

DTU



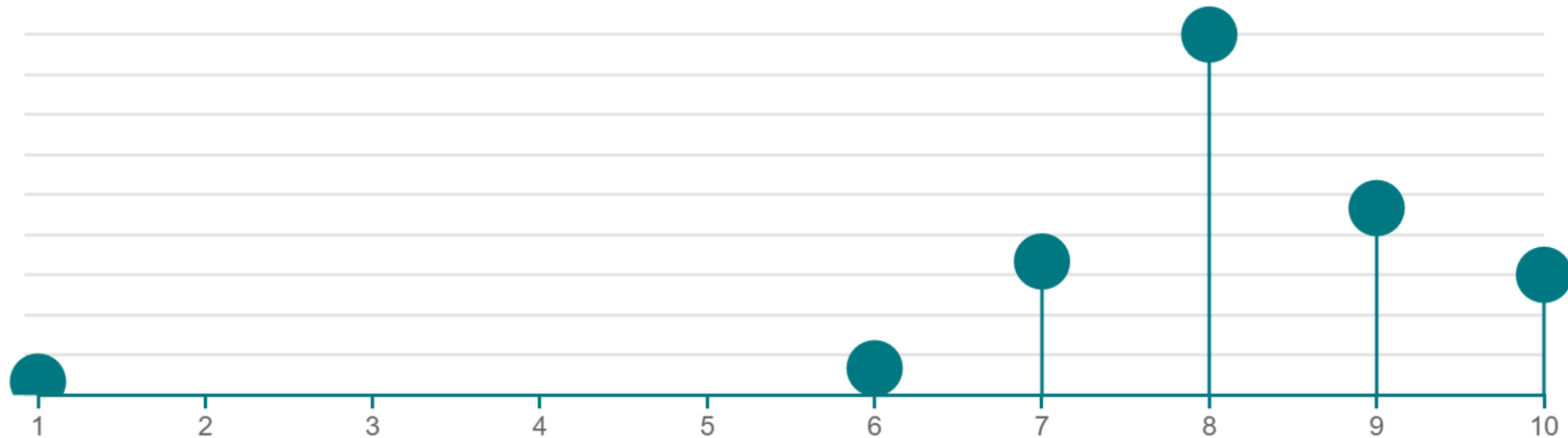


# Feedback & Follow-up

1 How good/bad was today? (scale 1-10)

63

Mean average: 8.17



# What you liked

More interactive lecture	Short and sweet!	The introduction of the course and future lessons were clear. The use of active participation.	Good and clear explanations	Very well structured, nice overview.	It was very short. This is very good more teachers should keep the first lecture short	The simple explanations on optimization as a recap.	Clear examples
The proactive teaching and participation of students	Dynamic class, exercises/quizzes help a lot, good to exercise your brain	Interactive interesting problems.	The teaching style is engaging, but I think I need some time to get use to actively engage myself.	I like the conciseness of the lecture No wasted words or time and all info is given	Great lecture	Locket the interactiveness	pratical
i like the way that we interact with each other.	Good overview of what we will do in this course.	Interesting and dynamic optimization exercises	The interactive approach to the lecture	Giving students the chance to come with a solution before presenting the right answer	The inter active lecture That we get to try an anser and that you clearly state what was correct and why (the why is the most important part, that is when I learn from my...	Short and concise, straight to points good structure.	Short and precise
Active learning	Not spending many hours on lectures, just start working.	I liked the very straight forward way of communicating of what the course will cover and how it is set up. The examples definitely made it easyler to understand.	The recap on optimization	Discovering optimization	Good lecture, easy to follow and understand	Active learning part	
Straight to the point class.	Great way of active learning and good participation in class, keeping lectures fun and engaging.	The dynamic interaction and continuous use of questions throughout the lecture made students apply prior concepts and possibly correct misconceptions....	Was informative.	Engaging lecture, vevox is working well Short lecture	Actively participating with instant feedback	7	
I like the honesty regarding on how the class may feel like, with the reasoning for that	Interactively.	Really interactive, keep it up!	Short and concise	It was a simple lecture. It is very nice that there is some sort of active learning during lectures. Also, you (lecturer) is good at explaining everything.	The active learning thing	The presentation format and the active participation	
That its clear from the beginning what is expected from us to do, and also that the lecture was very well structured.	The example in class and working on them at the same time, it's easier to understand	The examples were great and works as a refresher	Good with small simple examples to quickly assess knowledge	I did, the course seems demanding but interesting	Good tempo	Examples	
It was short and concise	You keep making the class to be an interactive class, and it's a fun way to learn for me	I like the way how concepts are explained with clear examples.	The structure with assignments and no exams.	The interactive part	Very clear !		
			The questions	Short and to the point, nice outline of the expectations to the course	That you were to the point, and showed examples!		

# What you disliked

All was good!

Could be a bit more quick on explanations

-

Not sure if i have enough pre requisits for the programming part of the course

Almost nothing

i like the way that we interact with each other. But it would be great if you can mention the use of Groubi as seems you only showed python code at course

I am not yet familiar with optimization programming

Too fast for me. Could it be little slower so that i can get all like processing time to understand the problem..

I am missing some deadlines/information on the two assignments and how they are combined with the tasks

My lack of knowledge on the programming part, hopefully I can make kt up or the learn page might have some simple tutorials about the language?

