Part 1: Exercise 5b

Load Dataset

The dataset consists of 990 observations and 14 variables.

```
vowel <- read.arff("vowel.arff")
head(vowel, 3)</pre>
```

```
##
     Train or Test Speaker Number
                                     Sex Feature 0 Feature 1 Feature 2 Feature 3
## 1
             Train
                             Andrew Male
                                             -3.639
                                                         0.418
                                                                   -0.670
                                                                              1.779
## 2
             Train
                             Andrew Male
                                             -3.327
                                                         0.496
                                                                   -0.694
                                                                              1.365
## 3
             Train
                             Andrew Male
                                             -2.120
                                                         0.894
                                                                   -1.576
                                                                              0.147
##
     Feature 4 Feature 5 Feature 6 Feature 7 Feature 8 Feature 9 Class
## 1
        -0.168
                    1.627
                              -0.388
                                          0.529
                                                   -0.874
                                                              -0.814
                                                                        hid
## 2
        -0.265
                    1.933
                              -0.363
                                          0.510
                                                   -0.621
                                                              -0.488
                                                                        hId
## 3
        -0.707
                    1.559
                              -0.579
                                          0.676
                                                   -0.809
                                                              -0.049
                                                                        hEd
```

Drop columns

In the first part of our analysis, we will exclude the first 3 features, *Train or Test*, *Speaker Number* and *Sex* as well as the column *Class* and then run K-means clustering algorithm. We will tune k hyper-parameter using methods *elbow* and *silhouette*.

```
vowel_drop <- select(vowel, -1, -2, -3, -14)
head(vowel_drop, 3)</pre>
```

```
##
     Feature 0 Feature 1 Feature 2 Feature 3 Feature 4 Feature 5 Feature 6
## 1
        -3.639
                    0.418
                              -0.670
                                          1.779
                                                    -0.168
                                                                1.627
                                                                          -0.388
## 2
        -3.327
                    0.496
                              -0.694
                                          1.365
                                                    -0.265
                                                                1.933
                                                                          -0.363
        -2.120
                    0.894
                              -1.576
                                          0.147
                                                    -0.707
                                                                1.559
                                                                          -0.579
## 3
##
     Feature 7 Feature 8 Feature 9
## 1
         0.529
                   -0.874
                              -0.814
## 2
         0.510
                   -0.621
                              -0.488
## 3
         0.676
                   -0.809
                              -0.049
```

K Means

K-means algorithm works as presented below:

- 1. Choose groups in the feature plan randomly
- 2. Minimize the distance between the cluster center and the different observations (centroid). It results in groups with observations
- 3. Shift the initial centroid to the mean of the coordinates within a group.

- 4. Minimize the distance according to the new centroids. New boundaries are created. Thus, observations will move from one group to another
- 5. Repeat until no observation changes groups

Since M-means is based on distances of among data points, there few different measures it take into account. For example, *Euclidean* distance is the most common method, though we could also use *Manhattan* and *Minlowski* distances as well. Below, present the mathematical formulation of *Euclidean* distance.

$$distance(x,y) = \sum_{i}^{n} (x_i - y_i)^2$$
(1)

Optimal K

One technique to choose the best k is called the *Elbow* method. This method uses within-group homogeneity or within-group heterogeneity to evaluate the variability. Another approach is called *Silhouette*. We will measure within groups sum of squares(variance) and the quality to clusters to determine the optimal value of k. For this, we will install the package *factoextra*.

Elbow

The elbow method is a method used to determine the number of clusters in a data set. It defines clusters in such a way that the total intra cluster variation (total within-cluster variation or total within-cluster sum of square) is minimized. We can formulate it as:

$$\min \sum_{k=1}^{k} W(C_k) \tag{2}$$

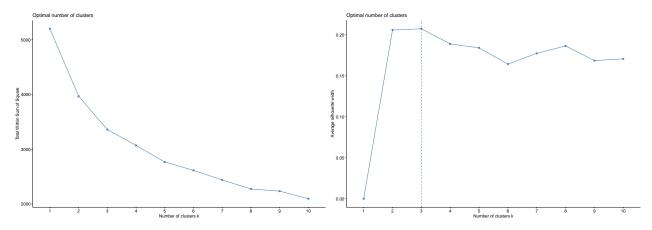
where C_k is the k^{th} cluster and $W(C_k)$ is the within-cluster variation. The total within-cluster sum of square measures the compactness of the clustering and we want it to be as *small* as possible

Silhouette

The average silhouette method measures the quality of a clustering. It determines how well each object lies within its cluster. A high average silhouette width indicates a good clustering. The average silhouette method computes the average silhouette of observations for different values of k. The optimal number of clusters k is the one that maximizes the average silhouette over a range of possible values for k.

