

DESIGN, FABRICATION, AND CHARACTERIZATION OF AN ACTIVELY-CONTROLLED
MACH 5 TO 8 WIND TUNNEL

A Dissertation Proposal

by

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NOMENCLATURE

Acronyms

ACE	Actively Controlled Expansion
AIAA	American Institute of Aeronautics and Astronautics
AGARD	Advisory Group for Aerospace Research and Development
BCDC	Bush Combat Development Complex
CAD	Computer Aided Design
CFD	Computational Fluid Dynamics
CNC	Computer Numerical Control
FEA	Finite Element Analysis
FEDC	Fischer Engineering Design Center
FOS	Factor of safety
HMI	Human Machine Interface
M6QT	Mach 6 Quiet Tunnel
MATLAB	Matrix Laboratory
MOC	Method of characteristics
NAHL	National Aerothermochemistry and Hypersonics Laboratory
NASA	National Aeronautics and Space Administration
PID	Proportional Integral Derivative
PLC	Programmable Logic Controller
PSIA	Pounds per Square Inch (Absolute)
RMS	Root Mean Squared
TAMU	Texas A&M University
US3D	Unstructured 3D CFD

Common Symbols

A	Area
A^*	Nozzle throat area
F	Isentropic Relation Function
K	Proportional Gain Constant
M	Mach number
R	Gas constant
Re'	Unit Reynolds number, $\rho U / \mu$
P	Static Pressure
T	Static Temperature
T_d	Derivative Time Constant
T_i	Integral Time Constant
U	Streamwise Velocity
a	Speed of sound
h^*	Nozzle throat height
\dot{m}	Mass flow rate

Greek Symbols

α	Shock angle
ρ	Density
γ	Ratio of specific heats (c_P / c_V)
μ	Dynamic viscosity
θ	Wedge-deflection angle
ξ	Pressure ratio across oblique shock

Common Subscripts

0	Stagnation condition
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∞	Freestream condition
set	Set condition for PID reference
D	Detachment condition
V	Von Neumann condition

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1. INTRODUCTION & LITERATURE REVIEW

1.1 Introduction

In recent decades, the continual improvement in hypersonic aerodynamics has emphasized the need for advancements in wind tunnel ground testing capabilities [1]. Conventional hypersonic wind tunnels rely on distinct fixed nozzle contours to accelerate the flow to the desired Mach number. This approach fixes the Mach number so it only provides a particular flow regime for experiments. Recognizing this, there is a clear need for a continuously variable Mach-number nozzle designed to overcome the limitations of conventional wind tunnels and enable more advanced dynamic hypersonic research.

The objective of this work is to introduce a continuously variable and actively controllable Mach-number nozzle. By dynamically adjusting the throat height and thereby the Mach number throughout the wind tunnel runs, the variable conditions experienced by hypersonic vehicles during different flight trajectories can be effectively modeled. This capability would enable the advancement of ground testing for a more comprehensive understanding of dynamic hypersonic flight and associated phenomena. Furthermore, the active control capability will increase experimental efficiency by allowing measurements at different Mach numbers within a single run and introduce the ability to fine tune the Mach number for improved data quality. However, this variable Mach number capability does introduce the challenge of maintaining desired Reynolds numbers, so feedback control will also be explored for the Reynolds number to counteract this and improve the overall experimental control.

The Actively Controlled Expansion (ACE) wind tunnel at Texas A&M University (TAMU) has served as a workhorse in hypersonic research since 2010 [2–8], and is due for improvements to meet the growing demand of hypersonics research. Although the facility was initially designed to facilitate the continuous variation of Mach number, the mechanical implementation ultimately proved to be cumbersome to adjust. Consequently, the nozzle has remained fixed at Mach 6 for

the majority of the tunnel's operation. Additionally, despite the geometry being fixed, the Mach number actually varies throughout a run by up to 5%. Considering this, it is apparent that an update to the ACE design could be beneficial in order to realize the full potential of the variable Mach number capability.

1.2 Research Objectives

The objectives of this research aim to lay the foundation for continuously variable and actively controlled Mach number capabilities at the National Aerothermochemistry and Hypersonics Laboratory (NAHL). Doing so will expand the current capabilities within the lab for more advanced hypersonic aerodynamics experiments. The existing ACE facility will be upgraded to achieve true active control and to potentially produce low-disturbance flow for higher Reynolds numbers. Its successor, ACE2.0, that is the subject of this work, will employ a feedback-control system with servo motors, linear actuators, and various instrumentation to enable the accurate and continuous variation of Mach number by changing the throat height. Additionally, active feedback-control of the Reynolds number will be developed and potentially implemented.

Once fabricated and calibrated, the ACE2.0 facility will provide:

1. Improved experimental control and efficiency

An active throat height control system will be implemented to enable active feedback-controlled Mach number variation and selection for Mach trajectories and accurate set points. The feedback aspect will attempt to control the Mach number to within 0.5% of the set value. An active control scheme will also be developed to enable feedback-controlled Reynolds number variation and selection that responds to changes in Mach number and stagnation temperature for accurate sweeps and set points. This will allow both constant or varying Reynolds number during a Mach trajectory. The Reynolds number controller will be fully designed but may not be implemented due to constraints.

The control of both of these parameters will yield improved experimental efficiency with a new capability to explore multiple flow configurations within a single run. Besides enhanc-

ing efficiency, the Mach number and Reynolds number control will enable more robust uncertainty quantification and more dynamic experiments that were not possible before. Both of these capabilities are demonstrated in the next objectives.

2. Characterization of freestream flow uniformity and disturbance levels throughout the nozzle and uncertainty quantification of flow parameters

A flow survey of the nozzle exit plane and centerline will be conducted to measure the freestream flow uniformity and disturbance levels throughout the nozzle and characterize its performance. This will validate the design and manufacturing of the nozzle and settling chamber and provide a basis for the quality of data gathered in future experiments. A rigorous uncertainty analysis will be performed to quantify the systematic and random uncertainty of the measured flow parameters P , P_0 , and T_0 and the resulting values of Mach number, M , and unit Reynolds number, Re' . This will establish the baseline uncertainty for the freestream flow parameters and enable improved data quality for future experiments. In order to fully characterize the tunnel behavior while actively controlled, an investigation of the potential existence of hysteresis phenomena will be performed. If discovered, any hysteresis will be characterized to fully understand the dynamics of the freestream flow as each parameter is varied.

3. Demonstration of Mach trajectory operation and potential hysteresis in a proof of concept experiment

The capabilities of ACE2.0 will be demonstrated in an experiment that will showcase shock wave interactions between two wedges during a Mach trajectory. This experiment will explore a well-known hysteresis in the transition from a regular reflection to a mach reflection and the ability to produce the phenomenon in this facility.

These objectives will effectively validate and demonstrate the capabilities and merit of the new ACE2.0 facility. In addition, the standard operating procedures for ACE2.0 will be updated to reflect the best practices deduced throughout the completion of these objectives. The resulting

control procedures and interface will be straightforward and well documented so that future users can easily learn to effectively operate the facility. The documentation will not only enhance the accessibility of ACE2.0 for subsequent research endeavors but also contribute to the broader scientific community by providing a robust framework for effective wind tunnel control and dynamic hypersonic vehicle aerodynamics exploration.

1.3 Literature Review

The literature review for this dissertation includes four parts related to hypersonic variable Mach-number wind tunnels and according to the above objectives: (1) variable mach number nozzle design, (2) parameter control, (3) flow quality characterization and uncertainty quantification, and (4) hysteresis in hypersonic flows. This review will discuss articles that establish the most current knowledge base and techniques in the relevant areas of hypersonic wind tunnel research.

1.3.1 Variable Mach-Number Wind Tunnels

Variable Mach number nozzles have been explored in many configurations since the 1950s such as interchangeable fixed-block, plug-type, asymmetric sliding blocks, tilting plate, fully flexible, and hinged/flexure [9]. Each of these designs have varying degrees of flow quality, cost effectiveness, and experimental efficiency that must be considered. Only the fully flexible and flexure designs maximize experimental efficiency without sacrificing flow quality. Of these two, the flexure design minimizes costs by reducing mechanical complexity and supporting structure. Therefore, the flexure design is the optimal choice considering these criteria.

The flexure type nozzle was first proposed in 1955 by Rosen [10] and improved upon separately by Erdmann in 1971 [11] and Rom and Etsion in 1972 [11,12] in order to minimize the mechanical complexity. This simple nozzle design operated by a single jack greatly reduces manufacturing and controls costs and allows for greater flexibility in active control to quickly and continuously vary the Mach number to model dynamic supersonic vehicle flight.

In the last decade, many variable mach number supersonic wind tunnels have been manufactured due to increased demand of hypersonic flight research. The majority of these are fully flexible

or flexure nozzle designs with varying implementations of actuation and control [13–21]. All of these facilities were developed to study vehicle flight trajectory and the hysteresis phenomenon therein.

The ACE tunnel at the TAMU NAHL the facility of interest for this work, has been in operation since 2010 [2–4]. The nozzle is a flexure type that produces Mach 5 to 8 flow in a 9 inch by 14 inch test section. The flexure design is effective in achieving the change in throat height, but it cannot be done continuously and actively during a run. This is the primary issue to be addressed in this work. An extensive discussion of the existing ACE tunnel is provided in the next chapter.

1.3.2 Parameter Control

A variable Mach number facility requires effective control schemes for the controllable parameters A^* , P_0 , T_0 , and the resulting Mach number, M , and unit Reynolds number, Re' , in order to vary each parameter independently and accurately. This control problem, acknowledged as early as the 1980s, prompted the development of diverse solutions implementing the various areas of control theory such as optimal control [22, 23], state feedback control, mathematical model prediction control, preprogrammed controllers [24], and PID control [25–27].

In recent years, researchers at numerous variable Mach number facilities have embraced advanced intelligent control methods. Techniques such as fuzzy logic, genetic algorithms, neural networks, adaptive control or gain scheduling, and their combinations have been applied [14, 28]. The methods that will be explored in this research are those of Hwang et al. [23], Matsumoto et al. [24], Ilić et al. [26], and Shahrababaki et al. [14] as they each introduce the different advantages and challenges of each control technique.

Hwang et al. [23] developed a robust LQG/LTR (Linear Quadratic Gaussian with Loop Transfer Recovery) controller enhanced by an anti-integrator windup and a modified Smith predictor to overcome unavoidable modeling errors, uncertainties, and time-delay effects. This controller demonstrated a faster stabilization and exhibited fewer oscillations in comparison to its PID counterpart. Given its superior performance, it presents an appealing prospect for implementation in ACE2.0, and a detailed exploration of this controller will be undertaken in a subsequent chapter.

Matsumoto et al. [24] took a simplified approach by replacing an existing real-time PID controller with a preprogrammed controller to avoid input time delays. This was advantageous for the facility used in that work because the run time was not much longer than the time delay for the PID controller to stabilize. This is the most straightforward approach to obtain specific constant or dynamic trajectories of multiple input parameters but it has limitations. The controller must have a new program for each individual desired parameter set condition or path, and each program must be iterated to minimize errors. Considering these limitations, a preprogrammed controller will be a backup option that will only be explored if necessary. Considering the longer run times of ACE2.0, a PID controller can be implemented with ample time to stabilize.

Ilić et al. [26] implemented a cascade nonlinear feedforward-feedback PID controller as a combined system to enhance a standard single-loop PID. The system's set point reference tracking is improved by the feedforward-feedback architecture, and the disturbance rejection is improved by the cascade architecture. With these two architectures combined in one multi-loop controller, large transient overshoots are eliminated, set point settling times are decreased, and the overall accuracy of the controlled parameters is maximized. Once again, the improved performance of this controller makes it another appealing prospect for ACE2.0, which will be discussed later.

Shahrbabaki et al. [14] utilized an artificial neural network and fuzzy logic to enhance a conventional PD controller to handle the complex nonlinearity of the variable mach number wind tunnel flow parameters. The advantages of fuzzy logic include its simplicity and adaptability of introducing new control rules to handle imprecise data, uncertainty, and unmodeled dynamics. The combined advantage that Shahrbabaki et al. explores pertains to the utilization of the neural network to develop the membership functions for the fuzzy logic controller. They designed and trained a feed-forward multilayer perceptron neural network according to the database from the mathematical model of the wind tunnel behavior in order to develop the optimal membership functions. This method will only be explored further for ACE2.0 if the methods of Hwang et al. or Ilić et al. do not yield sufficient performance.

1.3.3 Flow Quality Characterization and Uncertainty Quantification

The primary references regarding flow quality characterization will be the recent AIAA articles by Chou et al. [29] and Duan et al. [30] on hypersonic wind tunnel freestream disturbance measurements. These provide the latest measurement processes and procedures and reference over 50 publications on relevant topics from recent decades. In addition to these two references, a decade of NAHL experience and best practices will guide the characterization of ACE2.0 upon its fabrication and initial shakedown. Key NAHL ACE references on the freestream characterization of ACE are the AIAA paper by Semper et al. [5] and dissertations by Mai [6], Neel [7], and Leidy [8]. Additionally, Leidy performed an uncertainty analysis in the existing ACE tunnel that will provide a baseline reference for the uncertainty quantification for ACE2.0.

The primary references for the uncertainty quantification in this research will be the NASA report by Stephens et al. [31], the forthcoming AIAA Guide on Uncertainty Quantification [32], and the dissertation by Curriston [33]. The methodology in this NASA report combines the techniques of the prevalent literature on the subject from the last few decades to quantify the uncertainty of the flow parameters in a supersonic wind tunnel. Curriston's work provides a secondary reference as he thoroughly demonstrates this methodology and that of the forthcoming AIAA guide as a case study in a low speed wind tunnel. The approach described in these references includes a sophisticated treatment of systematic uncertainty using a Mont Carlo method combined with direct comparison of replicate data to characterize random error. Curriston [33] also extensively treats pre-test and real-time uncertainly quantification to enhance test campaign quality control and decision support.

1.3.4 Hysteresis in Hypersonic Flows

A review of the literature on hypersonic flow hysteresis yielded many publications discussing shock interactions and inlet start/unstart processes. The inlet start/unstart literature will not be referenced directly in this work but will be valuable for future research in ACE2.0. Focusing on the shock interactions, Hornung et al. [34] first predicted hysteresis in the transition from regular reflection to Mach reflection, but they were unable to experimentally produce the hysteresis

effect [35]. Recent literature reveals numerical investigations easily reproduce shock interaction hysteresis [36, 37], while experimental investigations prove more difficult due to the freestream noise in conventional facilities [16, 38]. The two processes that produce hysteresis in the shock interactions are wedge-angle variation and Mach-number variation [39]. Since it is significantly more complex to vary the Mach number, most experimental results are found by the wedge-angle-variation-induced hysteresis in open-jet, low-noise wind tunnels [40–45]. Some research groups with variable Mach number tunnels have attempted to reproduce shock interaction hysteresis experimentally by varying the Mach number, but they have all been unsuccessful due to the presence of high freestream disturbance levels [15, 46]. Methodologies from the numerical and experimental literature on Mach-number-variation-induced hysteresis will be studied in order to attempt to reproduce shock interaction hysteresis in ACE2.0.

2. DESIGN AND FABRICATION OF ACE2.0

2.1 Background and Motivation

As described above, the existing ACE tunnel was designed and manufactured between 2009 and 2010 and began operating in 2010 [2–4]. The variable Mach number capability is provided by a thin flexure portion near the end of the nozzle that allows the throat height to be varied from approximately 0.04 to 0.36 inches, which enables the test-section Mach number to be varied from Mach 5 to 8. Schematic of the full tunnel and the nozzle and settling chamber are shown in Figures 2.1 and 2.2.

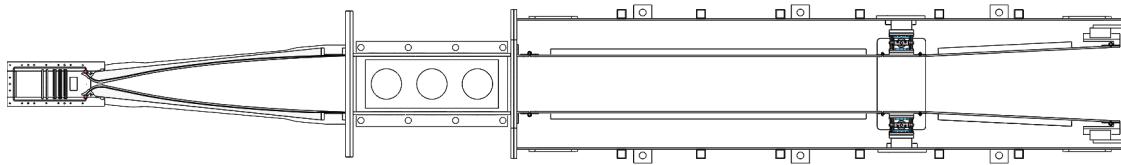


Figure 2.1: ACE tunnel schematic

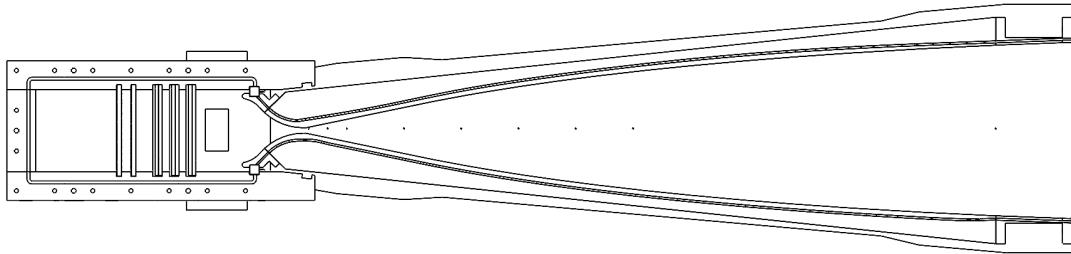


Figure 2.2: ACE nozzle and settling chamber

The original motivation for the present redesign was to remanufacture the nozzle to remedy the premature laminar-to-turbulent transition, which is discussed in the next section. However, as

the work progressed, it became apparent that this redesign was the best opportunity to improve the nozzle and settling chamber to also enable active control. This progression and the redesign process is detailed throughout this chapter.

2.1.1 ACE Turbulent Transition

ACE performance data [5–8] shows that below a unit Reynolds number of $Re' = \rho U / \mu \approx 3 \times 10^6 / \text{m}$ the RMS pressure fluctuations in the test section are less than 1%, and that above this unit Reynolds number the pressure fluctuation levels significantly increase. It was desired to increase the unit Reynolds number at which laminar flow can be maintained, so the mechanism causing laminar-to-turbulent transition of the nozzle boundary layers had to be determined. The hypothesis and supporting data regarding the pressure fluctuation levels increase and how it might be delayed to higher unit Reynolds numbers is summarized below.

