

An example *Geophysics* article, with a two-line title

*Joe Dellinger** and *Sergey Fomel†*

ABSTRACT

This is an example of using `geophysics.cls` for writing *Geophysics* papers.

INTRODUCTION

Full Waveform Inversion (FWI) is considered one of the most efficient seismic imaging methods due to its ability to utilize all seismic phases present in the data (Pratt and Shipp, 1999; Schuster, 2017; Tarantola, 1986; Virieux and Operto, 2009). This involves comparing synthetic data with observed data (Gómez and Pestana*, 2017; Liu et al., 2017; Métivier et al., 2018), where the difference between them is known as the objective function. The rate of change of the objective function with respect to model parameters (Plessix, 2006) is used to iteratively update the model until the synthetic data from the updated model matches the observed data.

The nonlinear relationship between synthetic data and model parameters (Crase et al., 1990; Geng et al., 2018; Guo et al., 2021) leads to a multimodal nonlinear objective function, characterized by multiple local minima and maxima (ten Kroode et al., 2013), as shown in FIGURE. FWI utilizes calculus-based optimization methods, such as gradient descent, BFGS, and conjugate gradient, which typically direct the solution towards the nearest extrema. This can lead to FWI becoming trapped in local minima if the starting model is not within the basin of attraction (Fitchner, ETH). Consequently, if the starting model is in a localized basin of attraction, achieving convergence to the global minimum becomes impossible. Therefore, it is crucial to initialize the inversion with a model that is close to the global minimum.

FWI has undergone extensive research to address nonlinearity, focusing on both modifying the objective function and developing effective methods for preparing initial models through global optimization. Approaches to modifying the objective function include multiscale strategies (Bunks et al., 1995; Ravaut et al., 2004; Schäfer et al., 2014; Sirgue and Pratt, 2004), which start with low-frequency data for initial inversions and gradually incorporate higher frequencies. The normalized cross-correlation objective function (Chi et al., 2015; Liu et al., 2017) emphasizes phase matching to mitigate amplitude variations, while the envelope-based objective function (Borisov et al., 2018; Chi et al., 2014) is used for updating long-wavelength models. More recent methods, such as the optimal transport function (Brossier et al., 2016; Métivier

et al., 2016, 2018), enhance the convexity of the basin of attraction, thereby increasing the likelihood that the initial model will fall within the basin of attraction for the global minimum.

In geophysics, common global optimization methods for preparing initial models in seismic inversion include Very Fast Simulated Annealing (VFSA), inspired by the annealing process in metallurgy (Ingber, 1989; Kirkpatrick et al., 1983; Sacks et al., 1989); Genetic Algorithm (GA), based on Darwin’s theory of survival of the fittest (Katoch et al., 2021; Michalewicz, 1996); and Particle Swarm Optimization (PSO), which utilizes the concept of swarm intelligence (Couceiro and Ghamisi, 2016; Kennedy and Eberhart, 1995; Shi and Eberhart, 1999; Wang et al., 2018). These methods, inspired by natural phenomena and expressed through mathematical formulations, are adept at exploring the entire search space to identify optimal solutions. The strategy involves a two-step process: initially using global optimization techniques to prepare the starting model, followed by FWI. This approach leverages the extensive exploration capabilities of global optimization methods (Dong et al., 2015; Ye and Pan, 2024). Once a reliable initial model is established, which is expected to be within the basin of the global minimum, local optimization methods are then applied due to their high exploitation efficiency.

Published implementations of these global optimization methods include a variety of approaches for geophysical data inversion. Datta and Sen (2016) used VFSA for initial model preparation in a two-step process, employing zero-offset sections for parameterization. Fu et al. (2021) introduced a parallel VFSA algorithm for 1.5D acoustic FWI, allowing simultaneous updates of model parameters across multiple threads. Shiba and Irikura (2005) demonstrated VFSA’s effectiveness in estimating earthquake displacement, showing its superiority over GA for this task. Mendes et al. (2024) utilized a training image to guide the generation of realistic velocity model samples, improving convergence. Datta et al. (2019) applied VFSA to represent sedimentary layers and salt bodies using interfaces and ellipses, respectively. On the GA front, Mazzotti et al. (2016) proposed a method with two grids—a coarse grid for inversion and a fine grid for modeling. Tran and Hiltunen (2012) highlighted GA’s potential for enhancing subsurface property characterization, while Zeng et al. (2011) explored GA for Rayleigh wave inversion. Aleardi and Mazzotti (2017) integrated GA with Markov Chain Monte Carlo (MCMC) methods to address search space uncertainties. In PSO applications, Yang et al. (2017) developed a PSO method for impedance inversion, Shaw and Srivastava (2007) demonstrated its effectiveness in natural resource exploration, and Ding et al. (2015) focused on applying PSO to a 1D-DC resistivity case. Additionally, Kaplanvural et al. (2020) showcased PSO’s ability to invert common-offset ground-penetrating radar (GPR) traces and estimate dielectric properties, while Fernández-Martínez et al. (2010) used PSO for reservoir characterization and Fern and Garc (2010) explored its application to the SP inverse problem.