Not so much new stuff if you have already had for example intro to OR

Nothing

Nothing so far

None

Didn't learn much (yet) - maybe focus more in the first lecture on what 'Decision Making Under Uncertainty' even is/give ideas of the methods we will learn to use

Slides not uploaded in the beginning

I am not sure there is anything that I dislike.

Elaborating before hand on the problems that we answered a little bit

Nothing

Nothing

What are we going to do in the assignment?

Slides were not uploaded before start of the lecture.

Ppt not available before class

Not much new material was presented but this is often the case on the first day

n/a

Everything was ok. Maybe just put some more time on the code explanation

Sometimes I felt things were a little rushed, especially for solving problems

Dont have anything for this lecture that I did not like

Not having the slides

Discovering optimization

Small problem with the mic making loud noises once in a while

Few time to think on the problems.

Missed a bit of basic knowledge recap/explanation.

Nothing. looking forward to the next one.

Nothing in particular

Nothing.

Maybe a little bit more explaining for those who can't understand

Maybe a time for group formation initiated by the lecturer would be nice

Lecture was pretty quick but I understand its so that the exercise part is maximized

I don't know if you this active learning this is a bit forced, but I want to see how it works later on too

I have not thought about anything that I dislike

I am not as ready in linear programming as I thought I guess

The active learning method.

We could discuss the optimization research problem with Carl more

Not much

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## 5. Mixed-integer linear programming

### Farmer Carl - Model formulation



MIP:

Decision variables:

$x_C$  = Number of cows, Carl should buy

$x_S$  = Number of sheep, Carl should buy

$$y_S = \begin{cases} 1, & \text{if Carl buys more than 100 sheep} \\ 0, & \text{if Carl buys no sheep} \end{cases}$$

$$y_C = \begin{cases} 1, & \text{if Carl buys more than 10 cows} \\ 0, & \text{otherwise} \end{cases}$$

$$\text{Max } \{(400 - 200)x_C + (70 - 30)x_S - 1000y_C\}$$

$$\text{s.t. } x_C \leq 50$$

$$x_S \leq 200$$

$$x_C + 0.2x_S \leq 72$$

$$150x_C + 25x_S \leq 10000$$

$$100y_S \leq x_S \leq 200y_S$$

$$11y_C \leq x_C \leq 10 + 40y_C$$

$$x_C, x_S \geq 0 \text{ and integer}$$

$$y_C, y_S \in \{0, 1\}$$

**Sanity Check!**



# Pyomo Code

Carl.py

```
from pyomo.environ import *

# Create a model
model = ConcreteModel()

# Declare variables
model.xC = Var(bounds=(0, 50), within=Integers)
model.xS = Var(bounds=(0, 200), within=Integers)
model.yS = Var(bounds=(0, 1), within=Binary)
model.yC = Var(bounds=(0, 1), within=Binary)

# Objective function: Maximization of profits
model.profit = Objective(
    expr=(400 - 200) * model.xC + (70 - 30) * model.xS - 1000 * model.yC,
    sense=maximize
)

# Constraints

#Constraint on available acres
model.Acres = Constraint(expr=model.xC + 0.2 * model.xS <= 72)

#Constraint on maximum working hours
model.WorkingHours = Constraint(expr=150 * model.xC + 25 * model.xS <= 10000)

#Minimum of 100 sheep constraint
model.AtLeast100Sheep1 = Constraint(expr=model.xS - 100 * model.yS >= 0)
model.AtLeast100Sheep2 = Constraint(expr=model.xS - 200 * model.yS <= 0)

#Maximum of 10 cows without milk machine
model.MilkMachine1 = Constraint(expr=model.xC - 10 - 40 * model.yC <= 0)
model.MilkMachine2 = Constraint(expr=model.xC - 11 * model.yC >= 0)

# Create a solver
solver = SolverFactory('gurobi') # Make sure Gurobi is installed and properly configured

# Solve the model
results = solver.solve(model, tee=True)
```

# Plan

→ ~~Task 0 : last week and at home~~

→ Today: Task 1

Building an evaluation framework for sequential decision-making methods

→ Weeks 3-4: Task 2

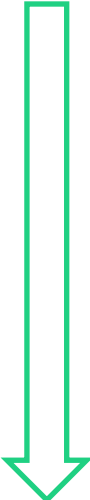
Stochastic Programming

→ Week 5: Assignment Work for Task 2 and Q&A

→ Weeks 6-7: Task 3

Approximate Dynamic Programming

→ Week 8: Assignment Work for Task 3 and Q&A



Task 4 is about reporting the results from Tasks 2 and 3

# The process of designing “Decision-making” frameworks

“Decisions”

- ❖ Choosing a career path?
- ❖ Deciding on which country to move next?
- ❖ Stay in a relationship or not?

