

```
clear all
clc
s = tf('s');
```

Plant transfer function.

```
G = 100/(s*(s+1)*(s+10))
```

G =

$$\frac{100}{s^3 + 11s^2 + 10s}$$

Continuous-time transfer function.

I chose canonical form from all the available options to get the state-space form of the system.

```
csys = canon(G, 'companion')
```

csys =

A =

	x1	x2	x3
x1	0	0	0
x2	1	0	-10
x3	0	1	-11

B =

	u1
x1	1
x2	0
x3	0

C =

	x1	x2	x3
y1	0	0	100

D =

	u1
y1	0

Continuous-time state-space model.

```
A = csys.A;
B = csys.B;
C = csys.C;
```

Compute the desired poles using the second-order approximation of the system. The plan is to place the third pole far away as compared to the two poles obtained from the calculation so that the third pole does not have much impact on the system.

```
MO = 20;
ts = 6;
```

Compute the damping ratio

```
z = -log(MO/100)/sqrt(pi^2 + (log(MO/100))^2)
```

$$z = 0.4559$$

Compute natural frequency

$$w = 4/(ts*z)$$

$$w = 1.4621$$

Finding desired poles of the system from the characteristic equation.

```
p = roots([1 2*z*w w^2]);
poles = [p(1) p(2) -10];
```

Place the poles at the desired location.

$$K = \text{place}(A,B,\text{poles})$$

$$K = 1 \times 3$$

0.3333	1.8045	-1.8045
--------	--------	---------

Set the observer poles far away from the controller poles so that the observer does not interfere with the system response.

$$l = [-80, -81, -82];$$

Place observer poles.

$$L = \text{place}(A',C',l)$$

$$L = 1 \times 3$$

$$10^3 \times$$

5.3136	0.1967	0.0023
--------	--------	--------

$$L = L';$$

Create a regulator for the plant using the obtained K and L values.

```
feedback = reg(csys,K,L);
AA = feedback.A;
BB = feedback.B;
CC = feedback.C;
DD = feedback.D;
```

Convert state-space to transfer function for the regulator.

```
[Ns,Ds] = ss2tf(AA,BB,CC,DD);
S = [s^3,s^2,s,1];
tf = (S*Ns')/(S*Ds')
```

tf =

$$\frac{-2122 s^2 - 3.258e04 s - 1.136e05}{s^3 + 243.3 s^2 + 1.976e04 s + 5.384e05}$$

Continuous-time transfer function.

Compute the closed loop transfer function.

```
TF = 100/((s*(s+1)*(s+10))-100*tf)
```

TF =

$$\frac{100 s^3 + 2.433e04 s^2 + 1.976e06 s + 5.384e07}{s^6 + 254.3 s^5 + 2.245e04 s^4 + 7.582e05 s^3 + 6.332e06 s^2 + 8.642e06 s + 1.136e07}$$

Continuous-time transfer function.

Convert the closed loop system to state-space canonical form.

```
sys = canon(TF, 'companion')
```

sys =

A =

	x1	x2	x3	x4	x5	x6
x1	0	0	0	0	0	-1.136e+07
x2	1	0	0	0	0	-8.642e+06
x3	0	1	0	0	0	-6.332e+06
x4	0	0	1	0	0	-7.582e+05
x5	0	0	0	1	0	-2.245e+04
x6	0	0	0	0	1	-254.3

B =

	u1
x1	1
x2	0
x3	0
x4	0
x5	0
x6	0

C =

	x1	x2	x3	x4	x5	x6
y1	0	0	100	-1100	1.11e+04	-1.111e+05

D =

	u1
y1	0

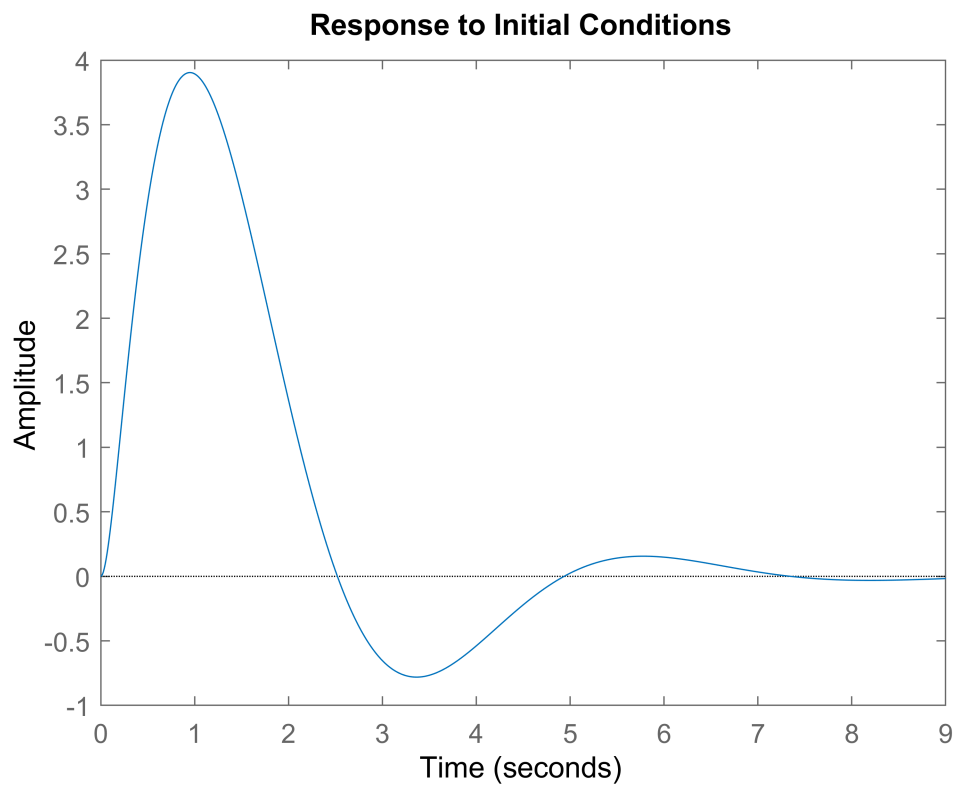
Continuous-time state-space model.

The poles of the combined system to identify the plant states:

```
pole(sys)
```

System response for using the initial conditions.

```
initial(sys,[1 0 0 0 0 0])
```



```
ans = 6×1 complex
  -0.6667 + 1.3013i
  -0.6667 - 1.3013i
  -10.0000 + 0.0000i
  -80.0000 + 0.0000i
  -81.0000 + 0.0000i
  -82.0000 + 0.0000i
```

System performance

```
stepinfo(sys)
```

```
ans = struct with fields:
    RiseTime: 1.0822
    SettlingTime: 5.7951
    SettlingMin: 4.3202
    SettlingMax: 5.6748
    Overshoot: 19.7439
    Undershoot: 0
    Peak: 5.6748
    PeakTime: 2.4868
```