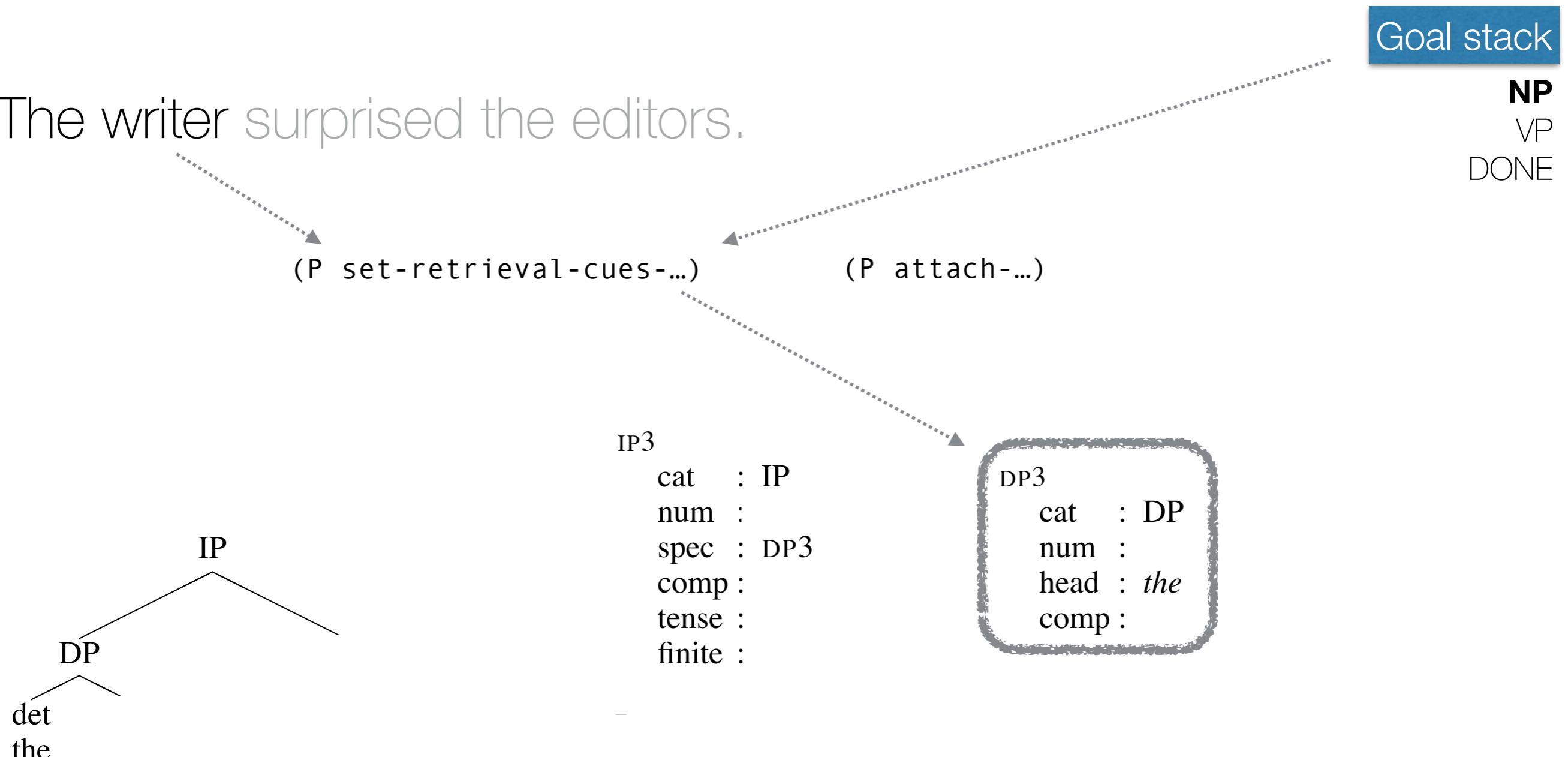
Lewis & Vasishth (2005) Parser

The writer surprised the editors.



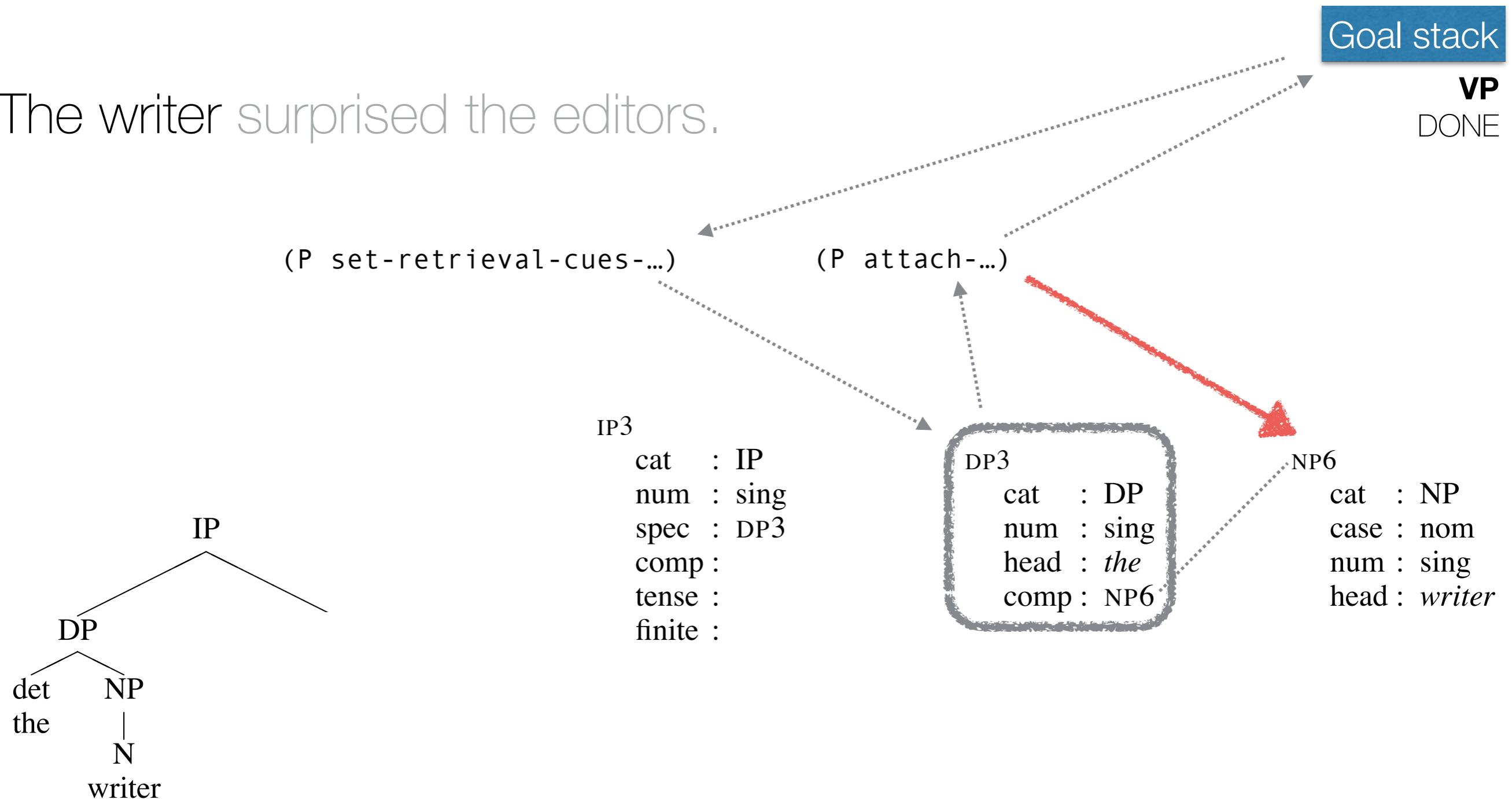
Lewis & Vasishth (2005) Parser

The writer surprised the editors.

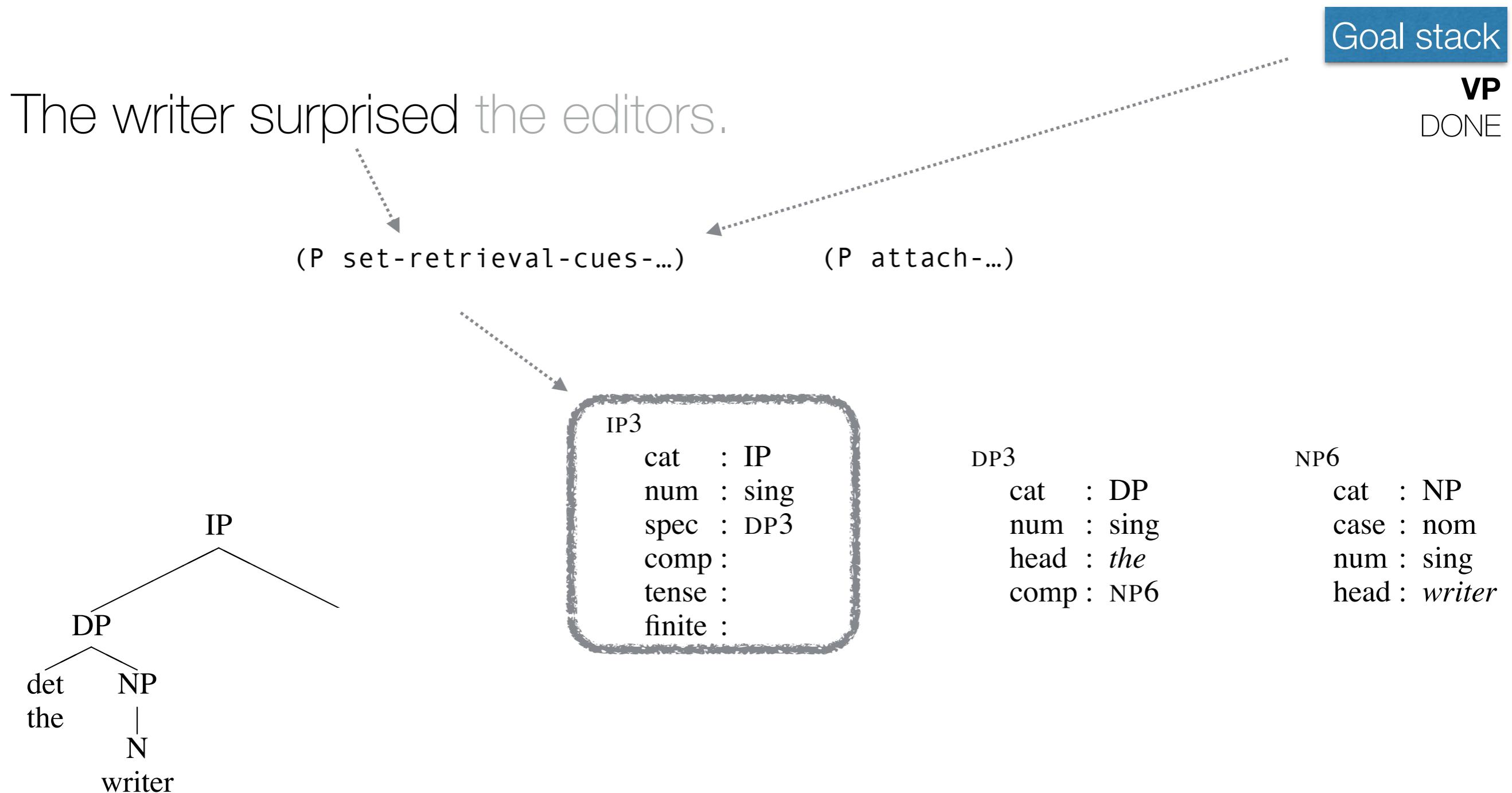


Lewis & Vasishth (2005) Parser

The writer surprised the editors.

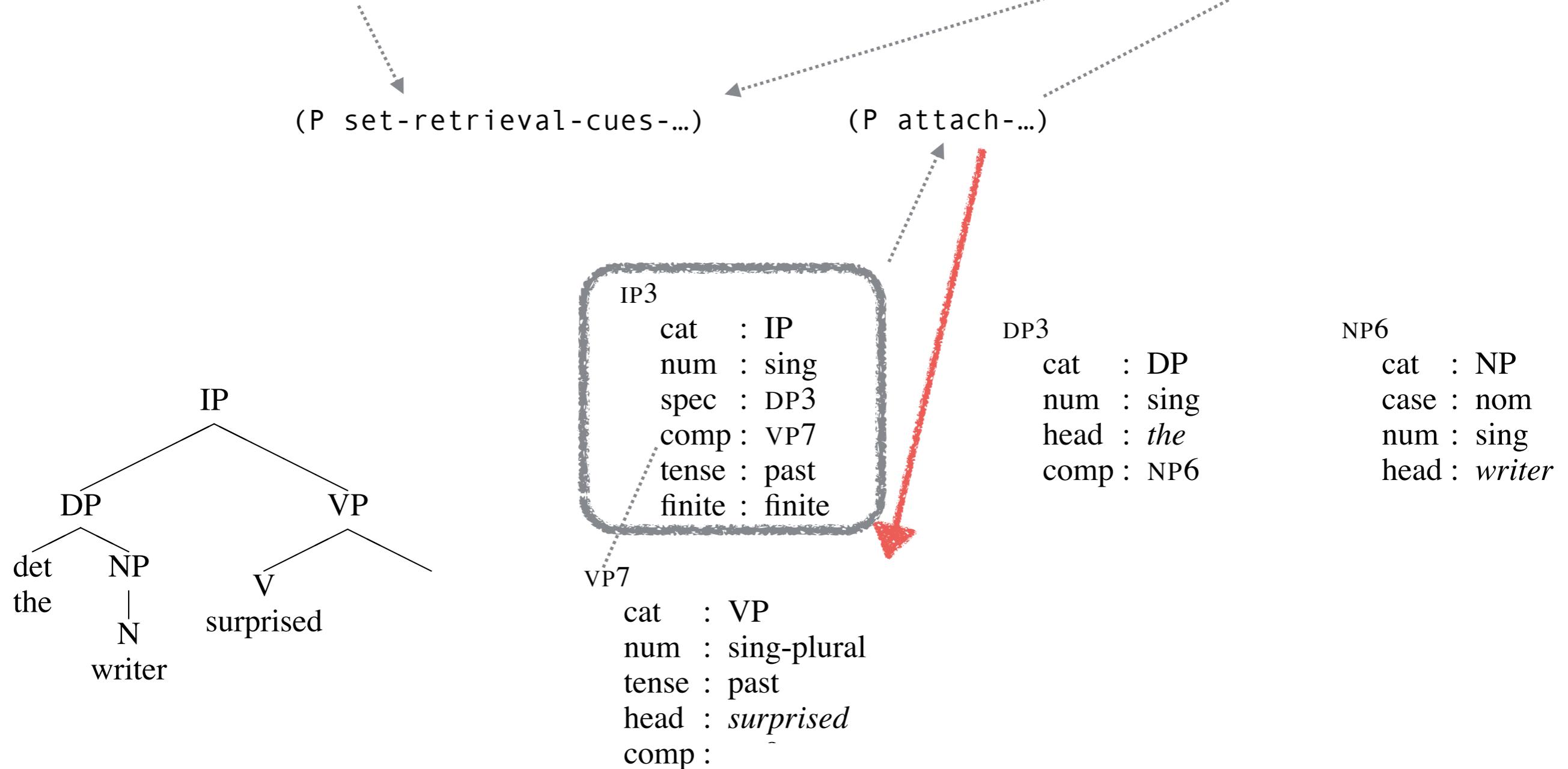


Lewis & Vasishth (2005) Parser



Lewis & Vasishth (2005) Parser

The writer surprised the editors.

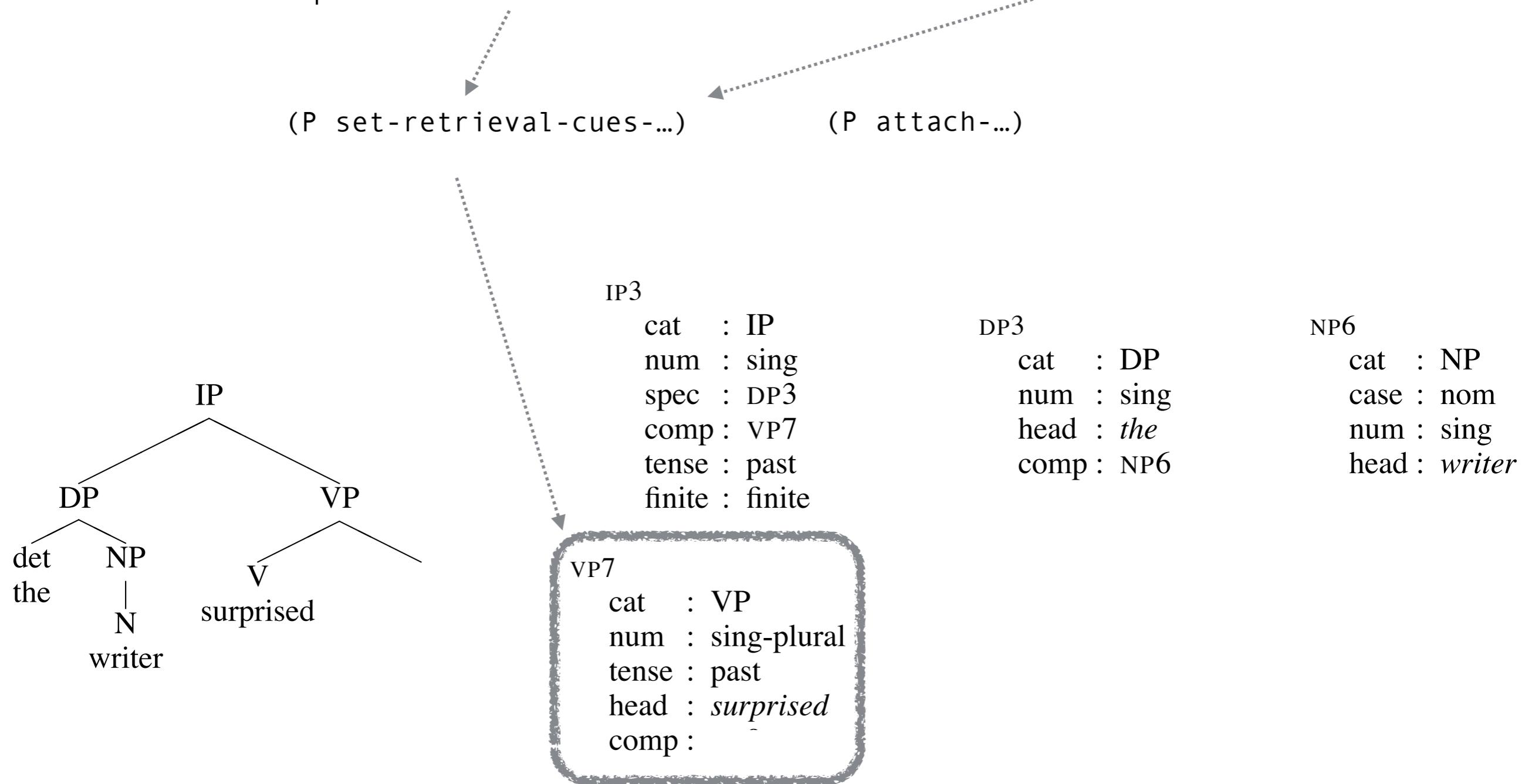


Lewis & Vasishth (2005) Parser

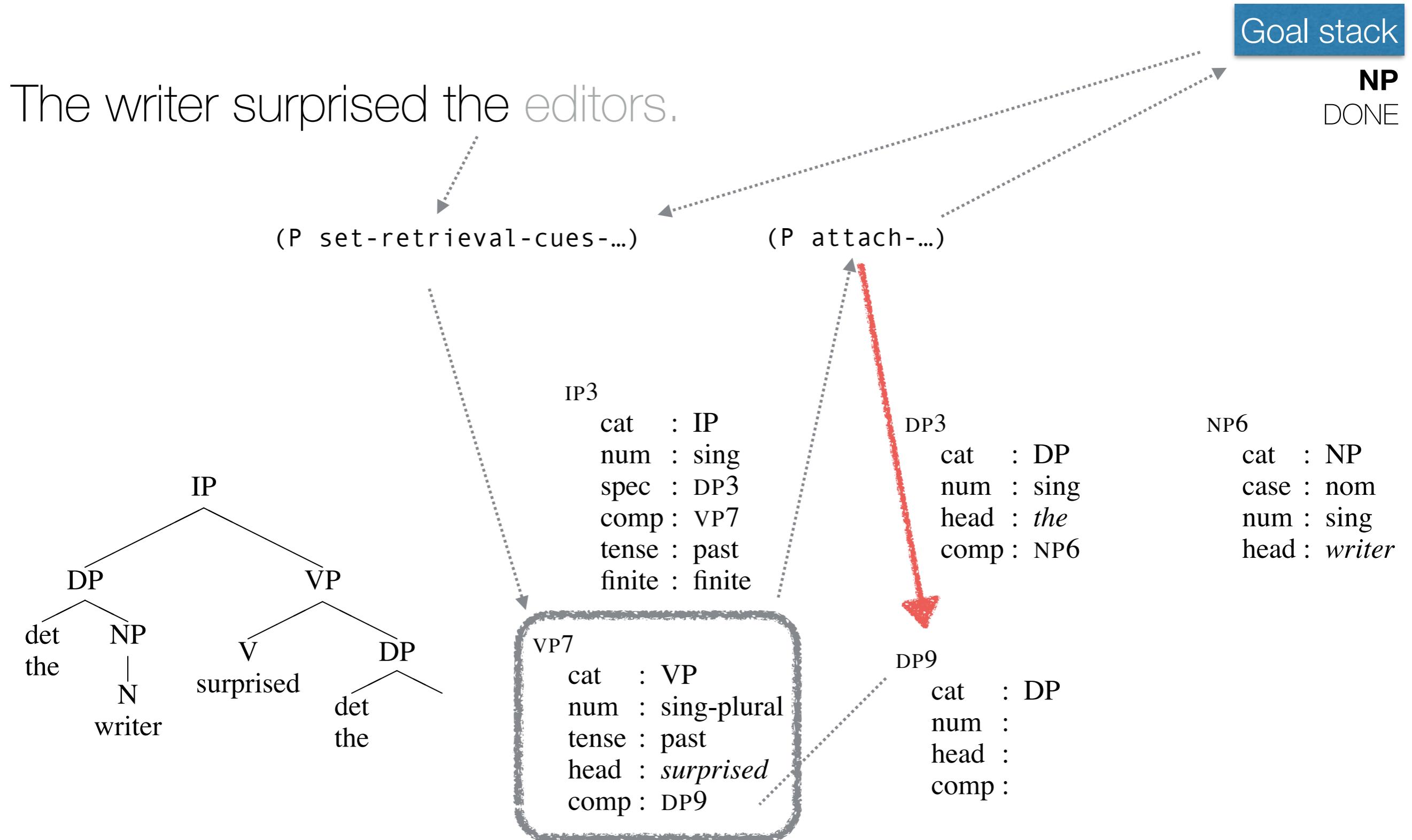
Goal stack

DP
DONE

The writer surprised the editors.