A research also has been conducted to identify more effective global optimization methods. A comparison of Genetic Algorithms (GAs) with Monte Carlo methods

found that GAs provide better fits with fewer model parameters and greater computational efficiency (Sambridge and Drijkoningen, 1992). Further analysis comparing GA with Particle Swarm Optimization (PSO) concluded that PSO generally outperforms GA (Ding et al., 2015; Mojica et al., 2019). Additionally, Sajeve et al. (2017) offers a comparative analysis of four stochastic optimization methods—adaptive simulated annealing (ASA), GA, neighborhood algorithm (NA), and PSO—for 1D elastic full-waveform inversion and residual static computation. The study indicates that the choice of optimization method should depend on the characteristics of the objective function and the dimensionality of the model space.

In this study, we present the application of PSO for generating an initial model for FWI, due to its ability to effectively balance exploration and exploitation within the solution space. The implementation of global optimization methods in seismic inversion faces the challenge of the curse of dimensionality due to the large number of model parameters involved (Dhabaria and Singh, 2024). This necessitates defining the model with a reduced number of parameters. To address this, we have defined the model in terms of depth and velocity at the interfaces, as well as the rate of change of velocity between these interfaces. The number of interfaces to be inverted is determined solely by the selected number of breaks. The depth and number of interfaces are constrained by the arrival times of major breaks observed in near-offset seismic trace, respectively. Meanwhile, the velocity at each interface and the rate of change of velocity are limited by realistic subsurface velocity values. For near-offset receivers, these major breaks are most likely caused by reflections. This inversion begins with a uniform 1D velocity-depth model and sources positioned at various horizontal locations. Using this method, the interfaces are inverted progressively from the surface to depth. The data inverted for a particular interface serves as the initial model for the inversion of the subsequent interface. This process is repeated for all shots, with 1D velocity-depth profiles interpolated to prepare a 2D initial model for FWI. We also conducted experiments to find the optimal combination of parameters. A multi-threaded computation is also implemented to simultaneously invert data for multiple shots.

This paper is organized into the following sections:

- **Methodology:** This section provides a detailed description of the Particle Swarm Optimization (PSO) algorithm, including experiments for selecting optimization parameters. It also covers the implementation of PSO, model parametrization, and offers a brief introduction to FWI.
- **Results:** This section presents the experiments conducted to prepare initial models for various benchmark seismic models to assess the reliability of the proposed method. It also includes the results of FWI applied to these initial models.
- **Discussion and Conclusion:** The section includes a discussion on the limitations of our method, its advantages over traditional techniques, and potential

directions for future research.

METHODOLOGY

This approach involves two steps. First, a coarse velocity model is prepared using PSO by optimizing the depth, interface velocity, and the rate of change of velocity between interfaces. This model serves as an initial model for conventional gradient-based FWI in the second step.

Particle Swarm Optimization

Particle Swarm Optimization (PSO) is a stochastic method developed by James Kennedy and Russell Eberhart in 1995. Inspired by the social behavior of birds flocking to find food, they formulated a mathematical model to simulate this behavior. This model is widely applied to solve various optimization problems. They identified that the fundamental principle guiding birds' food-finding behavior is their ability to communicate with each other. Each bird in the process knows its current position ($\mathbf{x}_i(t)$) and best position ($\mathbf{p}_i(t)$), determined by evaluating the fitness using a cost function. Additionally, each bird shares its best position with others, contributing to the collective knowledge of the flock's best position ($\mathbf{g}(t)$). Each bird's next movement is adjusted by its own best, the flock's best, and its current position. This iterative process continues at each step, ultimately converging towards a globally optimal position through the collaborative effort of all birds. This natural phenomenon is mathematically described by the velocity update equation 1 and the position update equation 2.