Five primary suspects for transition were identified:

1. A known manufacturing surface discontinuity at the nozzle throat
2. Sidewall mushroom vortices
3. Görtler vortices
4. Freestream turbulence in the incoming flow and/or upstream boundary layer
5. Wall roughness or waviness

The sections below evaluate each of these possibilities and support the conclusion that the throat discontinuity (1) is the most likely reason for the increased pressure fluctuations above $Re' \approx 3 \times 10^6 / \text{m}$. This conclusion is supported by pitot surveys, method-of-characteristics line tracing, and CFD simulations.

The throat discontinuity is the result of a decimal truncation error of about 0.0003 inches at the interface connecting the subsonic curve to the supersonic MOC contour in the original design files. The resulting discontinuity is shown in Figure 2.3. The artifact carried forward through the CNC machining and is present on the physical nozzle throat.

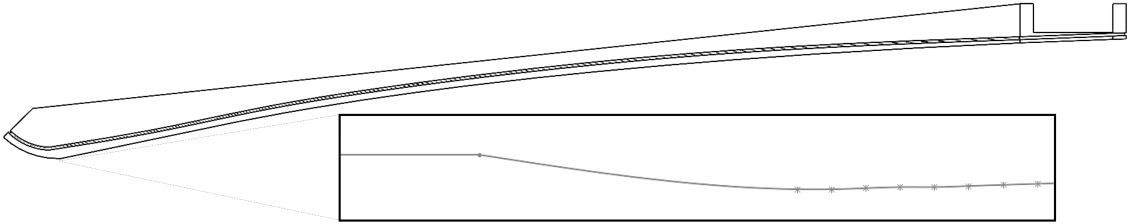


Figure 2.3: ACE throat discontinuity

Sidewall mushroom vortices (2) and Görtler vortices (3) would lead to transition too far downstream from the throat to be responsible for the pressure fluctuation levels increase. Incoming freestream turbulence (4) and wall surface quality (5) are potential causes of poor flow quality in all supersonic tunnels and are included for completeness. The specific mechanism by which these would cause transition is not known. While item 4 and 5 are not the primary suspects for the pressure fluctuation levels increase, improving these conditions will be addressed in the redesign intended to extend laminar flow to higher unit Reynolds numbers.

ACE Nozzle Noise Surveys

Three recent pitot surveys have been conducted in the ACE tunnel. The first by Mai in 2014 [6] revealed transition occurring around $Re' \approx 3 \times 10^6/\text{m}$, as shown in Figure 2.4. The same result was found by Neel in 2019 [7] shown in Figure 2.5 that transition occurs at this Re' value at a location 6 inches upstream of the nozzle exit. As part of this work, a final pitot survey in ACE was conducted to determine whether the pressure fluctuation levels increase occurred at different Re' values at positions farther upstream in the nozzle. It was found that pressure fluctuation levels increase at the same $Re' \approx 3 \times 10^6/\text{m}$ at a measurement location 24 inches upstream of the nozzle exit. These results in Figure 2.6 align with Mai's and Neel's data and clearly establish that the Reynolds number at which pressure fluctuation levels increase is the same at all locations in the nozzle. This suggests that transition is not moving upstream through the nozzle as Reynolds number is increased, as might be expected for typical boundary-layer instability processes.

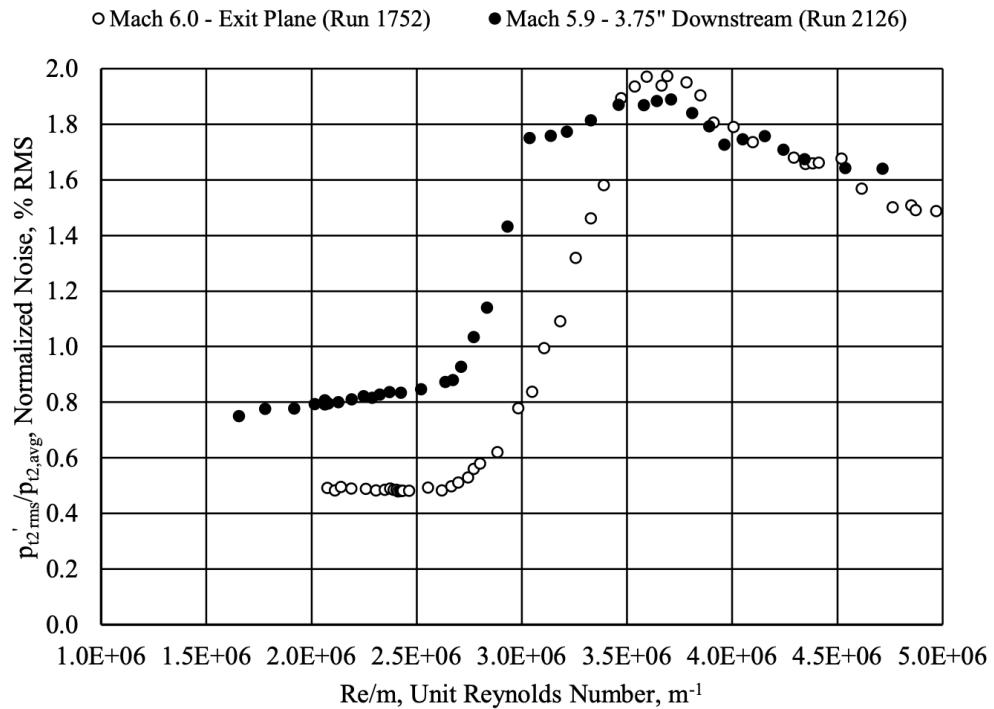


Figure 2.4: ACE freestream pressure fluctuations in the nozzle exit plane as measured in 2014 [6]

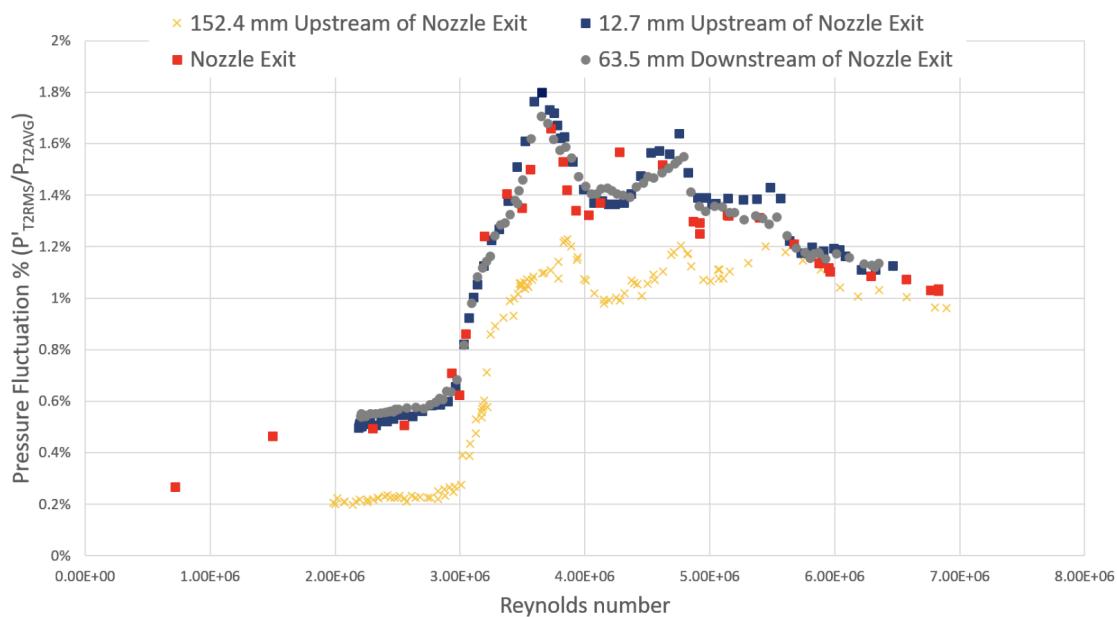


Figure 2.5: ACE freestream pressure fluctuations at various locations as measured in 2019 [7]

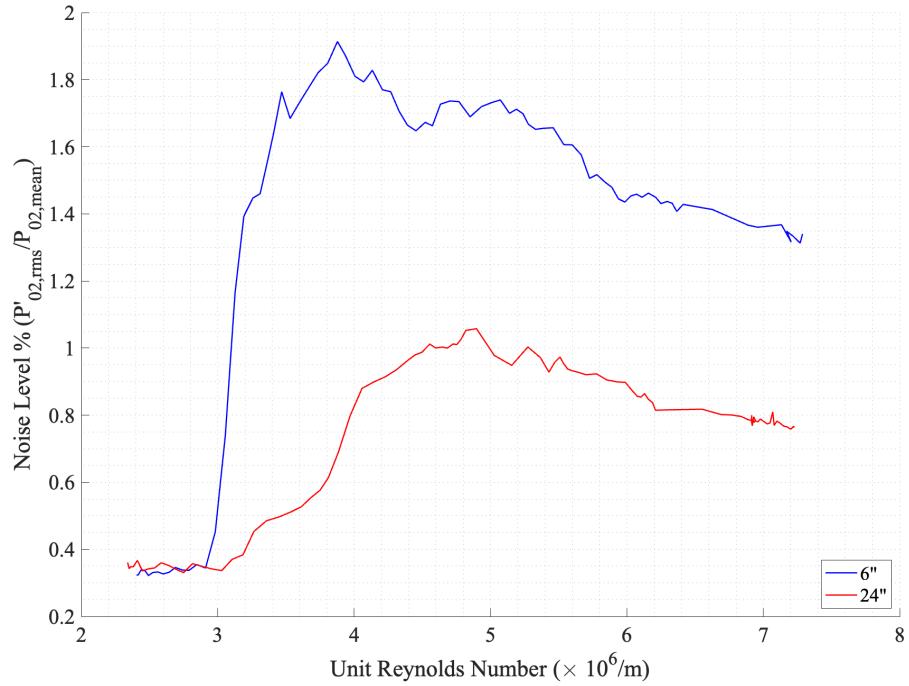


Figure 2.6: ACE freestream pressure fluctuations at 6 inches and 24 inches upstream of nozzle exit as measured in 2024

Suspect Mechanism Conclusions

The pressure fluctuation levels revealed the Re' value at which transition occurs but not the transition mechanism. The two mechanisms that were extensively investigated at the start of this work were sidewall mushroom vortices and Görtler vortices. Sidewall mushroom vortices arise from the pressure distribution in the low momentum flow in the sidewall boundary layers. The flow at the centerline expands to the test section pressure ahead of the top and bottom curved walls. The flow at the top and bottom lags behind the centerline flow with a higher pressure to create a vertical pressure gradient that introduces a secondary vertical flow in the sidewall boundary layers that flows from the corners to the centerline [47]. CFD simulations by Kocian (unpublished) show the sidewall mushroom vortices beginning to form approximately 24 inches upstream of the nozzle exit shown in Figure 2.7.

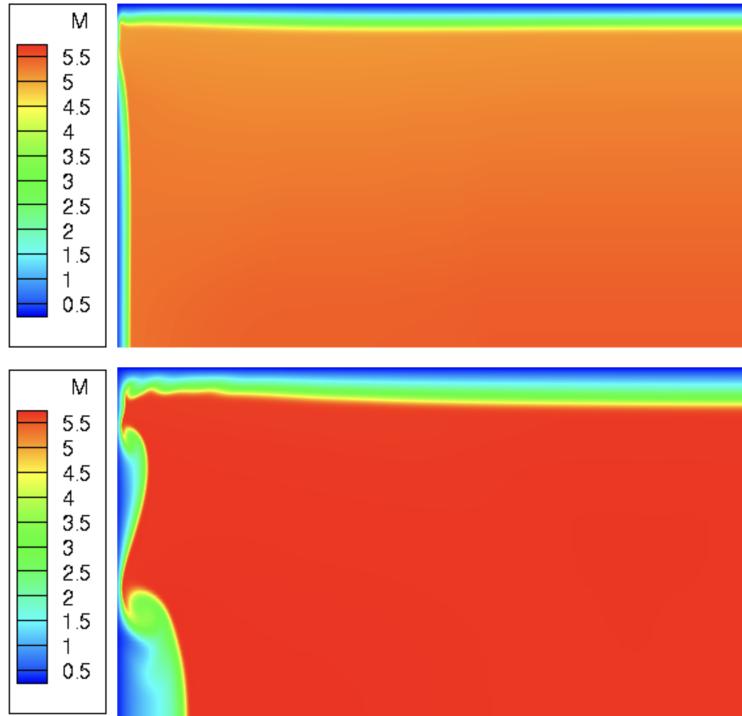


Figure 2.7: Sidewall mushroom vortex formation (upper quarter) at 24 inches upstream of nozzle exit (top) and at nozzle exit (bottom)

Görtler vortices are counter-rotating streamwise vortices that occur in boundary layers on concave surfaces [48]. To estimate where these may lead to transition, a CFD basic state simulation and N-factor analysis was performed by Kocian in 2022 (unpublished). The results, shown in Figures 2.8 and 2.9, indicate that Görtler vortices could induce transition around 8 inches from the nozzle throat.

The origin of the noise measured farthest upstream of the nozzle exit was determined by tracing characteristic lines from the measurement location at the centerline upstream to the wall. Both the side view and top view of this are shown in Figure 2.10. This was accomplished by choosing the characteristic output by the MOC code that intersects the centerline closest to the measurement point of 24 inches and tracing it back to its origin at the wall. The origin of the measured noise from the top view is upstream of the throat where sidewall mushroom vortices are not relevant, and the origin of the noise from the side view is on the straight section of the nozzle where Görtler is

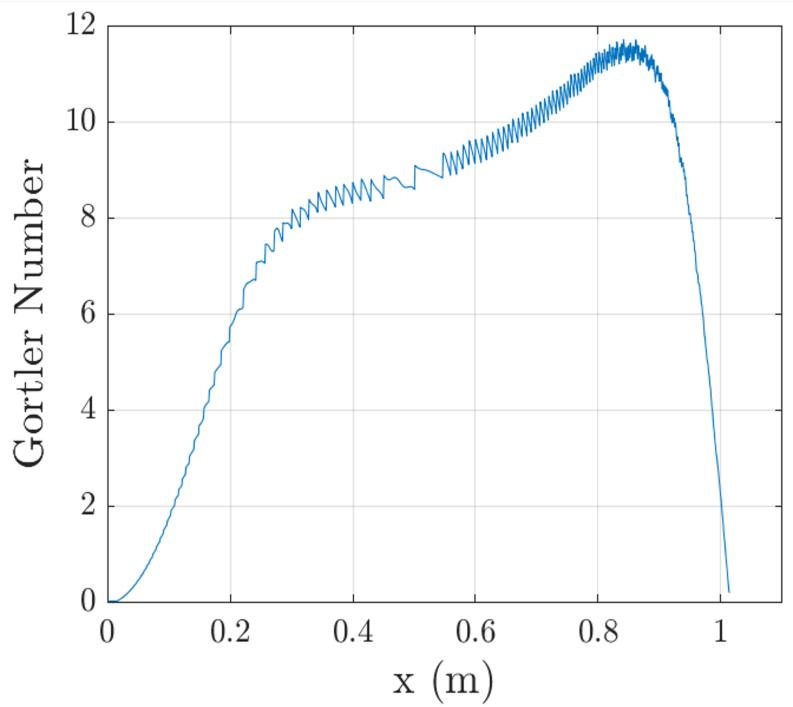


Figure 2.8: Görtler number from ACE nozzle CFD

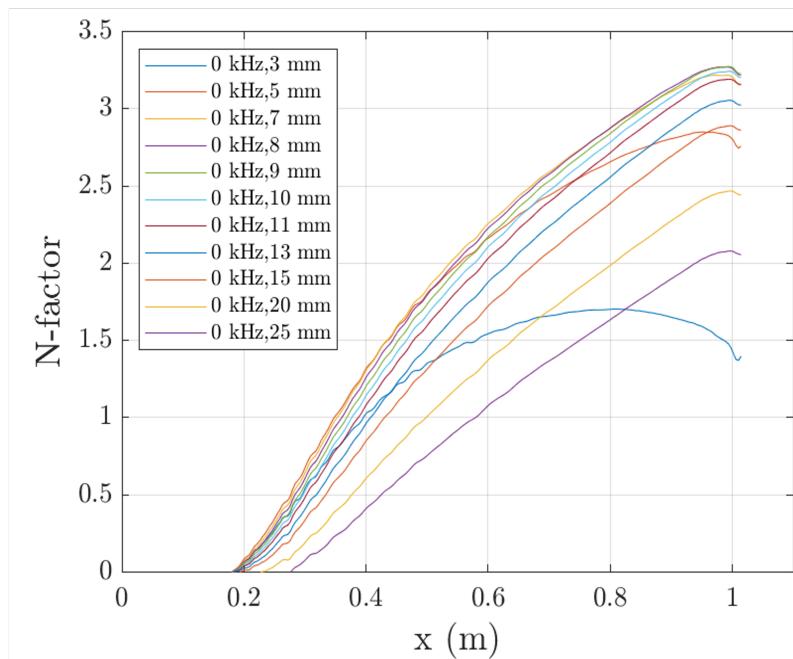


Figure 2.9: N-factors for Görtler in ACE nozzle

not relevant. While both sidewall vortices and Görtler vortices can play some role in transition in planar nozzles, they are no longer considered suspects for the pressure fluctuation levels increase at unit Reynolds numbers above $3 \times 10^6 / \text{m}$.