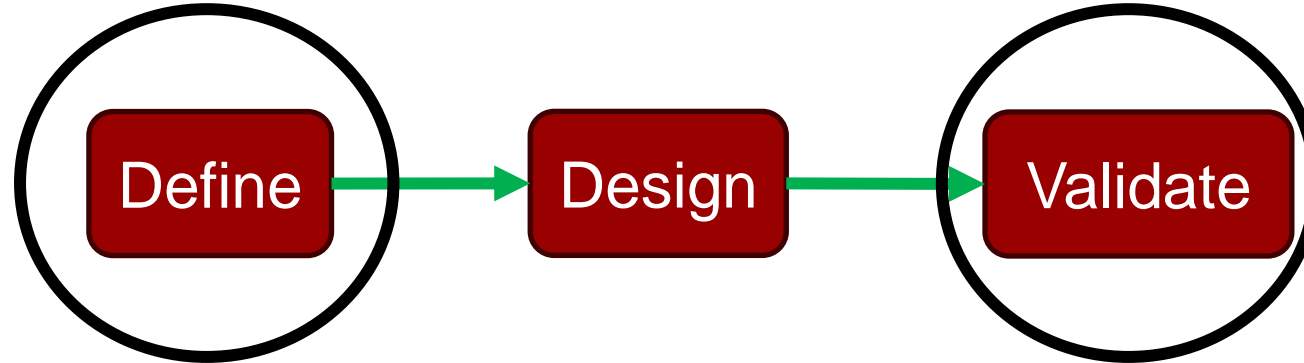


define the problem, what are you  
after? before talking about  
solutions

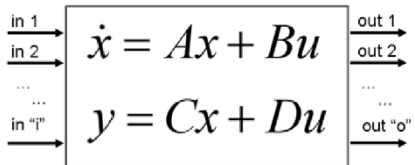
# The process of designing “Decision-making” frameworks

“Decisions”

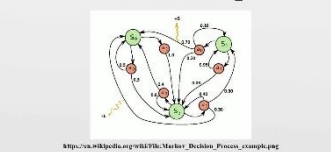
- ❖ Choosing a career path?
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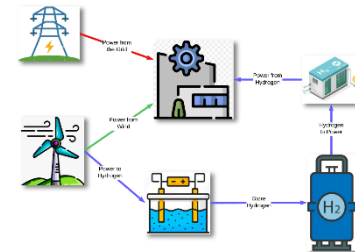
Coding a simulation  
Environment to evaluate  
*any* decision-making policy



Markov decision process



how good it is



# Agenda for today

1. Defining a problem of Sequential Decisions under Uncertainty
2. Examples
3. Coding an Evaluation Framework for the Assignment (Task 1)

# Markov Decision Process

- Stages  $t \in \mathcal{T}$
- State  $\mathbf{x}_t = \{x_{1,t}, x_{2,t}, \dots\}$
- Decision  $\mathbf{u}_t = \{u_{1,t}, u_{2,t}, \dots\}$
- Dynamics  $\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t)$
- Cost  $c_t = g(\mathbf{x}_t, \mathbf{u}_t)$

each stage you need to make a decision, what information we can get from the system - state - ex temperature

decision - what can we control

dyn - links the next stage function will be, as function current state and current decision - deterministic  
i take action to take to right but also depends on the wind, current state wind, and my decision

cost function - can be reward, what i want to achieve, each stage i take an action, as function of state and action i get an immediate reward or cost

# Markov Decision Process

- Stages  $t \in \mathcal{T}$
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The *State* variables  $\mathbf{x}_t$  enclose the necessary and sufficient information to model the system's behavior from stage  $t$  onwards.

everything we now from the system should go to the state variable

# Markov Decision Process

- Stages  $t \in \mathcal{T}$  evry day, every week

- State  $\mathbf{x}_t = \{x_{1,t}, x_{2,t}, \dots\}$

- Decision  $\mathbf{u}_t = \{u_{1,t}, u_{2,t}, \dots\}$

do i show up, do i make a question? something that affect cost function (grade, effort), time spend, how much effort, i put some effort now and more later

- Dynamics  $\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t)$

- Cost  $c_t = g(\mathbf{x}_t, \mathbf{u}_t)$

The *State* variables  $\mathbf{x}_t$  enclose the necessary and sufficient information to model the system's behavior from stage  $t$  onwards.

State

knowledge you have, skill, how does evolve on stat t,

deterministic - skill<sub>t+1</sub>=f(skill<sub>t</sub>,effor<sub>t</sub>),

stochastic - stress<sub>t+1</sub>=g(stress<sub>t</sub>,effort<sub>t</sub>), stress is more uncertain, skill more deterministic, we could add more stochastic stress<sub>t+1</sub> = g(stree, effort, weather) weather is uncertain, is not a decision, is a state variable, it has is own dynamics,

weather<sub>t+1</sub> = h(wwather<sub>t</sub>) --> exogenous state, not depending on decisions just on the stat

we need to make the optimal decision, in markov we need to design a policy, from state to decision, if i counter tis state i do this decision other i do toger decision

policy/method

optimal policy, one that minimizes the expected cost, over time, check if this makes sense

policy is a mapping from states to decisions, sum of cost trough the satates

## Solution Concept:

*Policy*  $\pi: \mathbf{u}_t = \pi(\mathbf{x}_t)$

## Optimal Policy:

$$\min_{\pi} \left\{ \sum_t E_{\mathbf{x}_t \sim \pi} [c_t] \right\}$$

state t+1 depends only on t, not in other times

~the skill now i dont need to know the skill before

statet=(skill\_T, skill\_t-1)  
state<sub>t+1</sub> = f(state<sub>t</sub>)