- $\mathbf{x}_i(t)$ be the position of particle i at iteration t .
- $\mathbf{v}_i(t)$ be the velocity of particle i at iteration t .
- $\mathbf{p}_i(t)$ be the personal best position of particle i until iteration t .
- $\mathbf{g}(t)$ be the global best position among all particles until iteration t .
- w be the inertia weight.
- c_1 and c_2 be the cognitive and social acceleration coefficients, respectively.
- r_1 and r_2 be random numbers uniformly distributed in the range $[0, 1]$.

The velocity and position update rules for each particle are given by:

$$\mathbf{v}_i(t+1) = w\mathbf{v}_i(t) + c_1r_1(\mathbf{p}_i(t) - \mathbf{x}_i(t)) + c_2r_2(\mathbf{g}(t) - \mathbf{x}_i(t)) \quad (1)$$

Example

$$\mathbf{x}_i(t+1) = \mathbf{x}_i(t) + \mathbf{v}_i(t+1) \quad (2)$$

Where:

- w controls the influence of the previous velocity (inertia).
- c_1 and c_2 represent the trust of the particle in itself and in the swarm, respectively.
- r_1 and r_2 introduce stochasticity to the particle's movement.

Optimization Parameters

The updates in the Particle Swarm Optimization (PSO) algorithm are influenced by several controlling parameters, including the inertia weight (w), acceleration coefficients (c_1 and c_2), population size of the swarm, and the number of iterations. Among these, the inertia weight is the most critical tuning parameter as it balances the exploration and exploitation capabilities of PSO by adjusting the contribution of the particle's previous velocity. An inertia weight value between 0.4 and 0.9 is generally found to provide good convergence. The cognitive and social coefficients (c_1 and c_2) represent the confidence in a particle's own best position and the swarm's best position, respectively, and they influence the updated velocity of the particles. The number of particles in the swarm also affects convergence; as the number of particles increases, the search space expands, potentially leading to better convergence. Experimental studies have shown that a swarm size of around 30 particles is generally effective for finding solutions within optimal iterations. The number of iterations, as with all iterative optimization algorithms, significantly impacts the performance of PSO.

This contribution of different parameters for success of PSO make it necessary to decide the combination of these parameters precisely. We have performed experiments to find the optimal combination of these values, for these experiments we have chosen four nonlinear functions Ackley, Griewank, Rastrigin, and Styblinski-Tang function shown in figure ??, ??, ??, and ?? respectively. These experiments are performed to determine the optimal value of the optimization coefficient and examine the relationship between the number of iterations and swarm size. Since both swarm size and iteration count impact computational time, it is essential to balance these factors to achieve effective optimization while minimizing computational costs. To fairly compare the effects of swarm size and the number of iterations, the rate of increase for both parameters is kept consistent. Following this, PSO is applied to the Schwefel function using the parameters chosen from the previous experiment to achieve the parameters that lead to the best convergence. To analyze performance, accuracy is evaluated based on the maximum deviation using equation 3. Further details of these

experiments are outlined below.

$$Accuracy(\%) = 100 - \left| \frac{\text{optimal value} - \text{evaluated value}}{\text{optimal value} - \text{maximum deviation}} \right| \times 100 \quad (3)$$

Where:

- *Optimal value*, best possible value of the objective function.
- *Evaluated value*, value of the objective function at a given point in the feasible domain.
- *Maximum deviation*, largest difference between the optimized value and the actual values.

1. Accuracy with Parameters: In this experiment, optimization is conducted for all specified test functions using varying values of c_1 , c_2 , and inertia weights, as illustrated in figures ??, ??, ??, and ??. To address the inherent randomness of this stochastic method, we perform 50 runs with 1000 iterations and calculate the average of these results as the final optimized values.

This experiment concludes that a combination of inertia weights between 0.5 and 0.8, c_1 values ranging from 0.6 to 2.0, and c_2 values between 0.6 and 1.8 results in improved accuracy.