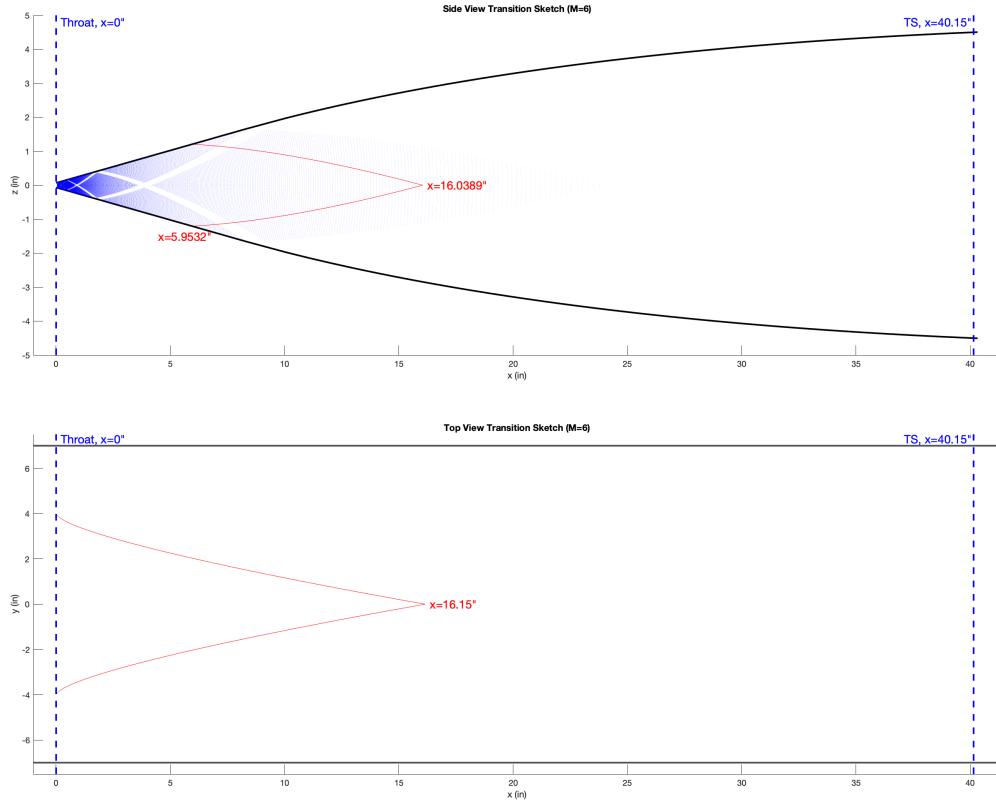


Figure 2.10: Mach lines for noise measured at 17" upstream on nozzle exit

Following the above conclusions and recommendations, the most likely reason the pressure fluctuations increase is laminar-to-turbulent transition due to a surface discontinuity at the throat. This conclusion is supported by pitot surveys, CFD, and method of characteristics line tracing described above. The remaining suspect mechanisms are still important to note and address in the redesign of the ACE tunnel.

Design Recommendations

The following improvements are recommended to maintain laminar flow above $Re' \approx 3 \times 10^6/m$:

1. Second-derivative-smooth subsonic-to-supersonic throat transition to eliminate nozzle throat discontinuity
2. Continuous curvature with analytical functions to eliminate waviness and surface discontinuities
3. Enhanced surface polishing to minimize surface roughness
4. Improved settling chamber design to maximize flow uniformity and minimize freestream turbulence upstream of the nozzle throat

One recommendation that is outside the scope of this work is to incorporate subsonic boundary layer suction to greatly reduce the incoming noise and potentially make ACE2.0 a "quiet" facility. Boundary layer suction is quite complex to effectively implement, but it will be accommodated for in the design in case it is explored in the future.

2.2 ACE2.0 Design

Following these recommendations, the nozzle will be redesigned and remanufactured to meet specific requirements that will ensure the best performance and potentially expand the laminar Reynolds number range. The decision to remanufacture the nozzle presents an opportunity to revise the nozzle and settling chamber design to achieve true active controllability, properly embodying the "ACE" name.

The rest of the chapter details the planned improvements to the ACE tunnel and specific design requirements that will achieve those improvements. In addition to a new nozzle, the settling chamber will also be redesigned to ensure the uniformity and reduce the turbulence of the flow into the nozzle. These improvements are to achieve the goal of increasing the unit Reynolds number at which laminar nozzle flow is maintained.

2.2.1 Design Requirements

ACE2.0 will maintain many characteristics while improving some, so many requirements are the same as the original ACE design. The new tunnel will still produce uniform Mach 5 to 8 flow in the 9 inches by 14 inches test section, withstand a total temperature of 530 K, and maintain a minimum engineering factor of safety (FOS) of 1.5 when operating at a total pressure of 200 psia.

Nozzle Requirements

The current ACE nozzle successfully produces uniform Mach 5 to 8 flow in its core. In order to maintain this good performance and not introduce unknown parameters, the new nozzle will retain a very similar contour with slight improvements. The requirements that remain the same are that the nozzle must produce uniform flow for the entire Mach range, achieve maximum height deflection with a minimum FOS of 1.5, and prevent leaks up to 200 psia.

The improvements to the nozzle and associated requirements will be a contour with continuous 1st and 2nd derivatives that is specified by analytical functions that will eliminate discontinuities and truncation error and a maximum allowable stress less than or equal to that found in the current ACE flexure at maximum deflection.

Settling Chamber Requirements

The current ACE settling chamber design provides multiple opportunities to improve flow conditioning and ease of maintenance. The new settling chamber design will increase the length and height and allow for variable aerogrid/screen configurations. The requirements that remain the same are low freestream turbulence, thin stable wall boundary layers, maximum uniformity, and preventing leaks at a pressure of 200 psia. The implementation of these requirements will be improved in the new design to achieve improved incoming flow into the nozzle.

Following Reshotko et al. [49], the length of the settling chamber shall accommodate a separation of 250 characteristic mesh sizes between screens allowing for adequate turbulence decay. The aerogrids will have a hexagonal perforation pattern to increase porosity and decrease pressure loss. The number of aerogrids and screens shall be variable to allow for future flow conditioning

experiments. The inlet shall include a baffle system that will provide an acceptable initial distribution and mixing of the air received from the high-pressure inlet piping. The overall design will accommodate the option for future boundary layer suction slots.

A settling chamber height of 6 inches was chosen to keep the velocity as slow as possible without going below 10 ft/s for the majority of the Mach number range. Pope and Goin [50] describe that this minimum prevents thermal convection vortices from dominating the flow at the walls. The interior of ACE2.0 will also be heated prior to the start of the run to help avoid thermal gradients.

2.2.2 Nozzle Contour Codes

The multiple reflections method-of-characteristics (MOC) Fortran script by Bowersox that produced the ACE nozzle contour was used for the new nozzle contour. In order to achieve continuous first and second derivative continuity, a section of the code was modified to produce a fourth-order expansion section instead of the original second-order curve. This allowed the expansion section to match the curvature of both the subsonic section and the straight section. The code modification is included in Appendix A, and a comparison of the original quadratic and the new quartic expansion sections is shown in Figure 2.11. In this figure, the ACE contour is directly from the MOC points and the ACE2.0 contour is specified by an analytic fourth-order polynomial. The waviness of the MOC points can be seen here, emphasizing the need to define the entire nozzle with analytic functions.

After the MOC points were produced by the Fortran script, they were imported into a MATLAB script to fit with analytic functions. The subsonic curve is given by a fifth-order polynomial with six boundary conditions of the settling chamber and throat heights and zero slope and curvature at both the start and throat. The straightening section is given by a function found using the `lsqcurvefit` function with a combination of power and logarithmic functions in MATLAB. The equations for each section are given in Appendix A.

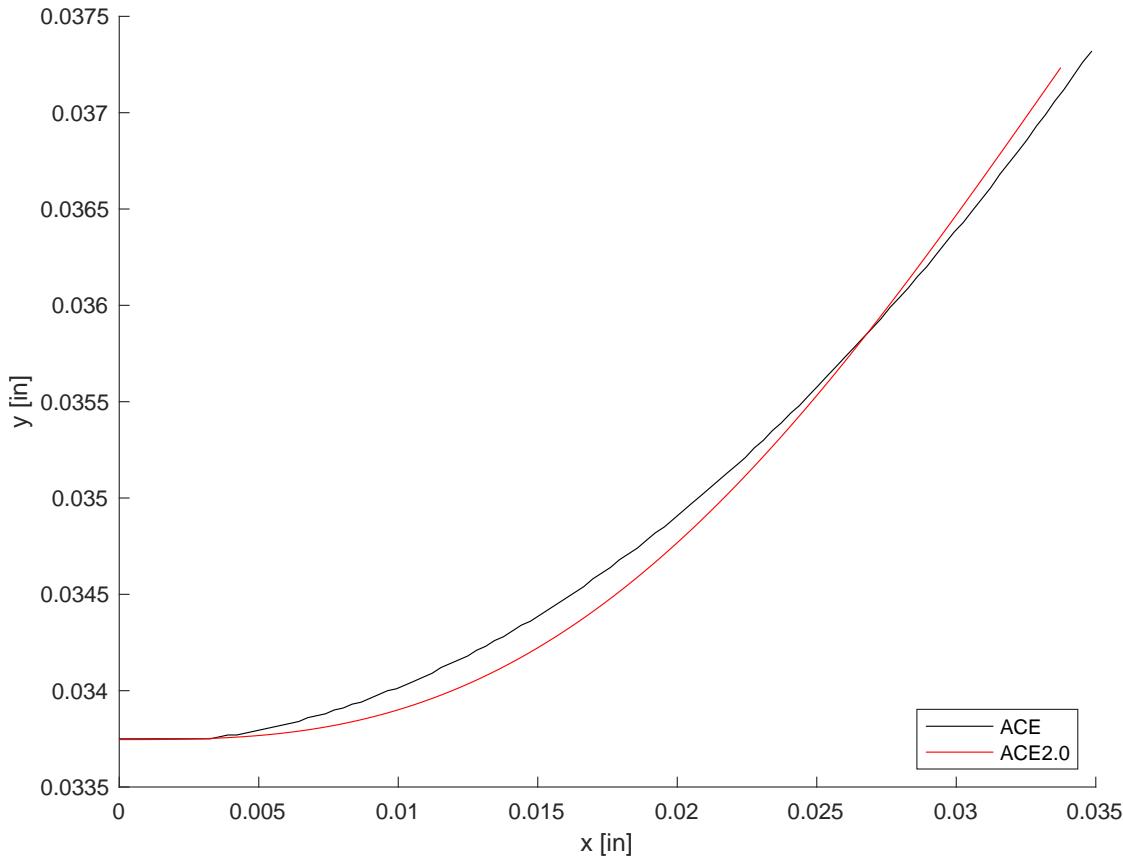


Figure 2.11: Comparison of ACE (quadratic) and ACE2.0 (quartic) expansion at throat

2.2.3 CFD

In order to verify the above nozzle contour performance compared to the original ACE contour, both contours were simulated in 2D CFD. First, a mesh was created in Pointwise for each contour with 400 equally spaced columns of cells in the x-direction. Each column had the spacing scaled to accurately capture the boundary layer with the smallest cell height around 4×10^{-6} inches at the curved wall and the largest around 0.2 inches at the centerline as seen in Figure 2.12. The CFD analysis was performed at a time when the settling chamber design was still at a height of 9 inches, so the analysis will be performed again to validate the 6 inch.

After creating a mesh for each, they were simulated using US3D on the Texas A&M supercomputer, Grace. A sample of the results is shown in Figure 2.13. The full ACE2.0 CFD input

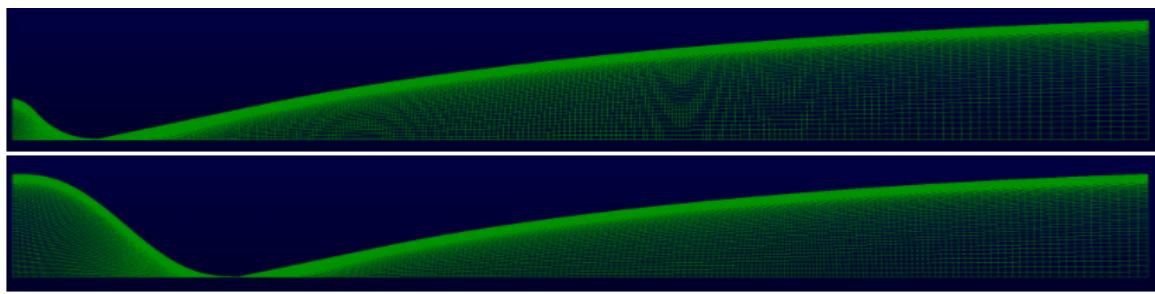


Figure 2.12: Mesh in Pointwise for ACE (top) and ACE2.0 (bottom) nozzle contours

conditions and results compared to ACE will be provided in a future appendix after performing the revised simulations in future work.

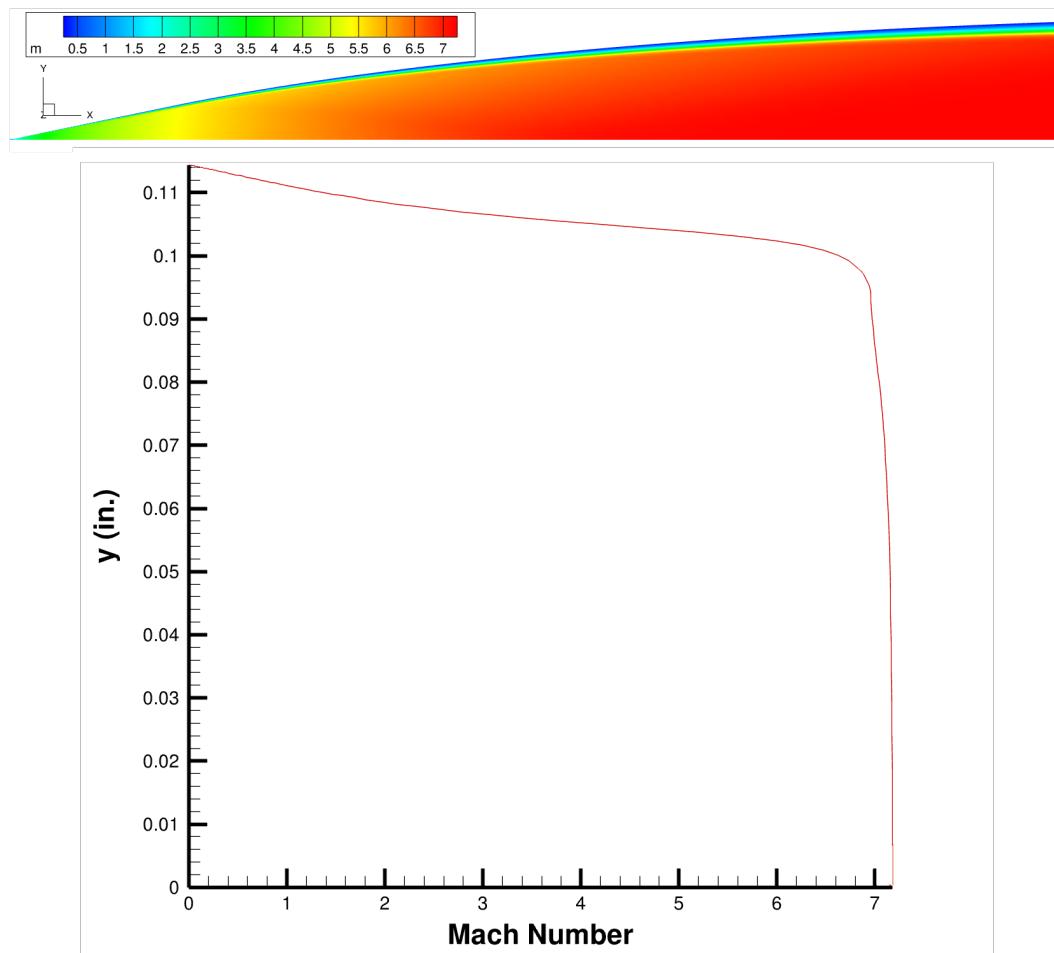


Figure 2.13: ACE2.0 CFD Mach number distribution at exit plane

2.2.4 General Nozzle and Settling Chamber Design

The resulting contour from above was imported into Solidworks using the analytic equations given in Appendix A, and the new ACE2.0 nozzle and settling chamber were designed following the above requirements. In order to accommodate the active control, the nozzle and settling chamber were combined into single rigid upper and lower pieces. Similar to ACE, the last 4 inches of the nozzle is a separate flexure piece to enable the variable Mach number capability. The overall length of the nozzle and settling chamber was increased by 19 inches with most of the added length contributed to the settling chamber. The settling chamber is 1.7 inches taller and has a few considerable improvements described in a later section.

The ACE design had the relative motion interface between nozzle and settling chamber with a large rubber seal that struggled to properly seal at higher Mach numbers. For ACE2.0, the end of the settling chamber is split into two pieces to allow the rotation of the nozzle blocks. This moves the potential sealing issue upstream of the flow conditioners where minor leaks are much less of a concern. The final ACE2.0 nozzle and settling chamber design compared to ACE is shown in Figure 2.14.

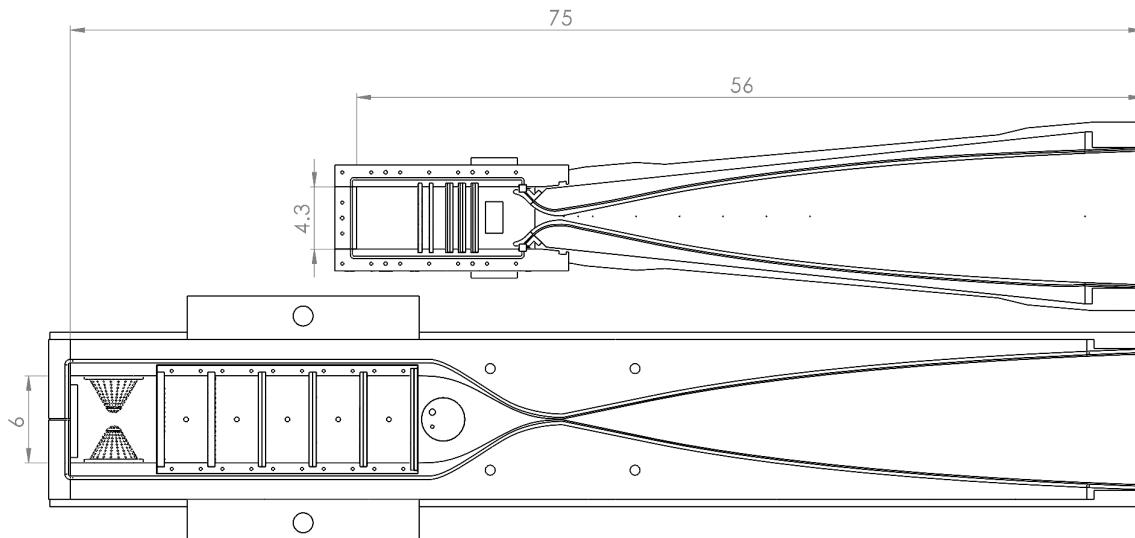


Figure 2.14: Comparison of ACE (top) and ACE2.0 (bottom) nozzle and settling chamber designs

All of the nozzle and settling chamber parts will be made from 304 stainless steel except for the flexures, which will be made from Condition A 17-4 PH stainless steel for maximum strength while maintaining flexibility.

