$y = \alpha u + (\alpha d)$ u = y - d - 0 α

 $C\left(x-\left(y+n\right)\right)-Q\left(M\left(y+n\right)-u\right)=u$ $C\left(x-y-n\right)-Q\left(My+Mn+d-y\right)=y-d$ $Cx-\left(y-Cn-QMy-QMn-Qd+Qy-y-d\right)$ $Cx-\left(y-Cn-QMy-QMn-Qd+Qy-y-d\right)$

a) To find Transfer function, $T = \frac{y}{R}$ assume d = 0, n = 0,

(r - cy - QMy + Qy = y (r - Cy - QMy + y (r - Cy - QMy + Qy = y (r - Cy - QMy + Qy = y (r - Cy - Q

For sensitivity function $S = \frac{E}{R}$ $\frac{J}{SL} = \frac{(Ur)}{I+UL+QMU-Q} = \frac{Q-QMU-I}{I+UL+QMU-Q} = \frac{E}{R}$

Collaborated with Ruchita Sinha Aditya Rathi b) Input sensitivity quaction 1, asune, n=0, 2=0 - Cy - aMy - ad + ay = 4 -d d(I+Q d(I-Q)= y(1+C+QM-Q) J I I Chr. + AMbr. - A y = br-Qbr
I+Cbr+QMbr-Q when Q=I, M=Cr 生一〇 Q acts as a fitter to account for the imperfections in the block M (to remove the disturbance).

Assume states
$$SN_1$$
, N_2S to be $\{0,0\}$

$$= N_1 = 0$$

$$N_1 = 0$$

$$N_2 = 0 = N_1$$

$$\Rightarrow N_2 = \frac{1}{2} \sin N_1 = \frac{1}{2} \sin N_2$$

$$\Rightarrow N_1 = \frac{1}{2} - \frac{1}{2} \sin N_1$$

$$= \frac{1}{2} \left[\frac{1}{2} - \frac{1}{2} \sin N_2 \right]$$

$$A = \frac{3f}{2\pi} = \left[\frac{9}{2} \cos N_1 \cos N_2 \right]$$
Assume $C = \begin{bmatrix} 1 & 0 \end{bmatrix} = \begin{bmatrix} N_2 & 2 & 0 \\ -1 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$
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Assume

A is defective of The system is unstable

 $\begin{cases} Sn = \begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix} Sn + \begin{bmatrix} 0 & 1 \\ mu^2 \end{bmatrix} SZ \\ Sy = \begin{bmatrix} 1 & 0 \end{bmatrix} Sn$

$$c_{R} = c \cdot (si_{1} - A) \cdot s_{1} + 0$$

$$= c \cdot (si_{2} - A) \cdot s_{1} + 0$$

$$= c \cdot (si_{3} - A) \cdot s_{1} + 0$$

$$= c \cdot (si_{3} - A) \cdot s_{2} + 0$$

$$= c \cdot (si_{3} - A) \cdot s_{3} + 0$$

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$$= c \cdot (si_{4} - A) \cdot ($$

(c) The system is stable for all pinitial conditions from [-1,7]. The system is able to achieve stready state for all possible configurations.

To check observability,
$$R = \begin{bmatrix} C \\ CA \end{bmatrix} = \begin{bmatrix} 4 & 2 \\ -0.5 & -0.5 \end{bmatrix}$$

To check observability, $R = \begin{bmatrix} C \\ CA \end{bmatrix} = \begin{bmatrix} 4 & 2 \\ -4 & 2 \end{bmatrix} \begin{bmatrix} -0.75 & -0.25 \\ -0.5 & -0.5 \end{bmatrix}$

The system is not observable

To check controllability, $P = \begin{bmatrix} B & AB \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \Rightarrow Rank (P) = 1 < 2$

The system is not controllable

For minimal realization, first perform controllable decomposition,

 $M = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} \Rightarrow A = M^{-1}AM$, $B = M^{-1}B$, $C = M$

 $M = \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $\Rightarrow \hat{A} = M^{T}AM, \hat{B} = M^{T}B, \hat{C} = CM$

$$\hat{\beta} = \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} -0.75 & -0.25 \\ -0.5 & -0.5 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} -1 & -0.55 \\ 0 & -0.25 \end{bmatrix}$$

$$\hat{\beta} = \begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

c = [42][10]=[64]

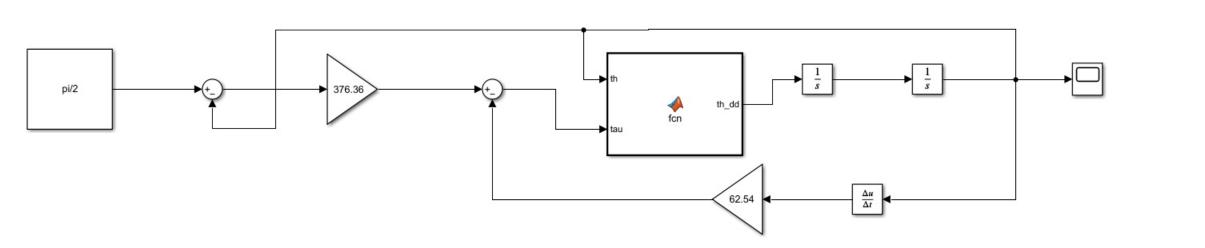
The controllable modes are, ne = Acne + Boue = -1 ne + 140 yc = Conc = 6 ne

Check observability of (x), 9= [6x(-1)] => Rank (9) = 1 > Observable

and observable

. A) is the minimal decomposition as it is both controllable

We know that G= C(SI-A) B+ D =6(s-(1))i+0(x = 6 SH) 3 5H) 34 To design a controller, the loop will look like the following digram, for the TF, Cx' = _b Time constant = 2 Compare it with, $C'' = \frac{6K}{S+1} = \frac{6K}{S+1+6K}$ T = 1+6k = 1000 > 1= 1000 + 600k ... A proportional gain [k = 166.5] will give is a time constant T=0.00/5





38.525 (/ks)

```
num = [376.36];
   den = [16 62.54 376.36];
   G = tf(num, den);
   t = 0:0.01:10;
   step(G,t)
   stepinfo(G)
mand Window
 struct with fields:
       RiseTime: 0.3031
   SettlingTime: 1.7338
    SettlingMin: 0.9371
    SettlingMax: 1.2508
      Overshoot: 25.0767
     Undershoot: 0
           Peak: 1.2508
       PeakTime: 0.7069
```