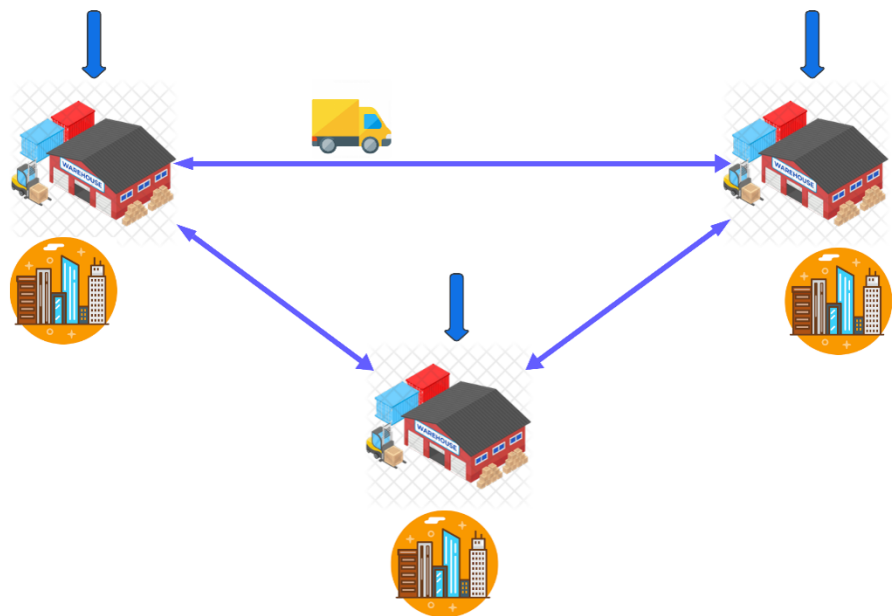
$$\mathbf{u}_t = \pi(\mathbf{x}_t), \quad \forall t$$

$$c_t = g(\mathbf{x}_t, \mathbf{u}_t), \quad \forall t$$

$$\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t), \quad \forall t$$

in order to preserve, we need to include aall that is relevant into the state





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Each warehouse can store coffee up to a capacity limit  $C^{store}$ . Denote the storage level of  $w$  at  $t$  by  $z_{w,t}$ . At stage  $t$ , each warehouse  $w$  can order an amount  $o_{w,t}$  of coffee from external suppliers at price  $p_{w,t}$ . The price is different for each warehouse and each day.

Similarly,  $y_{w,q,t}^{send}$  is the amount sent by  $w$  to  $q$ .

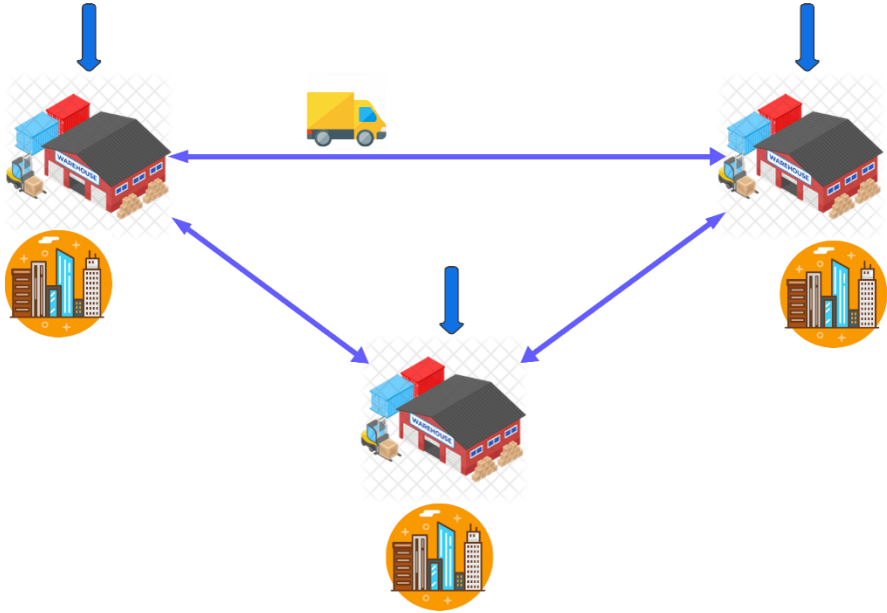
The amount sent in one stage is restricted by a transportation limit  $C^{trns}$ .

Each exchange comes at a per-unit transportation cost  $e_{w,g}$ .

Failing to meet a district's demand at any day comes at a per-unit cost of  $b_w$ .

Your job is to build a program that makes the day-by-day decisions for the coffee distribution system of the three warehouses, so that the city's coffee needs are met at the minimum expected cost.

# The Lead Example



- Stages  $t \in \mathcal{T}$
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Consider a city divided into three districts.

Each district features a dedicated warehouse  $w \in W = \{1, 2, 3\}$  which serves the district's demand  $D_{w,t}$  for coffee.

The coffee demand for each warehouse and day is known.

Each warehouse can store coffee up to a capacity limit  $C^{store}$ .

Denote the storage level of  $w$  at  $t$  by  $z_{w,t}$ .

At stage  $t$ , each warehouse  $w$  can order an amount  $o_{w,t}$  of coffee from external suppliers at price  $p_{w,t}$ .

The price is different for each warehouse and each day.

Neighboring warehouses can also exchange coffee between them.

