

# Price Discrimination Simulator

Xiaoqian Ma (xm2146)

Zhicheng Wan (zw2275)

Zhou Zhou (zz2181)

# Project Description

A simulation engine for pricing discrimination



# Related Work

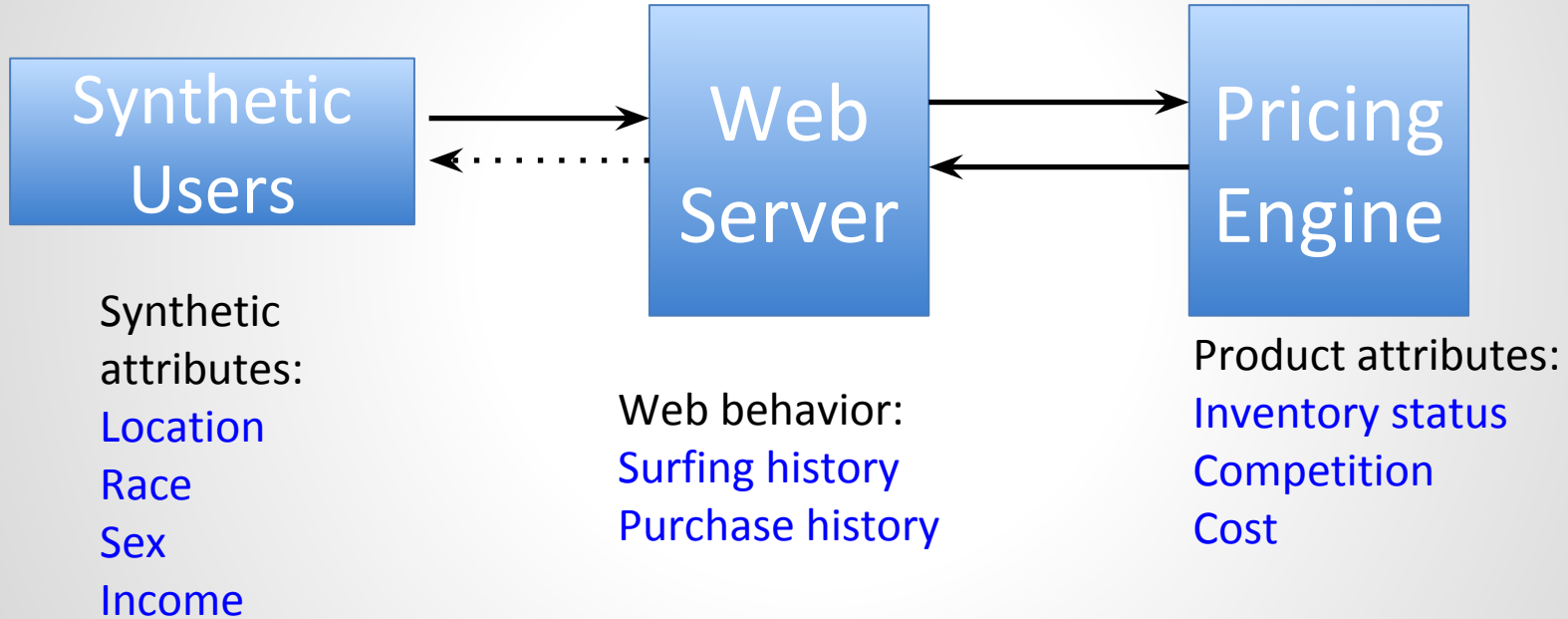
Mikians et al. [2]

- detection system as a watchdog

Hannak et al. [3]

- probed the existence of pricing steering

# Design



# Synthetic Users



40000 zip code

40000 queries to Census.gov

Retrieved each record with 16 attributes

Real probability density function used

# Synthetic Users



[1] = 'White, Not Hispanic or Latino'

[2] = 'Hispanic or Latino'

[3] = 'Black or African American'