2. Accuracy with iterations: Here, accuracy is assessed while maintaining a constant swarm size of 30 and an initial iteration count of 1000, which is then increased by factors of 1.67, 2.0, 2.67, 3.00, 5, and 10, to examine how the number of iterations impacts accuracy across all test functions. The results indicate that as the number of iterations increases, accuracy improves, reaching a maximum close to 100 % when iterations are increased to 10 times, as illustrated in figure ??.
3. Accuracy with swarm size: In this study, accuracy is evaluated across all tests by varying the swarm size, starting with 30 particles and increasing it by factors of 1.67, 2.0, 2.67, 3.00, 5, and 10, while keeping the number of iterations constant at 1000. The findings indicate that as the swarm size increases, accuracy improves to approximately 70 %.

From these experiments for finding the optimization parameters, it is concluded that an optimal combination of inertia weights between 0.5 and 0.8, c_1 values ranging from 0.6 to 2.0, and c_2 values between 0.6 and 1.8 leads to enhanced accuracy. Additionally, increasing the number of iterations relative to the number of particles is beneficial, as it provide improved accuracy while maintaining similar computational costs.

The parameters that performed well in the previous experiments with test functions are used to evaluate the rate of convergence for the Schwefel function, as shown in

figure ?? . This additional test function focuses solely on the objective function with respect to the number of iterations, as illustrated in figure ?? . The aim of this study is to identify a combination of optimization parameters that achieve a better rate of convergence, enabling optimized results to be obtained within fewer iterations. Figure ?? illustrates that higher values of inertia do not show convergence, while lower values of inertia exhibit a high rate of convergence but fail to reach the optimized value. An inertia value of 0.6 demonstrates good convergence with different c_1 and c_2 values. This analysis reveals that c_1 at 1.8 and c_2 at both 1.8 and 2.4 converge to zero, albeit slowly. In contrast, c_1 at 2.4 and c_2 ranging from 1.2 to 1.8 exhibit a good rate of convergence, reaching near zero within 100 iterations. Based on this analysis, the optimal parameters for further seismic inversion are set as inertia at 0.6, c_1 at 2.4, and c_2 between 1.2 and 1.8.

Model Parameterization

The seismic model includes physical parameters defined at densely packed grid points, often in the thousands, leading to an exponentially expanding search space that complicates the implementation of PSO. Therefore, it is essential to create a method for defining these velocity models with fewer parameters before implementing PSO, ensuring that the resulting output model can effectively serve as an initial model for FWI.

We propose a technique to define model with 1D depth-velocity profiles at sparse horizontal positions, as illustrated in Figure ?? with white vertical lines. This model is representing a layered marine environment, where the velocity gradually increases with depth, ranging from 1500 to 4700 m/s. Additionally, it features a low-velocity layer situated between two high-velocity layers. The depth of interface in terms of grid point (d_i^k), where i represents the i^{th} interface for the k^{th} depth-velocity profile, (g_i^k) denotes the rate of change of velocity between the $(i-1)^{th}$ and i^{th} interfaces, and (v_i^k) indicates the velocity of the model at the i^{th} interface. These multiple, sparsely located depth-velocity profiles are interpolated using cubic splines to create an initial model. It is also assumed that no two interfaces intersect, as this is geologically implausible. Furthermore, the search space is restricted to feasible physical parameters. With these constraints, PSO is employed to optimize the three parameters for each layer in the development of the initial model.

PSO for Preparing Initial Model

The workflow of this implementation is illustrated in Figure ?? . It shows that initial model preparation begins with a uniform 1D depth-velocity profile as the initial model, where the velocity is same as upper layer and three parameters—depth, velocity at the interface, and the rate of change of velocity—are used as input parameters initially which are set to zero. A synthetic trace for this model is generated using an 8^{th} -order spatial scheme and a 2^{nd} -order temporal scheme. The synthetic trace is

then compared to the observed data using the L2 norm, as described by equation 4. The observed data consists only near-offset data, where the major peaks are likely caused by reflectors directly beneath the shot location. The major peaks are selected from the observed data to guide the inversion process, with a focus on progressively inverting the reflectors defined by grid points. This approach falls into the category of over-parameterization as explained by (Sen Stoffa 1991), where the model is described by microlayers with thickness equal to the grid spacing. The inverted model justifying a particular peak used as an initial model for the next one. This process is repeated until the inversion successfully accounts for all the selected peaks for a shot. We allow flexibility in the timing of the selected peaks since it is not always precise to pinpoint the exact peak. The peaks resulting from multiples will not significantly impact the model because the interfaces causing these multiples have already been accounted. We sparsely select the shot locations and repeat this process for all chosen shots. Using the inverted reflectors from these shots, we create an initial model through interpolation and smoothing. This serves as the initial model for FWI.