2.2.5 Mechanical Design Iterations

There were a few distinct iterations throughout the design process of ACE2.0 that are worth mentioning briefly. As mentioned, enabling active control was not the original intent of the ACE redesign, so the initial mechanical design was limited. One major difference to note between all of the past iterations and the final iteration is that the nozzle and settling chamber upper and lower pieces are not single rigid parts in the past iterations. The plan was to have either a bolted or welded interface between the nozzle blocks and the settling chamber piece to save cost in stock material, but it was decided to accept the higher cost of material for maximum strength and rigidity with a single piece.

A preface to the mechanical designs is that the actual load on the settling chamber and nozzle at a maximum pressure of 200 psia is around 90,000 pounds per top and bottom. This is the result of the increased surface area of the settling chamber and subsonic portion of the nozzle, which together is 14 inches wide by 36 inches long.

The first iteration, shown in Figure 2.15, had a system of worm gears and lead screws to simultaneously adjust both nozzle blocks, and it required a jam nut on each lead screw and large wedges on the settling chamber to lock the position during a run. This design was not intended to be active, so it could not dynamically support the loads during a run. This design revealed that active control was not far from reach, so the next iteration began with the intention to enable it.

The second iteration, shown in Figure 2.16, built off from the idea of the wedges on the settling chamber to fully support against the loads during a run. This design relied on specially contoured oil-impregnated bronze sliding plates that were actuated by a similar system of worm gears and lead screws. The purpose of the contours instead of a simple flat wedge was to (1) provide a constant rate of change for the Mach number given a constant lead screw translation rate input and (2) maintain all points of contact as the nozzle rotated. The primary concern with this design was the

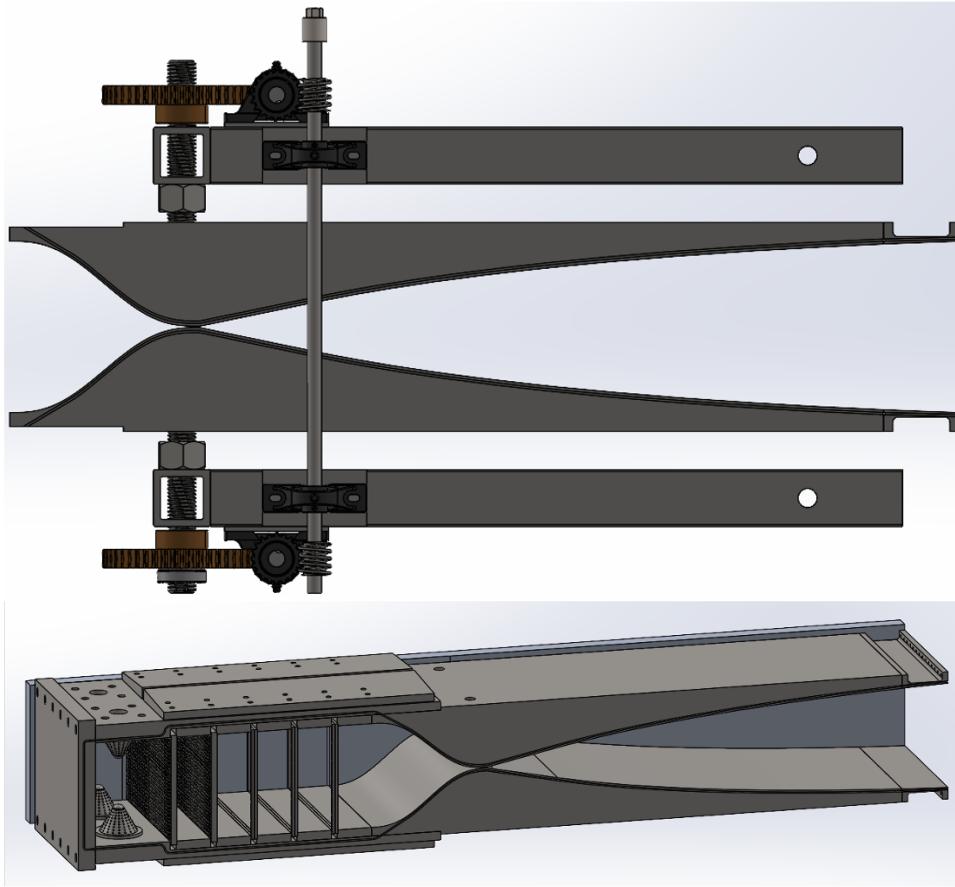


Figure 2.15: Iteration 1 of ACE2.0: Non-active

expected wear and required actuation force due to friction, which would be around 20,000 pounds assuming a friction coefficient of 0.2 between the stainless steel and oil-impregnated bronze. This design also had the introduction of the disc spring stacks at the settling chamber end to hold the nozzles apart at the set position while not under load.

The third iteration, shown in Figure 2.17, improved upon the previous approach by introducing rollers and bearings to eliminate the friction and linear actuators for simpler and more robust control. This design was abandoned for two primary reasons: (1) a realization that the reverse load while under full vacuum was unsupported and (2) feedback from machinists about concerns of wear in bearings and difficulty in machining the roller plate. The load under full vacuum across the entire nozzle and settling chamber is around 16,000 pounds, which requires substantial support to maintain the set Mach number when initiating a run and to minimize excess loads on the flexure.

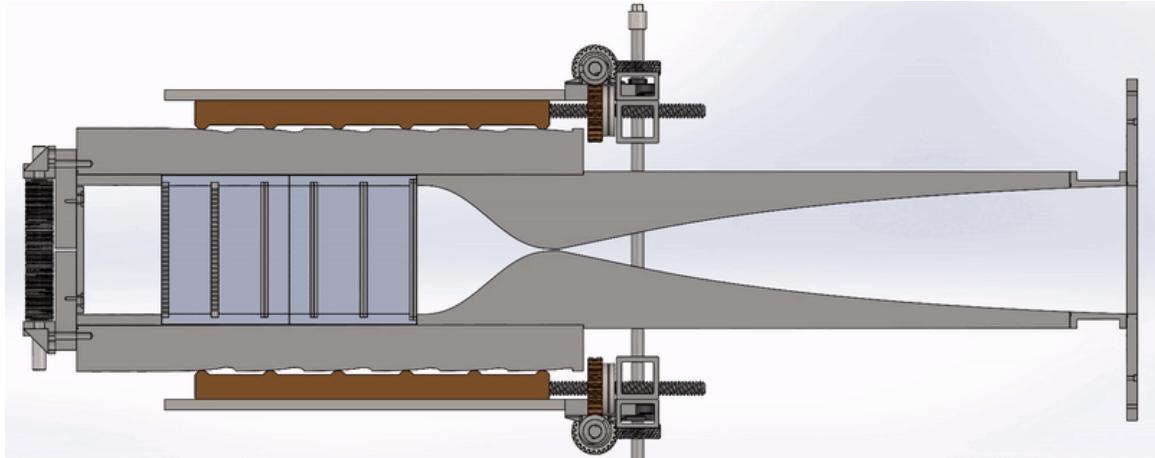


Figure 2.16: Iteration 2 of ACE2.0: Sliding Wedge

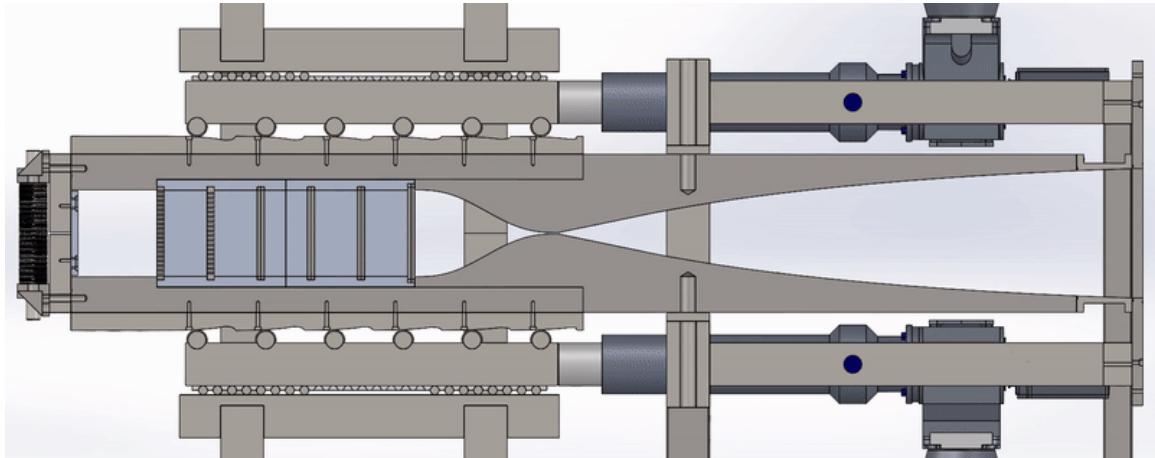


Figure 2.17: Iteration 3 of ACE2.0: Rollers and Actuators

The fourth and final iteration turned to a complete different approach of using 20-ton ball screw linear actuators to fully support both the maximum pressure and full vacuum loads. This final iteration is the most simple mechanically while also providing the most versatility in controlling the Mach number.

2.2.6 20-Ton Linear Actuators Design

The final design of ACE2.0 utilizes two 20-ton ball screw linear actuators on both the upper and lower nozzle blocks to actively control the Mach number by varying the throat height. The

final design of the nozzle and settling chamber with the actuators can be seen in Figure 2.18.

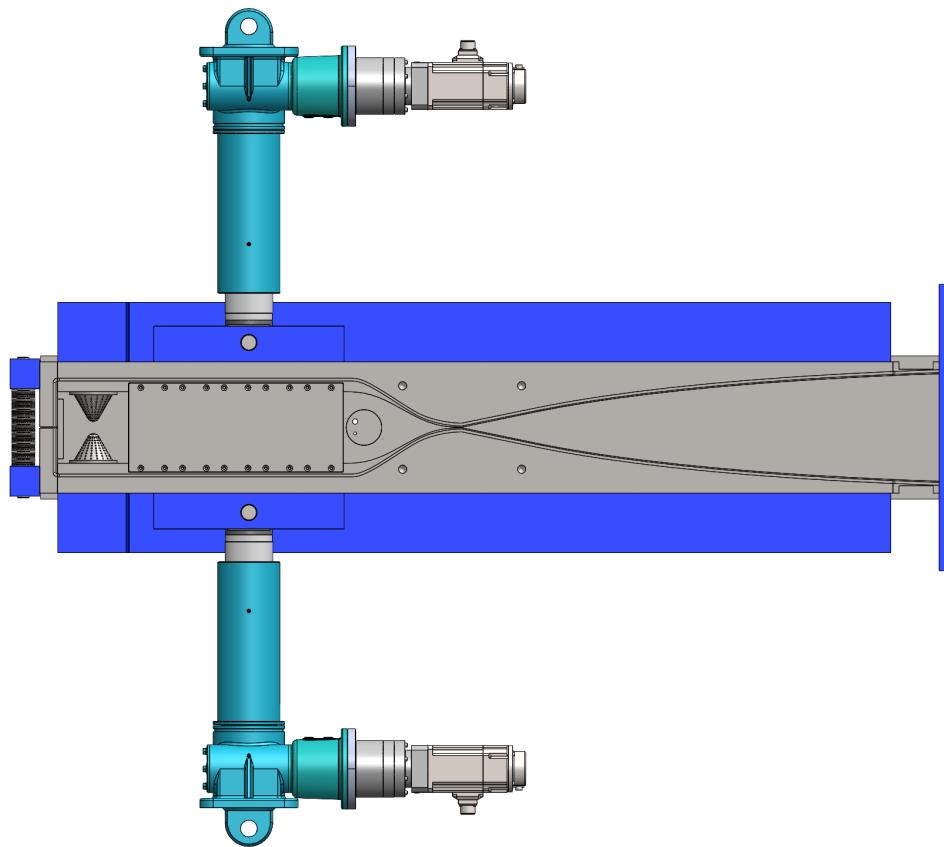


Figure 2.18: ACE2.0 final nozzle and settling chamber with actuators

Nozzle and Settling Chamber Design

Using linear actuators does present the challenges of introducing stress concentrations at the attachment location and not providing support along the length of the nozzle and settling chamber. These were overcome by making the mating clevis on the settling chamber a 16 inch bar to distribute the load and adding a 5 inch by 2.5 inch beam along the length of the nozzle and settling chamber to provide rigidity, as seen in Figure 2.18.

The sidewalls are 1.5 inches thick and made from 304 stainless steel. They are suspended from the frame by two brackets each, and a series of custom bar clamps will provide the support against

the load under pressure. One sidewall has all of the ports and sensors, which allows the other to be the main access for maintenance.

The settling chamber consists of four inlet flow spreading cones and a standalone box where the flow conditioners enclosed that allows for easy maintenance and future modifications of screen configurations. The inlet flow spreading cones were added to allow uniform mixing of the incoming air before flowing through the aerogrids, and they will be made from 304 stainless steel. The flow conditioner box is made from four 0.75-inch thick 304 stainless steel plates. This assembly floats between the nozzles and is secured by the sidewalls in a slot. The overall height doubles as a safety limit so the nozzles will contact each side of the box before contacting each other. Housed inside the box are two aerogrids and four screens in the current configuration, but any configuration can easily be designed and swapped in the future. The initial configuration provides 3 inches between each aerogrid and screen for adequate turbulence decay. The flow conditioner box is shown in Figure 2.19.

The aerogrids are made from 0.5-inch thick 304 stainless steel. As shown in Figure 2.20, they each have around 2750 0.125-inch diameter holes for an open area of 40%. The resulting maximum pressure drop across each aerogrid is approximately 18 times the dynamic pressure, which is 0.3 psia at a 200 psia inlet stagnation pressure. The initial choices of wire mesh for the screens will be explored prior to installation. The first screen will likely have a wire diameter of 0.0035 inches, an opening size of 0.0085 inches, and an open area of 50%. The last screen will likely have a wire diameter of 0.0023 inches, an opening size of 0.0033 inches, and an open area of 34%. The maximum pressure drop across these screens will be approximately 5 and 15 times the dynamic pressure, respectively.

The variable flow conditioner box will allow future optimization for the best incoming flow quality. The objective in this work is to maintain the flow quality of ACE, so some optimization of the flow conditioners will be performed depending on results during the characterization of ACE2.0.

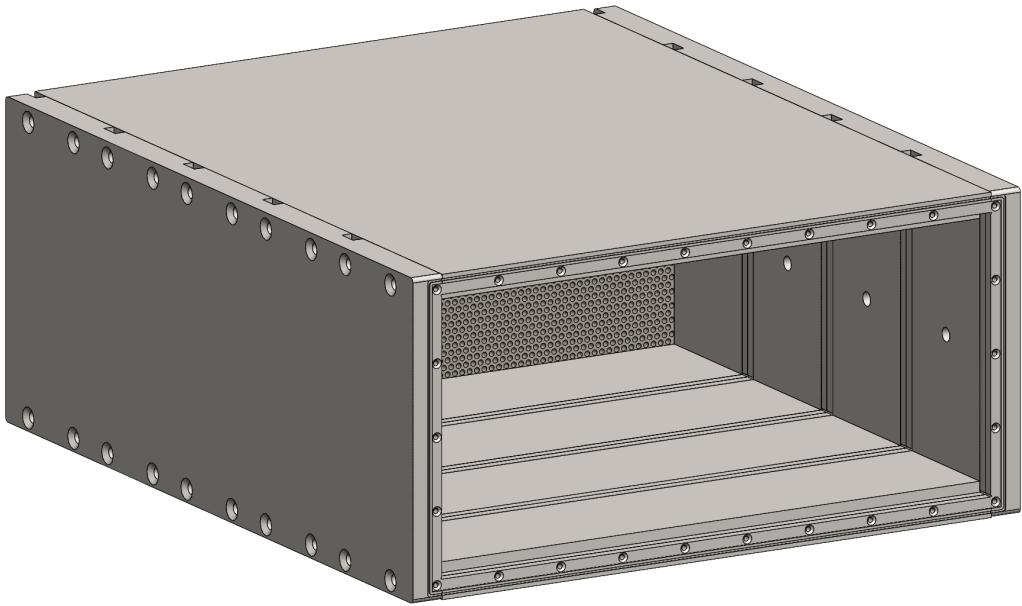


Figure 2.19: CAD model of flow conditioner box

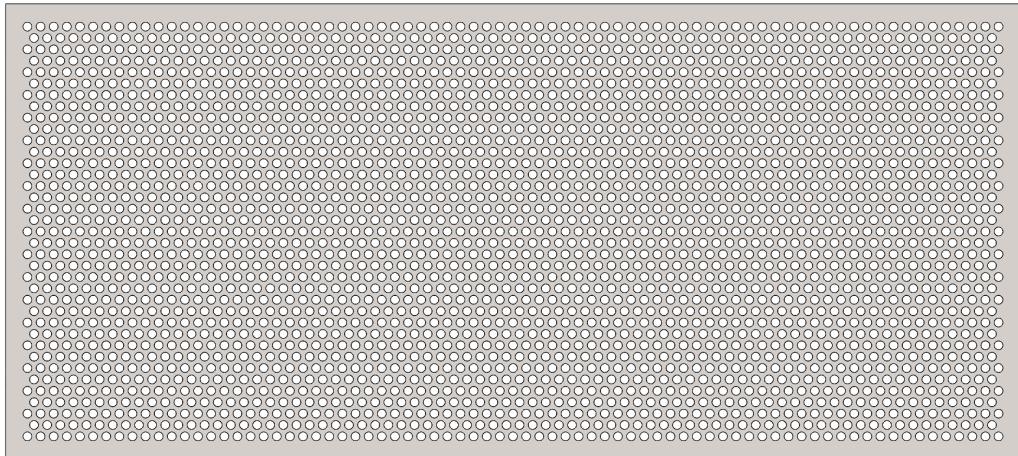


Figure 2.20: CAD model of aerogrid

Frame Design

The frame was designed around the linear actuators to best support the extreme loads. In order to maximize strength, a single piece brace was designed to symmetrically bear the loads from the

actuators. The rest of the frame was designed between the brace and the nozzle-test-section flange to support the sidewalls. The entire frame will be made from 3 inch thick 4140 alloy steel plates and bars, and it all bolts together instead of welding. All exposed faces will be powder coated in order avoid rust and wear over time.