Both of the above process can be computed by the following code snippet.

```
set.seed(123)
fviz_nbclust(vowel_drop, kmeans, method = "wss")
fviz_nbclust(vowel_drop, kmeans, method = "silhouette")
```



We see the best value of k for the given dataset is 3.

Add Class attribute

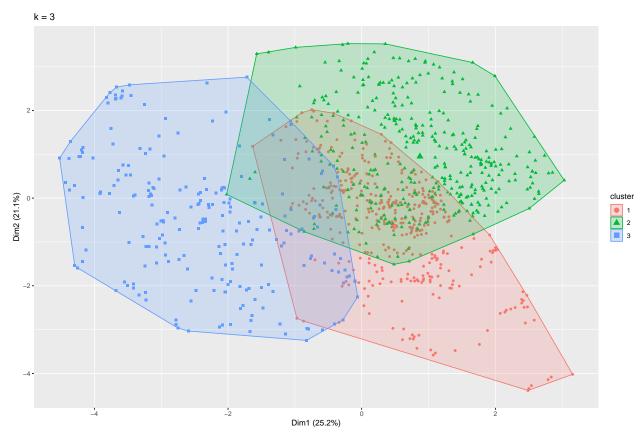
Now, we will add the class attribute to the dataset $vowel_drop$ and will repeat the same process of previous section.

```
vowel_drop_2 <- select(vowel, -1, -2, -3)
unique(vowel_drop_2$Class)</pre>
```

[1] hid hId hEd hAd hYd had hOd hod hUd hud hed ## Levels: hid hId hEd hAd hYd had hOd hod hUd hud hed

We observe that the levels of the column *Class* are 11. Though, it appears that there are duplicates in classes cause of typos, case-sensitivity etc. The unique classes in the dataset are 6. We have found previously that the optimal value of k is 3. We will plot the clusters.

```
k3 <- kmeans(vowel_drop, centers = 3, nstart = 25)
fviz_cluster(k3, geom = "point", data = vowel_drop) + ggtitle("k = 3")</pre>
```



The clusters overlap quite a bit cause of the nature of the dataset. Especially the red and green clusters appear to be misplaced. It does not seem that there is a good correlation among true-clusters and the 3 clusters of k-means.

Classification

In this section we will try to address the same problem from a different perspective. We will try two classifiers (Naive Bayes, SVM) and will measure their performace.

Naive Bayes

##

hid 76 10

The fundamental Naive Bayes assumption is that each feature is independent and equal with each other.

```
library(e1071)
nb_model = naiveBayes(as.factor(Class) ~., data=vowel_drop_2)

modelPred <- predict(nb_model, vowel_drop_2)
cMatrix <- table(modelPred, vowel_drop_2$Class)
confusionMatrix(cMatrix)

## Confusion Matrix and Statistics
##
##
## modelPred hid hId hEd hAd hYd had hOd hod hUd hud hed</pre>
```