Lewis & Vasishth (2005) Parser

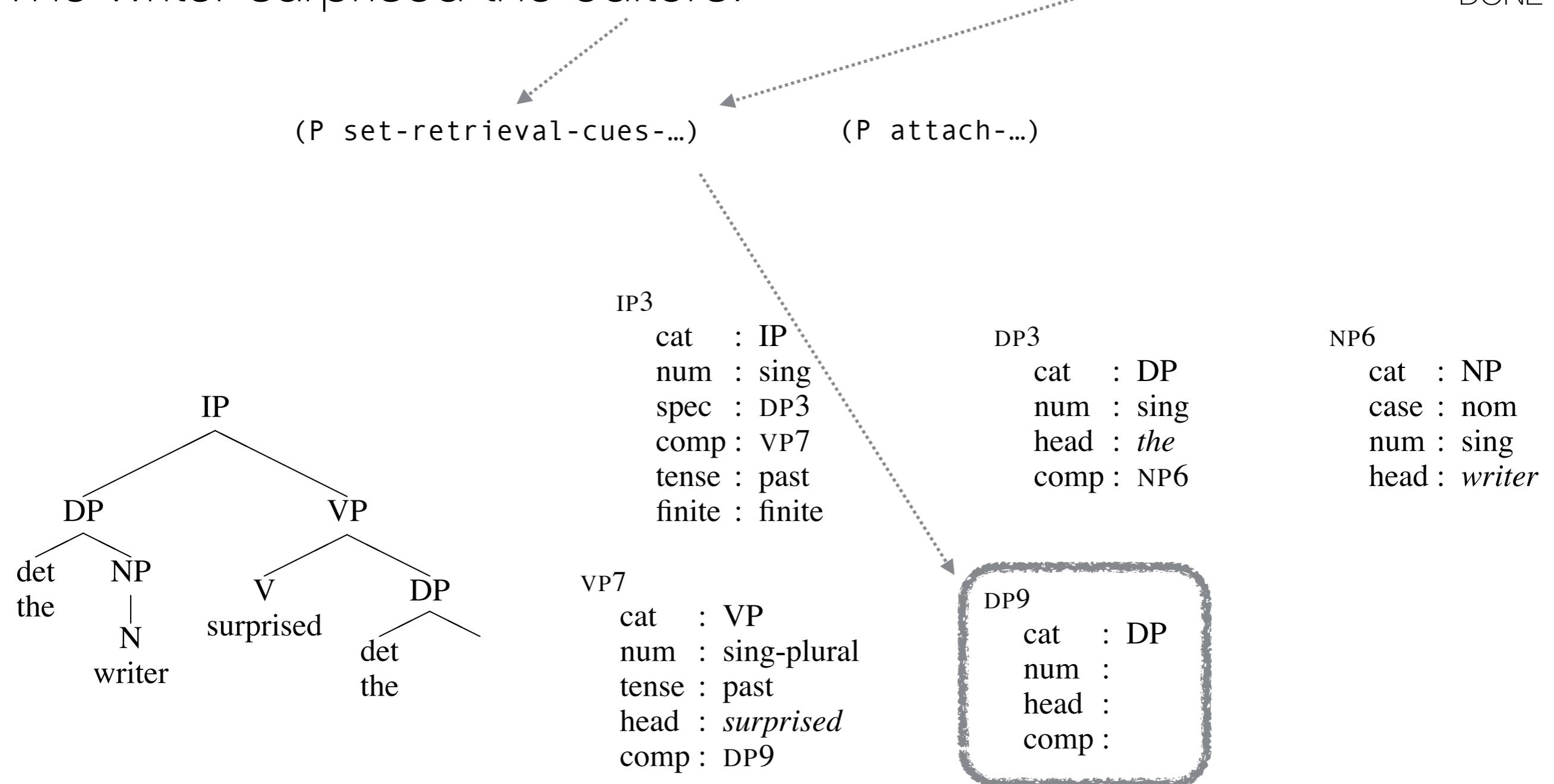


Lewis & Vasishth (2005) Parser

Goal stack

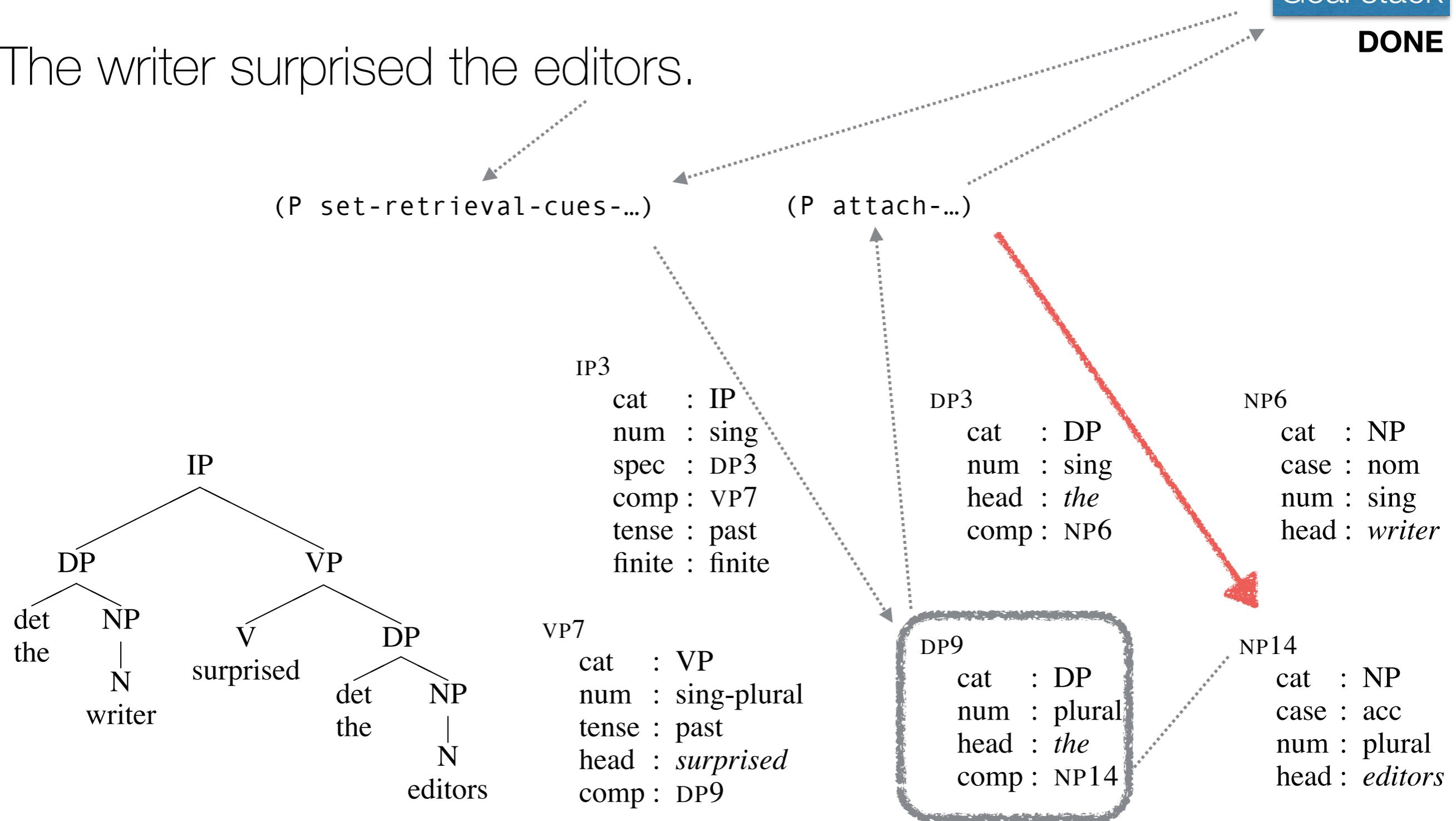
NP
DONE

The writer surprised the editors.



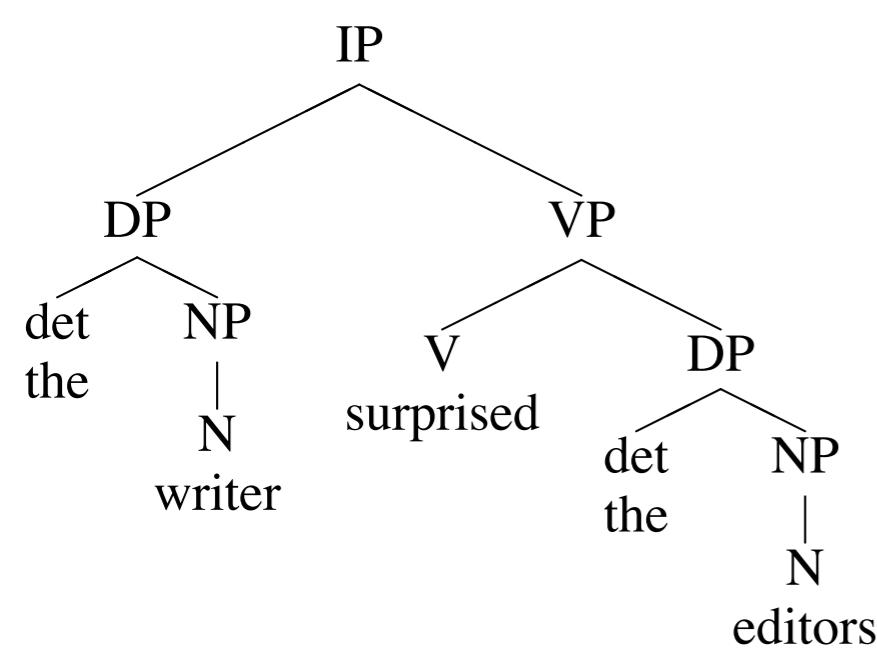
Lewis & Vasishth (2005) Parser

The writer surprised the editors.



Lewis & Vasishth (2005) Parser

The writer surprised the editors.



IP3	
cat	: IP
num	: sing
spec	: DP3
comp	: VP7
tense	: past
finite	: finite

DP3	
cat	: DP
num	: sing
head	: <i>the</i>
comp	: NP6

NP6	
cat	: NP
case	: nom
num	: sing
head	: <i>writer</i>

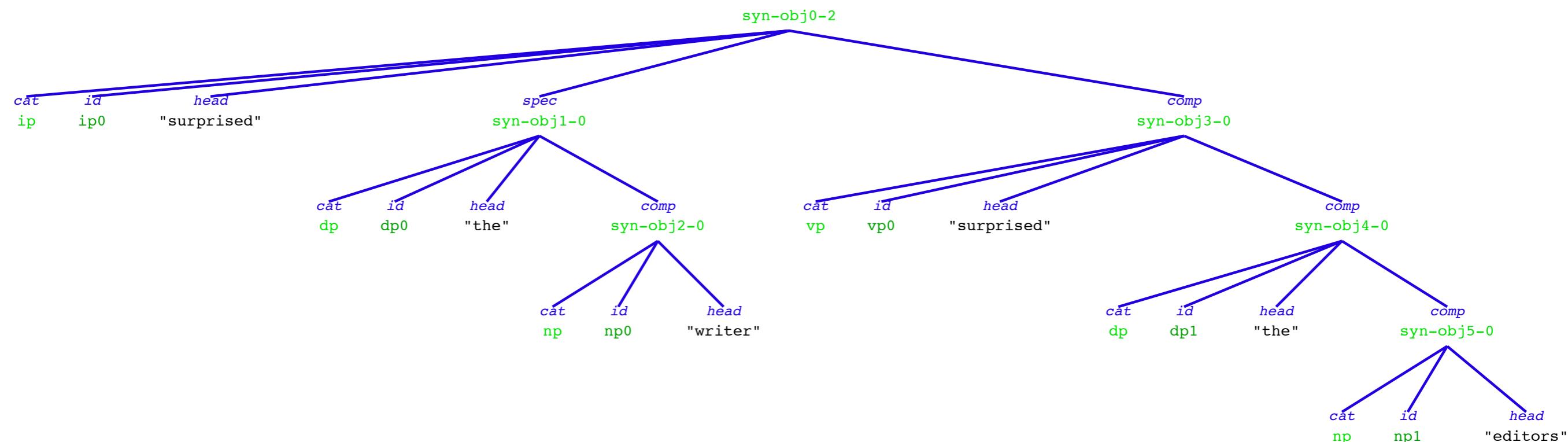
VP7	
cat	: VP
num	: sing-plural
tense	: past
head	: <i>surprised</i>
comp	: DP9

DP9	
cat	: DP
num	: plural
head	: <i>the</i>
comp	: NP14

NP14	
cat	: NP
case	: acc
num	: plural
head	: <i>editors</i>

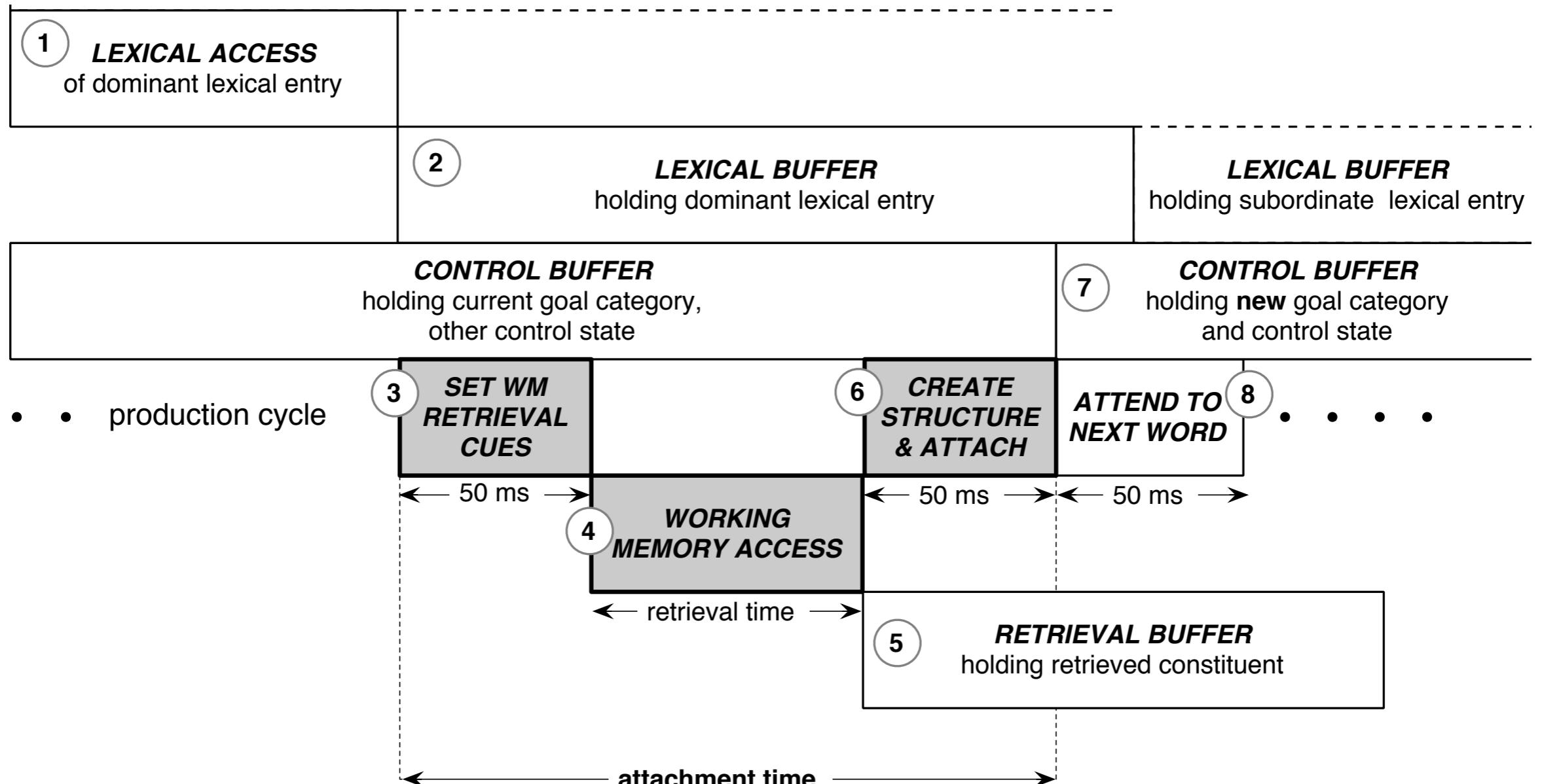
Lewis & Vasishth (2005) Parser

The writer surprised the editors.