The frame will have four 5000-pound capacity steel swivel casters for easy maneuvering when aligning for installation. Once in position, the weight of the assembly will be transferred to rigid feet on threaded rods. All of these details can be seen in Figure 2.21.

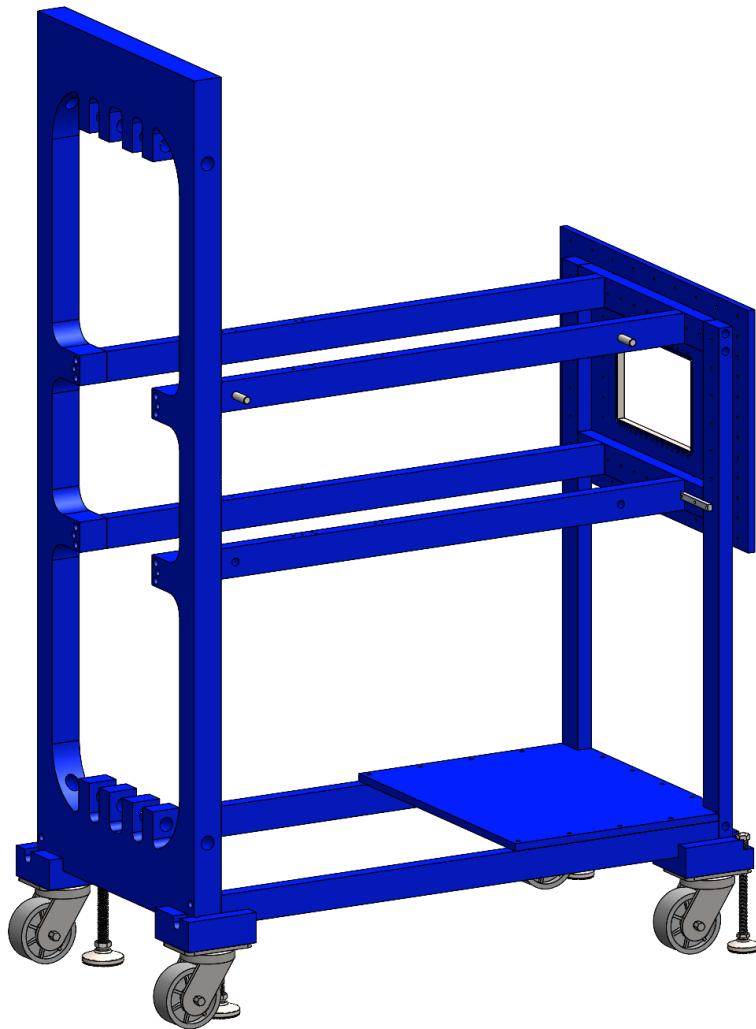


Figure 2.21: CAD model of full frame assembly

Actuation System Design

The actuation system for ACE2.0 is comprised of many components that enable the active feedback-back control of the Mach number. Only a high level overview will be provided here for sake of brevity, but a full detailed description of the entire system will be provided in a future appendix.

The linear actuators are each rated for 40,000 pounds with a minimum FOS of 7. They have a double clevis design to rotate freely and have a custom motor mount for the selected gear box and servo motor, as shown in Figure 2.22. The actuators are comprised of a 24:1 worm gear reducer that turns a ball nut to drive a 0.5 inch lead ball screw. The ball nut has a long service life that will allow over 400,000 full throat deflections before maintenance is required. Another 20:1 gear box will be mounted to each actuator for an overall travel of approximately 0.001 inch per servo motor turn.

The required input torque for the actuators at maximum load with the additional gearbox is 28 inch-pounds. The rated continuous torque and the momentary peak torque of the selected servo motor are 28 and 84 inch-pounds, respectively, and the rated continuous speed and the momentary peak speed are 3000 and 5000 revolutions per minute, respectively. The change in throat height from Mach 5 to 8 for each half of the nozzle is around 0.157 inches, so a full Mach sweep at maximum pressure can be achieved in around 3 seconds within the continuous operation range of the servo motor. The servo motors have a power-off brake hold a set Mach number and to prevent motion and any potential damage in a power outage.

In order to minimize the backlash in the actuators, two inverted stacks of Belleville disc springs were added to the end of the settling chamber as shown in Figure 2.23. With a nominally linear relationship between force and compression, a stack height of 8 inches and minimum compression of 0.875 inches was chosen to produce a combined minimum force of 3000 pounds to always lift the upper nozzle block and keep the actuators in compression.

The four servo motors are each driven by individual servo drives powered by 240 VAC 3-phase. These four drives and servo motors are controlled synchronously by a programmable logic con-

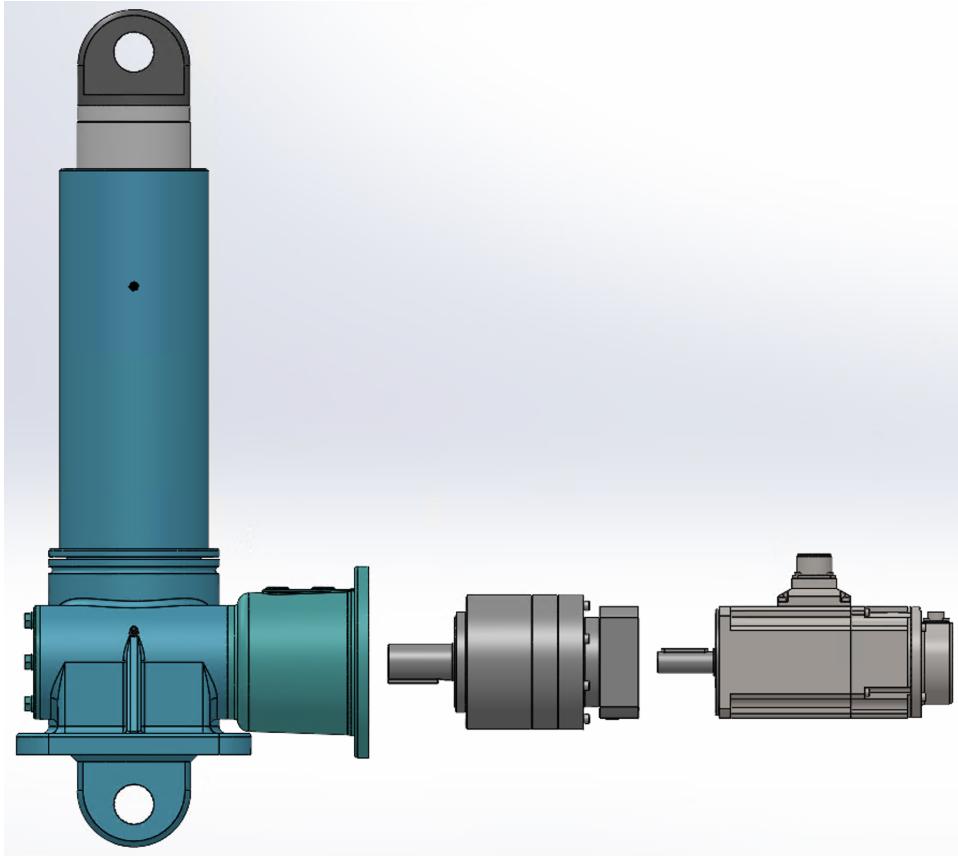


Figure 2.22: CAD model of 20-ton linear actuator, 20:1 gear box, and servo motor.

troller (PLC) through EtherCAT, the fastest industrial Ethernet communication protocol. The PLC logic programs are written in its associated software, Sysmac Studio. This software is a graphical ladder logic environment designed to integrate many automation devices across EtherCAT.

The specific program to control the Mach number will be created in future work. This program will initially be designed with four control objectives: (1) precise set Mach number, (2) Mach number sweep with specified start, stop, and time, (3) Mach number schedule, and (4) feedback-control for Mach number. The completed Mach number control program will be provided in a future appendix. Additionally, three analog modules were added to the PLC to input the static pressure, stagnation pressure, and temperature measured by the corresponding sensors to enable feedback-control.

Additional components of the system include two safety limit switches for each actuator, an

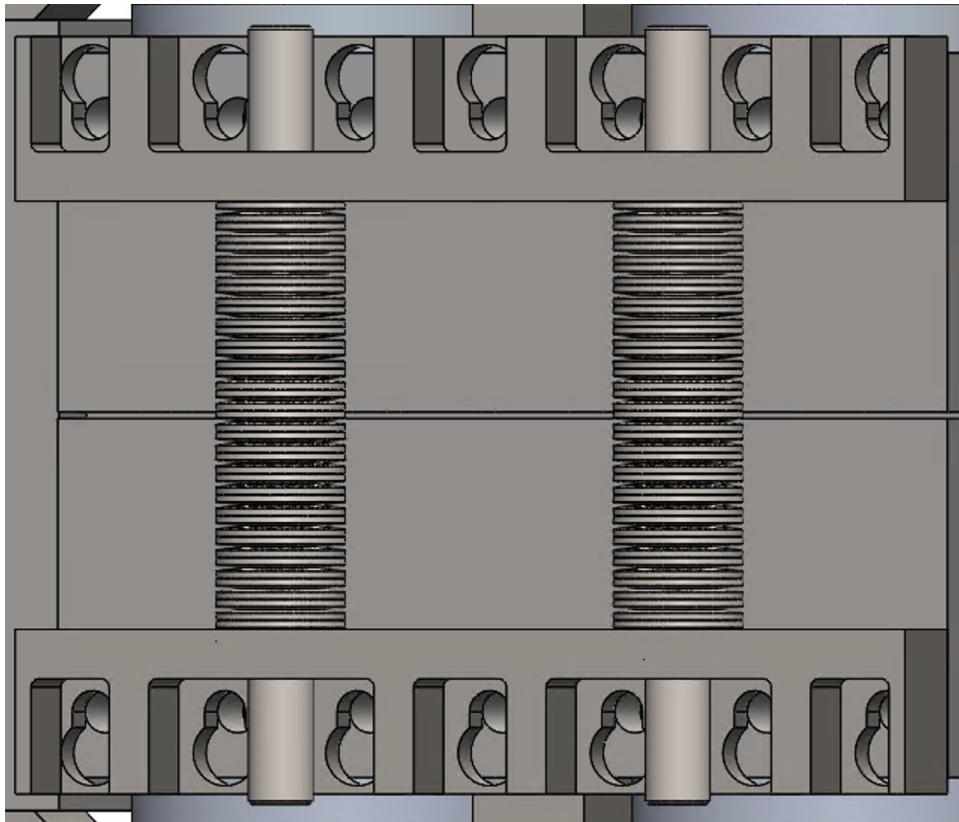


Figure 2.23: Inverted disc springs stacks at the end of the settling chamber

external encoder for each actuator for additional physical feedback, various power supplies and relays, an emergency stop button, and a 7" human machine interface (HMI) for a simple control interface that can be updated and expanded for any desired controls.

Final Overall Design

The final design with all modeled components is shown in Figures 2.24 and 2.25. The entire design will integrate with the existing ACE test section and other infrastructure. The overall length from the nozzle-test-section flange to the inlet of the 4-way manifold is 94 inches, about 12 inches longer than the existing system.

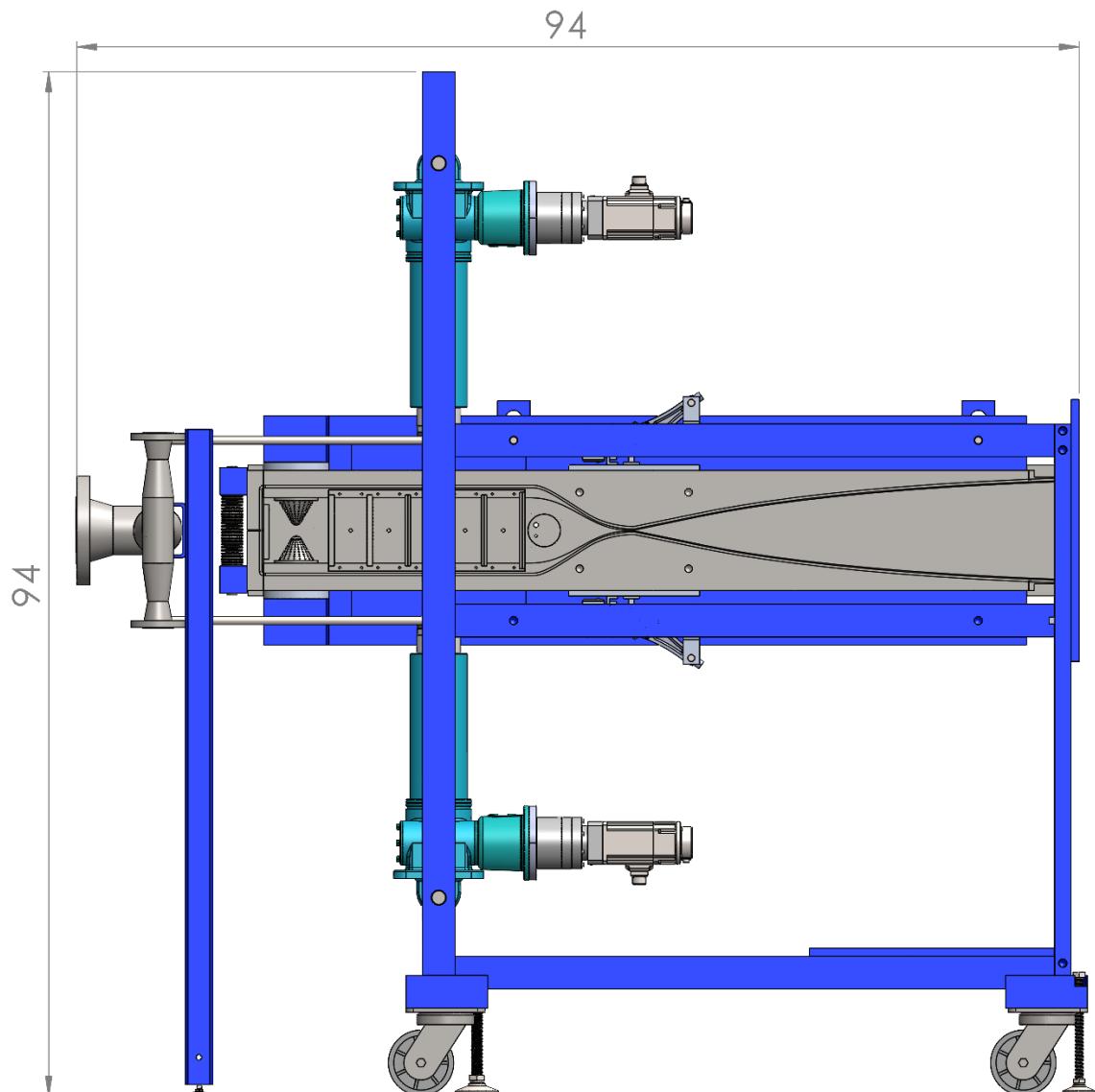


Figure 2.24: Side view of ACE2.0 in Solidworks

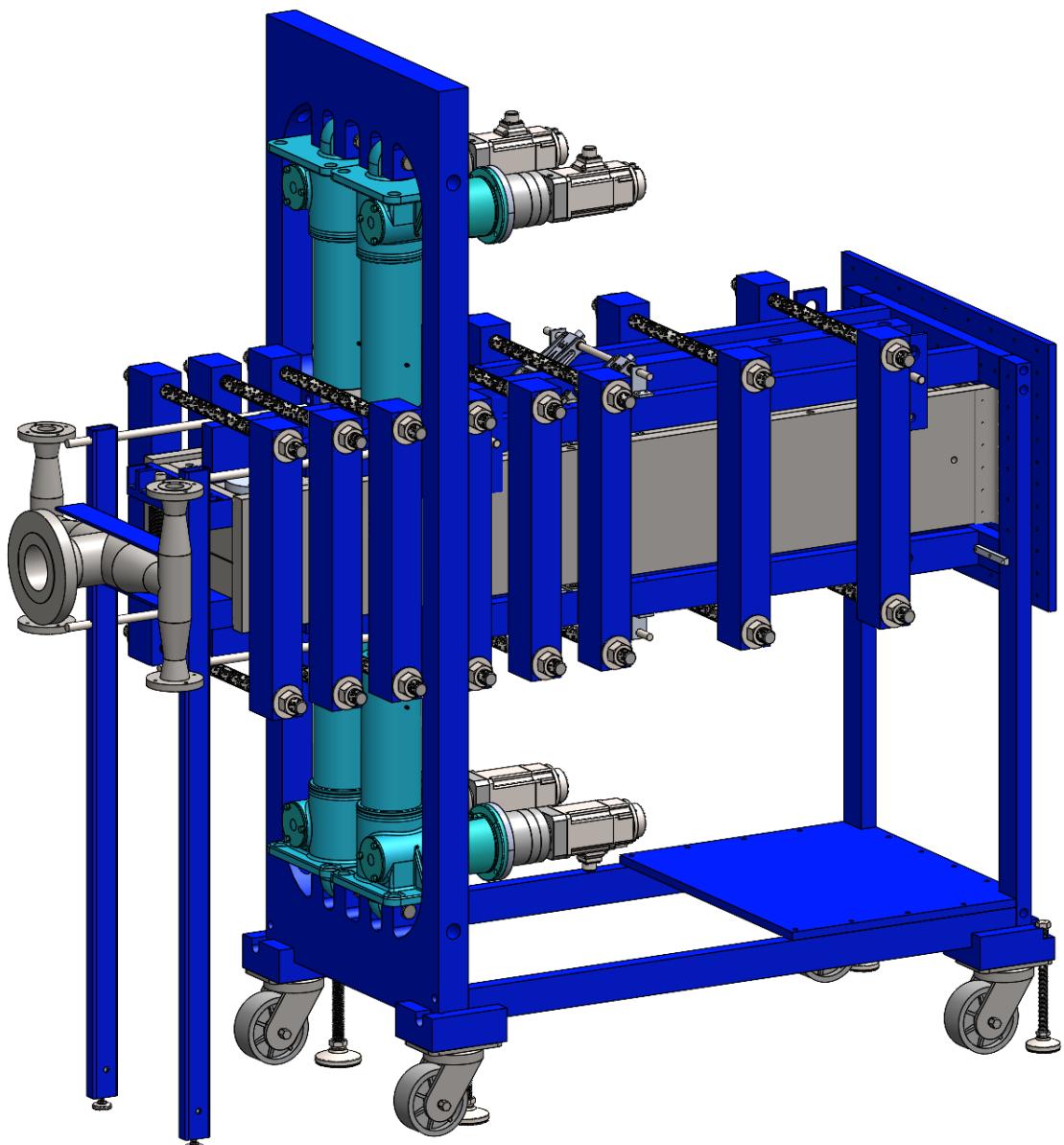


Figure 2.25: Full CAD model of ACE2.0 in Solidworks

FEA

The structural integrity of the final design was simulated using finite element analysis (FEA) in Solidworks. There were four primary simulations conducted: (1) lower nozzle and settling chamber at 200 psia with gravity, (2) upper nozzle and settling chamber at full vacuum with gravity, (3) sidewall with clamps at 200 psia, (4) and flexure fatigue at maximum deflection. Other simulations were also conducted for a many of the individual components such as the flow spreaders, aerogrids, and various hardware.

