

Q3. (a)

Given system,

```
%Create VCM Plant Model
%Note: This model is from "Design and testing of track-following
%controllers for dual-state servo systems with PZT actuated suspensions" by
%Li and Horowitz, Microsystem Technologies, 2002
Gv = 10; %DC Gain
Gv1 = tf((2*pi*135)^2,[1 2*0.1*2*pi*135 (2*pi*135)^2]);
Gv2 = tf((2*pi*5500)^2,[1 2*0.03*2*pi*5500 (2*pi*5500)^2]);
Gv3 = tf((2*pi*8640)^2,[1 2*0.05*2*pi*8640 (2*pi*8640)^2]);
Gv4 = 7300^2/7650^2*tf([1 2*.015*2*pi*7650 (2*pi*7650)^2],[1 2*.03*2*pi*7300 (2*pi*7300)^2]);
VCM = Gv*Gv1*Gv2*Gv3*Gv4;

Gp = 0.1; %DC gain
Gp1 = tf((2*pi*8460)^2,[1 2*0.01*2*pi*8460 (2*pi*8460)^2]);
Gp2 = 5500^2/5650^2*tf([1 2*.03*2*pi*5650 (2*pi*5650)^2],[1 2*.03*2*pi*5500 (2*pi*5500)^2]);
Gp3 = 7300^2/7650^2*tf([1 2*.015*2*pi*7650 (2*pi*7650)^2],[1 2*.03*2*pi*7300 (2*pi*7300)^2]);
Gp4 = 8070^2/8250^2*tf([1 2*.02*2*pi*8250 (2*pi*8250)^2],[1 2*.015*2*pi*8070 (2*pi*8070)^2]);
Gp5 = 10650^2/10530^2*tf([1 2*.015*2*pi*10530 (2*pi*10530)^2],[1 2*.01*2*pi*10650 (2*pi*10650)^2]);
PZT = Gp*Gp1*Gp2*Gp3*Gp4*Gp5;
```

Create a DISO model

```
G = [VCM,PZT]
```

G =

From input 1 to output:

$$2.306e25 \, s^2 + 3.325e28 \, s + 5.327e34$$

$$\frac{2.306e25 \, s^2 + 3.325e28 \, s + 5.327e34}{s^8 + 1.042e04 \, s^7 + 6.279e09 \, s^6 + 4.088e13 \, s^5 + 1.23e19 \, s^4 + 3.829e22 \, s^3 + 7.419e27 \, s^2 + 1.282e30 \, s + 5.327e33}$$

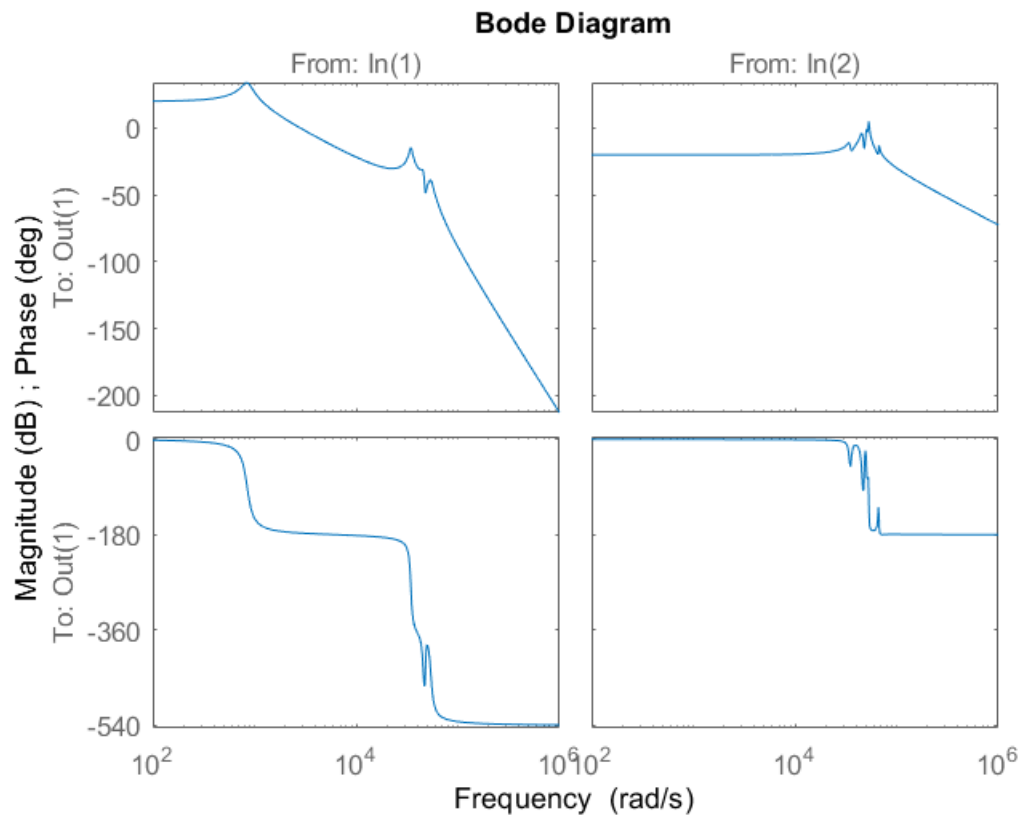
From input 2 to output:

$$\frac{2.386e08 \, s^8 + 1.821e12 \, s^7 + 2.543e18 \, s^6 + 1.453e22 \, s^5 + 9.549e27 \, s^4 + 3.65e31 \, s^3 + 1.497e37 \, s^2 + 2.893e40 \, s + 8.173e45}{s^{10} + 8748 \, s^9 + 1.32e10 \, s^8 + 9.411e13 \, s^7 + 6.675e19 \, s^6 + 3.637e23 \, s^5 + 1.616e29 \, s^4 + 5.985e32 \, s^3 + 1.868e38 \, s^2 + 3.523e41 \, s + 8.173e46}$$

Continuous-time transfer function.

Bode plot of the diso model

```
bode(G)
```



Q3. (b)

Initialize transfer function and the weight parameters as done in Q2 (a), (c)

```
s = tf('s');
Wu_V = 1/100;
Wu_P = 1/10;
Wu = [Wu_V 0; 0 Wu_P];
GAM = 10;
BW = 3000*2*pi;
BW_step = 25;
M = 10^(6/20);
A = 1000;
```

Optimization loop

```
while GAM>1
    Wp = (s/sqrt(M)+BW)^2/(s+BW/sqrt(A))^2;
    Wt = makeweight(0.5,5*BW,1000);
    [K,CL,GAM,info] = mixsyn(G,Wp,Wu,Wt);
    BW = BW - BW_step;
end
```