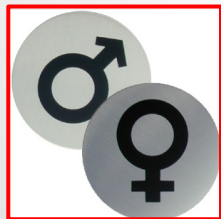
[4] = 'American Indian and Alaska Native'

[5] = 'Asian'

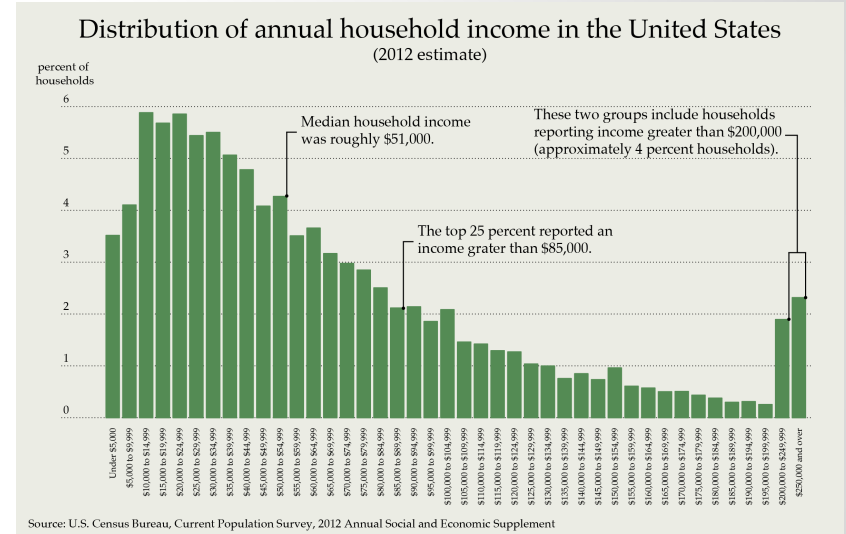
[6] = 'Native Hawaiian and Other Pacific Islander'

[7] = 'Some Other Race'

[8] = 'Two or More Races'



# Synthetic Users



A vector of 4 random seeds ----> A synthetic user

Tools: Flask, Heroku, MySQL, JSON

# Middle Layer

## Application Server

- Generate user: get new data from user pool
- Simulate: get the prices from pricing engine

## Control Panel

- Adjust pricing coefficient

Development tools: django, sqlsite



# Pricing Discrimination Simulator

Cost: \$150 CompetitorPrice: \$175

## User 29

income:236106.0 sex:0 race:1 zipcode:89423 hasVisited:1  
isVisitedPriceHighOrLow:1 hasPurchased:0  
isPurchasedPriceHighOrLow:1 stock:41

Price: \$156.0

## User 30

income:8674.0 sex:1 race:1 zipcode:17603 hasVisited:0  
isVisitedPriceHighOrLow:0 hasPurchased:1  
isPurchasedPriceHighOrLow:1 stock:200

Price: \$274.0

## User 31

income:4935.0 sex:1 race:1 zipcode:95838 hasVisited:1  
isVisitedPriceHighOrLow:1 hasPurchased:1  
isPurchasedPriceHighOrLow:1 stock:197

Price: \$285.0

## User 32

income:23308.0 sex:1 race:2 zipcode:29651 hasVisited:0  
isVisitedPriceHighOrLow:0 hasPurchased:0  
isPurchasedPriceHighOrLow:1 stock:33

Price: \$208.0

# Pricing Coefficients Adjustment

Household Income(%): 10



Race(%): 52



Sex(%): 28



Zipcode(%): 81



Has Visited(%): 45



Is Visited High or Low(%): 68



Has Purchased(%): 34



Is Purchased High or Low(%): 62



Cost(%): 37



Competitor Price(%): 10



Stock(%): 79



save

# Middle Layer(to be done)

## Application Server

- Custom input user data
- Access control: administrator

## Control Panel

- Choose industry category and price model
- Correlation analysis

# Pricing Engine - Communication

Two Set of APIs:

- System Configuration
- Specific Product Pricing Request

JSON Response:

- Client ID
- Price

```
{  
  price: 100,  
  id: 123456  
}
```

# Pricing Engine - Parameters

## Domestic

Location  
(Zipcode)

## Shopping Behavior

Browsing History  
(hasHistory,  
ProductPricingRange)

Purchase History  
(hasHistory,  
ProductPricingRange)

## Business

Cost  
Inventory  
Level

Competition  
(Competitor's Price)

# Pricing Engine - Algorithm

Price =

LocationCoefficient(ZipCode)

\*BrowsingHistoryCoefficient(hasVisited,isVisitedPriceHighOrLow)

\*PurchaseHistoryCoefficient(hasPurchased,isPurchasedPriceHighOrLow)

\*CompetitiveCoefficient(competitorPrice, stock)

\*Cost

# Pricing Engine - Algorithm

## **LocationCoefficient(ZipCode)**

For each of the location, collect real online stores pricing statistics and use machine learning approach to calculate coefficient for every valid zip code

## **Online Store Explored**

- Currently available: Best Buy, Amazon, Ebay
- Not available: Home Depot, Staples
- Possible candidate: Hotels.com, Expedia, Cheaptickets, Orbitz

# Pricing Engine - Algorithm

**BrowsingHistoryCoefficient(hasVisited,isVisitedPriceHighOrLow)**

**PurchaseHistoryCoefficient(hasPurchased,isPurchasedPriceHighOrLow)**

Users are classified into High/Low categories according to the price of the products they have browsed/purchased

Price is inflated with a small markup for high valued customers

Initial pricing for first time visitor/buyer is also possible



# Pricing Engine - Algorithm

**CompetitiveCoefficient**  
**(competitorPrice, stock)**

Competitive Algorithms for Online Pricing<sup>1</sup>

Adapted from IEOR research

Taking inventory level, highest price a customer is willing to pay(capped by the competitor's price)

Adjust Price with the listed Algorithm

1. Zhang, Yong, Yuxin Wang, Francis Y. L. Chin, and Hing-Fung Ting. "Competitive Algorithms For Online Pricing." Discrete Mathematics, Algorithms and Applications 04.02 (2012): 1250015. Web.

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## Algorithm 1. Pricing

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```
1: Let  $y_j$  be the largest amount that user  $i$  is willing to buy given price  $2^j$  and  
   satisfying  $y_j \leq m$ .  
2: Let  $k = \arg \max_j y_j \cdot 2^j$   
3: if  $x_k \neq 0$  then  
4:   Set unit price to be  $p_i = 2^k$ .  
5:   Assign  $m_i = \min\{x_k, y_k\}$  items to user  $i$ .  
6:   Modify Available Amount of Items.  
7: else  $x_k = 0$   
8:   Let  $k' = \arg \max_{j > k} y_j \cdot 2^j$  such that  $x_{k'} > 0$   
9:   Set the unit price to be  $p_i = 2^{k'}$ .  
10:  Assign  $m_i = \min\{x_{k'}, y_{k'}\}$  items to user  $i$ .  
11:  Modify Available Amount of Items.  
12: end if
```

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## Algorithm 2. Modify Available Amount of Items: ( $p_i = 2^k$ and $m_i = \min\{x_k, y_k\}$ )

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```
1: if  $m_i = x_k$  then  
2:    $x_j = 0$  for  $0 \leq j \leq k$   
3: else  $m_i = y_k$   
4:   Let  $\ell = \arg \max_j x_k - x_j \geq y_k$ .  
5:   for  $j = \ell + 1$  to  $k$  do  
6:      $x_j = x_k - y_k$   
7:   end for  
8: end if
```

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# What's next?

April 6<sup>th</sup>: Progress report

April 13<sup>th</sup>: Application server analysis module refined

April 20<sup>th</sup>: Pricing engine based on theoretical models

April 24<sup>th</sup>: Pricing engine based on machine learning, data should be gathered

April 27<sup>th</sup>: Pricing engine based on machine learning, models should be trained

Before Final: Synthetic user data, application server to be further refined; UI refined.

Thank you!