From all of these simulations, the minimum FOS for any component was 1.8. The displacement of the nozzle due to maximum load is shown in Figure 2.26. The maximum stress in the flexure shown in Figure 2.27 is much less than the fatigue limit of 17-4 PH stainless steel.

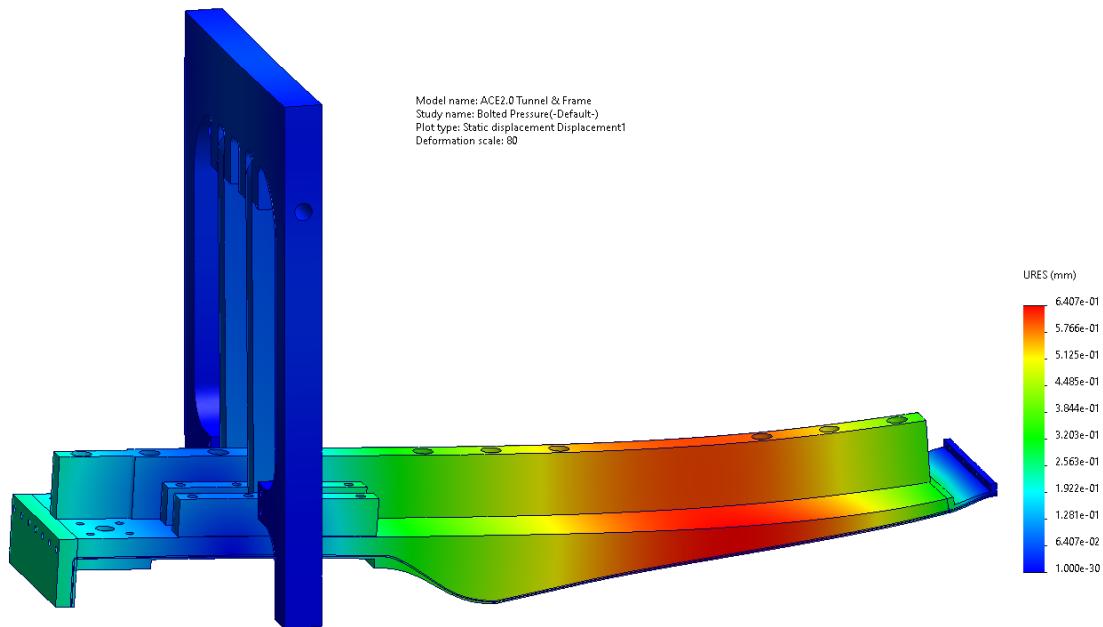


Figure 2.26: Displacement with 200 psia in settling chamber, 15 psia on exterior, gravity acting up, and bolted interfaces

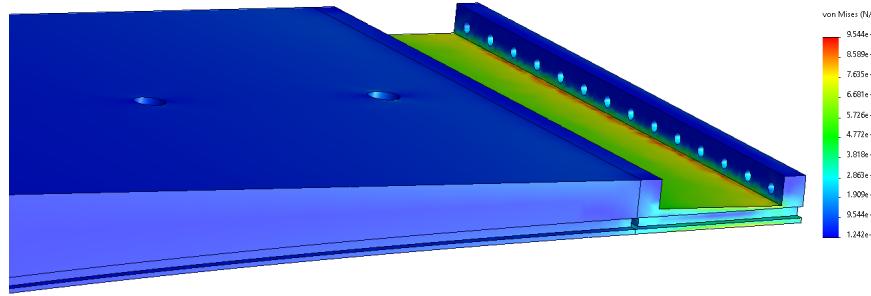


Figure 2.27: Flexure stress at maximum deflection of 0.25 inches

2.3 Fabrication Plans

At present, all of the ACE2.0 parts are finished machining besides the nozzles and sidewalls. The fabrication is following the schedule shown in Figure 2.28, which shows the completed tasks in gray, the current tasks in green, orange, or red depending on status, and future tasks in white. The frame pieces were machined at the Texas A&M Fischer Engineering Design Center (FEDC). An image of the brace after being cut out on the water jet is shown in Figure 2.29. The pallet of finished frame parts is shown in Figure 2.30.

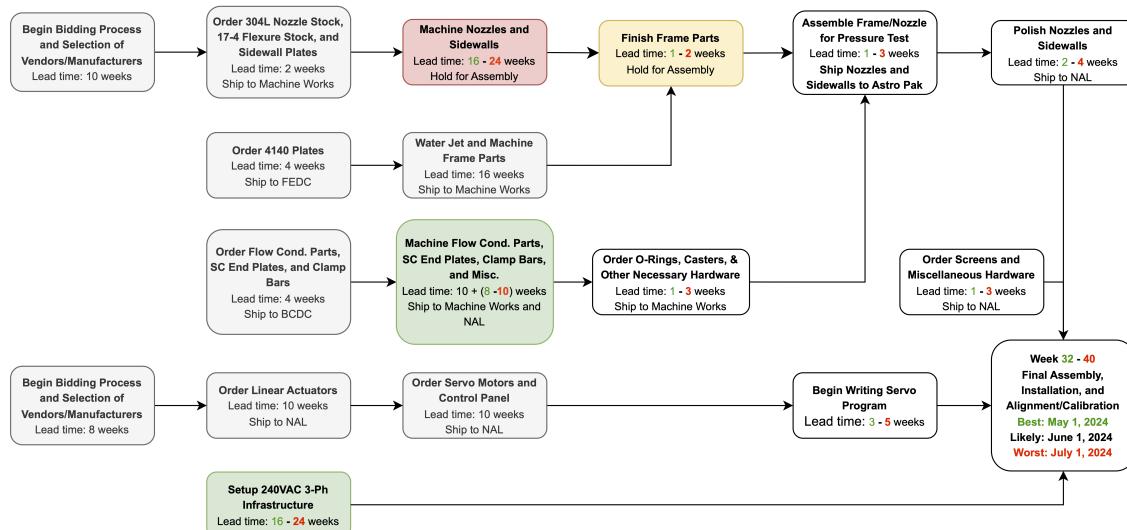


Figure 2.28: Manufacturing schedule beginning from September 25, 2023



Figure 2.29: Rough cut brace on water jet

The nozzles and sidewalls are currently being machined at Machine Works Inc. in Bryan, TX. The nozzles were first saw cut to a rough profile to minimize the amount of time on the CNC mill, as shown in Figure 2.31. They are currently being machined to a rough contour, and then the back of each will be machined flat prior to finishing the contour. For the final passes, the nozzle blocks and flexures will be bolted together to ensure there is no step between the two pieces. Machine Works will also finish the brace for the frame by drilling and tapping holes.

The rest of the parts were machined at the Texas A&M Bush Combat Development Complex (BCDC). All of these parts are finished, but only the parts necessary for the pressure test have been picked up. Figures 2.32, 2.33, and 2.34 show the flow conditioner box, an aerogrid, and a flow spreading cone. BCDC will be the primary machine shop for any future fabrication throughout this work.

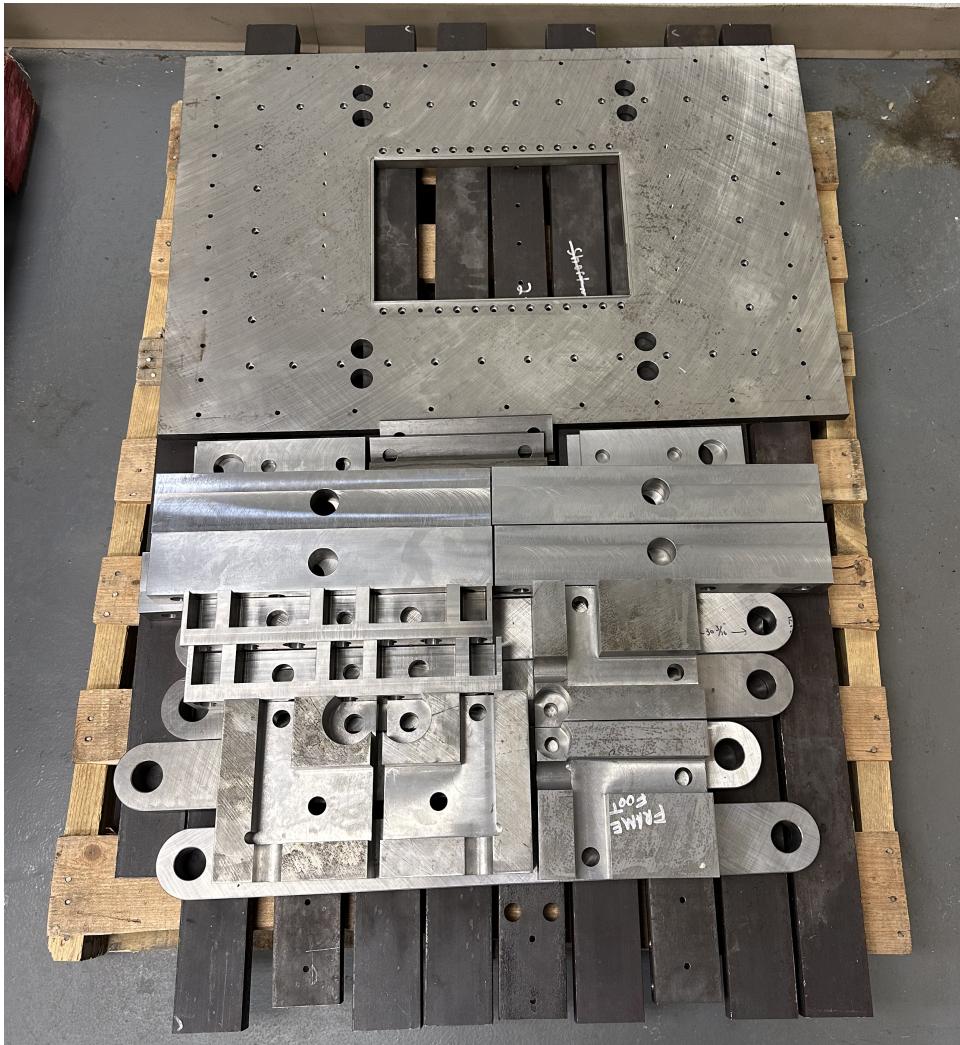


Figure 2.30: Pallet of finished frame parts from FEDC



Figure 2.31: Nozzle block saw cut to rough profile



Figure 2.32: Machined flow conditioner box

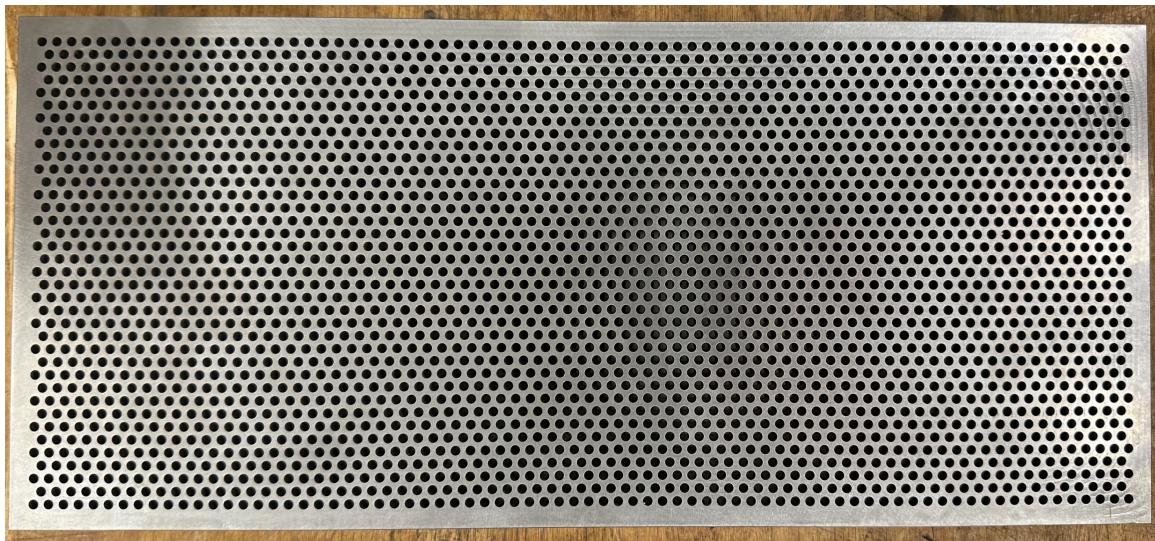


Figure 2.33: Machined aerogrid



Figure 2.34: Machined flow spreading cone

2.3.1 Pressure Test

The hydro-pressure test will be performed at Machine Works prior to sending the nozzles and sidewalls to be polished. The base tunnel will be assembled with steel bars to simulate the actuators. The tunnel will be filled with water and pressurized to 200 psia for one hour, and the pressure will be monitored throughout. The primary goal of the pressure test is to ensure structural integrity at maximum pressure. Any major leaks will also be addressed.

2.3.2 Polishing

Following the completion of the pressure test, the nozzles and sidewalls will be shipped to Astro Pak for polishing. All interior surfaces will be mechanically polished to a 1 Ra¹ finish, and electropolishing will be used if necessary. In order to safely ship these pieces, the nozzle blocks will be assembled as shown in Figure 2.35 and custom wooden crates will be built.

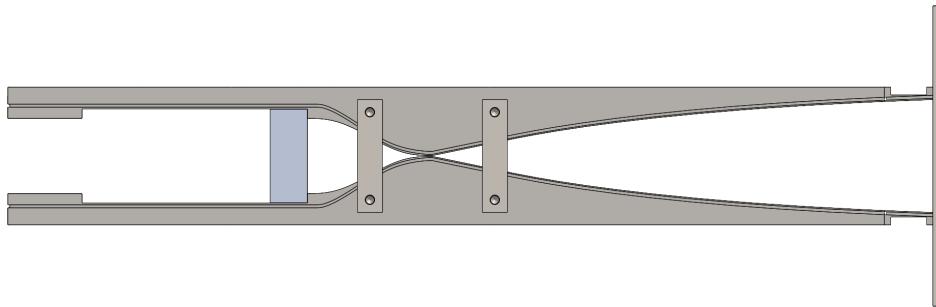


Figure 2.35: Nozzle assembly for shipping to polishing vendor

2.4 Final Assembly, Installation, and Calibration

The final assembly will occur at the NAHL once the nozzle and sidewalls are delivered from polishing. Once nozzles and actuators are assembled in the frame, ACE2.0 will be rolled into the lab to replace ACE. All hoses, wires, and instrumentation attached to the nozzle and settling

¹Surface roughness average of 1 microinch

chamber will be removed and ACE will be rolled out of the lab. ACE2.0 will roll in and reconnect all hoses, wires, and instrumentation.

The nozzles will be leveled and aligned and then the servos will homed with the limit switches to calibrate the actuation system. The pressure and temperature instrumentation will be calibrated prior to reconnecting to the new facility. The sidewalls will then be mounted for the shakedown run, which will include a pitot rake at the nozzle exit to ensure uniformity in the test section.

3. EXPERIMENTAL APPROACH & OBJECTIVES

Following the completed installation and calibration discussed above, each of the three primary objectives will be accomplished or demonstrated sequentially. First, the improved experimental control and efficiency as a result of the above ACE2.0 design will be demonstrated by establishing and verifying the feedback-controlled active Mach variation and selection capability as well as the Reynolds number control scheme, if implemented. Second, the freestream flow produced by the calibrated nozzle will be characterized in terms of freestream flow uniformity and disturbance levels with uncertainty quantification and an exploration hysteresis. Third, the flow parameter control capabilities will be demonstrated in a proof of concept experiment of shock interactions during a Mach trajectory and any potential hysteresis exhibited. As a result of this work, the foundation will be set for future researchers to explore dynamic hypersonic aerodynamic in a more sophisticated and efficient manner with the control capabilities of ACE2.0.

3.1 Improved Experimental Control and Efficiency

The overall objective here is to establish and substantiate the mechanisms of ACE2.0 that allow greater control of the tunnel input parameters for both more efficient and dynamic experiments. The primary design objective of ACE2.0 was to enable active Mach number control during a run, which alone provides many key experimental advantages. However, there is still much to be desired with the parameter control capabilities to achieve full aerodynamic similarity for any flight trajectory. Thus, more precise control methods for Mach number and Reynolds number will be explored through the following objectives.