$$O(syn^k, obs^k) = \sqrt{\sum_{i=1}^N (syn^k - obs^k)^2} \quad (4)$$

Where obs^k and syn^k indicate the observed data and synthetic data generated from the model, respectively; k refers to the shot number, and N represents the total samples.

Full Waveform Inversion

The model prepared using PSO serves as an initial model for FWI. Synthetic data is generated with this model and compared with the observed data, a process known as misfit calculation. Common methods for this calculation include the L2 norm, normalized cross-correlation function, Huber norm, and optimal transport function. The gradient of the objective function with respect to the model parameters is then calculated, which aids in updating the model. This iterative process ultimately leads to the recovery of velocity model.

ACKNOWLEDGMENTS

I wish to thank Ivan Pšenčík and Frédéric Billette for having names with non-English letters in them. I wish to thank Červený (2000) for providing an example of how to make a bib file that includes an author whose name begins with a non-English character and Forgues (1996) for providing both an example of referencing a Ph.D. thesis and yet more non-English characters.

APPENDIX A

APPENDIX EXAMPLE

```

%\documentclass[paper]{geophysics}
\documentclass[paper, revised]{geophysics}
\usepackage{cleveref} %for cref

% An example of defining macros
\newcommand{\rs}[1]{\mathstrut\mbox{\scriptsize\rm #1}}
\newcommand{\rr}[1]{\mbox{\rm #1}}
\usepackage{natbib}
\bibliographystyle{plainnat}
\begin{document}

\title{An example \emph{Geophysics} article, \\ with a two-line title}

\renewcommand{\thefootnote}{\fnsymbol{footnote}}

\ms{GEO-Example} % paper number

\address{
\footnotemark[1]BP UTG, \\
200 Westlake Park Blvd, \\
Houston, TX, 77079 \\
\footnotemark[2]Bureau of Economic Geology, \\
John A. and Katherine G. Jackson School of Geosciences \\
The University of Texas at Austin \\
University Station, Box X \\
Austin, TX 78713-8924}
\author{Joe Dellinger\footnotemark[1] and Sergey Fomel\footnotemark[2]}

\footer{Example}
\lefthead{Dellinger \& Fomel}
\righthead{\emph{Geophysics} example}

\maketitle

\begin{abstract}
  This is an example of using \textsf{geophysics.cls} for writing
  \emph{Geophysics} papers.
\end{abstract}

\section{Introduction}

```

Full Waveform Inversion (FWI) is considered one of the most efficient seismic imaging

The nonlinear relationship between synthetic data and model parameters \citep{Crase1999}

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Published implementations of these global optimization methods include a variety of a

A research also has been conducted to identify more effective global optimization met

In this study, we present the application of PSO for generating an initial model for

This paper is organized into the following sections:

- \begin{itemize}
- \item Methodology: This section provides a detailed description of the Particle Swarm
- \item Results: This section presents the experiments conducted to prepare initial mod
- \item Discussion and Conclusion: The section includes a discussion on the limitations
- \end{itemize}
- \ref{method}
- \section{Methodology}

This approach involves two steps. First, a coarse velocity model is prepared using PS

Particle Swarm Optimization (PSO) is a stochastic method developed by James Kennedy a

- \begin{itemize}
- \item $\mathbf{x}_i(t)$ be the position of particle i at iteration t .
- \item $\mathbf{v}_i(t)$ be the velocity of particle i at iteration t .
- \item $\mathbf{p}_i(t)$ be the personal best position of particle i until iteration t .
- \item $\mathbf{g}(t)$ be the global best position among all particles until iteration t .
- \item w be the inertia weight.
- \item c_1 and c_2 be the cognitive and social acceleration coefficients,
- \item r_1 and r_2 be random numbers uniformly distributed in the range $[0, 1]$.
- \end{itemize}

The velocity and position update rules for each particle are given by:

- \begin{equation}
- $$\mathbf{v}_i(t+1) = w \mathbf{v}_i(t) + c_1 r_1 (\mathbf{p}_i(t) - \mathbf{x}_i(t)) + c_2 r_2 (\mathbf{g}(t) - \mathbf{x}_i(t))$$

\label{eqn:ps0_1}

\end{equation}

\begin{equation}

```

\mathbf{x}_i(t+1) = \mathbf{x}_i(t) + \mathbf{v}_i(t+1)
\label{eqn:ps0_2}
\end{equation}

```

Where:

```

\begin{itemize}
\item \(\omega\) controls the influence of the previous velocity (inertia).
\item \(\phi_1\) and \(\phi_2\) represent the trust of the particle in itself and in the
\item \(\psi_1\) and \(\psi_2\) introduce stochasticity to the particle's movement.
\end{itemize}

```

\subsubsection{Optimization Parameters}

The updates in the Particle Swarm Optimization (PSO) algorithm are influenced by several

This contribution of different parameters for success of PSO make it is necessary to define

```

\begin{equation}
Accuracy (\%) = 100 - \left| \frac{\text{optimal value} - \text{evaluated value}}{\text{optimal value}} \right|
\label{eqn:accuracy}
\end{equation}

```

Where:

```

\begin{itemize}
\item \(\text{Optimal value}\), best possible value of the objective function.
\item \(\text{Evaluated value}\), value of the objective function at a given point in the
\item \(\text{Maximum deviation}\), largest difference between the optimized value and the
\end{itemize}

```

```

\begin{enumerate}

```

\item Accuracy with Parameters: In this experiment, optimization is conducted for all

```

%\begin{figure}
% \includegraphics[width=\paperwidth]{Fig/ackley.png}
% \caption{Ackley function.}
% \label{fig:ackley}
%\end{figure}
%\begin{figure}
% \includegraphics[width=\paperwidth]{Fig/griewank.png}
% \caption{Griewank function.}
% \label{fig:griewank}
%\end{figure}
%\begin{figure}
% \includegraphics[width=\paperwidth]{Fig/rastrigin.png}
% \caption{Rastrigin function.}
% \label{fig:rastrigin}
%\end{figure}
%\begin{figure}
% \includegraphics[width=\paperwidth]{Fig/styblinski.png}
% \caption{Styblinski-Tang function.}
% \label{fig:styblinski}

```

%\end{figure}

This experiment concludes that a combination of inertia weights between 0.5 and 0.8,

% \begin{sidewaysfigure}

% \includegraphics[width=\paperwidth]{Fig/ackley_para_vs_accuracy.jpeg}

% \caption{Optimization of the Ackley function with varying inertia weights, \((c_1)\),

% \label{fig:acc_ackley}

% \end{sidewaysfigure}

% \begin{sidewaysfigure}

% \includegraphics[width=\paperwidth]{Fig/griewank_para_vs_accuracy.jpeg}

% \caption{Optimization of the Griewank function with varying inertia weights, \((c_1)\),

% \label{fig:acc_griewank}

% \end{sidewaysfigure}

% \begin{sidewaysfigure}

% \includegraphics[width=\paperwidth]{Fig/rastrigin_para_vs_accuracy.jpeg}

% \caption{Optimization of the Rastrigin function with varying inertia weights, \((c_1)\),

% \label{fig:acc_rastrigin}

% \end{sidewaysfigure}

% \begin{sidewaysfigure}

% \includegraphics[width=\paperwidth]{Fig/styblinski_para_vs_accuracy.jpeg}

% \caption{Optimization of the Styblinski-Tang function with varying inertia weights,

% \label{fig:acc_styblinski}

% \end{sidewaysfigure}

\item Accuracy with iterations: Here, accuracy is assessed while maintaining a constant

% \begin{figure}

% \includegraphics[width=0.8\paperwidth]{Fig/iteration_vs_accuracy.jpeg}

% \caption{Accuracy variation with iterations keeping the swarm size at 30 for all test

% \label{fig:acc_itr}

% \end{figure}

\item Accuracy with swarm size: In this study, accuracy is evaluated across all test

\end{enumerate}

From these experiments for finding the optimization parameters, it is concluded that

\\

The parameters that performed well in the previous experiments with test functions are