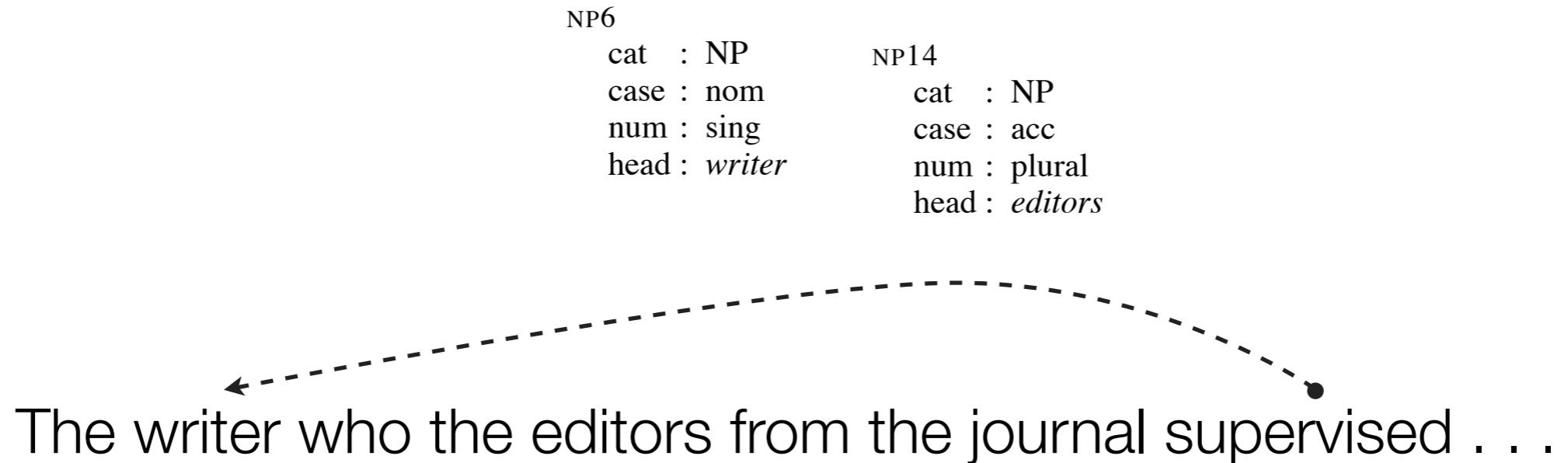


```
(ps "the writer surprised the editors *")  
or just:  
(demo) for „the dog bit the boy“
```

Lewis & Vasishth (2005) Parser



Lewis & Vasishth (2005) Parser



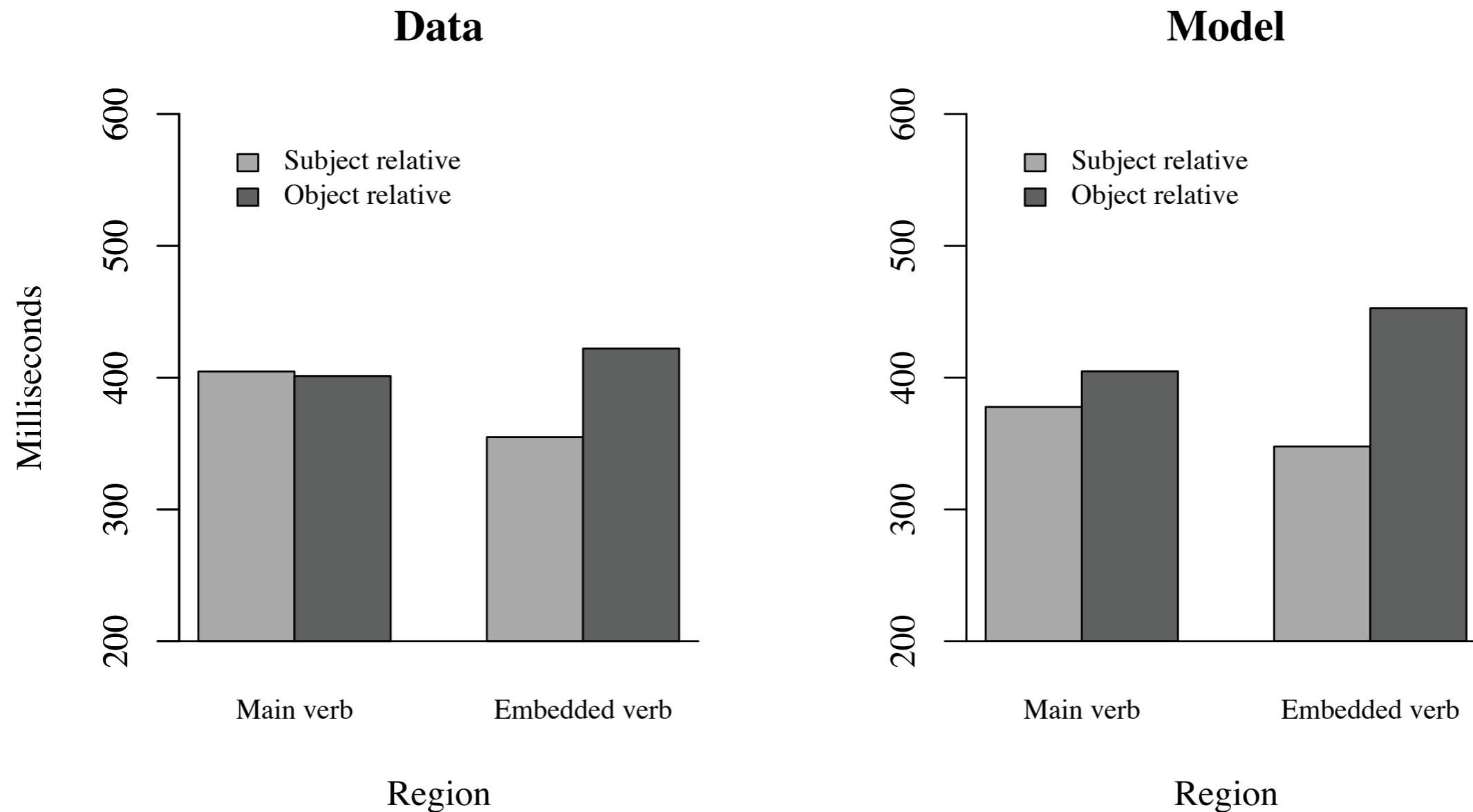
- Activation decay → distance effects
- Associative retrieval → Similarity-based interference
- Deterministic rule application → Expectation effects, reanalysis

Example: Relative Clauses

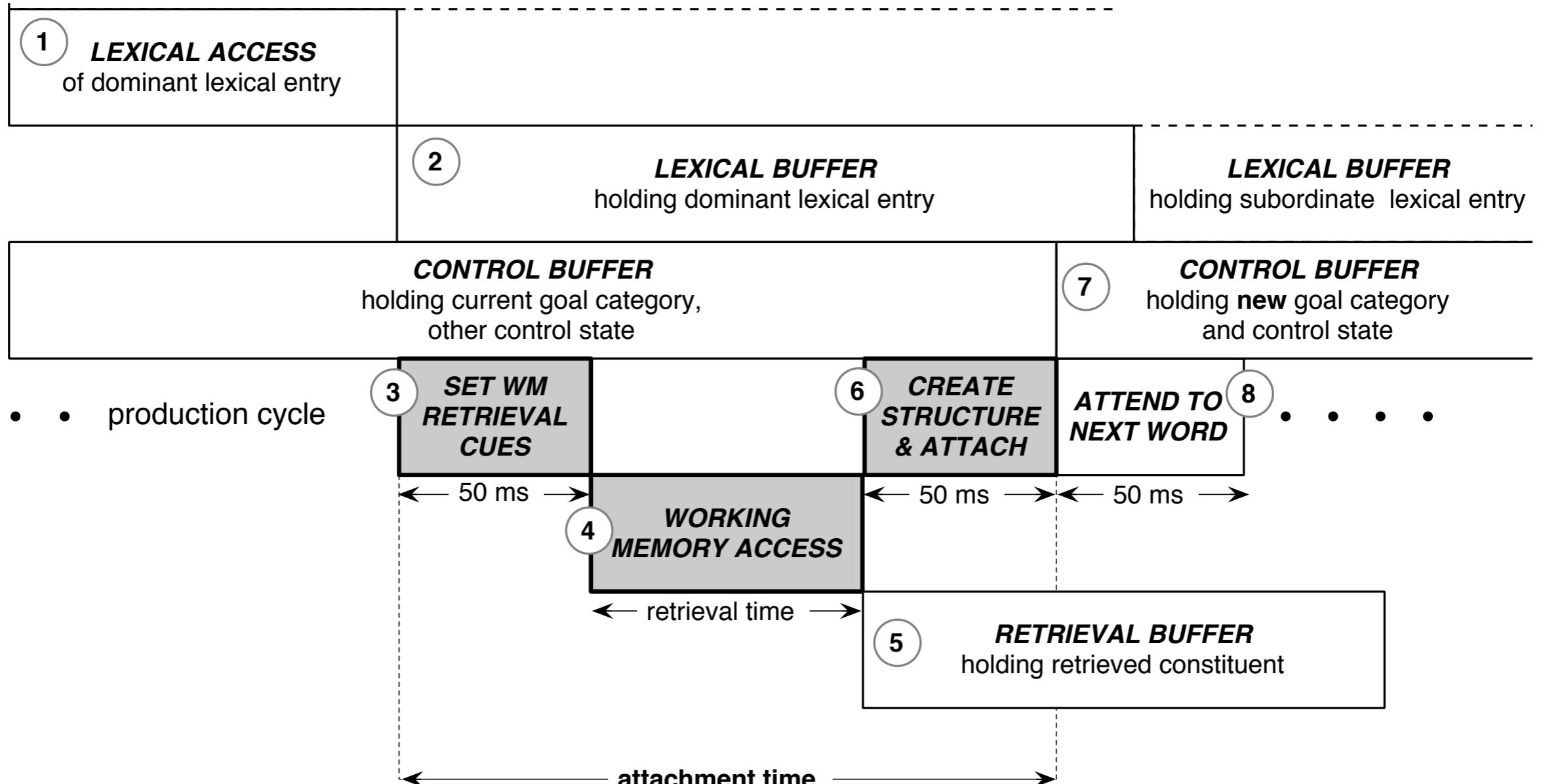
Grodner & Gibson (2005)

SR: The reporter who sent the photographer to the editor hoped for a story.

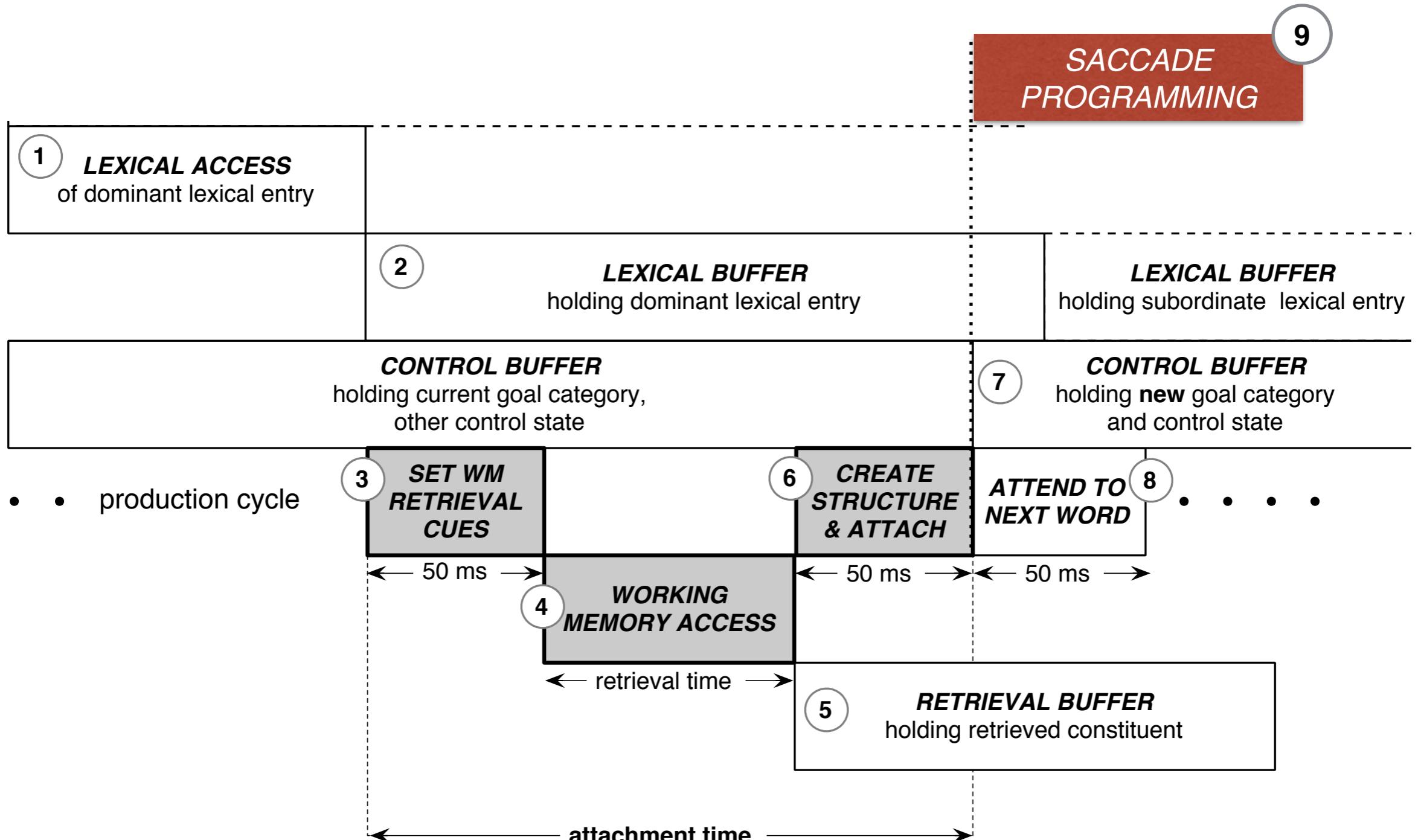
OR: The reporter who the photographer sent to the editor hoped for a story.



Eye Movements

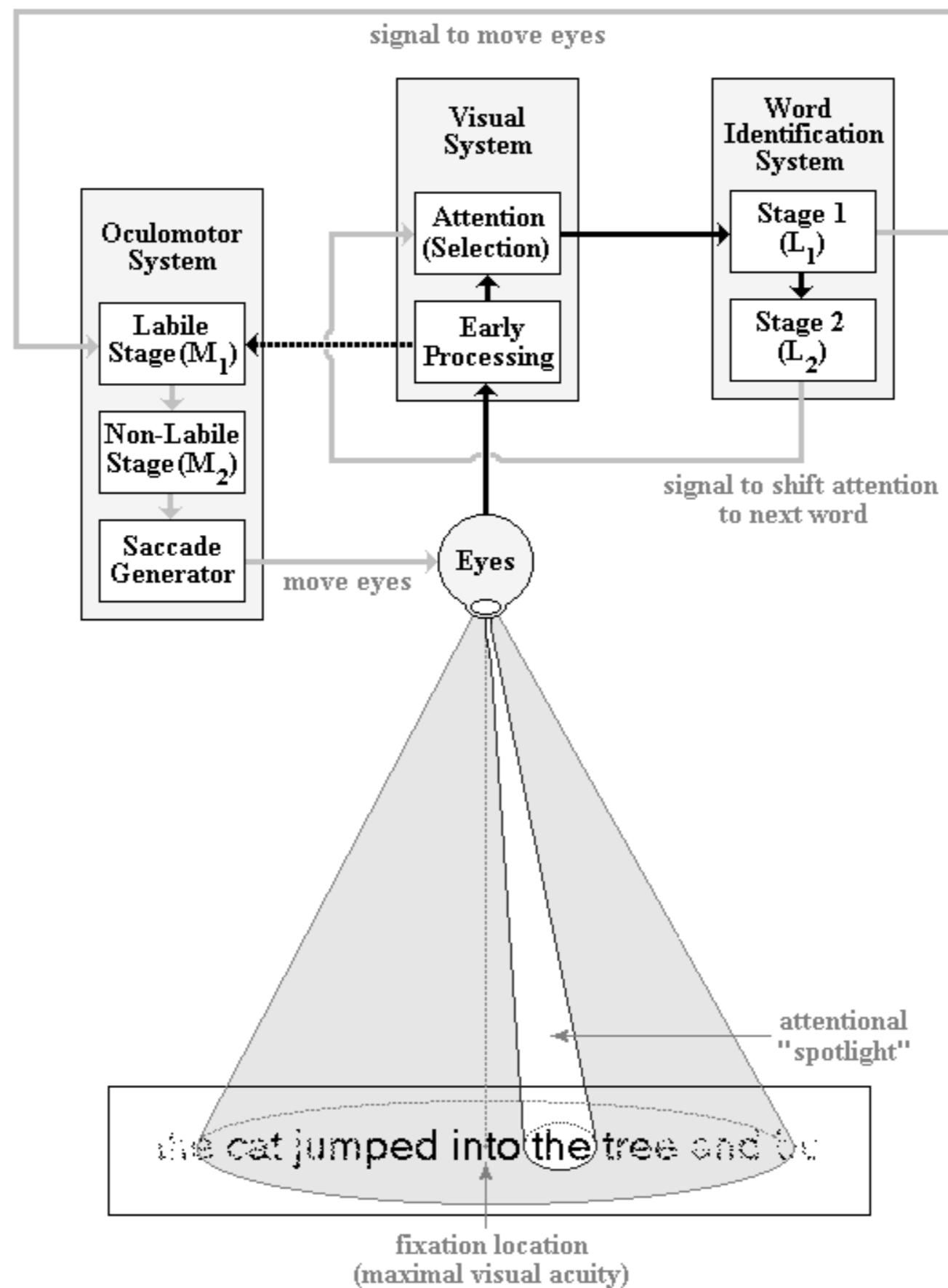


Eye Movements



E-Z Reader 7 (Reichle et al., 2003)

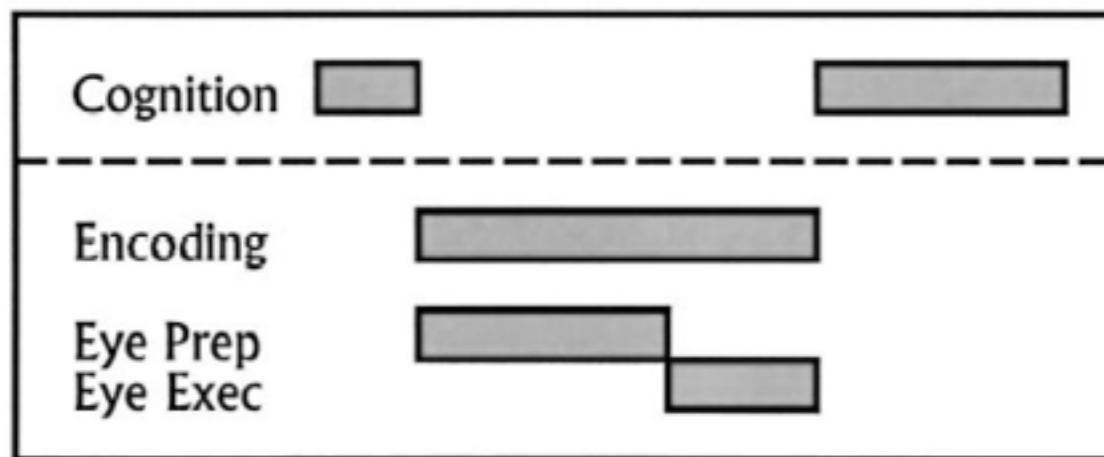
SACCADE PROGRAMMING



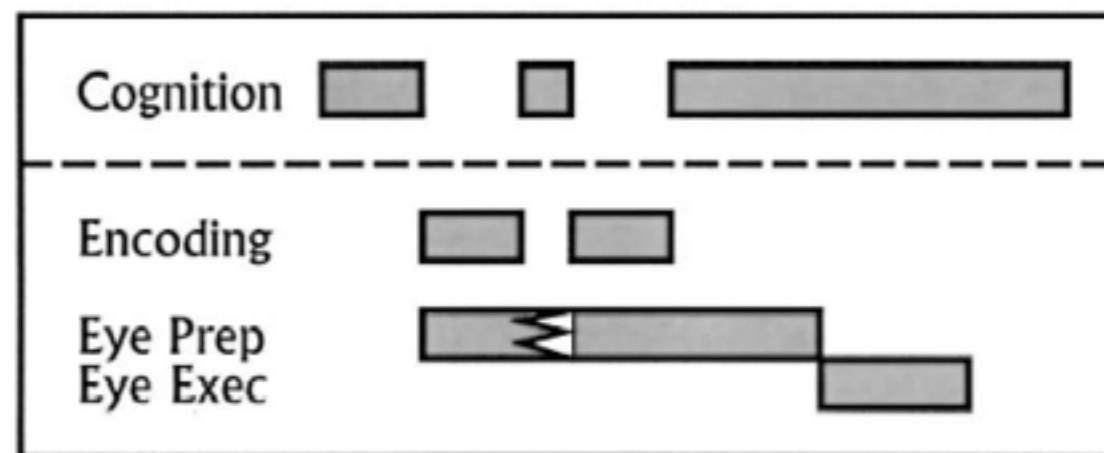
EMMA (Salvucci, 2001)

A simplified version of E-Z Reader for cognitive control models

Normal progression:



Skipping:



Encoding time:

$$T_i = K(-\log f_i) e^{k\varepsilon_i}$$

Encoding factor Word frequency Encoding exponent Word eccentricity

Saccades:

- 135 ms preparation (Salvucci default)
- 50 ms motor programming
- Execution: 20 ms execution + 2 ms per degree of visual angle

Parameters:

:VISUAL-ENCODING-FACTOR	0.002
:VISUAL-ENCODING-EXPONENT	0.4
:SACCADE-PREPARATION-TIME	0.110

How to interact with parsing?

- We know that parsing lags behind eye movements (late effects and spill-over) but, still, integration difficulty influences fixation targets and durations.

Selective Reanalysis (Frazier & Rayner, 1982): Regressions are tightly coupled with linguistic operations.