3.1.1 Feedback-Controlled Active Mach Number Variation and Selection

As stated, the primary design objective of ACE2.0 was to enable active control of the Mach number, but this capability will be taken one step further to accurately maintain the desired Mach number once set. During a tunnel run, the Mach number may vary because both pressure and thermal loads can cause the throat height to vary. Current experience shows that the Mach number

can vary by up to 5%. The goal of this work is to implement active feedback control and reduce this error to less than 0.5%.

The general approach for this feedback control is straightforward by designing a PID controller with an input of the measured Mach number and output of actuator position or velocity. The measured Mach number is calculated from the measured stagnation pressure and static pressure by solving the isentropic relation:

$$M = \sqrt{\frac{2}{\gamma - 1} \left[\left(\frac{P_0}{P} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right]} \quad (3.1)$$

The relationship between the throat height and the Mach number is given by:

$$\frac{A^*}{A} = \frac{h^*}{h_{\text{exit}}} = M \left[\left(\frac{2}{\gamma + 1} \right) \left(1 + \frac{\gamma - 1}{2} M^2 \right) \right]^{-\frac{\gamma+1}{2(\gamma-1)}} \quad (3.2)$$

This is then subtracted from the set throat height to get the error signal for the PID transfer function:

$$E(s) = h_{\text{set}} - H(s) \quad (3.3)$$

There are many design options for PID controllers depending on the desired performance characteristics. The standard approach is simply a PI controller due to the derivative action amplifying measurement noise and potential causing instability [25]. However, the derivative effect of limiting overshoot and settling time is desirable, so it will not be neglected entirely. One final option is to add high frequency filtering into the derivative term to mitigate the effects of measurement noise. Each of these options will be explored, and the following equations show the transfer functions for

PI, PID, and PID with high frequency noise filtering respectively:

$$G(s) = \frac{H(s)}{E(s)} = K \left(1 + \frac{1}{T_i s} \right) \quad (3.4a)$$

$$= K \left(1 + \frac{1}{T_i s} + T_d s \right) \quad (3.4b)$$

$$= K \left(1 + \frac{1}{T_i s} + \frac{T_d s}{1 + \frac{T_d s}{N}} \right), \quad N = 2 \text{ to } 20 \quad (3.4c)$$

In practice, the Sysmac software used to write the logic for the PLC has a built-in PID function with gain autotuning capability. This will be explored in detail first in simulations in Sysmac followed by active tests in ACE2.0. This built-in PID loop will be used permanently if the resulting Mach number control is sufficient. Otherwise, the PID controller described above will be fully developed and implemented. In either case, a gain schedule will also be developed to modify the controller response throughout the Mach range to best handle the nonlinearity of the throat height and Mach number relationship.

3.1.2 Reynolds Number Control Scheme

In subscale model experiments, the Reynolds number plays an important role in maintaining similarity with real-world situations. Controlling the Reynolds number more effectively will enable more accurate and intentional experiments. The primary goal of this objective is to provide a feedback control scheme that allows the Reynolds number to be held at a set value that is either constant or dynamic. For the purposes of this discussion, any mention of the Reynolds number will be referring to the unit Reynolds number, $Re' = \frac{\rho U}{\mu}$.

The main control parameter for Reynolds number will be the settling chamber stagnation pressure. The Reynolds number is coupled with respect to pressure, temperature, and Mach number. The goal will be to control the stagnation pressure to counteract changes in both temperature and Mach number. For reference, the settling chamber stagnation temperature typically increases during a run by up to 40 K, and, of course, the Mach number can vary between 5 and 8. The effect of temperature will be examined during both simulations and experiments to determine if a more ad-

equate control system is required to maintain constant temperature or if this effect on the Reynolds number can be compensated by changing the pressure.

A mathematical model will be developed to be implemented for future physical PID control of the pressure regulator and the Reynolds number as a result. The physical implementation of this controller in this work will be dependent on budget and schedule constraints. The primary constraint here will be the ability to quickly replace the existing regulator manual valve control with a controlled valve. The M6QT utilizes the same air supply infrastructure, so any complications throughout the valve replacement process would result in both facilities being inoperable and a delay in all planned research for this work and others.

One other factor to be considered in the stagnation pressure control is the time response delay due to both the distance between the regulator and the tunnel and the maximum operating speed of the regulator. The distance from the regulator to the settling chamber inlet is around 25 feet, resulting in a maximum response time in the range 20 to 150 milliseconds. This range considers the minimum sound speed of $a = \sqrt{\gamma RT_0} = 3.28\sqrt{(1.4)(287)(300)} \approx 1140 \frac{ft}{s}$ for the pressure waves and the minimum pipe flow velocity of $v_{pipe,min} = \dot{m}_{min}/\rho/A_{pipe} \approx 164 \frac{ft}{s}$ for the corresponding mass flow to reach the settling chamber. The full response time cannot be calculated currently because the maximum regulator operating speed is unknown. With this in mind, the response time will be investigated experimentally if the Reynolds number control is implemented in this work.

The following derivation provides a starting point for the mathematical model.

$$\frac{T_0}{T} = \left(1 + \frac{\gamma - 1}{2} M^2\right) = F \quad (3.5)$$

$$\frac{P_0}{P} = \left(1 + \frac{\gamma - 1}{2} M^2\right)^{\frac{\gamma}{\gamma+1}} = F^{\frac{\gamma}{\gamma+1}} \quad (3.6)$$

$$\rho = \frac{P}{RT} = \frac{P_0 F^{\frac{-\gamma}{\gamma+1}}}{RT_0 F^{-1}} = \frac{P_0}{RT_0 F^{\frac{1}{\gamma+1}}} \quad (3.7)$$

$$U = M \sqrt{\gamma RT} = M F^{-\frac{1}{2}} \sqrt{\gamma RT_0} \quad (3.8)$$

$$Re' = \frac{\rho U}{\mu} = \frac{1}{\mu} \frac{P_0}{RT_0 F^{\frac{1}{\gamma+1}}} M F^{-\frac{1}{2}} \sqrt{\gamma RT_0}$$

$$Re' = \sqrt{\frac{\gamma}{RT_0}} \frac{MP_0}{\mu} F^{-\frac{\gamma+1}{2(\gamma-1)}} \quad (3.9)$$

Differentiating Re' assuming γ and R are constant and with $\frac{dF}{dt} = (\gamma - 1)M \frac{dM}{dt}$ gives:

$$\frac{d(Re')}{dt} = \sqrt{\frac{\gamma}{RT_0}} \frac{MP_0}{\mu} F^{-\frac{\gamma+1}{2(\gamma-1)}} \left[\frac{\frac{dM}{dt}}{M} + \frac{\frac{dP_0}{dt}}{P_0} - \frac{\frac{dT_0}{dt}}{2T_0} - \frac{\frac{d\mu}{dt}}{\mu} - \frac{\gamma+1}{2} MF^{-1} \frac{dM}{dt} \right] \quad (3.10)$$

With μ defined from Sutherland's Law with $T_\mu = 273$, $S_\mu = 111$, and $\mu_0 = 1.716 \times 10^{-5}$:

$$\mu = \mu_0 \frac{T_\mu + S_\mu}{T + S_\mu} \left(\frac{T}{T_\mu} \right)^{\frac{3}{2}} \quad (3.11)$$

$$\mu = \frac{\mu_0(T_\mu + S_\mu)}{T_\mu^{\frac{3}{2}}} \frac{T_0^{\frac{3}{2}} F^{-\frac{3}{2}}}{T_0 F^{-1} + S_\mu} \quad (3.12)$$

Following the same logic as before, either a PI, PID, or PID with high frequency noise filtering will be implemented based on experimental results of Reynolds number control. However, in this case the calculated Reynolds number will be subtracted from the set condition to get the error signal and the controlled parameter will either be the stagnation pressure or the respective regulator position.

$$E(s) = Re'_{\text{set}} - Re'(s) \quad (3.13)$$

$$G(s) = \frac{P_0(s)}{E(s)} \text{ or } \frac{X(s)}{E(s)} = K \left(1 + \frac{1}{T_i s} \right) \quad (3.14a)$$

$$= K \left(1 + \frac{1}{T_i s} + T_d s \right) \quad (3.14b)$$

$$= K \left(1 + \frac{1}{T_i s} + \frac{T_d s}{1 + \frac{T_d s}{N}} \right), \quad N = 2 \text{ to } 20 \quad (3.14c)$$

At the very least, this model will be fully developed and simulated to ensure minimal future work for implementation. The physical control mechanism will also be explored and potentially purchased to allow install at the earliest convenience between the ACE2.0 and M6QT schedules.

3.2 Freestream Flow Uniformity and Disturbance Levels Characterization

In order to establish a baseline of performance characteristics for future work within the ACE2.0 facility, a pitot and hot-wire survey will be performed to measure and characterize the freestream flow uniformity and disturbance levels (noise) throughout the nozzle. The survey will utilize both a pitot rake and a single pitot probe with Kulite pressure transducers mounted on a traverse to characterize the pressure fluctuations and uniformity and a hot-wire anemometer to measure mass flux fluctuation levels.

A final noise survey was performed in ACE to establish a control for comparison with ACE2.0 as well as provide a preliminary exploration of noise hysteresis. The survey utilized a single pitot probe to measure the noise along the centerline at 6 and 24 inches upstream of the nozzle exit as shown in Figure 3.2. For each run, the Reynolds number was increased above the transition value ($Re' = 3 \times 10^6 / m$) discussed in the previous chapter and then decreased back down to the initial value below the transition value. These measurements provided baseline data for pressure fluctuation hysteresis. The results are shown in Figure 3.1. As seen, there is some discernible hysteresis in the freestream pressure fluctuation levels as the Reynolds number is swept up and back down. This survey will be repeated using a hot-wire anemometer to measure mass flux fluctuation levels if the remaining schedule for ACE permits.

The anticipated characterization test matrix for ACE2.0 is shown in Table 3.1. The pitot rake will be used to characterize the freestream flow uniformity in the nozzle exit plane and a plane 6 inches upstream. The single pitot probe and hot-wire anemometer will be used to measure the freestream pressure fluctuation and mass flux fluctuation levels, respectively, along the centerline up to 24 inches upstream of the nozzle exit. The runs in each test matrix are divided into a few distinct objectives: (1) uniformity, (2) uncertainty quantification, (3) disturbance levels transition, and (4) hysteresis. The last five runs will be replicates of the first five to better quantify the uncertainty in Mach number, Reynolds number, and flow uniformity. This entire process will be documented so that flow-quality verification tests can be repeated as part of ongoing lab operations.

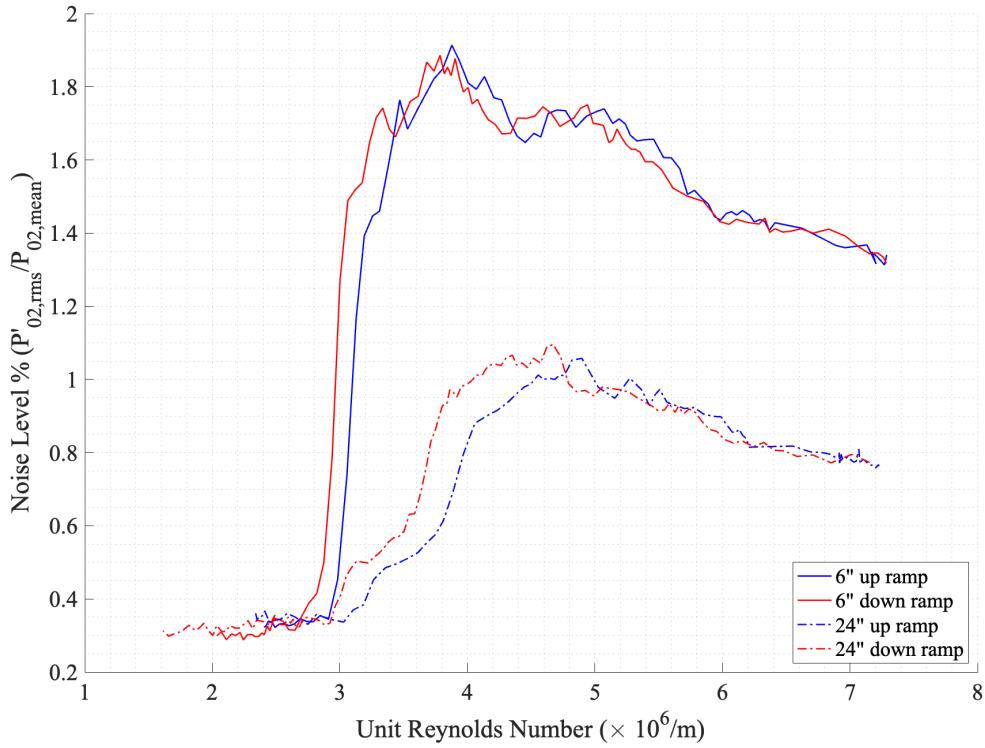


Figure 3.1: ACE freestream pressure fluctuations at 6 inches and 24 inches upstream of nozzle exit

3.2.1 Freestream Uncertainty Quantification

The process to quantify the uncertainty of the various parameters for this work will closely follow Stephens's et al. [31] and Curriston's [33] approaches by simply focusing on establishing a baseline for the uncertainty and making recommendations for improvement if necessary. The three steps to establish this baseline uncertainty for ACE2.0 will be (1) gather/measure systematic elemental uncertainties, (2) input into a Monte Carlo code along with data reduction equations to simulate systematic uncertainties, and (3) measure repeat data points through a few replicate experiments and calculate random uncertainties.

First, the systematic elemental uncertainties can be gathered and measured from the various sensors, which includes the static pressure transducer, stagnation pressure transducer, stagnation temperature thermocouple, and servo motor internal encoders. Each of these has a predefined man-



Figure 3.2: Pitot probe measuring 24 inches upstream of nozzle exit

ufacturer uncertainty that can be used, but some of these are very conservative and not ideal. The pressure sensors and temperature sensor will be tested against a working standard to measure the true uncertainty, which is often found to be an order of magnitude less than the manufacturer uncertainty [33]. The systematic uncertainty of any sensors utilized in future experiments is outside the scope of this work and must be considered when calculating the total uncertainty of measurements in each experiment.

Next, these systematic elemental uncertainties will be propagated through a Monte Carlo simulation along with the specific data reduction equations for the facility. This output will provide the total systematic uncertainty for each parameter of interest, which will be added to the random uncertainty to give the total uncertainty. Additionally, this simulation will also be used provide a sensitivity analysis of the uncertainty to the various input parameters. This will be insightful on

Run	X (in.)	Y (in.)	Z (in.)	Mach	$Re' (10^6)$	Instrument	Purpose
1	0	-3:1:3	0	6*	3*	Rake	Uniformity
2	0	-3:1:3	-3:1:3	8	3	Rake	Uniformity
3	0	-3:1:3	-3:1:3	7	3	Rake	Uniformity
4	0	-3:1:3	-3:1:3	6	3	Rake	Uniformity
5	0	-3:1:3	-3:1:3	5	3	Rake	Uniformity
6	-6	-3:1:3	-3:1:3	5	3	Rake	Uniformity
7	-6	-3:1:3	-3:1:3	6	3	Rake	Uniformity
8	-6	-3:1:3	-3:1:3	7	3	Rake	Uniformity
9	-6	-3:1:3	-3:1:3	8	3	Rake	Uniformity
10	0	0	0	8	2→7→2	Pitot	Noise
11	0	0	0	7	2→7→2	Pitot	Noise
12	0	0	0	6	2→7→2	Pitot	Noise
13	0	0	0	5	2→7→2	Pitot	Noise
14	0	0	0	5→8→5	3	Pitot	Noise
15	-6	0	0	5→8→5	3	Pitot	Noise
16	-6	0	0	5	2→7→2	Pitot	Noise
17	-6	0	0	6	2→7→2	Pitot	Noise
18	-6	0	0	7	2→7→2	Pitot	Noise
19	-6	0	0	8	2→7→2	Pitot	Noise
20	-17	0	0	6	2→7→2	Pitot	Noise
21	-17	0	0	5→8→5	3	Pitot	Noise
22	-24	0	0	5→8→5	3	Pitot	Noise
23	-24	0	0	6	2→7→2	Pitot	Noise
24-37	Repeat runs 10-23 with Hot-wire						Noise
38-42	Replicate runs 1-5						Uncertainty

Table 3.1: Test matrix for ACE2.0 freestream characterization.

how to best improve the uncertainty if necessary.

Finally, repeat data points will be measured by repeatedly settling on and off the set condition for the parameter of interest. While data will be gathered throughout the entire characterization test matrix, runs 1 and 20 will be solely for repeat data measurements. These two runs will provide a direct comparison of replicates that will account for any correlations that were not considered or unquantifiable. The standard deviation of this data will be added in quadrature to the systematic uncertainty to calculate the total uncertainty for each parameter of interest for the freestream flow.

3.2.2 Freestream Disturbance Hysteresis

Dynamic sweeps of both Mach number and Reynolds number will be performed to explore any potential hysteresis effects in either the noise or the control parameters. Specifically, this will be accomplished during the dynamic runs in the characterization test matrix in Table 3.1. The goal is simply to identify the existence of any hysteresis effects to inform future work within ACE2.0. The Reynolds number sweep runs are necessary to determine the value at which transition occurs, so sweeping the Reynolds number back down will not add any additional work and will ensure that there is no hysteresis. For the Mach number however, there is no past data to determine the existence of hysteresis, so these runs will establish a baseline. The noise level is known to decrease with an increase in Mach number, so identifying any hysteresis in this will be necessary to inform future experiments.

3.3 Mach Trajectory and Potential Hysteresis Proof of Concept Experiment

This objective will primarily serve as a demonstration of the capabilities for ACE2.0 and will also provide preliminary insight into the hysteretic behavior of dynamic Mach number experiments. The flow characteristic that will be specifically explored in this research will be shock interactions using schlieren. The goal will be to observe hysteresis in the transition from regular reflection to Mach reflection by varying the Mach number. The challenge of this is that the only facilities that have successfully produced this hysteresis had low freestream disturbance levels and an open-jet test section, while ACE2.0 has a closed test section and is not considered a "quiet" facility. In order to provide the best conditions for hysteresis to be observed, these experiments will be performed at higher Mach numbers and a lower unit Reynolds number where freestream disturbance levels are lowest.