%\begin{figure}

% \includegraphics[width=0.8\paperwidth]{Fig/schwefel.png}

% \caption{Schwefel function.}

% \label{fig:schwefel}

%\end{figure}

%\begin{figure}

% \includegraphics[width=0.8\paperwidth]{Fig/con_vs_itr.jpg}

% \caption{Objective function versus iteration for Schwefel function.}

```
% \label{fig:con_schwefel}
%\end{figure}
```

```
\subsection{Model Parameterization}
```

The seismic model includes physical parameters defined at densely packed grid points, \\

We propose a technique to define model with 1D depth-velocity profiles at sparse hori

```
%\begin{figure}
% \includegraphics[width=0.8\paperwidth]{Fig/parameterization.jpg}
% \caption{layered model.}
% \label{fig:parameterization}
%\end{figure}
```

```
\subsection{PSO for Preparing Initial Model}
```

The workflow of this implementation is illustrated in Figure \ref{fig:work_flow}. It We sparsely select the shot locations and repeat this process for all chosen shots. U

```
%\begin{figure}
% \includegraphics[width=0.5\paperwidth]{Fig/flow_chart.png}
% \caption{Work-flow.}
% \label{fig:work_flow}
%\end{figure}
```

```
\begin{equation}
0(\text{syn}^k, \text{obs}^k) = \sqrt{\sum_{i=1}^N \left( \text{syn}^k - \text{obs}^k \right)^2}
\label{eqn:l2norm}
\end{equation}
```

Where (obs^k) and (syn^k) indicate the observed data and synthetic data generated

```
\subsection{Full Waveform Inversion}
```

The model prepared using PSO serves as an initial model for FWI. Synthetic data is ge
\label{method}

```
\begin{acknowledgments}
```

I wish to thank Ivan P{\v{s}}en{\v{c}}\'{\i}k and Fr\'{e}d\'{e}ric Billette for having names with non-English letters in them. I wish to thank \cite{Cervený} for providing an example of how to make a bib file that includes an author whose name begins with a non-English character and \cite{forgues96} for providing both an example of referencing a Ph.D. thesis and yet more non-English characters.

```
\end{acknowledgments}
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\append{Appendix example}

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\append{The source of the bibliography}

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APPENDIX B

THE SOURCE OF THE BIBLIOGRAPHY

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  year = 2004
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    year   = {1996}
}

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abstract = {Full-waveform inversion (FWI) has become a popular method to estimate ela
author = {Datta, Debanjan and Sen, Mrinal K.},
doi = {10.1190/GEO2015-0339.1},
file = {:C:/Users/VIKAS/AppData/Local/Mendeley Ltd./Mendeley Desktop/Downloaded/Datt
issn = {19422156},
journal = {Geophysics},
mendeley-groups = {global_optimization},
number = {4},
pages = {R211--R223},
title = {{Estimating a starting model for full-waveform inversion using a global opti
volume = {81},
year = {2016}
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mendeley-groups = {global_optimization},
pages = {1--3},
title = {{A new parallel simulated annealing algorithm for 1 . 5D acoustic full-wavef
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abstract = {A source inversion method using very fast simulated annealing is proposed
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doi = {10.1186/BF03351837},
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issn = {18805981},
journal = {Earth, Planets and Space},
keywords = {Waveform inversion,characterized source model,effective stress,empirical
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number = {7},
pages = {571--590},
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abstract = {the large number of simulations needed to adjust the simulation parameter
author = {Mendes, Rafael and Kaelin, Bruno and Mart{\`{i}}nez-Sansigre, Alejo and Bar
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journal = {Geophysics},
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keywords = {2D,acoustic,full-waveform inversion,optimization,salt},
mendeley-groups = {global_optimization},
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pages = {64-85},
keywords = {Full-waveform inversion, Elastic, Stochastic},
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journal = {Geophysical Prospecting},
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number = {Special Issue 1},
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title = {{Comparing the performances of four stochastic optimisation methods using an
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mendeley-groups = {books/finite difference,numerical{\_}modelling},
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issn = {1365246X},
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keywords = {Inverse theory,Seismology,Waveform inversion},
number = {1},
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abstract = {Optimal transport distance has been recently promoted as a tool to measur
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issn = {19422156},
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number = {2},
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issn = {21918201},
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volume = {60},
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abstract = {},
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@article{Brossier2016,
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title="Particle Swarm Optimization",
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year="2016",
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