Gamma Value

GAM

GAM = 0.9985

Sensitivity function

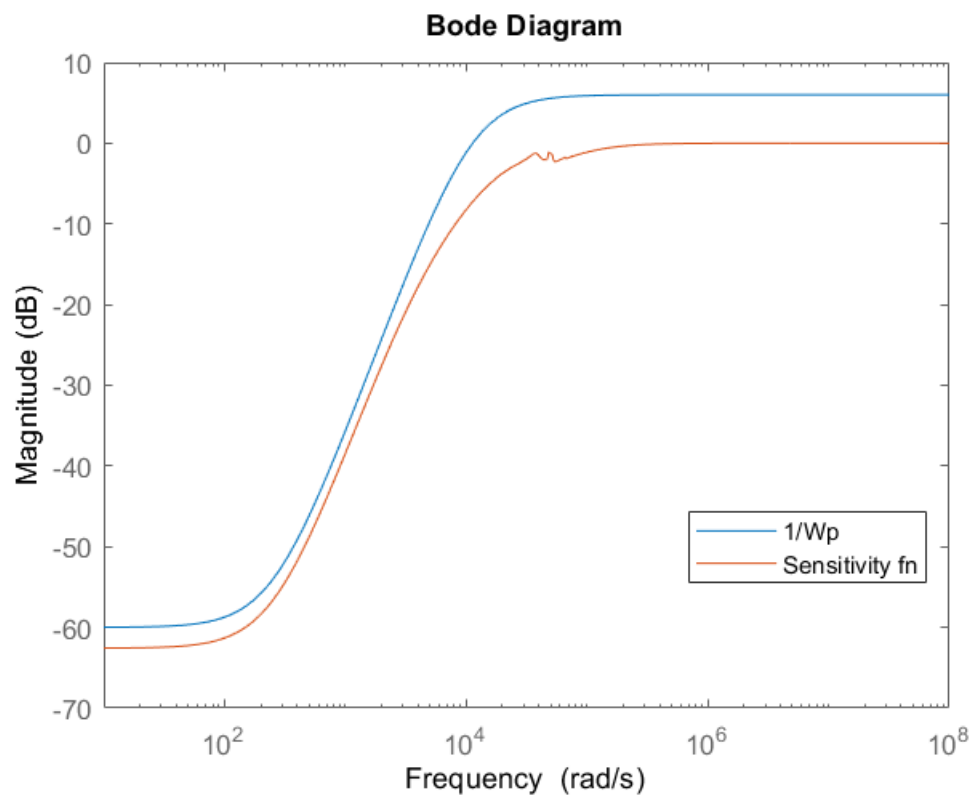
```
S = inv(eye(1)-G*K);
```

Supplementary sensitivity function

```
T = 1-S;
```

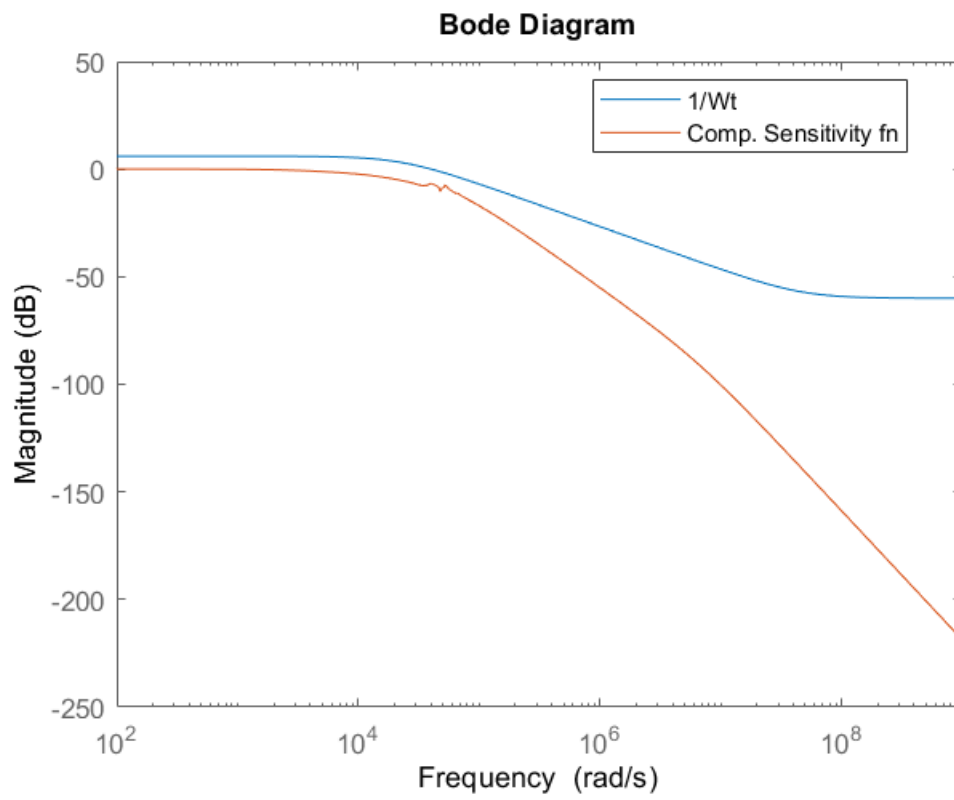
Bode plot of sensitivity function

```
bodemag(1/Wp,S)  
legend('1/Wp','Sensitivity fn','Location','best')
```



Bode plot of complementary sensitivity function

```
bodemag(1/Wt,T)  
legend('1/Wt','Comp. Sensitivity fn','Location','best')
```



Bode magnitude plot of $W_u \cdot K \cdot S$

```
bodemag(Wu*K*S)
```