The experiments will be based on the methodologies and results from Durand et al. [15] and Tao et al. [46] in addition to the experimental setup of Mai [6]. The Mach number will be varied across either the Von Neumann condition or the detachments criteria to force the transition from regular reflection to Mach reflection or vice versa. In order to choose the wedge angle and Mach number

range for each experiment, Figure 3.3 was created following the processes shown by Mouton [43] for each condition. Using the pressure ratio and flow deflection angle for an oblique shock, the shock angle is solved numerically as a function of the freestream Mach number for each condition. The shock angle and Mach number are then used to produce the detachment and Von Neumann condition relationship between wedge angle and Mach number. Below the Von Neumann condition, only regular reflections are possible as shown in Figure 3.4. Above the detachment condition, only Mach reflections are possible as shown in Figure 3.5. Between these two condition, either shock formation is possible.

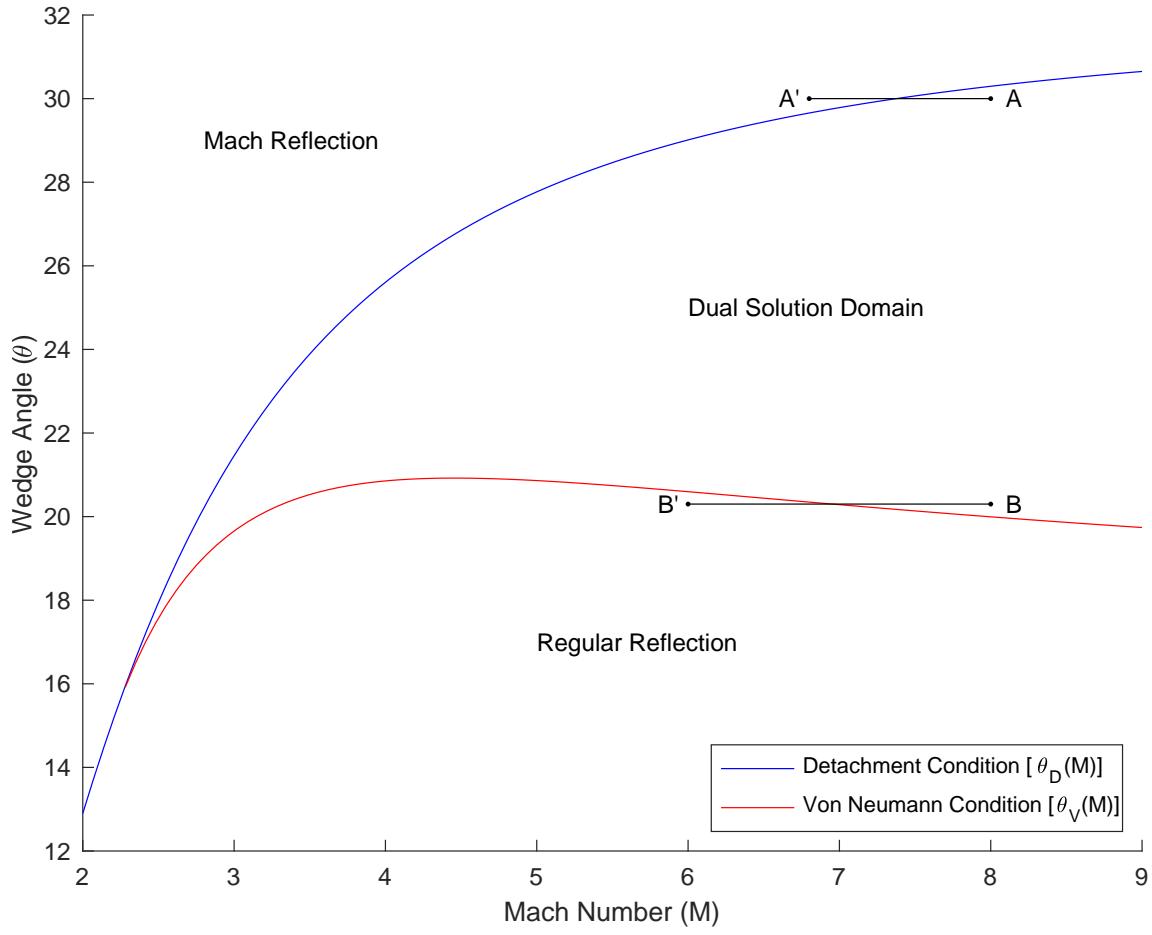


Figure 3.3: Shock wave reflection configuration domains for Mach number and wedge angle

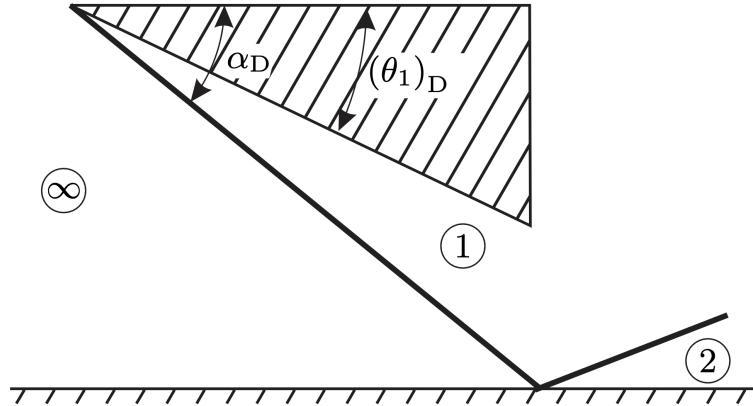


Figure 3.4: Flow over wedge resulting in Mach reflection of shock [43]

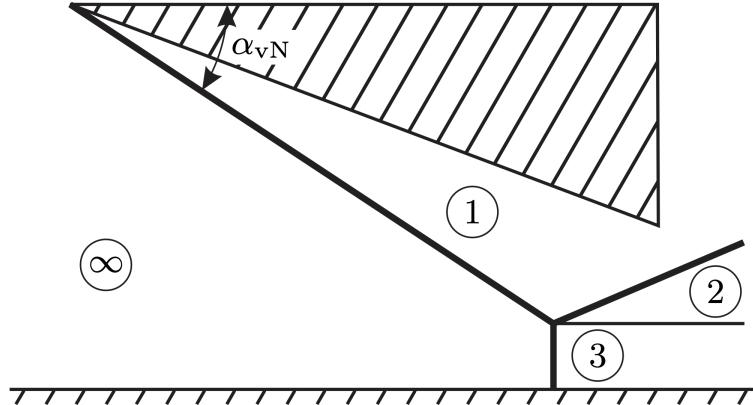


Figure 3.5: Flow over wedge resulting in regular reflection of shock [43]

The two experimental setups are shown as A and B in Figure 3.3. For A, the wedge angle is 30° and the Mach number range is 7 to 8. For B, the wedge angle is 20.3° and the Mach number range is 6 to 8. For both paths, the Mach number will start at the point in the dual solution domain, decrease across either the detachment condition or the Von Neumann condition, and then increase back into the dual solution domain (i.e. AA'A, BB'B). The reverse of these will also be explored if hysteresis is not observed initially.

The physical model for these experiments will be very similar to the double wedge setup used by Mai [6] in ACE as shown in Figure 3.6. If 3D printing with Rigid 10K produces an acceptable

leading edge, then a pair will be printed for each angle needed. If future research will utilize this double wedge setup, then a hinged mechanism will be designed and fabricated to use a single pair of wedges for any desired angle.

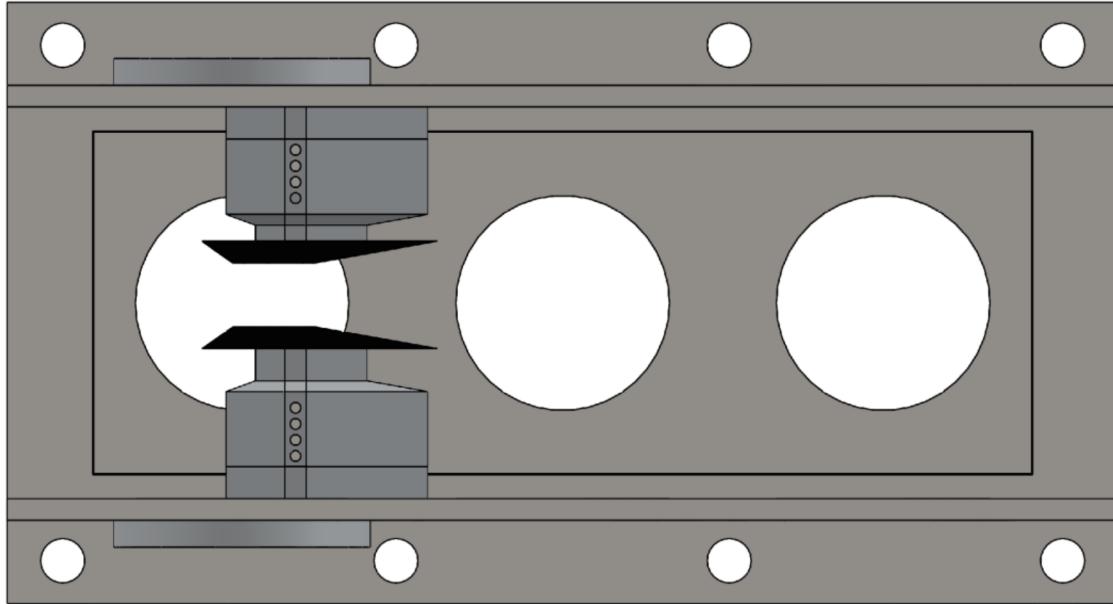


Figure 3.6: Double wedge experiment setup [6]

The expected results should appear similar to the numerical results from Ben-Dor et al. [38], Durand et al. [15], and Tao et al. [46] with an example shown in Figure 3.7. Although the Mach number range and wedge angle are different, the hysteresis should be the same for the chosen paths in this experiment. The path in Figure 3.7 is representative of path AA'A, which crosses the detachment condition. There have not been any simulations published that cross the Von Neumann condition by varying the Mach number, so path B will be explored secondary to path A.

In either case, the final objective will be to guide future experiments by determining if ACE2.0 is capable of reproducing the hysteresis in shock interactions or incapable due to freestream noise.

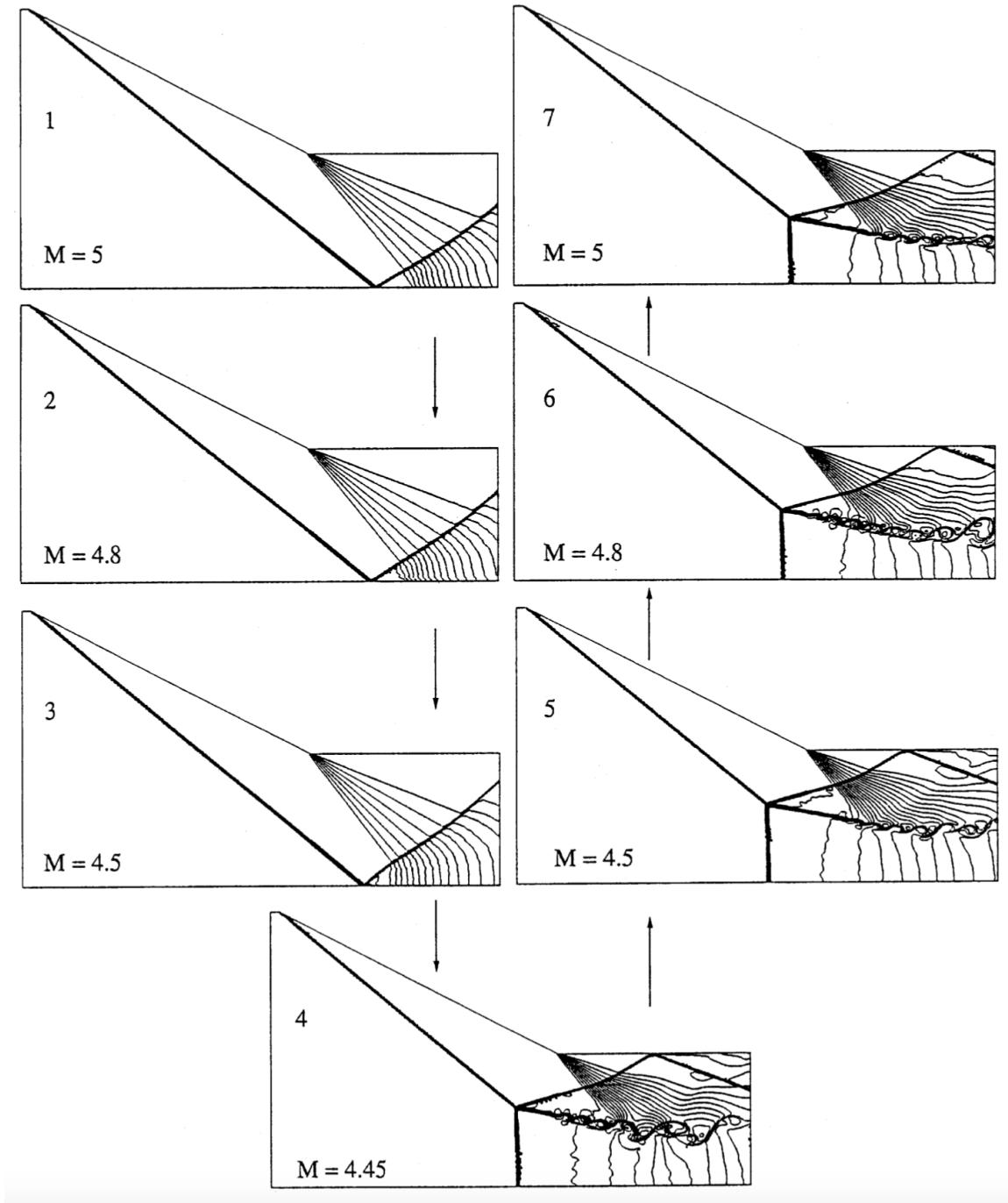


Figure 3.7: Mach-number-variation-induced hysteresis for 27° wedge [38]

4. REAMAINING WORK

The path forward will follow the manufacturing schedule shown in Figure 2.28. The pressure test will be performed as soon as the nozzles are finished machining, tentatively May 1, 2024. Depending on the results of the pressure test, the process could be anywhere from a single day to two weeks. Once complete though, the nozzles and sidewalls will be shipped to the polishing vendor, which should have a quick turn around of two weeks. Upon arrival to the NAHL, the full ACE2.0 nozzle will be finally assembled and installed. With proper planning prior to the final installation, the process should not take more than a week to begin shakedown and characterization.

In the meantime, the servo control program will be written between now and the pressure test. The Mach number feedback will be implemented, and the Reynolds number control capability will be explored and potentially implemented before the final install. Again, this will primarily depend on the test schedule for the M6QT and the amount of time needed to replace the manual valve with a controlled valve.

The characterization and hysteresis experiments will be performed immediately following installation and initial calibration. The primary goal is to ensure complete function of ACE2.0 along with a demonstration of the capabilities and potential for future research. Additionally, the documentation for the nozzle operation will be written based on the best practices deduced throughout the experiments.

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APPENDIX A

ACE2.0 NOZZLE CONTOUR

The section of the Fortran code that was modified is shown before and after below. This modification replaced the specified quadratic throat expansion curve with a quartic to enforce zero slope and zero curvature at the throat.

Before:

```
do 10 i=1, nch
  theta(i) = dthetai + float(i-1)*dth
  x(i) = tan(theta(i))/2./k
  xw(i) = x(i)
  y(i) = 1.0 + k*x(i)**2
  yw(i) = y(i)
10 continue
```

After:

```
do 10 i=1, nch
  theta(i) = dthetai + float(i-1)*dth
  xthetai = sqrt(tan(thetai)/k)
  k4 = -k/2./xthetai
  pc = -9.*(k**2)/3./((4.*k4)**2)
  qc = (2.* (3.*k)**3 - 27.* ((4.*k4)**2)*tan(theta(i)))
& /27./((4.*k4)**3)
  npi = 2.*pi/3.
  tc = 2.*sqrt(-pc/3.)
& *cosacos((3.*qc/2./pc)*sqrt(-3./pc))/3. - npi)
  if((3.*qc/2./pc)*sqrt(-3./pc).lt.-1.) then
    tc = 2.*sqrt(-pc/3.)*cosacos(-1.)/3. - npi)
  end if
  x(i) = tc - k/4./k4
  xw(i) = x(i)
  y(i) = 1.0 + k*x(i)**3 + k4*x(i)**4
  yw(i) = y(i)
10 continue
```

The resulting analytic equations from MATLAB for each section are given by the following (in inches):

$$\text{Subsonic: } -0.0002679752287799994x^5 - 0.0066993807195x^4 - 0.04466253813x^3 + 0.033746187$$

for $-10 < x < 0$

Throat: $-2689.610971179115x^4 + 181.528229581324x^3 + 0.033746187$ for $0 < x < 0.033746187$

Straight: $0.206725280364801x + 0.030258092015591$ for $0.033746187 < x < 6.1460114$

Straightening: $2.180909737850381x^{0.960492634168194} + 5.934566177927477 \times 10^{284}x^{-367.9331632104439}$
 $-1.684363604007221x^{1.011336503949665} - 0.023814395465567 \ln(0.418646933043039x)$
 -0.585293189697896 for $6.1460114 < x < 40.07774$

The contour specified by these functions is shown in Figure A.1. The maximum deviation of the fitted equation for the straightening section from the MOC points is 0.0005 inches.

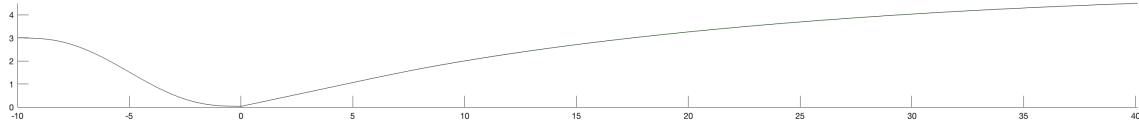


Figure A.1: Final nozzle contour defined by analytic functions.