Time Out proposal (Mitchell et al., 2008): „Regressions are programmed not to facilitate repair, but merely to buy time for the linguistic processor to catch up with its existing backlog of processing.“

Reichle et al. (2009): „The average length of readers' initial regressive eye movements are often quite short, moving the eyes back only a word or two.“

Mitchell et al. (2008): „Regression sequences triggered by syntactic disambiguation are placed under relatively loosely-coupled control with the guidance of successive fixations being shared between both linguistic and non-linguistic mechanisms.“

How to interact with parsing?

Implementation of a Time Out mechanism in Reichle et al. (2009)'s E-Z Reader 10 in terms of a linear-order requirement:

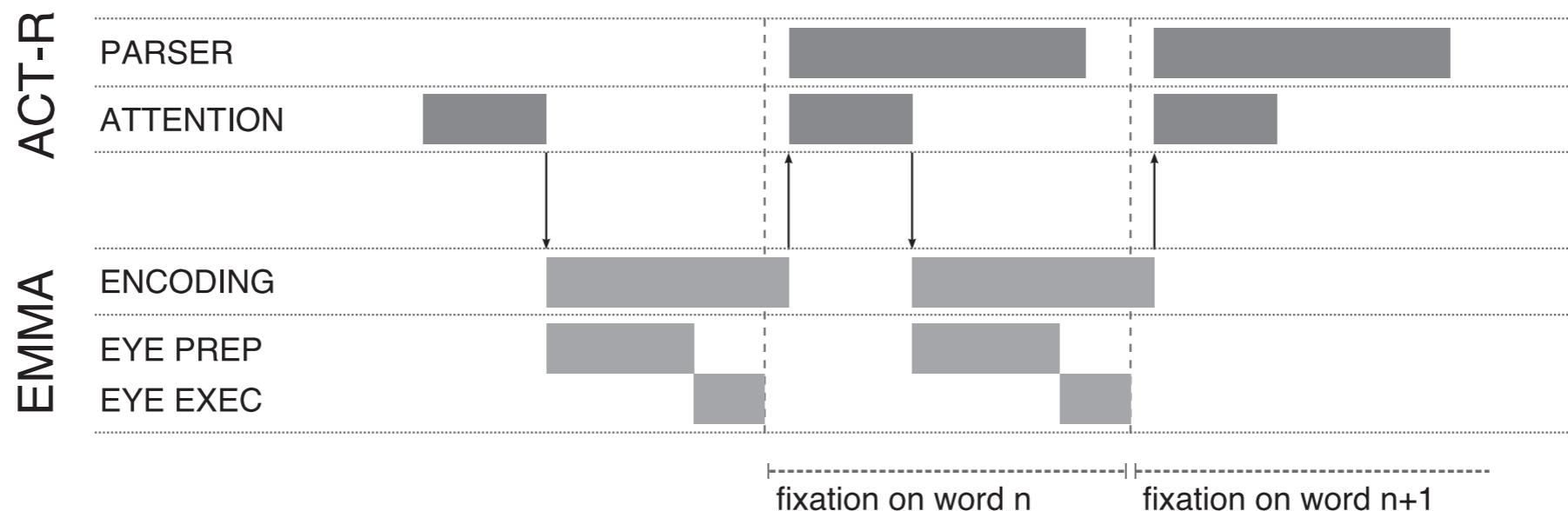
„.... word n+1 is identified ... before word n has been integrated, which ... halts both the post-lexical processing ... of word n and the forward movement of the eyes ... so that both attention and the eyes can be directed back ...“

- But what about fixation durations?

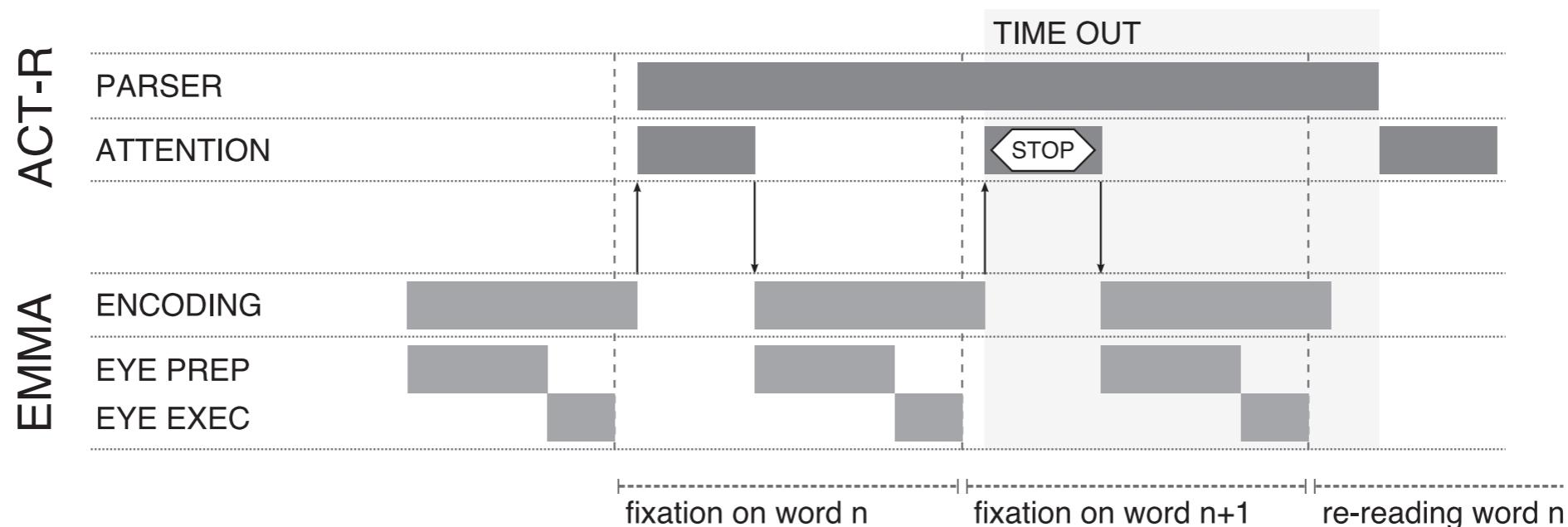
Slowed reading as a by-product of Time Out: When the delayed integration finishes before the regression is executed, the extra processing time of the then cancelled saccade leads to an inflated reading time.

Time Out (Mitchell et al., 2008)

SR: The reporter who **sent** the photographer to the editor hoped for a story.



OR: The reporter who the photographer **sent** to the editor hoped for a story.



```

(p start-time-out
=goal>
  ISA                  comprehend-sentence
  state                "wm-retrieval"
  em-state             "attending"
  attend-to            "next-word"
  time-out             nil
?visual>
  processor           free          ;; no current encoding
  execution           free          ;; no current saccade execution
=visual>
  ISA                  text
  screen-pos          =visual-location
==>
!bind! =eye-loc (first (current-eye-loc))
!bind! =parse-loc (parsing-get-loc)
=goal>
  em-state             "looking"
  last-loc              =visual-location
  time-out              t
+visual-location>
  ISA                  visual-location
  < screen-x           =eye-loc          ;; target before current fixation
  screen-x              highest          ;; target nearest to the left
!eval! (start-time-out =parse-loc)
!eval! (trialmessage "timeout" =eye-loc)
)

```

Corpus Evaluation

```
:lf 0.2  
:VISUAL-ENCODING-FACTOR    0.002  
:VISUAL-ENCODING-EXPONENT   0.4  
:SACCADE-PREPARATION-TIME  0.110
```



TOPICS
TOPICS IN COGNITIVE SCIENCE

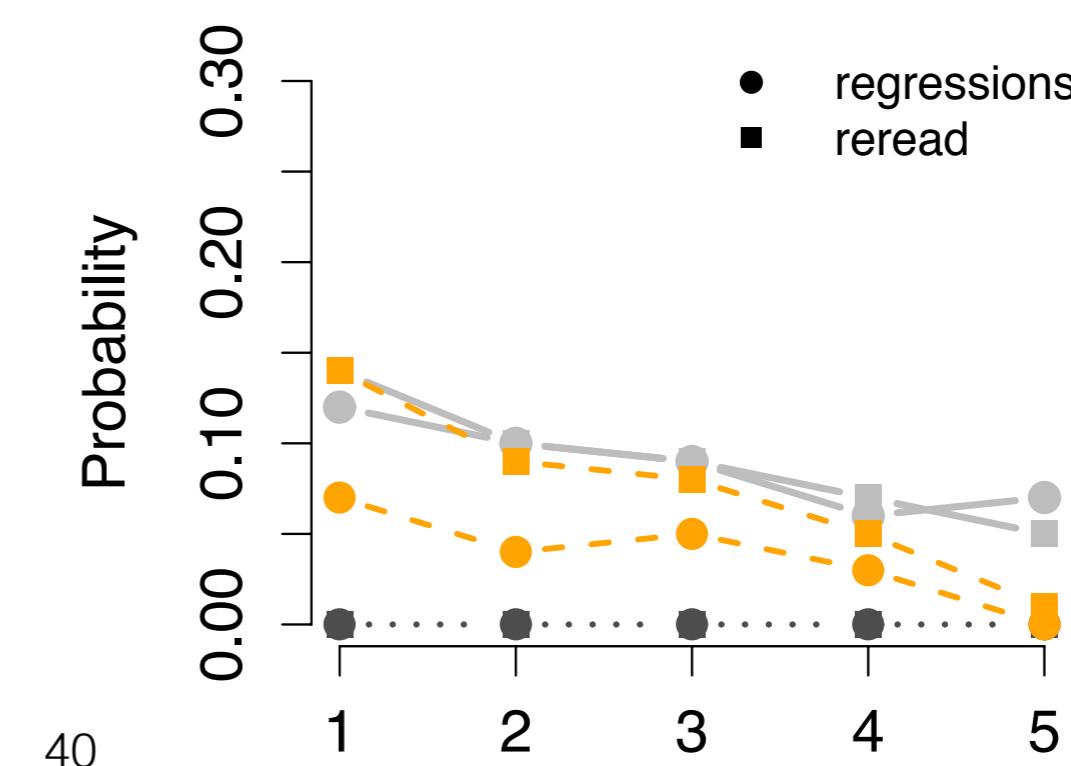
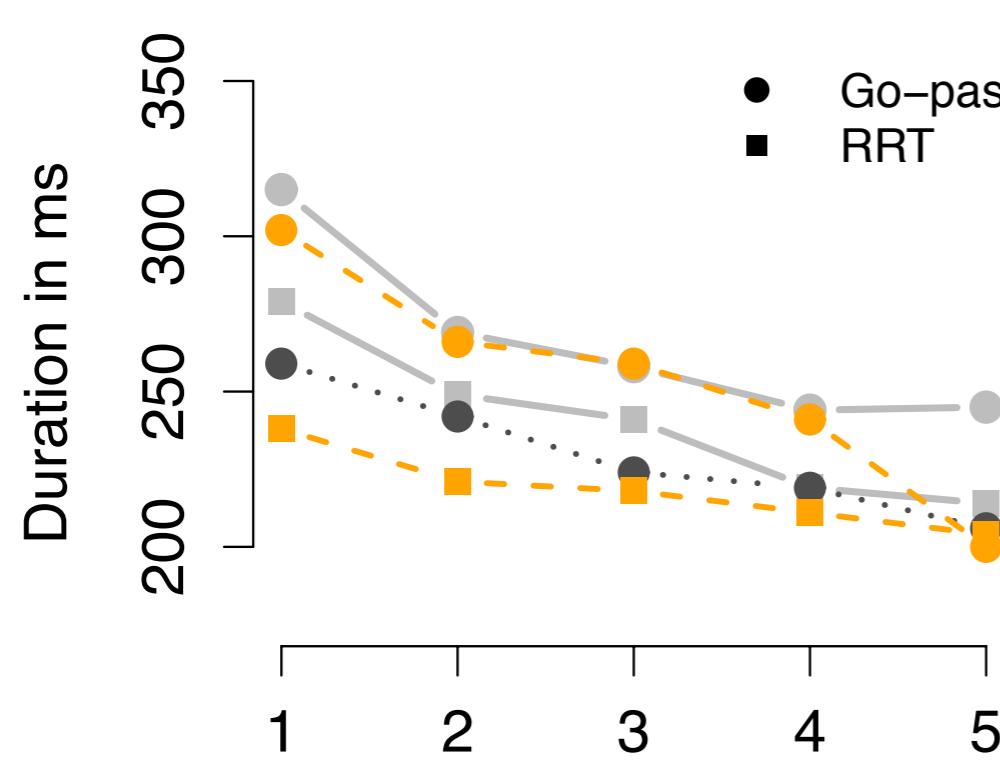
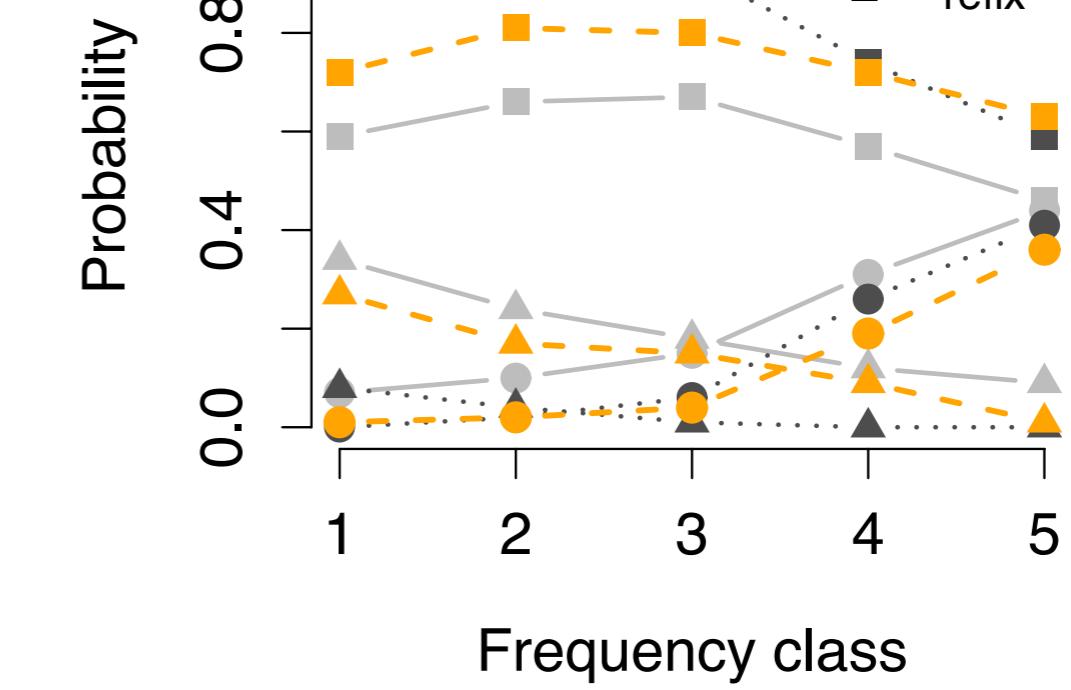
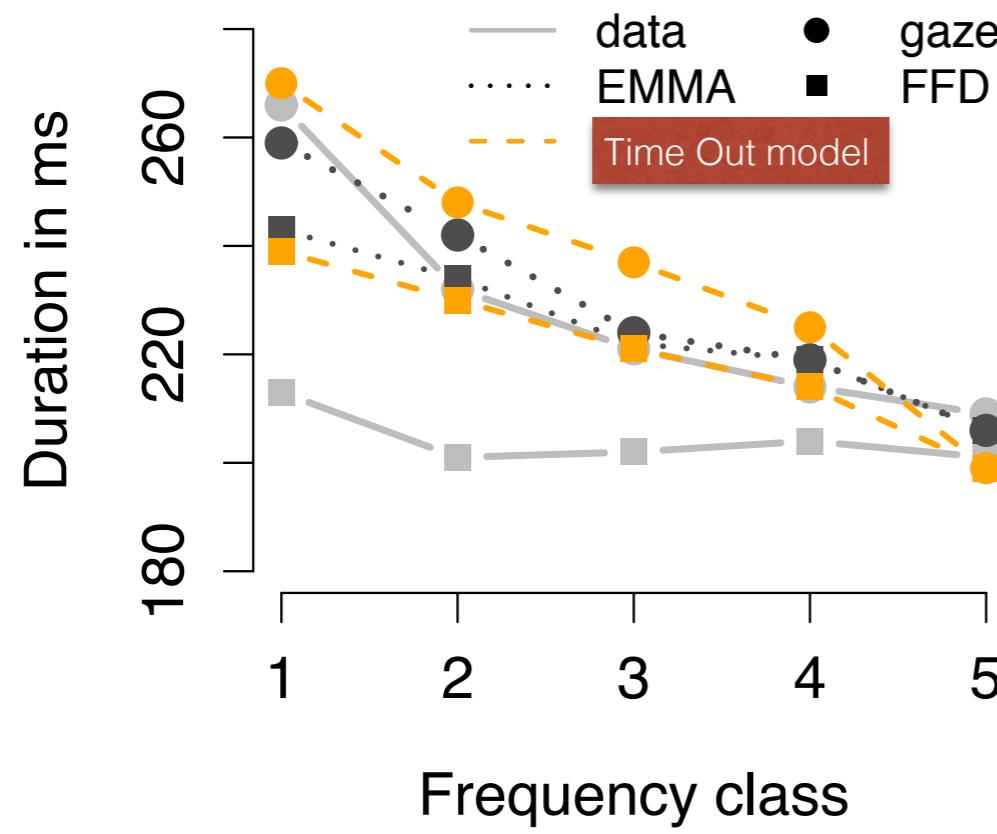


Topics in Cognitive Science (2013) 1–23
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ISSN:1756-8757 print / 1756-8765 online
DOI: 10.1111/tops.12026

A Framework for Modeling the Interaction of Syntactic Processing and Eye Movement Control

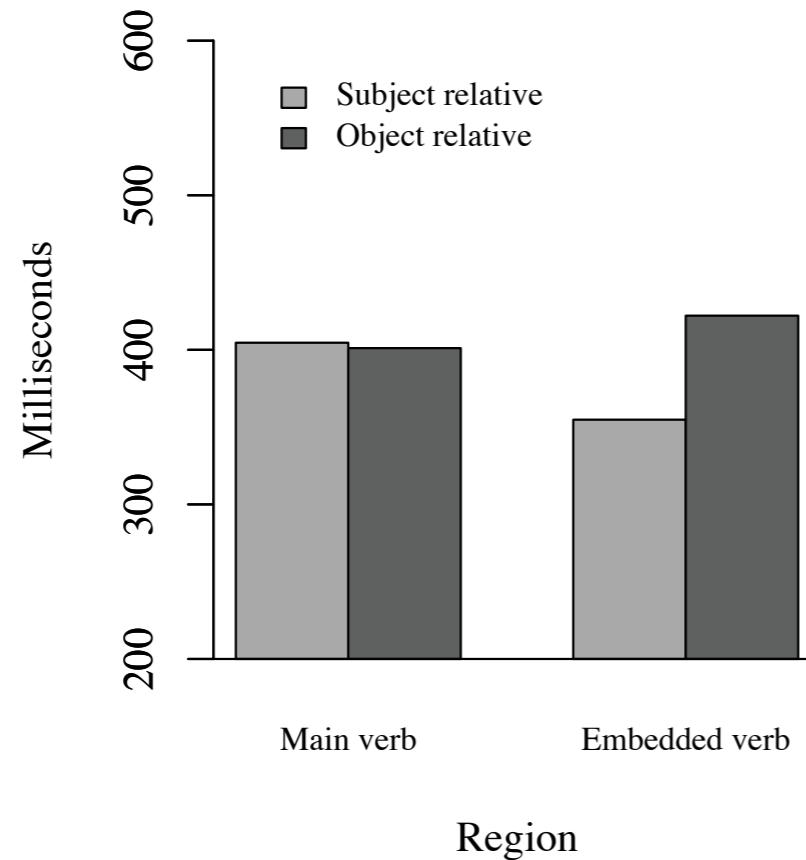
Felix Engelmann, Shravan Vasishth, Ralf Engbert, Reinhold Kliegl