0

0

```
##
         hId
                   58
                        3
                             0
                                 0
                                                           0
                                                   1
##
         hEd
                0
                    6
                       78
                             8
                                 0
                                      0
                                          0
                                              0
                                                   0
                                                       0
                                                           0
##
         hAd
                0
                        6
                            67
                                 0
                                      7
                                          0
                                              0
                                                           0
##
         hYd
                0
                    0
                        0
                             3
                                71
                                    19
                                         16
                                              0
                                                  0
                                                       0
                                                           8
##
         had
                0
                    0
                         0
                             6
                                 5
                                    49
                                          0
                                              0
                                                  0
                                                       0
                                                          13
##
         h0d
                0
                    0
                        0
                                12
                                      0
                                         56
                                             12
                             0
                                                 11
                                                       0
                                                           1
##
                                 0
                                      0
                                          8
                                             70
                                                  12
                                                           0
         hod
                0
                    0
                         0
                             0
                                                       1
                                                 52
         hUd
                                          7
##
                0
                    0
                         0
                             0
                                 1
                                      1
                                              6
                                                      13
                                                           0
##
         hud
               11
                   12
                         1
                             0
                                 0
                                      0
                                          0
                                              2
                                                 10
                                                      66
                                                           4
##
                                    14
                                                       2
         hed
                0
                         2
                                 1
                                          0
                                              0
                                                          64
##
   Overall Statistics
##
##
                   Accuracy: 0.7141
##
                     95% CI: (0.6849, 0.7421)
##
       No Information Rate: 0.0909
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa: 0.6856
##
##
    Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                          Class: hid Class: hId Class: hEd Class: hAd Class: hYd
## Sensitivity
                             0.84444
                                         0.64444
                                                     0.86667
                                                                 0.74444
                                                                             0.78889
## Specificity
                             0.98778
                                         0.98111
                                                     0.98444
                                                                 0.98556
                                                                             0.94889
  Pos Pred Value
                             0.87356
                                                     0.84783
                                         0.77333
                                                                 0.83750
                                                                             0.60684
## Neg Pred Value
                             0.98450
                                         0.96503
                                                     0.98664
                                                                 0.97473
                                                                             0.97824
## Prevalence
                             0.09091
                                         0.09091
                                                     0.09091
                                                                 0.09091
                                                                             0.09091
## Detection Rate
                             0.07677
                                         0.05859
                                                     0.07879
                                                                 0.06768
                                                                             0.07172
## Detection Prevalence
                             0.08788
                                         0.07576
                                                     0.09293
                                                                 0.08081
                                                                             0.11818
## Balanced Accuracy
                             0.91611
                                         0.81278
                                                     0.92556
                                                                 0.86500
                                                                             0.86889
##
                          Class: had Class: hOd Class: hUd Class: hUd Class: hud
## Sensitivity
                             0.54444
                                         0.62222
                                                     0.77778
                                                                 0.57778
                                                                             0.73333
                             0.97333
                                         0.96000
                                                     0.97667
## Specificity
                                                                 0.96889
                                                                             0.95556
## Pos Pred Value
                             0.67123
                                         0.60870
                                                     0.76923
                                                                 0.65000
                                                                             0.62264
## Neg Pred Value
                             0.95529
                                         0.96214
                                                     0.97775
                                                                 0.95824
                                                                             0.97285
## Prevalence
                             0.09091
                                         0.09091
                                                     0.09091
                                                                 0.09091
                                                                             0.09091
## Detection Rate
                             0.04949
                                         0.05657
                                                     0.07071
                                                                 0.05253
                                                                             0.06667
## Detection Prevalence
                                         0.09293
                                                                 0.08081
                             0.07374
                                                     0.09192
                                                                             0.10707
## Balanced Accuracy
                             0.75889
                                         0.79111
                                                     0.87722
                                                                 0.77333
                                                                             0.84444
                          Class: hed
## Sensitivity
                             0.71111
## Specificity
                             0.96333
## Pos Pred Value
                             0.65979
## Neg Pred Value
                             0.97088
## Prevalence
                             0.09091
## Detection Rate
                             0.06465
## Detection Prevalence
                             0.09798
## Balanced Accuracy
                             0.83722
```

The overall accuracy of Naive Bayes classifier is 71.4%

Support Vector Machines (SVM)