Let  $y_{w,q,t}^{rcv}$  denote the amount received by  $w$  from a neighboring warehouse  $q$ , at  $t$ .

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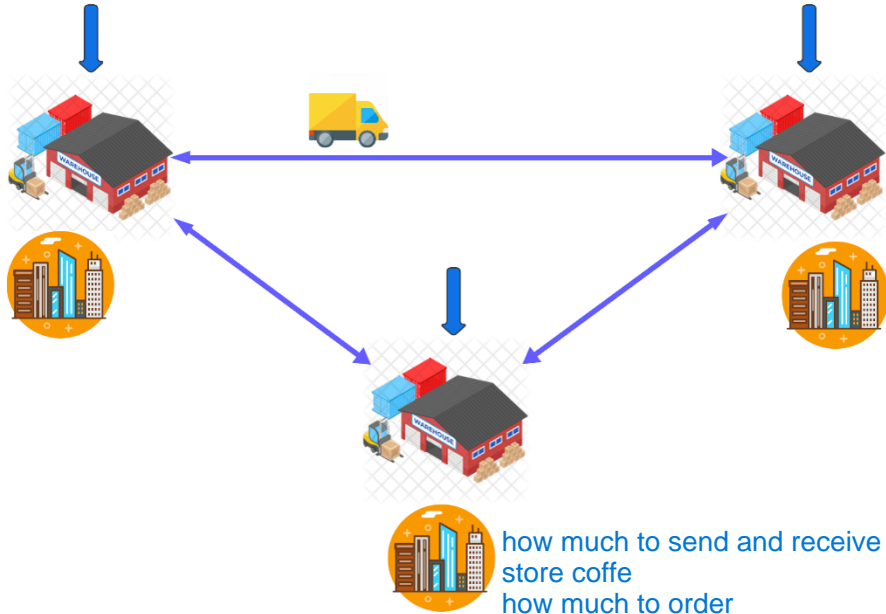
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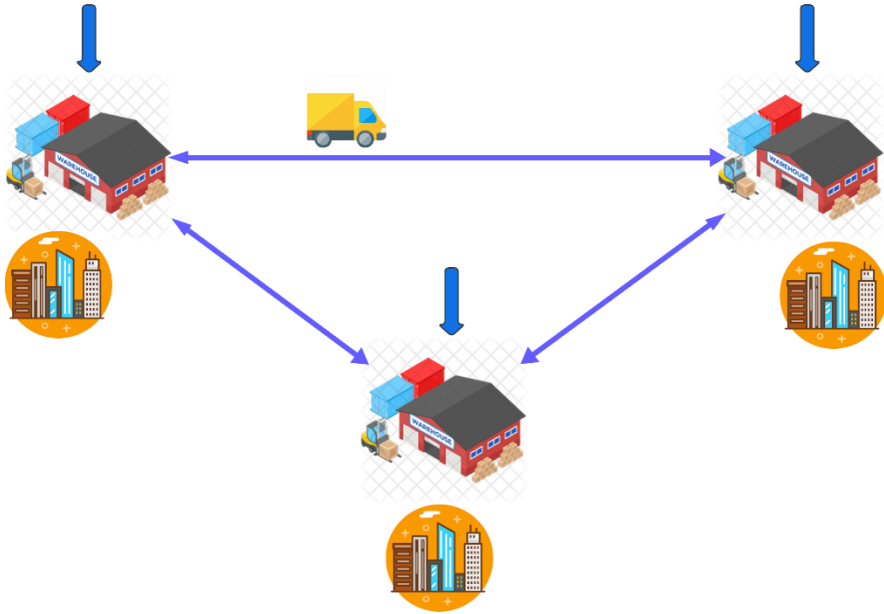
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storage level,