Corpus Evaluation



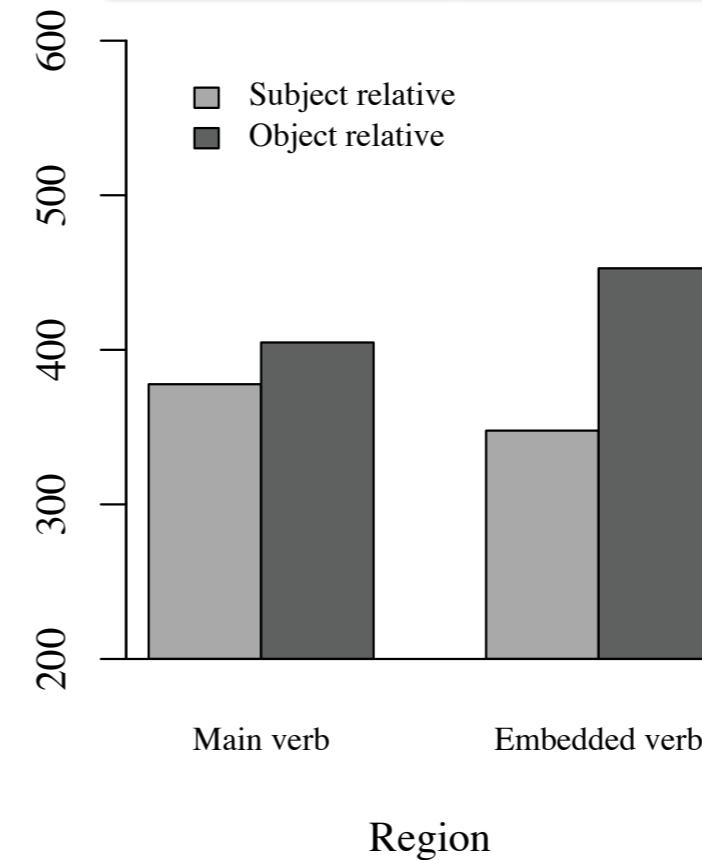
Grodner & Gibson (2005)

Subject relative
Object relative



Attachment LV05 model

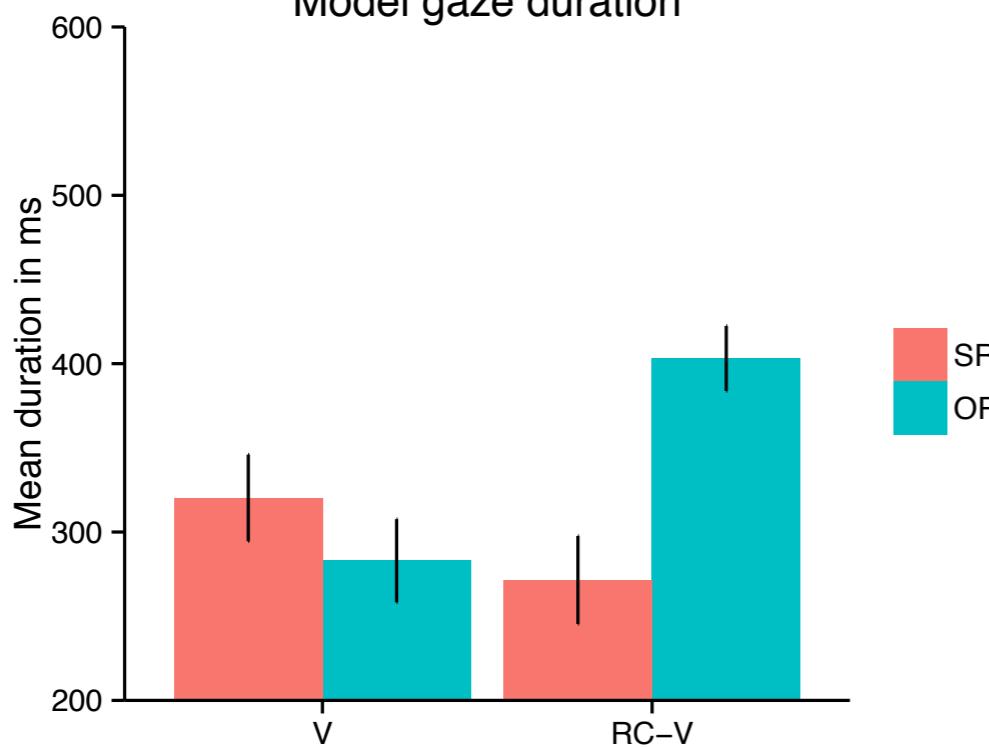
Subject relative
Object relative



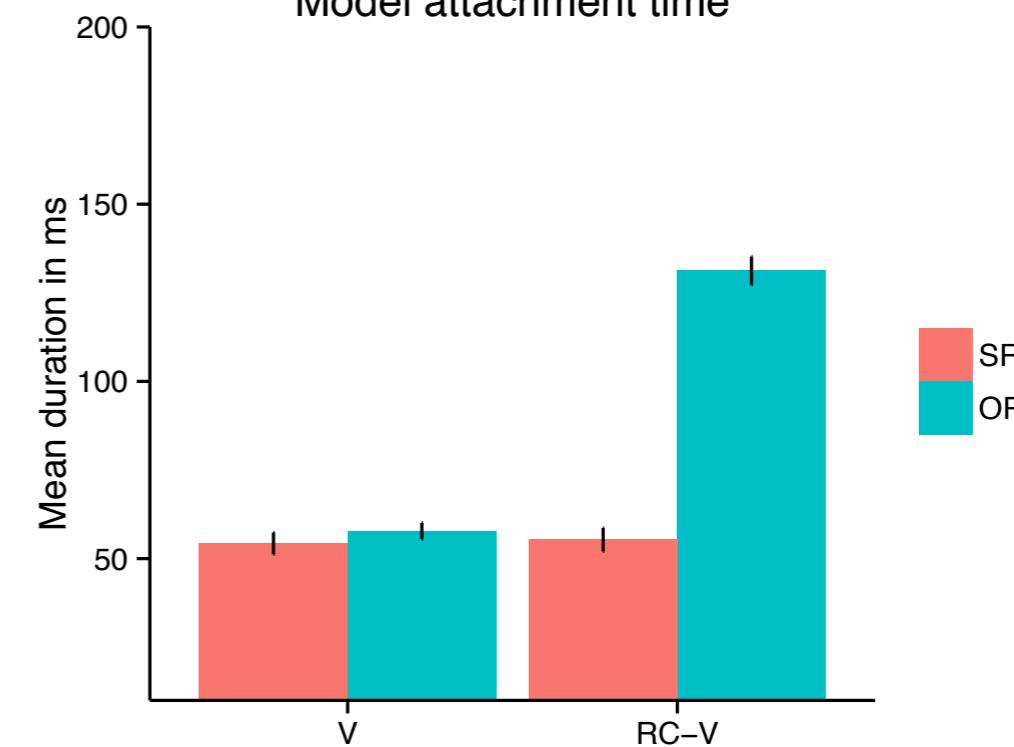
Region

Time Out model

Model gaze duration

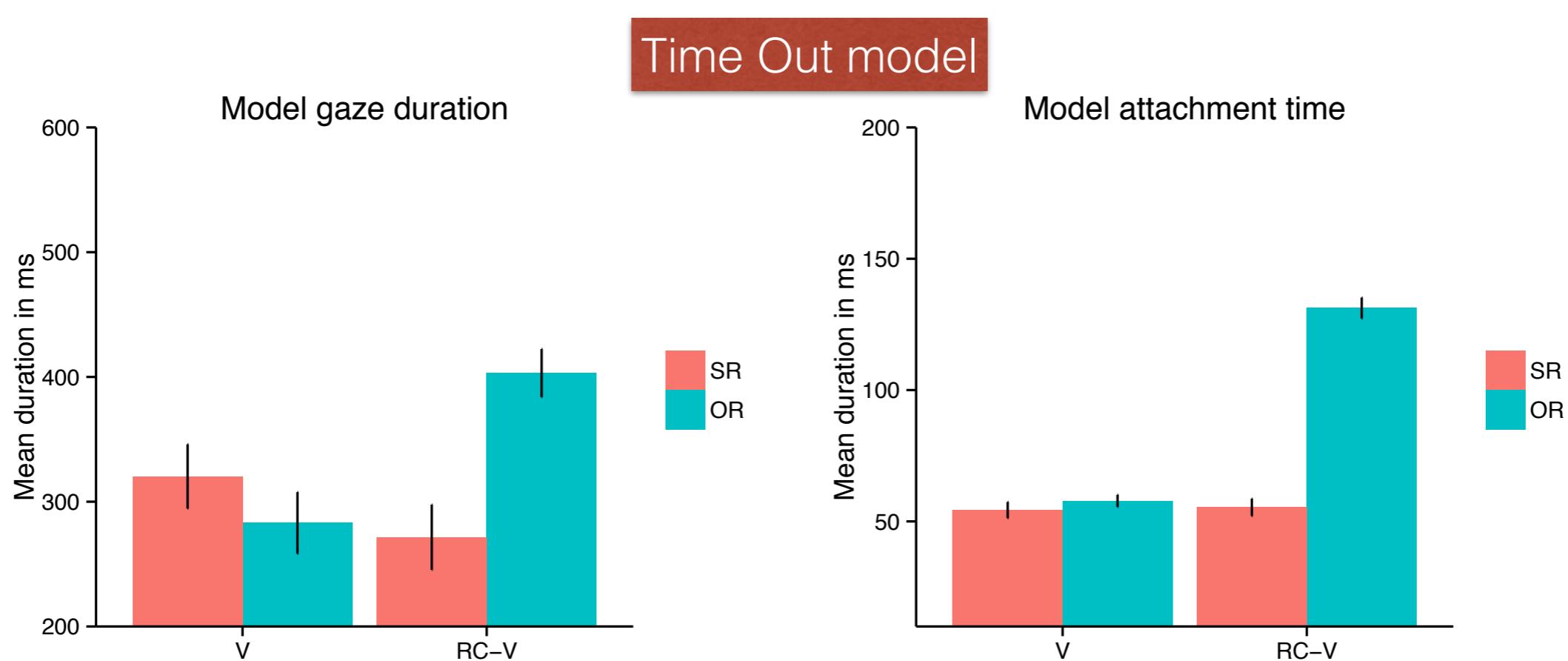


Model attachment time



Grodner & Gibson (2005)

```
(re 'gg-exp1 100)
(cwd "output/")
(run-program "Rscript" '("gg05-analysis.R"))
(cwd "../")
```



Reanalysis: Staub (2010)

Subject-relative:

The employees that noticed the fireman hurried across the open field.

Object-relative:

The employees that the fireman noticed hurried across the open field.



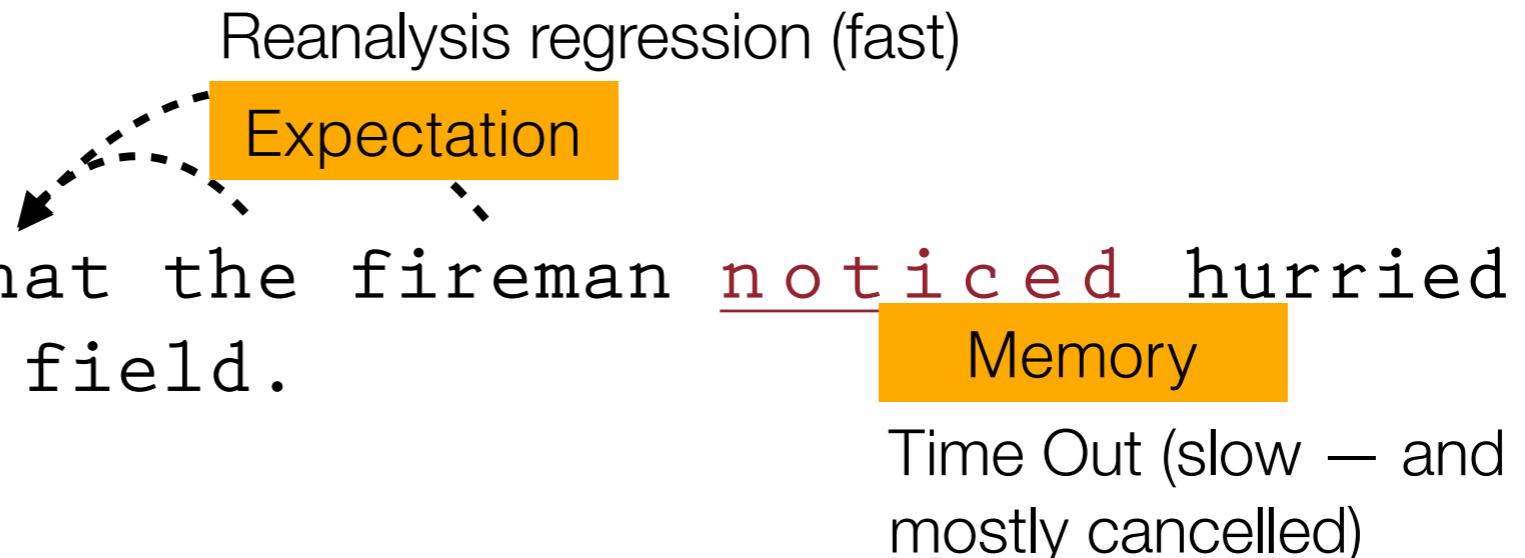
Reanalysis: Staub (2010)

Subject-relative:

The employees that noticed the fireman hurried across the open field.

Object-relative:

The employees that the fireman noticed hurried across the open field.



„The difficulty that emerges on the ORC subject and verb are apparently different in kind.“

(Staub, 2010)

```

(P attach-DP-as-subject-of-predicted-IP-gapped
  =goal>
    ISA           comprehend-sentence
    state         "wm-retrieval"
    goal-cat     VP-gapped-goal
  =retrieval>
    isa           syn-obj
    cat           IP
    head          nil
    subj-word    =subj-word
    waiting-for-cat wait-for-VP
    spec          =empty-op
    gap           spec
  =lex>
    isa           lexical-entry
    cat           DET
    word          =word
==>
  !bind! =ID-DP (new-name DP)
  =goal>
    state         "wm-retrieval"
    cue1          =empty-op
    attend-to    "left"
+DPb>
  isa           syn-obj
  cat           DP
  ID            =ID-DP
  case          nom
  head          =word
  spec-of       =retrieval
  waiting-for-case wait-for-nom
  waiting-for-cat wait-for-NP
  next-goal     next-VP-gapped-goal
  =retrieval>
    number        sing-plural
    spec          =ID-DP
    gap           open
+retrieval>
  ISA           syn-obj
  CAT           DP
  ID            =empty-op
  filler        DONE
)

```

```

(P revise-subject-relative
  =goal>
    ISA           comprehend-sentence
    state         "wm-retrieval"
    goal-cat     VP-gapped-goal
  =retrieval>
    isa           syn-obj
    filler        done
==>
  =goal>
    state         "read"
    goal-cat     NP-goal
    attend-to    "next-word"
  =retrieval>
    ;; reinstate filler as active
    filler        yes-filler
    !eval! (set-end-time)
)

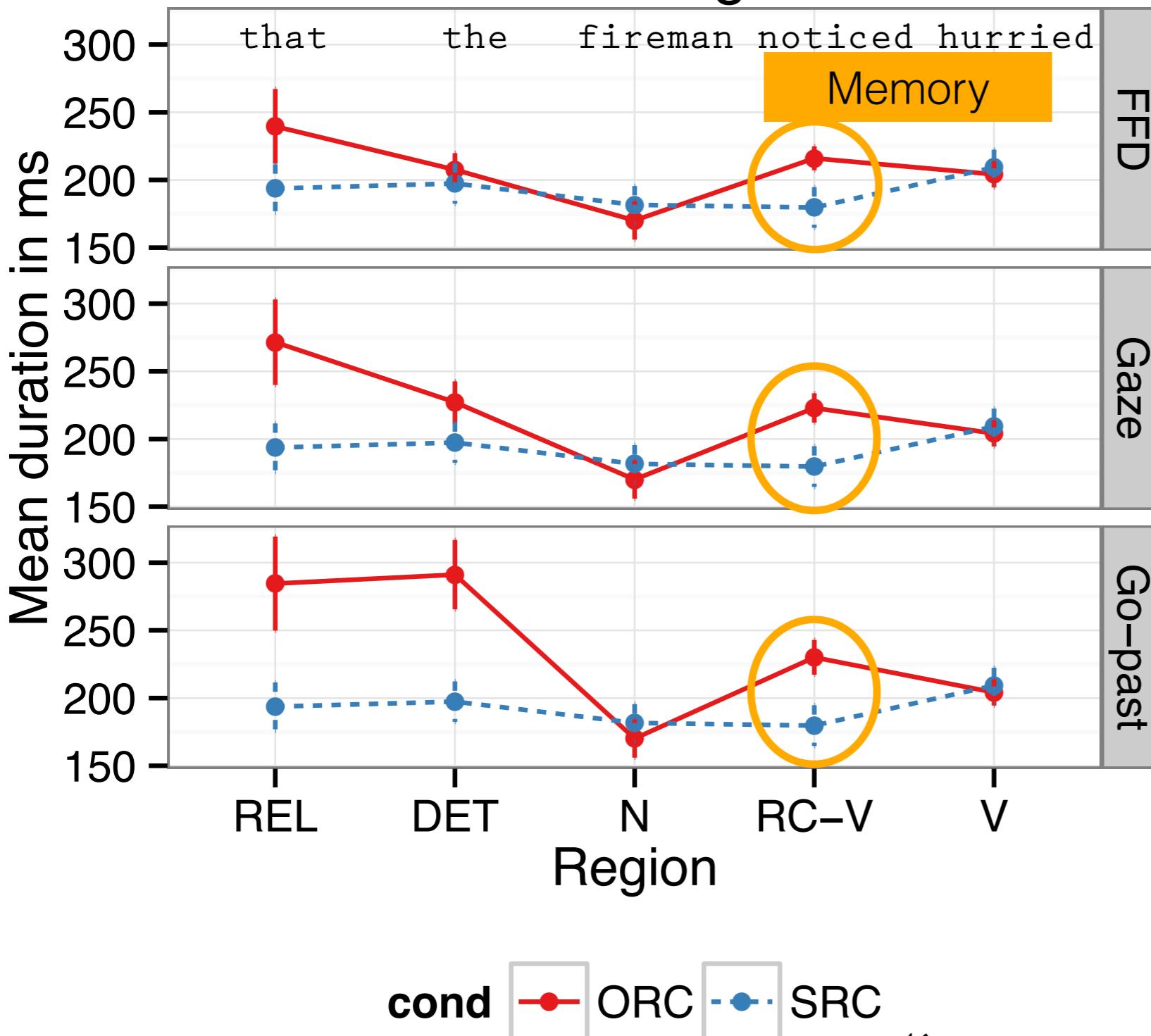
```

Reanalysis regression (fast)

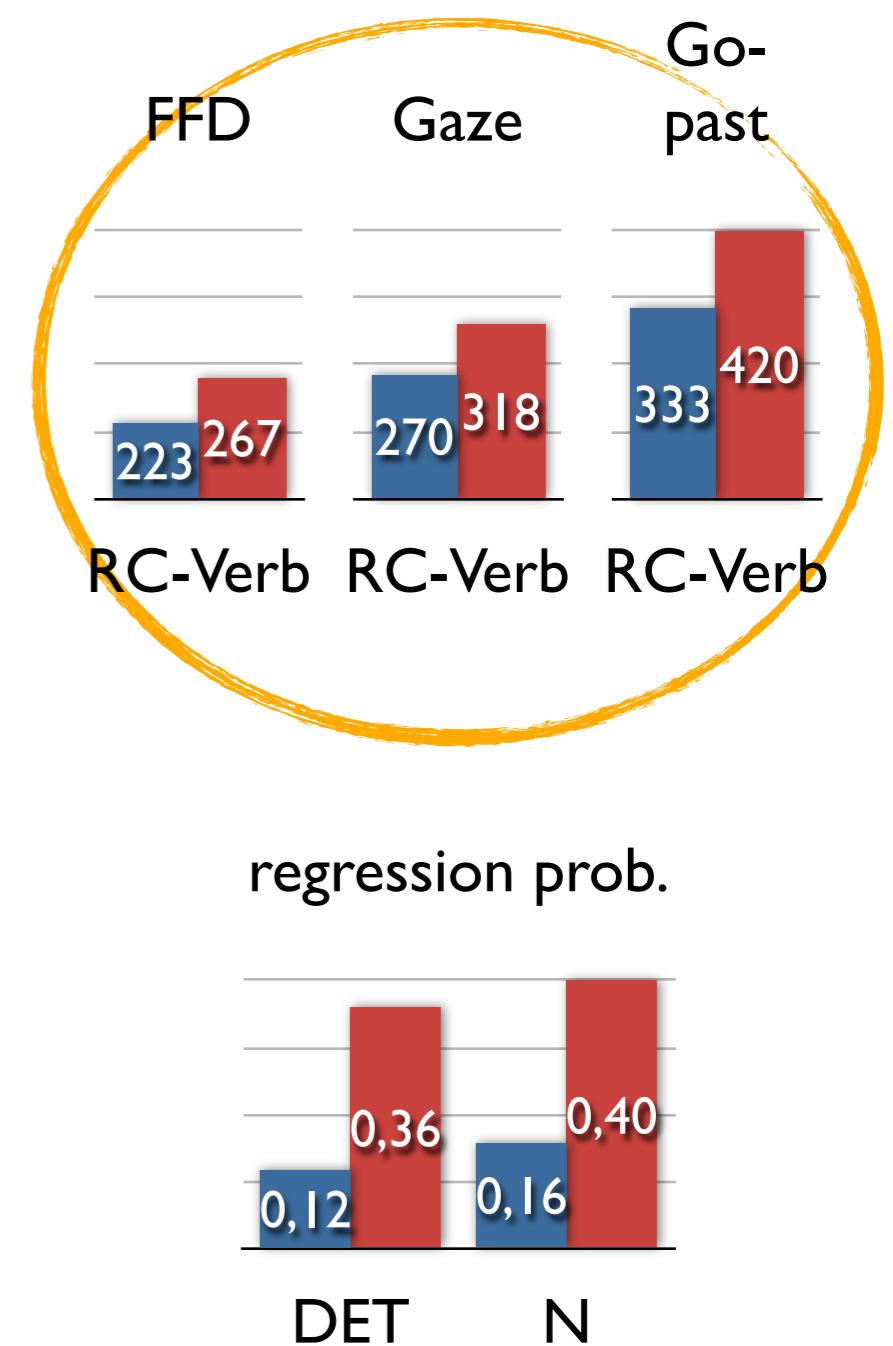
The employees that the fireman

Staub (2010)

