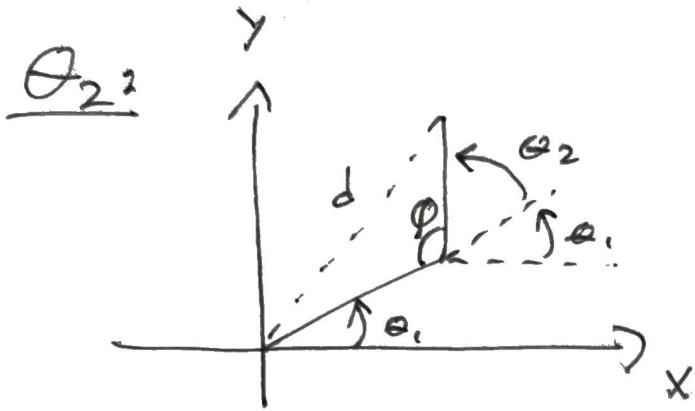


$$X = L_1 \cos(\theta_1) + L_2 \cos(\theta_1 + \theta_2)$$

$$Y = L_1 \sin(\theta_1) + L_2 \sin(\theta_1 + \theta_2)$$

IK:



cos satser:

$$d^2 = L_1^2 + L_2^2 - 2L_1L_2 \cos(\phi) \quad (1)$$

$$d = \sqrt{x^2 + y^2}, \quad \phi = 180^\circ - \theta_2$$

$$(1) \quad \cos(\phi) = \frac{L_1^2 + L_2^2 - x^2 - y^2}{2L_1L_2}$$

$$\phi = \arccos\left(\frac{L_1^2 + L_2^2 - x^2 - y^2}{2L_1L_2}\right)$$

$$180^\circ - \theta_2 = \arccos\left(\frac{L_1^2 + L_2^2 - x^2 - y^2}{2L_1L_2}\right)$$

$$\theta_2 = 180^\circ - \arccos\left(\frac{L_1^2 + L_2^2 - x^2 - y^2}{2L_1L_2}\right)$$

Actually \pm , there are 2 solutions

IK:

Q₁: From FK: $X = L_1 C_1 + L_2 C_{1+2}$
 $Y = L_1 S_1 + L_2 S_{1+2}$

Trig identities:

$$X = L_1 C_1 + L_2 C_1 C_2 - L_2 S_1 S_2 = L_1 (L_1 + L_2 C_2) - L_2 S_1 S_2$$

known from before

$$Y = L_1 S_1 + L_2 S_1 C_2 + L_2 S_2 C_1 = S_1 (L_1 + L_2 C_2) + L_2 S_2 C_1$$

with $a = L_1 + L_2 C_2$, $b = L_2 S_2$:

$$X = L_1 a - b S_1 \quad (1)$$

$$Y = L_1 b + a S_1 \quad (2)$$

$$(1) \quad L_1 = \frac{X + b S_1}{a} \quad (3)$$

$$(2) \text{ \& } (3) \quad b \left(\frac{X + b S_1}{a} \right) + a S_1 = \frac{bX + b^2 S_1}{a} + a S_1 = X$$

$$\Rightarrow S_1 = \frac{Ya - bX}{b^2 + a^2} \quad (4)$$

$$(3) \text{ \& } (4) \quad L_1 = \frac{X + b \left(\frac{Ya - bX}{b^2 + a^2} \right)}{a} = \dots = \frac{Xa + bY}{b^2 + a^2}$$