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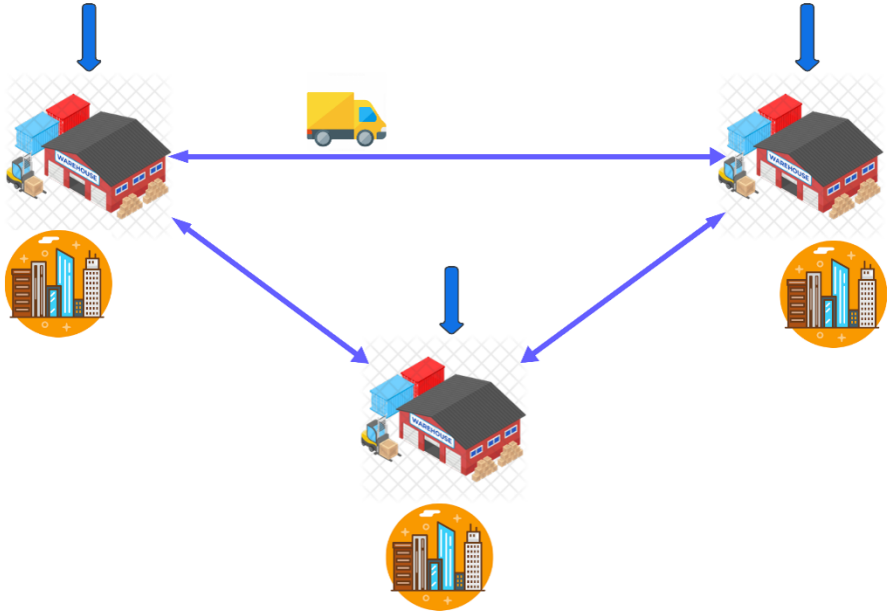
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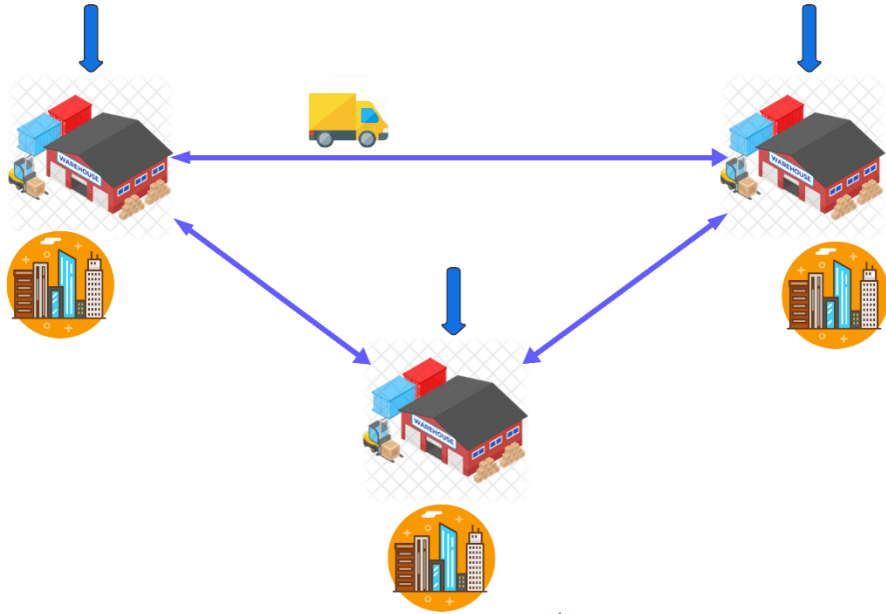
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- Stages  $t \in \mathcal{T}$
- State  $\mathbf{x}_t = \{x_{1,t}, x_{2,t}, \dots\}$
- Decision  $\mathbf{u}_t = \{u_{1,t}, u_{2,t}, \dots\}$
- Dynamics  $\mathbf{x}_{t+1} = f(\mathbf{x}_t, \mathbf{u}_t)$
- Cost  $c_t = g(\mathbf{x}_t, \mathbf{u}_t)$



# The Lead Example



cost  
price \* how much order  
+ sent between \* proce  
+ fail to meet demand \* cost

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# The Lead Example

$$z_{w,t+1} = z_{w,t} - d_{w,t} + o_{w,t} + \sum_{q \in W} y_{w,q,t}^{rcv} - \sum_{q \in W} y_{w,q,t}^{send}$$

- Stages  $t \in \mathcal{T}$
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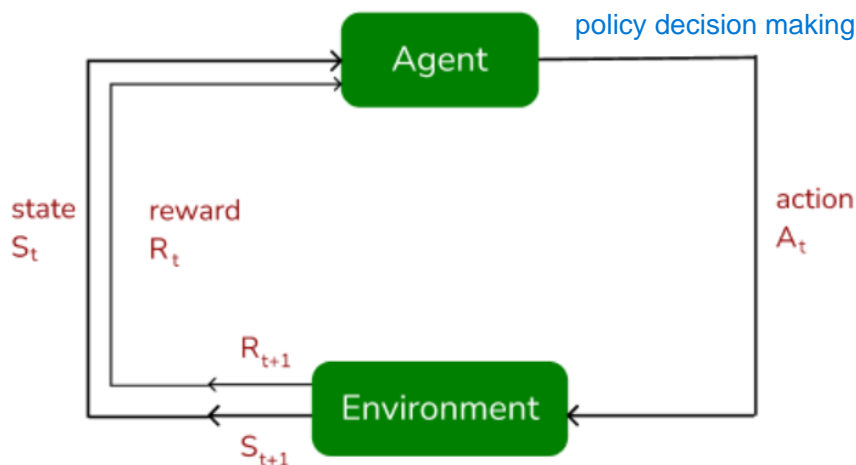
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# Simulation Environment



## task 1

it presents the agent with the current state, agent gives an action state, and gives back to environment and then it gives a reward cost based