Model reading times

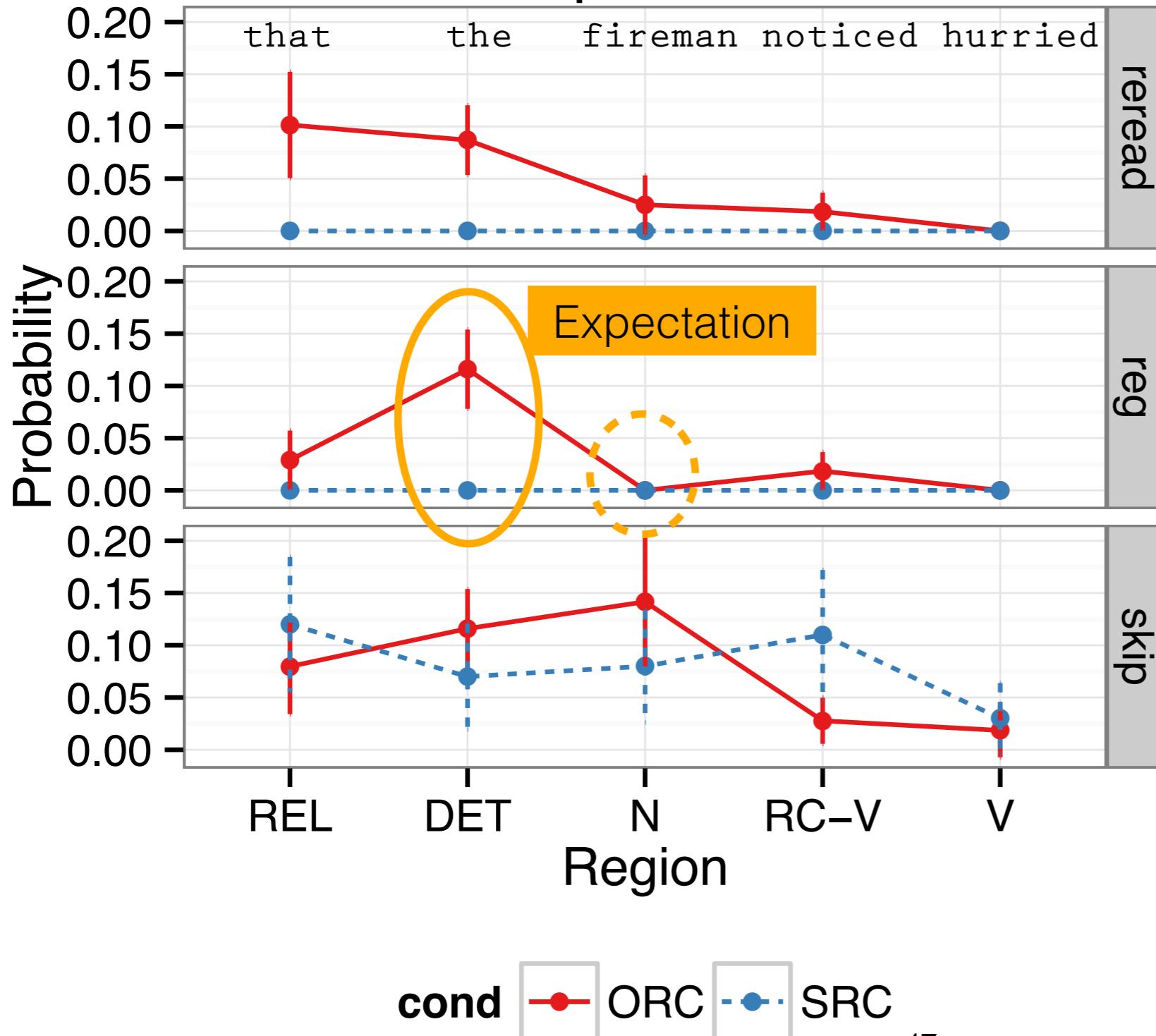


Data

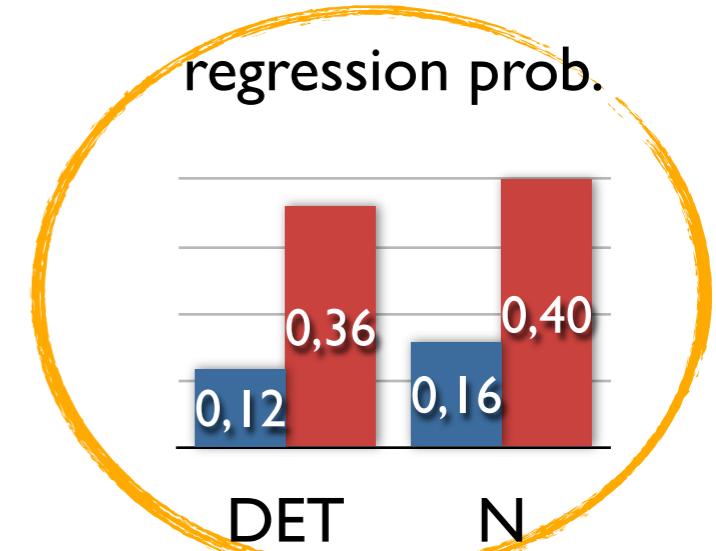
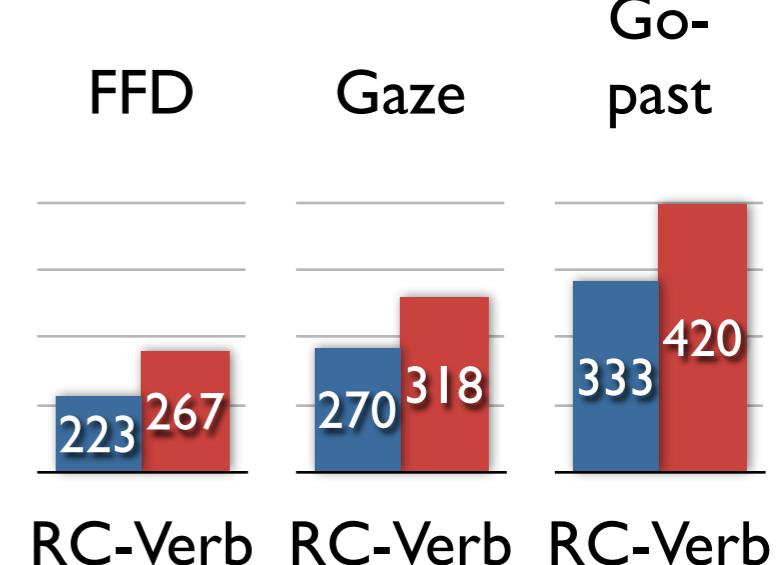


Staub (2010)

Model probabilities



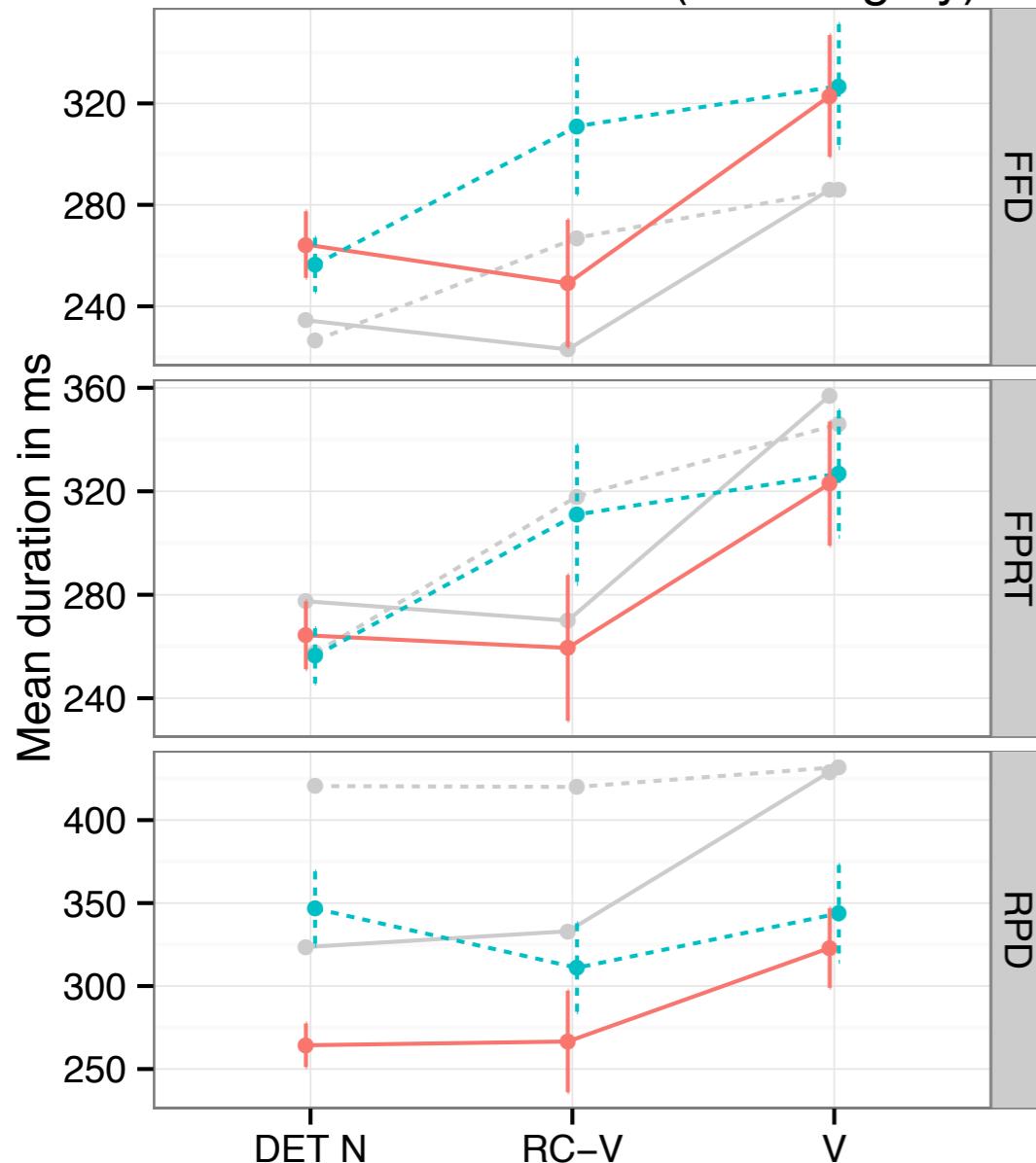
Data



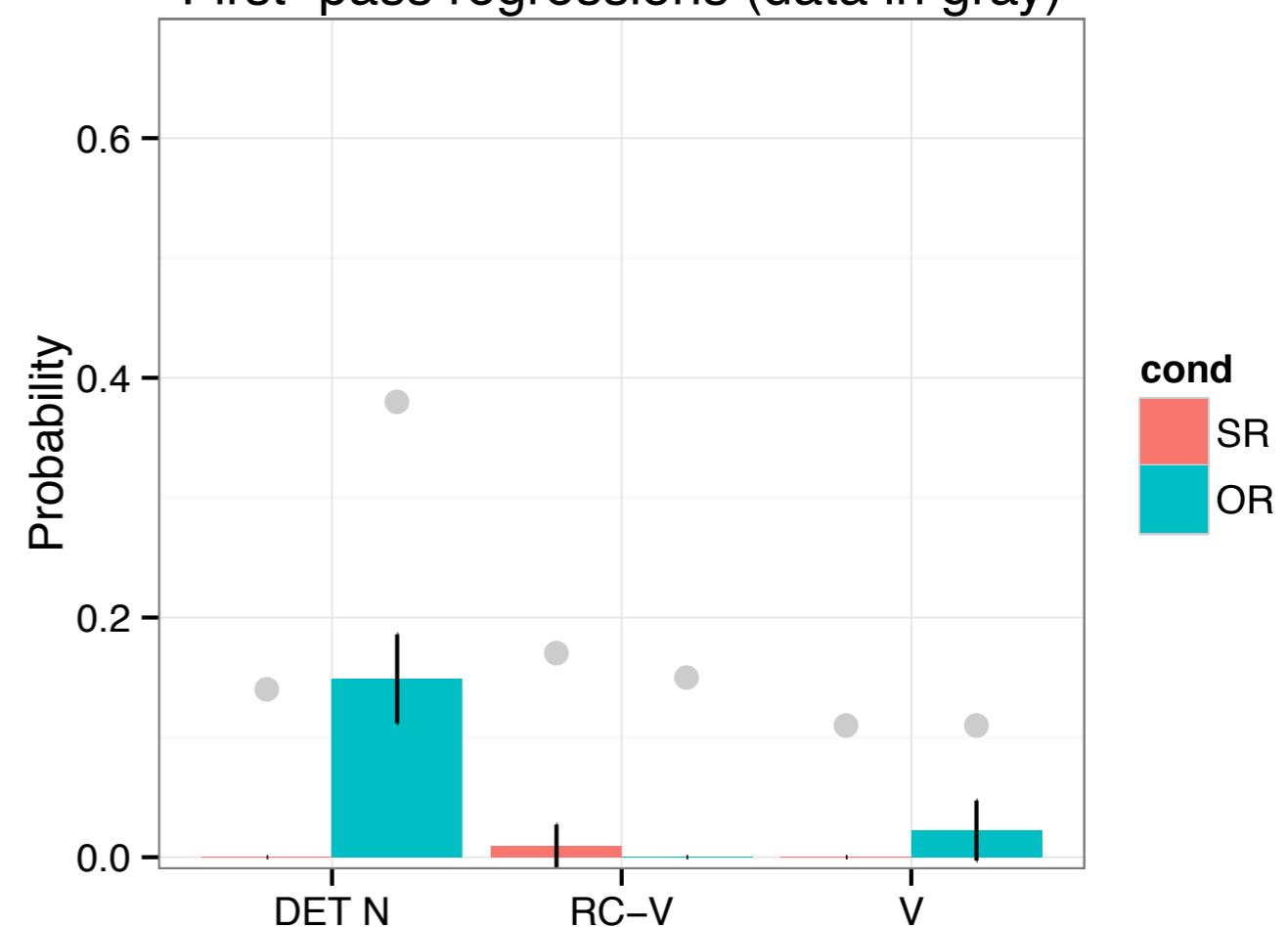
Staub (2010)

```
(re 'staub10 100)
(cwd "output/")
(run-program "Rscript" '("staub10-analysis.R"))
(cwd "../")
```

First fixation duration (data in gray)

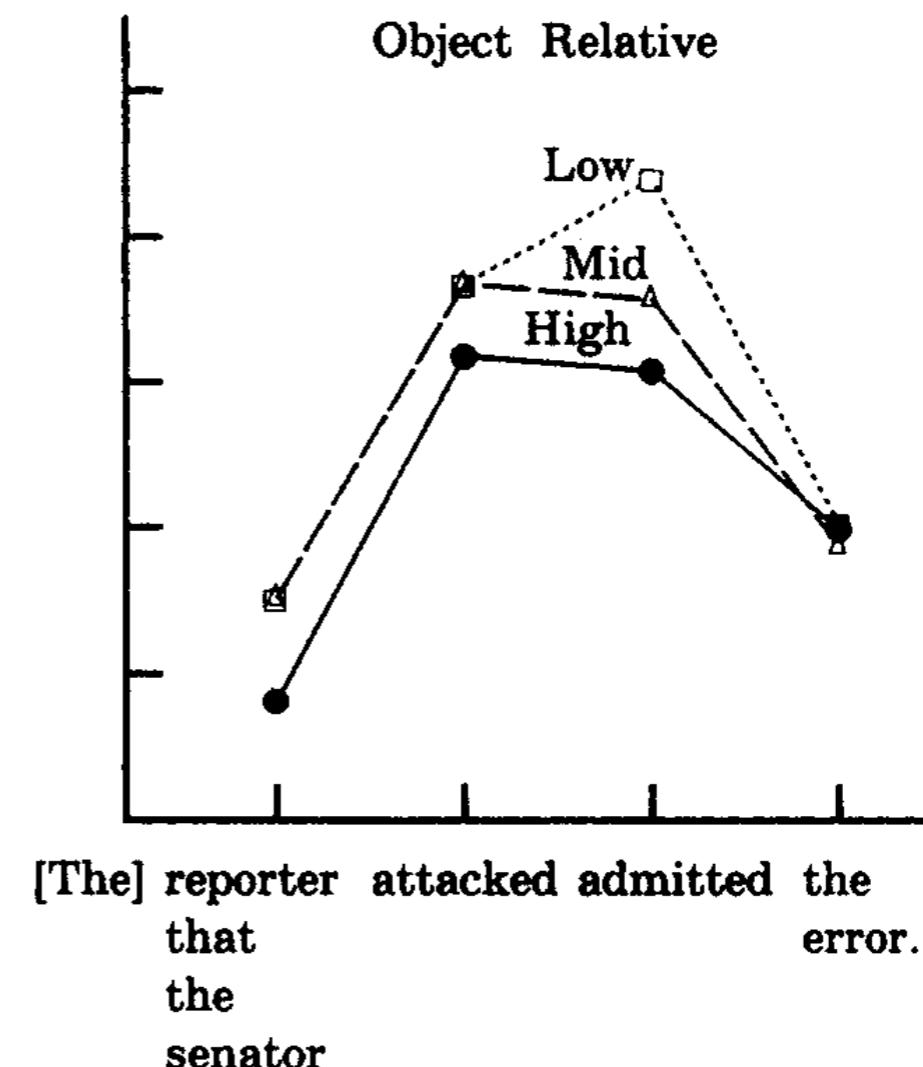
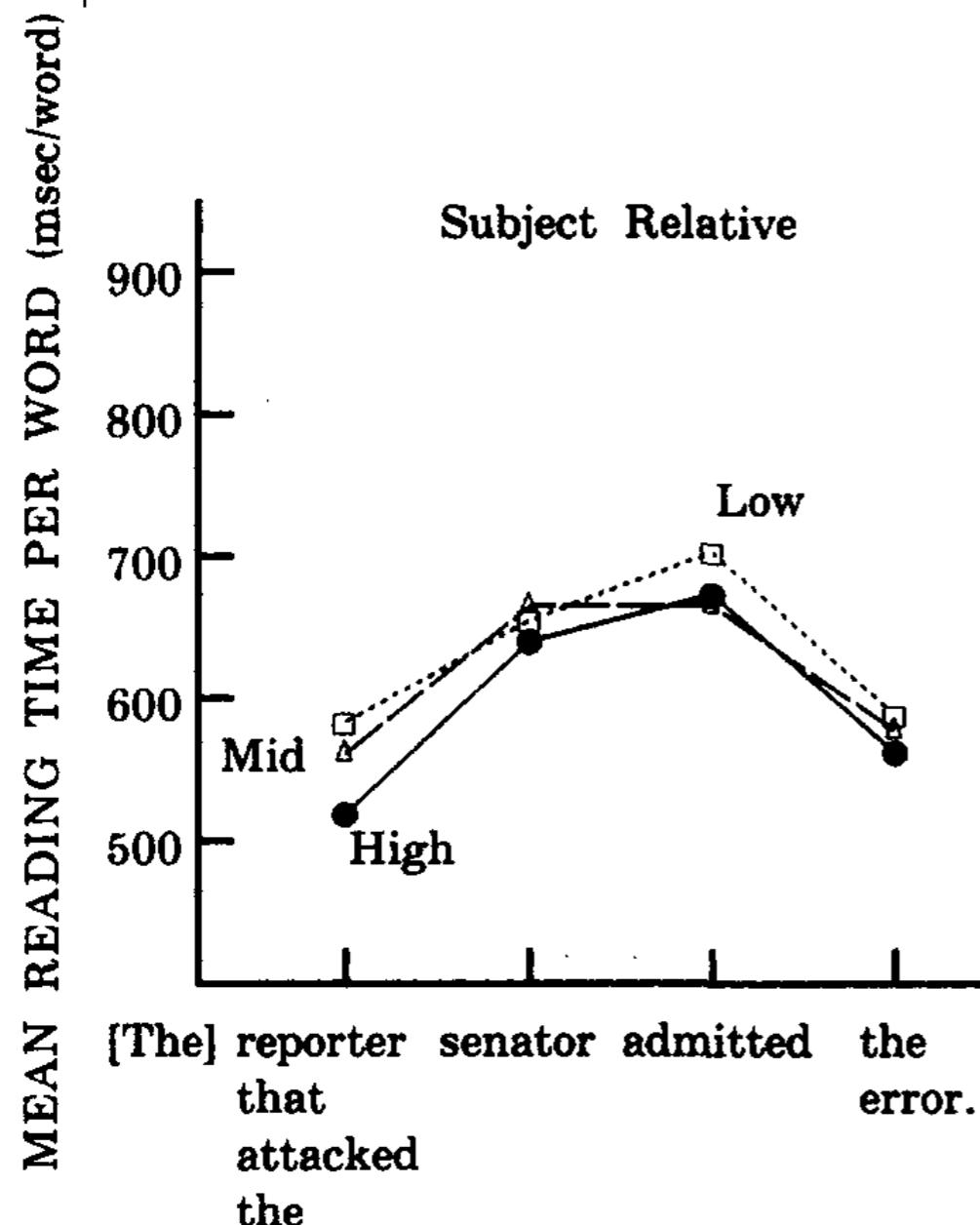


First-pass regressions (data in gray)



Individual Differences

Just and Carpenter (1992): Theory of linguistic working memory capacity. King & Just (1991) showed that WMC as measured by the reading span task (Daneman & Carpenter, 1980) affects sentence comprehension:



Modeling Individual Differences

Latency factor F (:lf)

→ **Speed**

Decay parameter d (:bl)

→ **Speed, forgetting**

Source activation W_k of buffer k (e.g., goalbuffer :ga)

This activation is distributed among goal-related chunks.