Detection Rate

We will use SVM with linear kernel and compare its accuracy to Naive Bayes.

```
svmfit = svm(as.factor(Class) ~ ., data = vowel_drop_2, kernel = "linear", cost = 10, scale = FALSE)
modelPred <- predict(svmfit, vowel_drop_2)</pre>
cMatrix <- table(modelPred, vowel_drop_2$Class)</pre>
confusionMatrix(cMatrix)
## Confusion Matrix and Statistics
##
##
##
  modelPred hid hId hEd hAd hYd had hOd hod hUd hud hed
##
         hid
              89
                    2
                        1
                             0
                                 0
                                     0
                                          3
                                              0
                                                  0
                                                       0
                                                           0
##
         hId
                   84
                       10
                                 0
                                          0
                                              0
                                                           0
                1
                                     1
         hEd
                    4
                       77
                                 0
                                              0
                                                  0
                                                       0
                                                           0
##
                0
                             2
                                     3
                                         0
##
         hAd
               0
                    0
                        2
                           80
                                 0
                                     7
                                          0
                                              0
                                                  0
                                                       0
                                                           2
##
         hYd
               0
                    0
                        0
                            0
                                67
                                    13
                                          4
                                              0
                                                       0
                                                           0
                                                  1
                             8
                                    63
                                              0
                                                           7
##
         had
               0
                    0
                        0
                                15
                                         0
                                                       0
                                                  2
##
         h0d
               0
                    0
                        0
                                 7
                                     0
                                              5
                             0
                                        81
                                                       0
                                                           4
                                 0
                                                  7
##
         hod
               0
                    0
                        0
                            0
                                     0
                                         0
                                             76
                                                      2
                                                           0
##
         hUd
               0
                        0
                                 0
                                     0
                                         0
                                              9
                                                 78
                                                       3
                    0
                             0
                                                           1
##
         hud
               0
                    0
                        0
                             0
                                 0
                                     0
                                         0
                                              0
                                                  1
                                                     85
                                                           0
                                          2
                                                         76
##
         hed
                0
                    0
                        0
                             0
                                 1
                                     3
                                              0
                                                  1
                                                       0
##
## Overall Statistics
##
##
                   Accuracy : 0.8646
##
                     95% CI: (0.8417, 0.8854)
##
       No Information Rate: 0.0909
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa: 0.8511
##
##
    Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                         Class: hid Class: hId Class: hEd Class: hAd Class: hYd
## Sensitivity
                             0.98889
                                        0.93333
                                                    0.85556
                                                                0.88889
                                                                            0.74444
## Specificity
                             0.99333
                                        0.98667
                                                    0.99000
                                                                0.98778
                                                                            0.98000
## Pos Pred Value
                             0.93684
                                        0.87500
                                                    0.89535
                                                                0.87912
                                                                            0.78824
## Neg Pred Value
                             0.99888
                                        0.99329
                                                    0.98562
                                                                0.98888
                                                                            0.97459
## Prevalence
                             0.09091
                                        0.09091
                                                    0.09091
                                                                0.09091
                                                                            0.09091
## Detection Rate
                             0.08990
                                        0.08485
                                                    0.07778
                                                                0.08081
                                                                            0.06768
## Detection Prevalence
                             0.09596
                                        0.09697
                                                    0.08687
                                                                0.09192
                                                                            0.08586
## Balanced Accuracy
                             0.99111
                                         0.96000
                                                    0.92278
                                                                0.93833
                                                                            0.86222
##
                         Class: had Class: hOd Class: hUd Class: hUd Class: hud
## Sensitivity
                             0.70000
                                        0.90000
                                                    0.84444
                                                                0.86667
                                                                            0.94444
## Specificity
                             0.96667
                                        0.98000
                                                    0.99000
                                                                0.98556
                                                                            0.99889
## Pos Pred Value
                             0.67742
                                        0.81818
                                                    0.89412
                                                                0.85714
                                                                            0.98837
## Neg Pred Value
                             0.96990
                                        0.98990
                                                    0.98453
                                                                0.98665
                                                                            0.99447
## Prevalence
                                        0.09091
                             0.09091
                                                    0.09091
                                                                0.09091
                                                                            0.09091
```

0.07677

0.07879

0.08586

0.08182

0.06364

```
## Detection Prevalence
                            0.09394
                                       0.10000
                                                   0.08586
                                                              0.09192
                                                                          0.08687
## Balanced Accuracy
                            0.83333
                                       0.94000
                                                   0.91722
                                                              0.92611
                                                                          0.97167
##
                         Class: hed
## Sensitivity
                            0.84444
## Specificity
                            0.99222
## Pos Pred Value
                            0.91566
## Neg Pred Value
                            0.98456
## Prevalence
                            0.09091
## Detection Rate
                            0.07677
## Detection Prevalence
                            0.08384
## Balanced Accuracy
                            0.91833
```

Accuracy is 86.4% which is better than Naive Bayes.

Add first 3 features

In the first section we excluded 3 features of our analysis. Now we will see whether they could impact our analysis.

```
unique(vowel$`Train or Test`)
## [1] Train Test
## Levels: Train Test
unique(vowel$`Speaker Number`)
   [1] Andrew Bill
                      David Mark
                                     Jo
                                            Kate
                                                    Penny Rose
                                                                  Mike
                                                                          Nick
               \mathtt{Tim}
## [11] Rich
                      Sarah
                              Sue
                                     Wendy
## 15 Levels: Andrew Bill David Mark Jo Kate Penny Rose Mike Nick Rich ... Wendy
unique(vowel$Sex)
## [1] Male
              Female
## Levels: Male Female
```

References

kmeans [@https://towardsdatascience.com/k-means-clustering-algorithm-applications-evaluation-methods-and-drawbacks-aa03e644b48a/].

```
naive bayes [@https://en.wikipedia.org/wiki/Support-vector_machine].
```

svm [@https://scikit-learn.org/stable/modules/naive_bayes.html].