it takes policy, splits a reward and next stage

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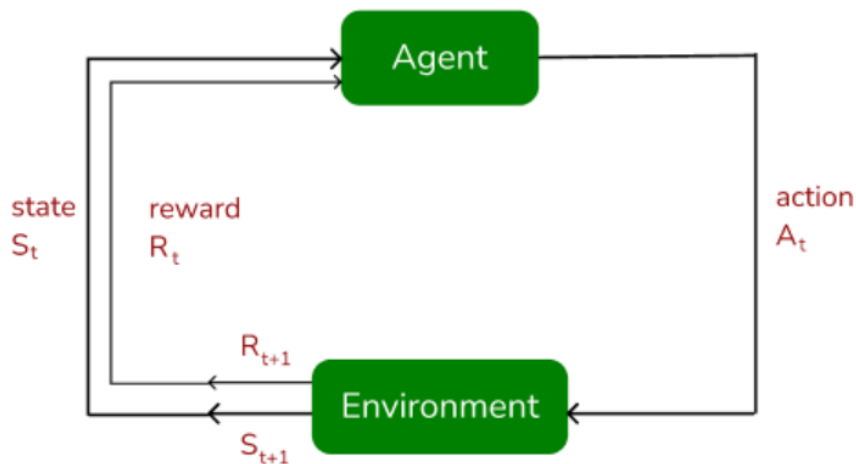
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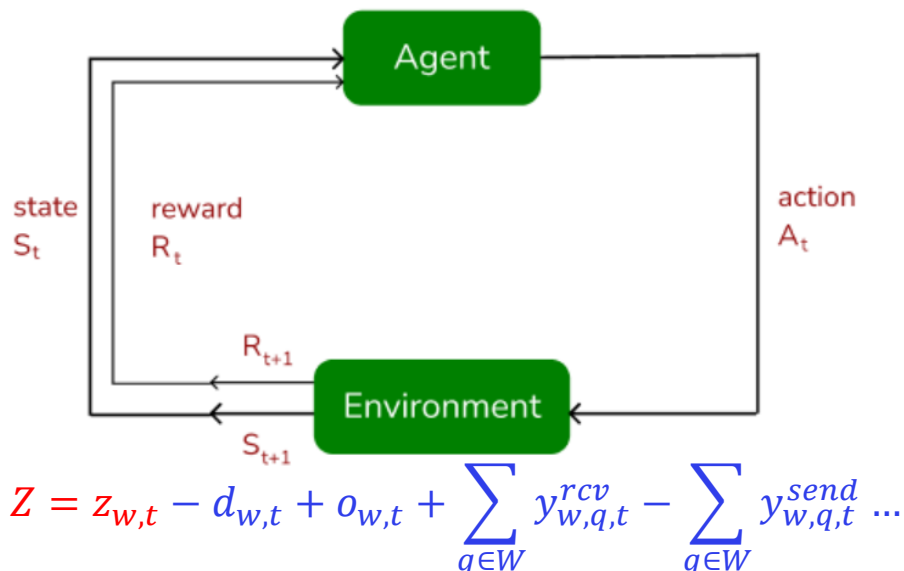
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# Simulation Environment



```

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else:  $z_{w,t+1} = Z$ 

```

decision making policy can do order more coffee as much as i like, it is the env to make sure problem is consistent, cannot store more coffee than can store, we need code in the environment, that takes the action and check the previous storage level and calculate new storage level, any extra coffee is thrown away  
 we might type positive and order negative amounts, we need to take into account crazy things, we don't want negative amounts  
 storage 10, i order 2, i don't receive or order, i have 12 available, demand is 14, i have 12, demand goes there and i need to set, demand serve as 12 and missing 2

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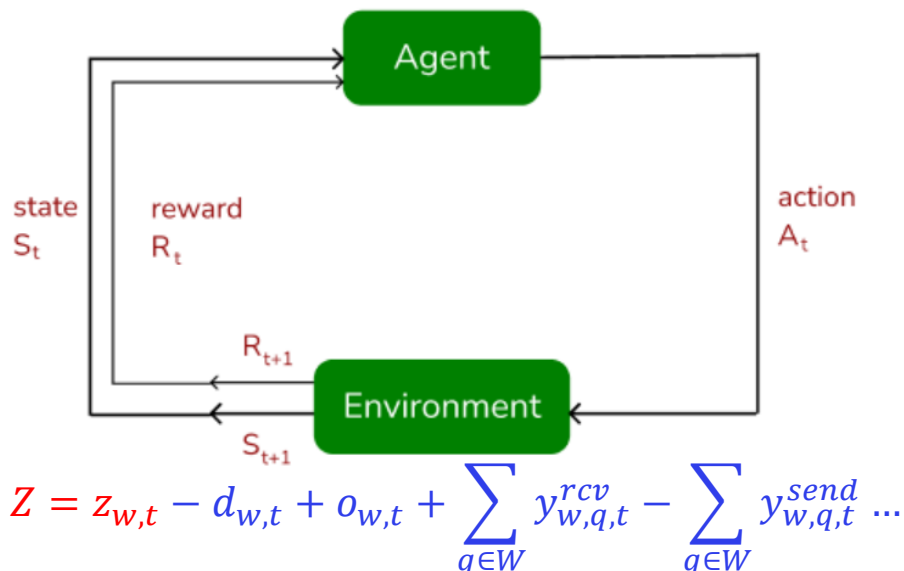
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if  $y_{w,q,t}^{send} > \min\{z_{w,t}, C^{trnsnp}\}$ :
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```