→ **Accuracy (goal-relevant), speed**

Mismatch penalty P (:mp)

→ **Error sensitivity**

Similarity M_{ki} between the value k in the retrieval specification and the value in the corresponding slot of chunk i

→ **Association between cue and target**

$$RT = Fe^{-(f^*A_i)}$$

$$B_i = \ln\left(\sum_{j=1}^n t_j^{-d}\right) + \beta_i$$

$$A_i = B_i + S_i + P_i + \varepsilon_i$$

$$S_i = \sum_k \sum_j W_{kj} S_{ji}$$

$$P_i = \sum_k PM_{ki}$$

Working Memory Capacity

Goal buffer source activation W: The amount of activation from source j in the goal buffer is the source activation W divided by the number of sources j in that buffer.

!!! This means that activation spread is less when there are more slots in the goal buffer (filled slots, those with nil do not count) !!!

$$A_i = B_i + \sum_{j=1}^n \frac{W}{n} S_{ji}$$

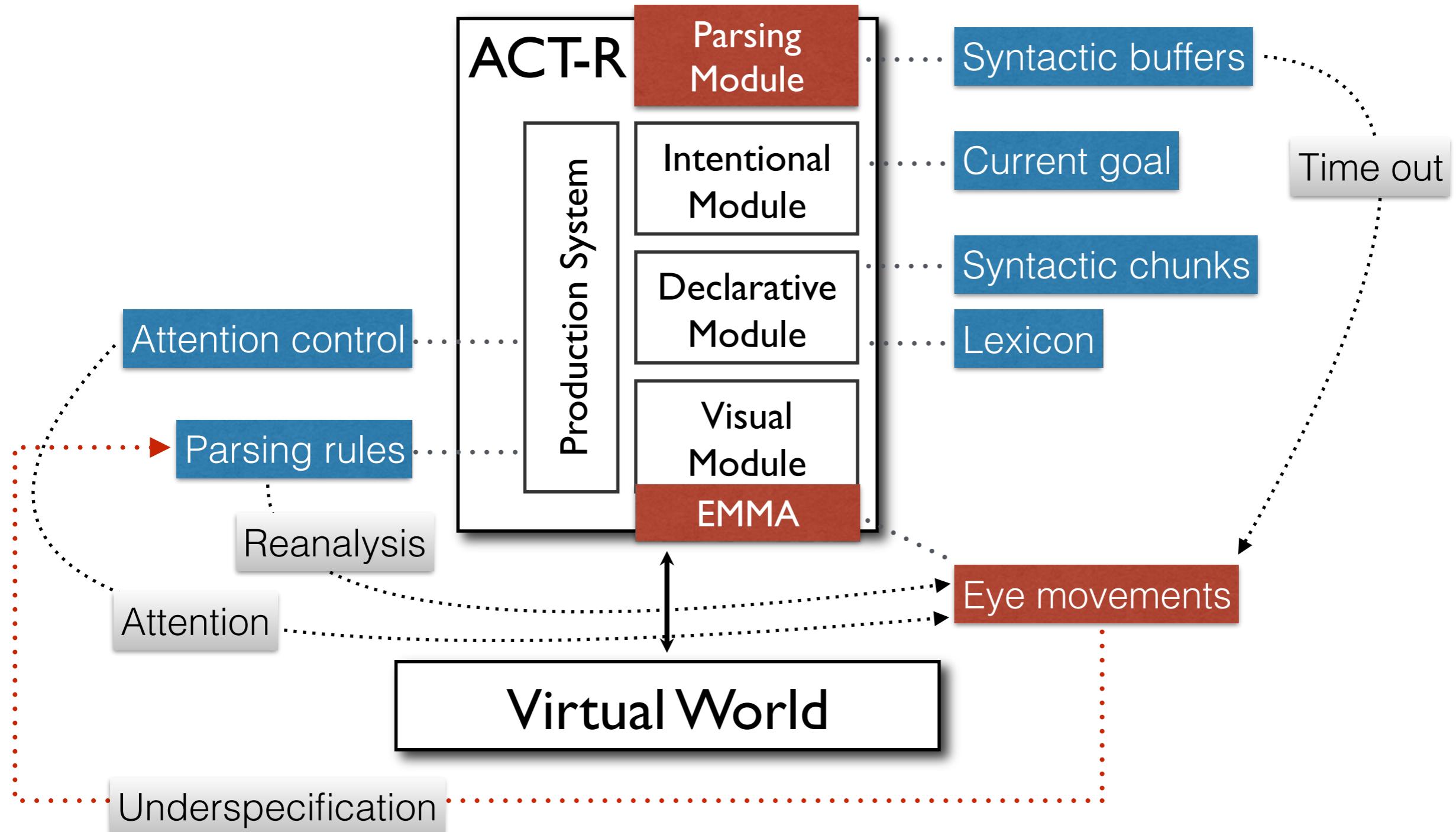
An ACT-R model of WM (Digit span task, Lovett et al., 1999):

Daily, L. Z., Lovett, M. C., & Reder, L. M. (2001). Modeling individual differences in working memory performance: A source activation account. *Cognitive Science*, 25(3), 315–353.

WM modeled in language processing:

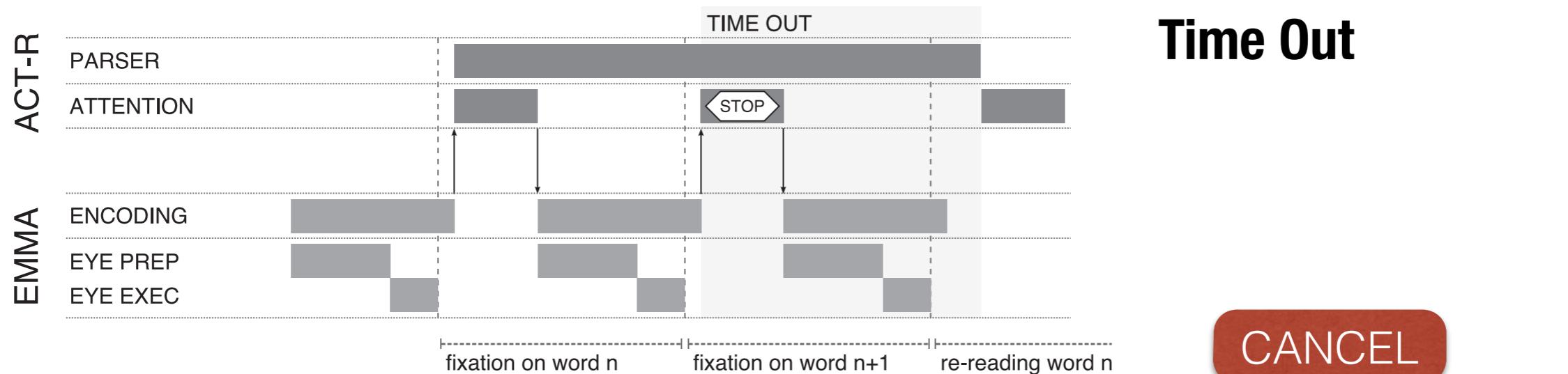
van Rij, J., van Rijn, H., & Hendriks, P. (2013). How WM load influences linguistic processing in adults: A computational model of pronoun interpretation in discourse. *Topics in Cognitive Science*.

Underspecification Model

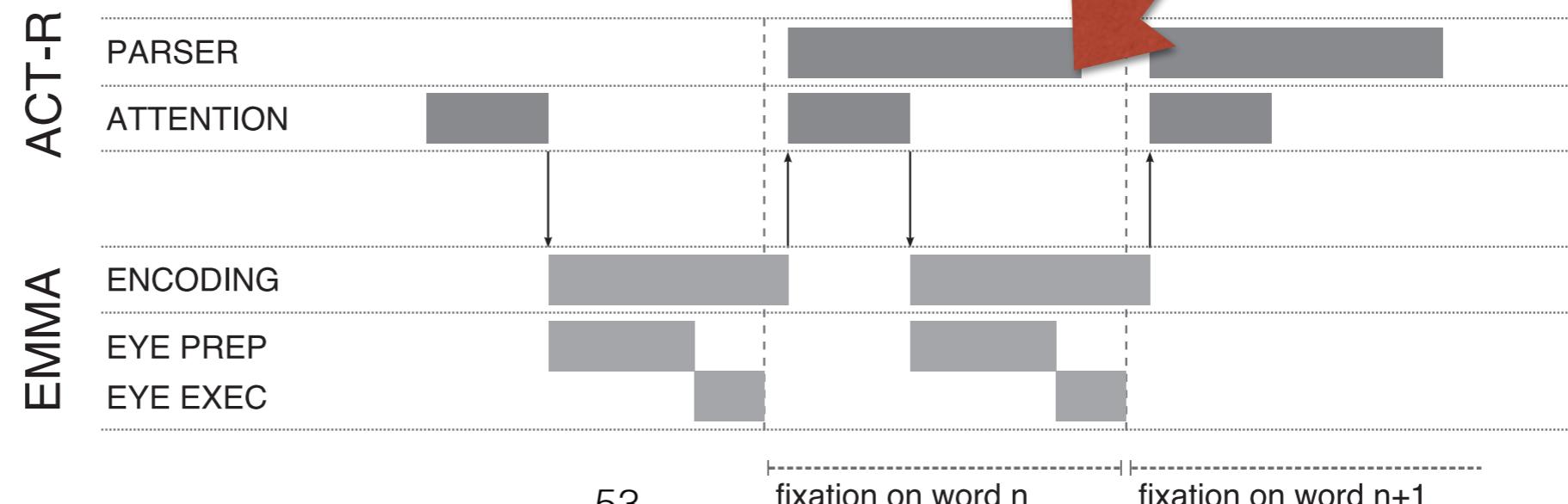


Underspecification Model

Some dependency relations are less important for the current task than others and might stay incomplete under time pressure. The time pressure in reading is imposed by the eye movement control system. The mechanism producing underspecification is the same as for Time Outs regressions:



Under-specification



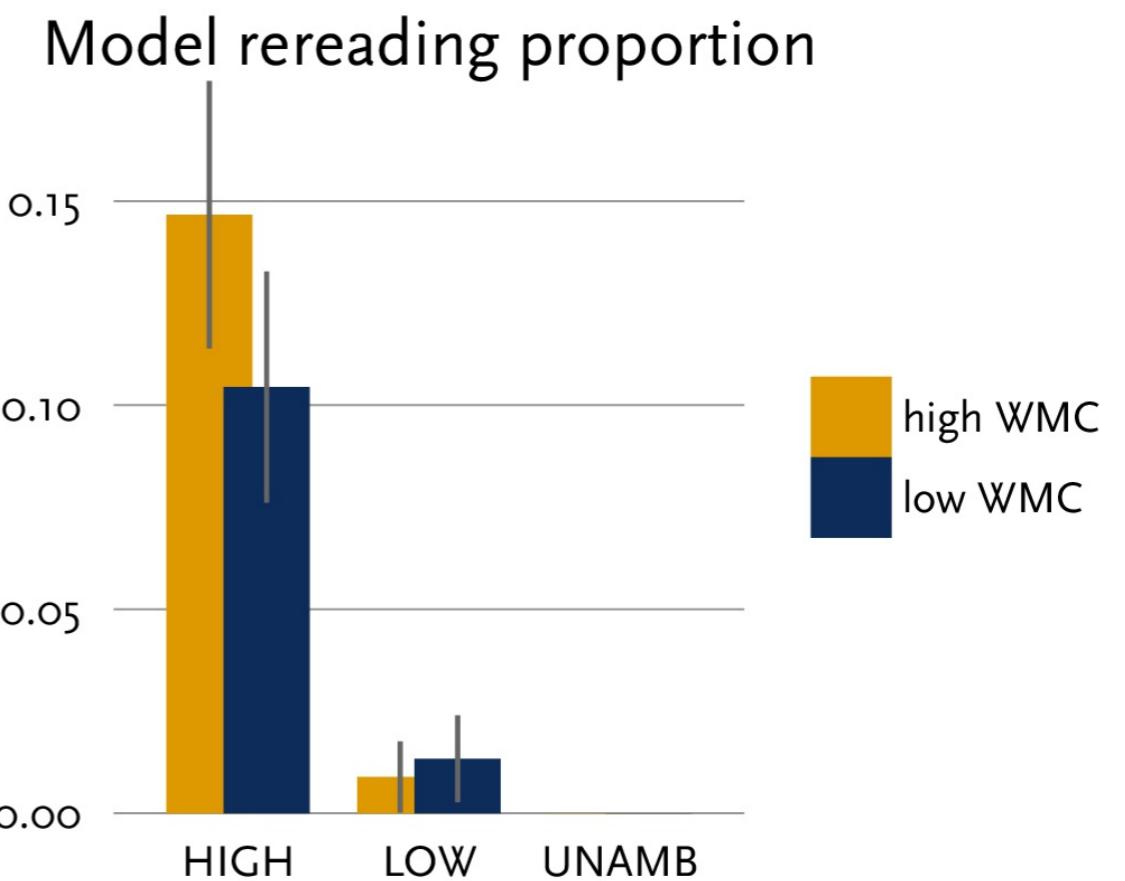
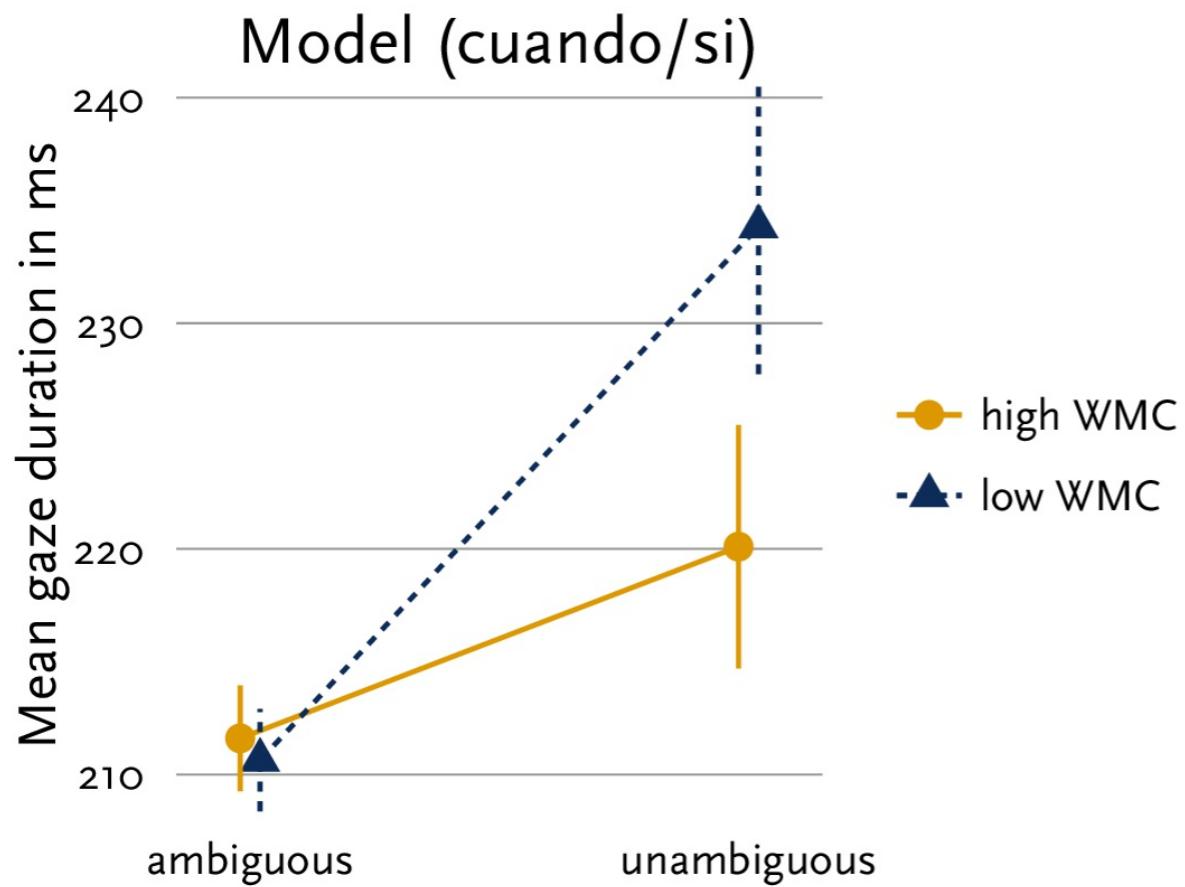
Underspecification Model

The difference to the Time Out mechanism is that, with underspecification, the eye movement proceeds uninterrupted.

Swets et al. (2008):

"According to construal [Frazier & Clifton, 1996], syntactic relations can be divided into primary and secondary types. Whereas **primary relations (roughly, arguments)** are immediately attached [...], **secondary relations (roughly, adjuncts)**, including relative clauses and other modifiers initially are indeterminately 'associated' with the current thematic domain, at which point other information can be called upon to resolve the association into a determinate attachment."

The rate of underspecification is affected by **task demands** like the type of comprehension questions (Swets et al., 2008) and by **working memory capacity** (von der Malsburg & Vasishth, 2012).



Von der Malsburg & Vasishth (2012)

reanalysis for high-capacity readers

El profesor dijo que los alumnos se levantaran del asiento...

The teacher said that the students had to stand up from their seats...

ambiguity
advantage for
low-capacity
readers

a. **cuando los directores entraron en la clase de musica.**

when the directors **came** into the class.

HIGH attachment

b. **cuando los directores entraran en la clase de musica.**

when the directors **come** into the class.

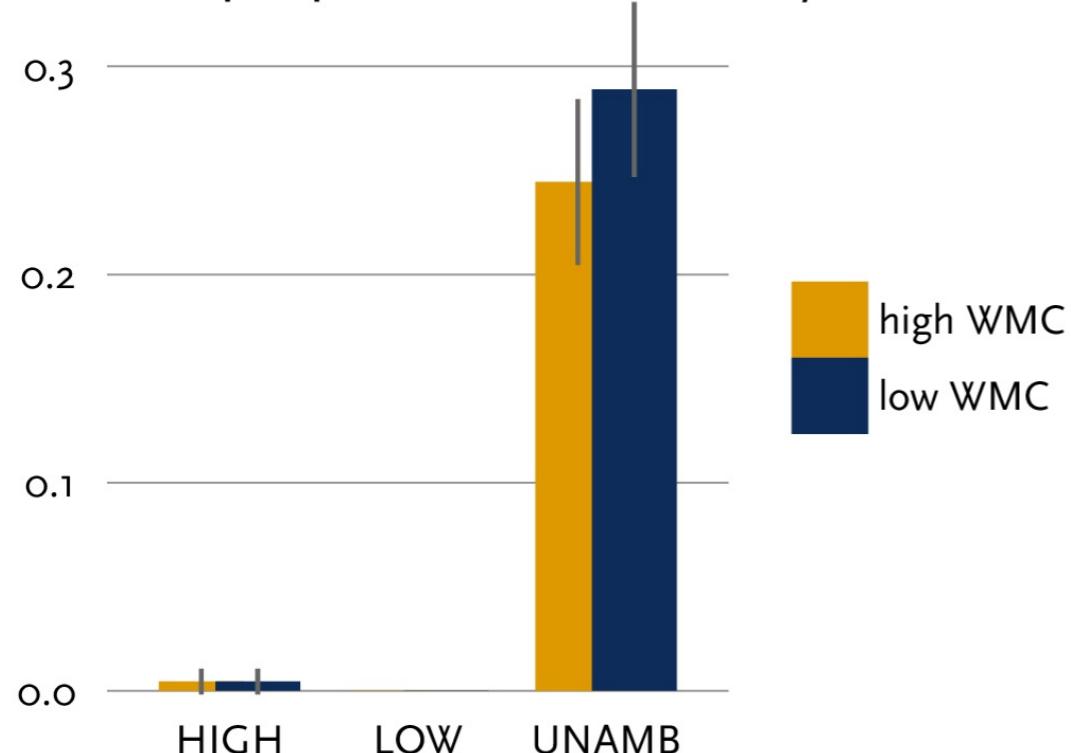
LOW attachment

c. **si los directores entraban en la clase de musica.**

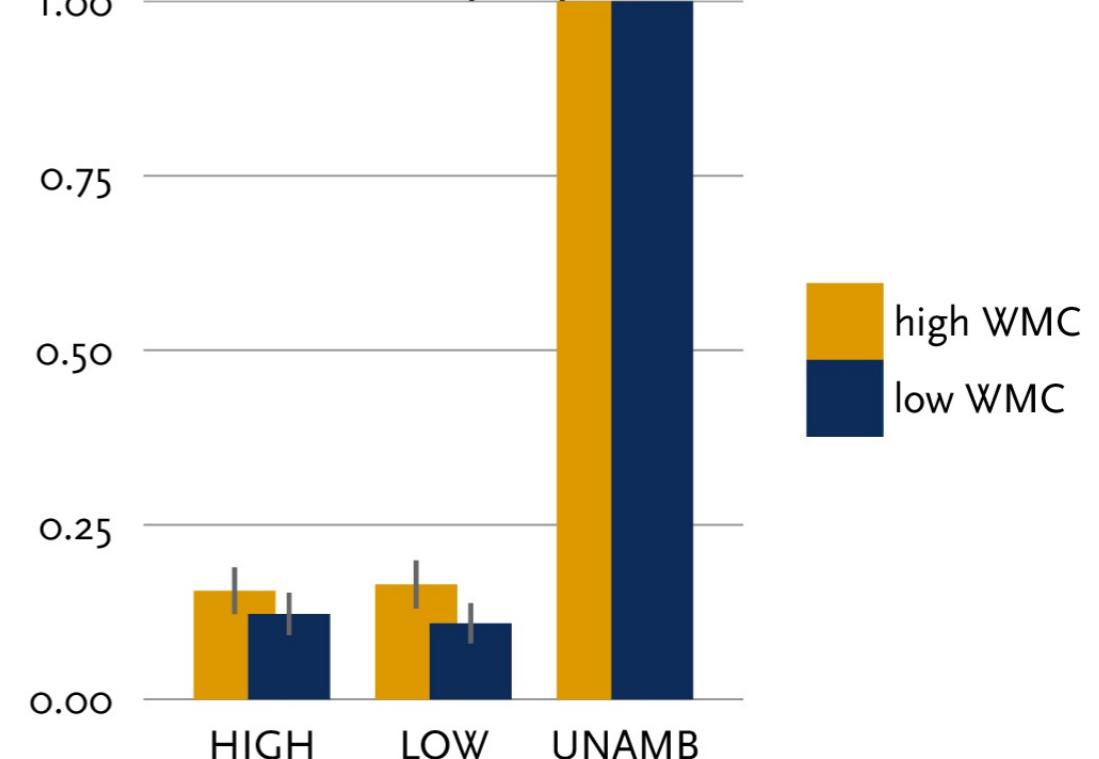
if the directors **come** into the class.

UNAMB (low)

Time out proportion on cuando/si



Attachment proportion



Von der Malsburg & Vasishth (2012)

reanalysis for high-capacity readers

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b. **cuando los directores entraran en la clase de musica.**

when the directors **come** into the class.

LOW attachment

c. **si los directores entraban en la clase de musica.**

if the directors **come** into the class.

UNAMB (low)

Modeling Individual Subjects

Run subjects

10 iterations, 5 subjects: (res 'gg-exp1 10 5)

For each subject, goal activation W is drawn from a normal distribution with mean = 1 and standard deviation = 0.25.

Parameter estimation

```
(setf *paramspace* '(((:lf .2 .4 .1)
                      (:mp 1.5 2 .5)))
(search-param-space-em gg-exp1 5 *paramspace*)
(search-param-space-subjects-em gg-exp1 5 3 *paramspace*)
```

Parsing Module

Parallel retrieval

Two new retrieval buffers
that work in parallel:

GRAMMATICAL>
LEXICAL>

And a context buffer:

CONTEXTUAL>

Chunk creation

STRUCTURAL>
STRUCTURAL2>
STRUCTURAL3>

Parameters

Force-merge merges modified chunk
copies back with their originals.

+grammatical>

ISA

waiting-for-cat

syn-obj

wait-for-NP

+lexical>

ISA

word

lexical-entry

=word

+structural>

ISA

cat

head

spec-of

syn-obj

DP

=word

=grammatical>

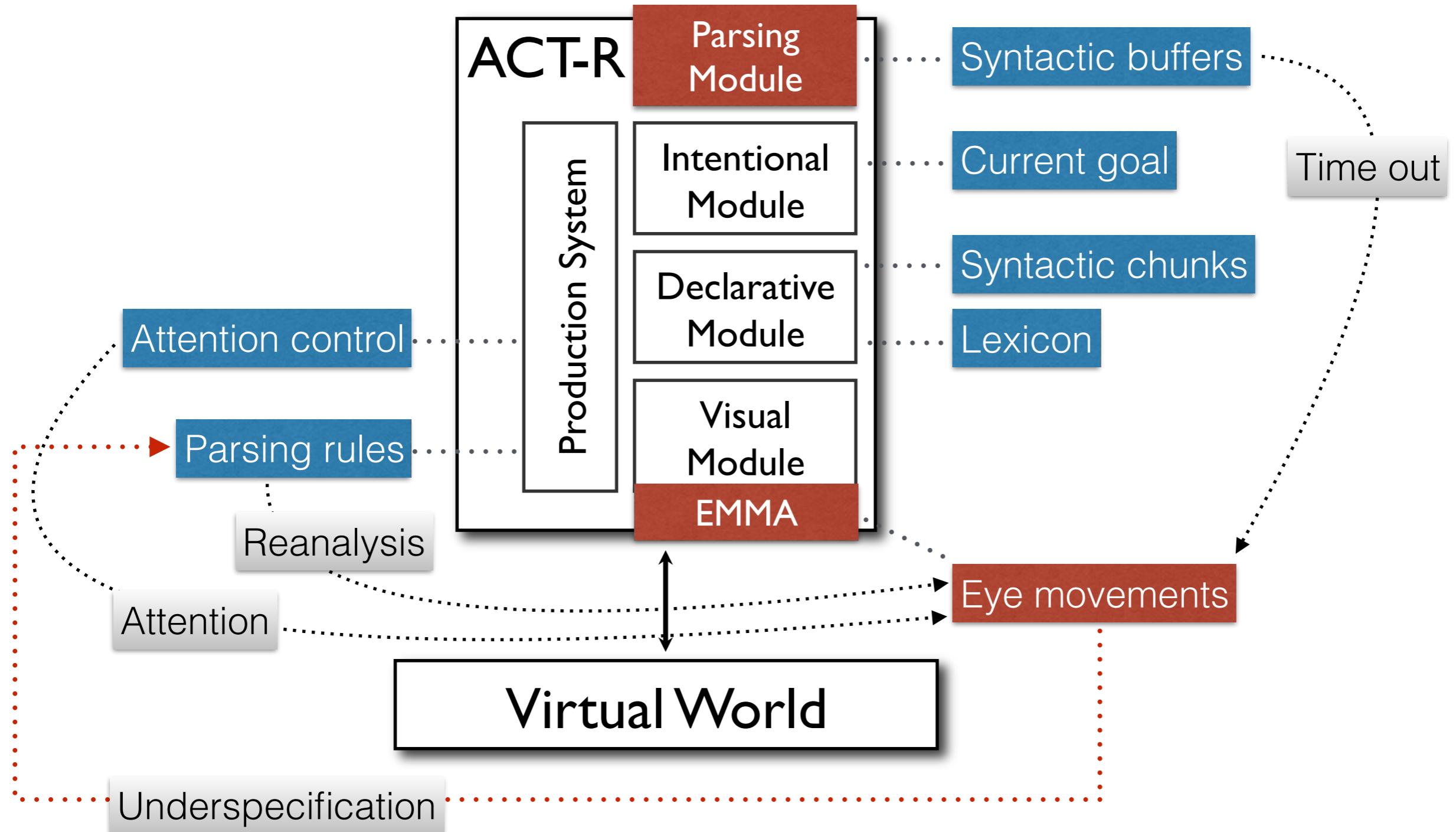
:gram-force-merge T

:gram-lf :lex-lf

:gram-rt :lex-rt

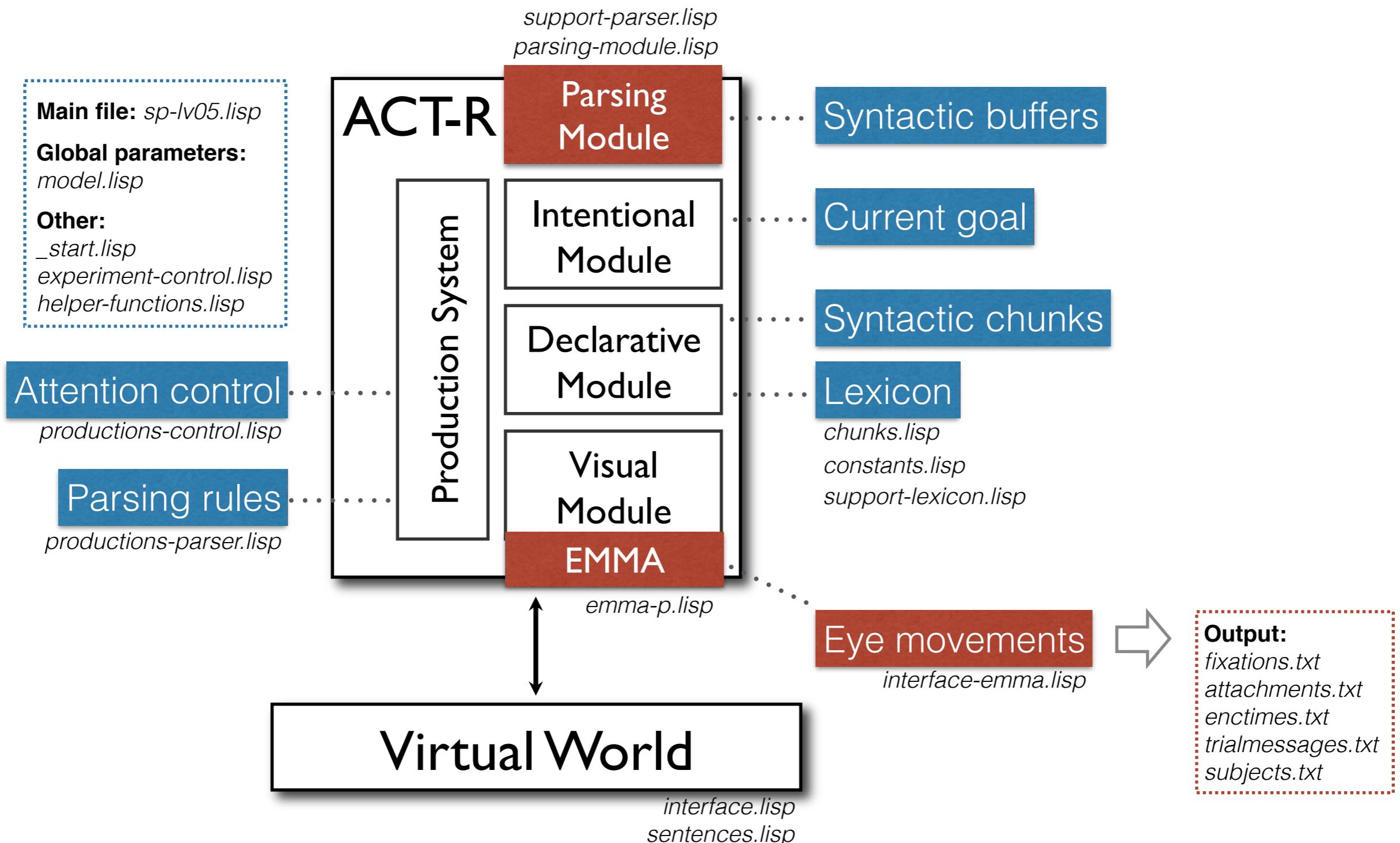
Model Structure

Eye Movement Interaction



Model Structure

File Structure



Function Summary

Run sentence

```
(ps SENTENCE :params PARAMS)    ;; single presentation  
(rps SENTENCE ITERATIONS :params PARAMS)   ;; repeated presentation  
Example: (ps *gg-or* :params '(:lf 0.8))    ;; (params are optional)  
Example: (rps "the dog bit the boy *" 100)  
  
(demo) (demo1) (demo2) (demo3) ;; Run demo sentence
```

Reload model

```
(rl)    ;; Reload model  
(clear-sp)  ;; Reload all files
```

Run experiment (with individual subjects)

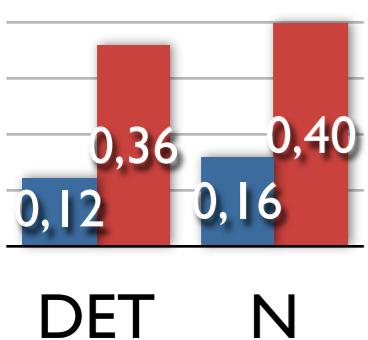
```
(re NAME ITERATIONS :params PARAMS)  
Example: (re 'gg-exp1 50 :params '(:lf 0.8 :mp 2))    ;; (params are optional)  
  
(res NAME ITERATIONS SUBJECTS :params PARAMS)  
Example: (res 'gg-exp1 20 50)
```

Search parameter space

```
(search-param-space-em EXPERIMENT ITERATIONS PSPACE)  
(search-param-space-em EXPERIMENT ITERATIONS SUBJECTS PARAMSPACE)  
Example: (search-param-space-subjects-em gg-exp1 20 50 *paramspace1*)
```

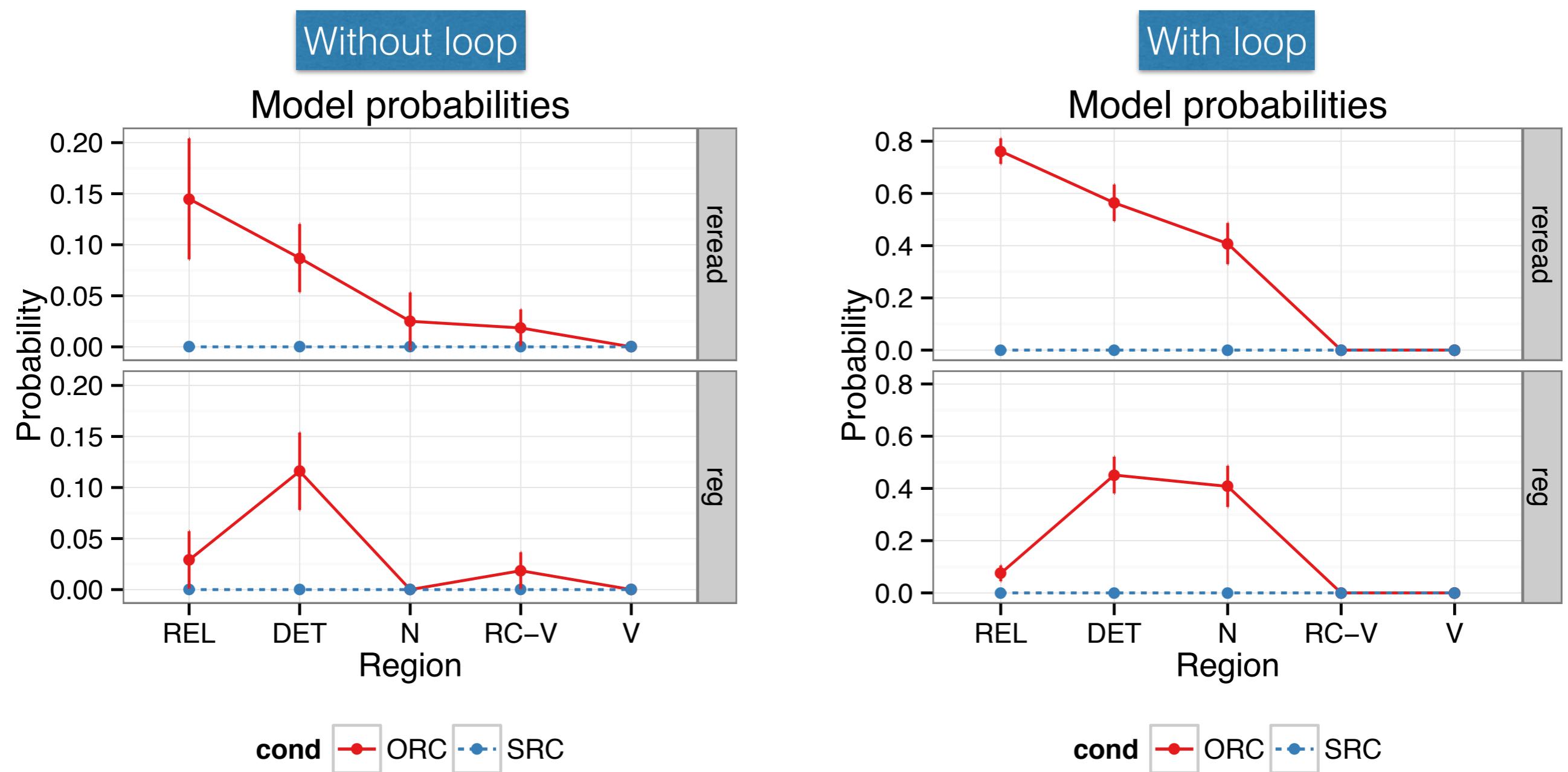
Possible Extension: The Articulatory Loop

Data FP-Regr



Articulatory Loop

Staub (2010) revisited



Articulatory Loop

```
(p subvocalize
  =goal>
    ISA
    state
    em-state
  =visual>
    ISA
    value
  ?vocal>
    preparation free
==>
  =goal>
    em-state
  +vocal>
    ISA
    string
)
(p attend-subvocalized-word ...)
(p lexical-retrieval-request-of-subvocalization ...)
```

Articulatory Loop

Predictions:

- Delayed effects of parsing depend on articulatory loop
- In some cases retrieval not necessary because two words can be integrated in one step
- „Wrap-up effects“ at phrasal boundaries due to clearing the loop (especially when storing more than one word)

Questions:

- How to decide between Time Out and Loop?
- How many words to store? (Decide based on structural expectations?)

→ **Run experiments with blocking subvocalization**

Class Projects

Individual differences in relative clause processing

King & Just (1991); Just & Carpenter (1992)

Locality effects in eye tracking

Grodner & Gibson (2005) Exp. 2 replicated in eye tracking
by Bartek, Lewis, Vasishth & Smith (2011)

Negative polarity intrusion with eye movements

Vasishth, Brüssow, Lewis & Drehhaus (2008)

Scalar implicatures and working memory

Bott & Noveck (2004)