ii cannot send more than what is allowed and what is previously stored

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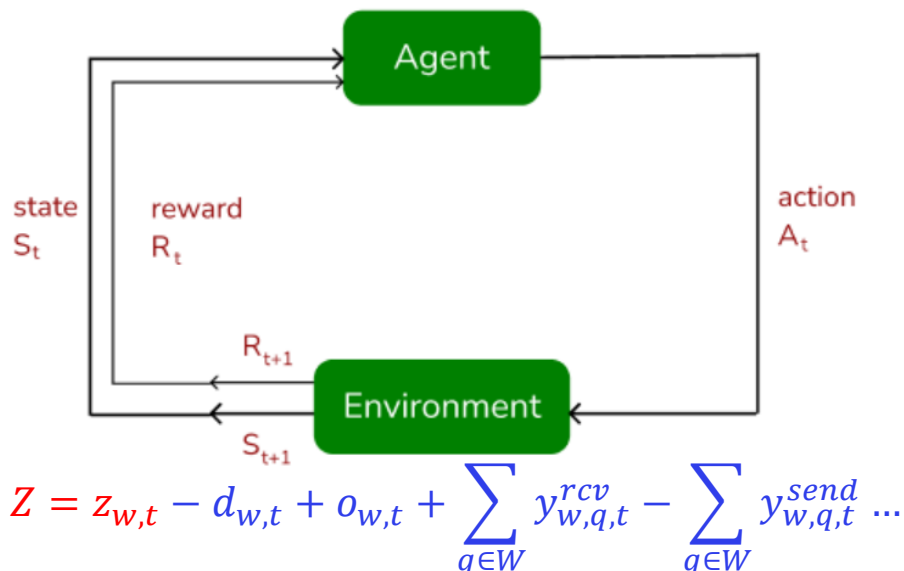
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```

if  $y_{w,q,t}^{rcv} \neq y_{w,q,t}^{send}$ :
    then  $y_{w,q,t}^{rcv} = y_{w,q,t}^{send}$ 

```

what receives should be consistent with what the other sends, we set it equal

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$$c_t = \sum_{w \in W} (p_{w,t} o_{w,t} + e_{w,q} y_{w,q,t}^{send} + b_w (D_{w,t} - d_{w,t}))$$

cost function, we need to return to environment every time we take a decision

$$Z = z_{w,t} - d_{w,t} + o_{w,t} + \sum_{q \in W} y_{w,q,t}^{rcv} - \sum_{q \in W} y_{w,q,t}^{send} \dots$$

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if  $d_{w,t} < 0$ :  
then  $d_{w,t} = 0$

demadn might go negative, cannot serve more demadn more then ther is

$$Z = z_{w,t} - d_{w,t} + o_{w,t} + \sum_{q \in W} y_{w,q,t}^{rcv} - \sum_{q \in W} y_{w,q,t}^{send} \dots$$

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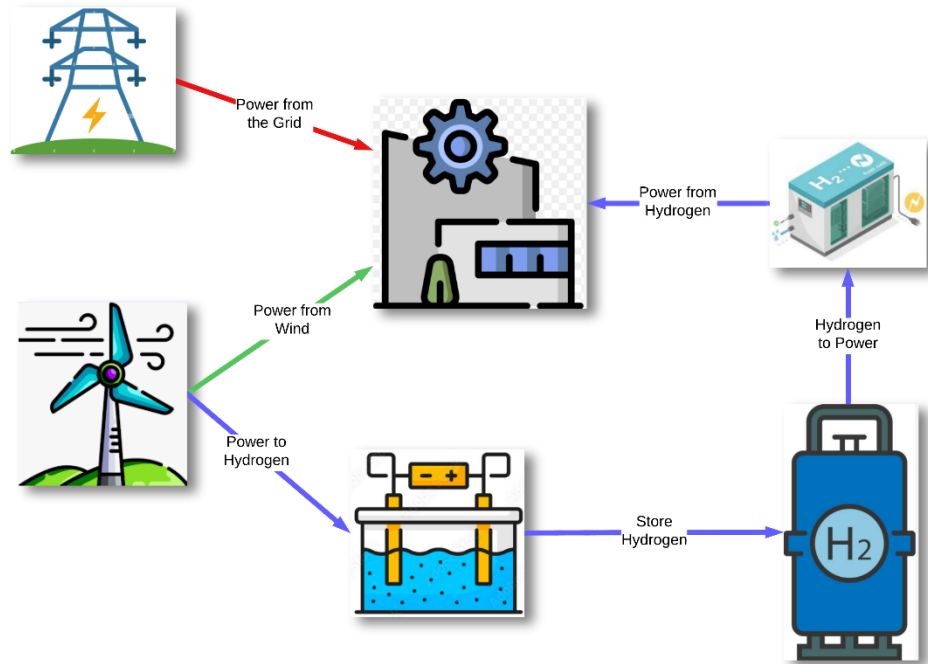
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# Assignment A, Task 1

if we do a lot of experiments, various prices, we will simulate what decisions will it make, what decisions would occur, this is how the policy would work in real



## Deliverable 1: MDP

State variables  $x_t = \{x_{1,t}, x_{2,t}, \dots\}$

to simulate wind, simulations of random process of

Decision variables  $u_t = \{u_{1,t}, u_{2,t}, \dots\}$

Dynamics  $x_{t+1} = f(x_t, u_t)$

Cost function  $c_t = g(x_t, u_t)$

if i just use one, it can be an outlier, out of the statistics, we do several to have a good idea of the policy costs

## Deliverable 2: Policy Evaluation Framework

**Input:** *policy* (python function that returns decisions)

**Initialize** state variables

**For** experiment 1 to E:

**For** stage 1 to H:

decisions = *policy*(state)

check/correct decisions if inconsistent

calculate cost for this stage and experiment

calculate state at next stage

calculate total cost of policy for this experiment

**Return:** expected policy cost (average over experiments)



# Questions and Survey

- Group selection is open until Friday

random decision is a policy, we can design better  
policy is a decision of the state

you design the policy and then each state we just apply policy