## MATHEMATICA QUICK REFERENCE

```
Run Mathematica
  mathematica
                            (evoke Mathematica frontend)
                                                                 Quit[] or Exit[]
                                                                                                       (exit Mathematica)
Arithmetic
+, -, * (or a space _{\sqcup}), /, ^ (power), e.g. a*x^2 + 2 x - 3/5
                                                                        (ax^2 + 2x - 3/5)
                                                                                                n^{-}digits
                                                                                                              base n number
Mathematical Functions
                                 \text{Exp}[x] or \text{E}^x
                                                        (e^x)
  Sqrt[x]
                                                                 Log[x]
                                                                                      (\ln x)
                                                                                                Log[b, x]
                        (\sqrt{x})
                                                                                                                    (\log_b x)
                                                                                                                  (\sin^{-1}x)
                                 Cos[x]
                                                                                                 ArcSin[x]
  Sin[x]
                      (\sin x)
                                                      (\cos x)
                                                                 Tan[x]
                                                                                     (\tan x)
                                                   (\tan^{-1} x)
                   (\cos^{-1} x)
  ArcCos[x]
                                 ArcTan[x]
                                                                 Sinh[x]
                                                                                                 Cosh[x]
                                                                                                                   (\cosh x)
                                                                                    (\sinh x)
                                                  (\sinh^{-1}x)
  Tanh[x]
                    (\tanh x)
                                 ArcSinh[x]
                                                                                 (factorial)
                                                                                                 Abs[x]
                                                                                                                       (|x|)
  Mod[n, m]
                 (n \mod m)
                                 Max[x, y, \ldots]
                                                                 Min[x, y, \ldots]
                                                                                      (min)
                                                                                                Binomial [n, m]
                                                                                                                      (C_m^n)
                                                      (max)
  \text{Re}[z]
                  (real part)
                                 Im[z] (imaginery part)
                                                                 Conjugate [z]
                                                                                         (\bar{z})
                                                                                                 Arg[z]
                                                                                                                (argument)
  LegendreP[n,x] (P_n(x))
                                 HermiteH[n,x] (H_n(x))
                                                                 LaguerreL[n,a,x] (L_n^a(x)) BesselJ[n,z]
                                                                                                                    (J_n(z))
              (\frac{2}{\sqrt{\pi}}\int_{0}^{x}e^{-t^{2}}dt)
  Erf[x]
                                 Gamma[z]
                                               (Euler \Gamma(z))
                                                                 Zeta[s] (Riemann \zeta(s))
                                                                                                 Random[]
                                                                                                                  (number)
Mathematical Constants
                                                                                 (i=\sqrt{-1})
  Ρi
              (\pi \approx 3.14159)
                                 Ε
                                              (e \approx 2.71828)
                                                                 Ι
                                                                                                 Infinity
                                                                                                                       (\infty)
Data Objects
  123
             (integer)
                           3/7
                                      (rational)
                                                                             2 + 8I (complex)
                                                                                                       "text"
                                                                                                                    (string)
  \{a, b, \dots \}
                                                                 h[a, b, \ldots] (expression/w head h, elements a, b, \ldots)
                              (list with elements a, b, \ldots)
  expr[[i]]
                    (i-th element of the expression expr)
                                                                                                          (indexed object)
                                                                 a[i]
Arbitrary-Precision Calculation
                                                                                   (value of expr with n-digit precision)
  expr//N or N[expr]
                                 (numerical value of expr)
                                                                 N[expr, n]
  Rationalize [x]
                         (rational number approximation)
                                                                 Precision[x]
                                                                                          (significant decimal digits in x)
Defining Variables, Functions, and Rules
                                                                 expr /. x \rightarrow a
  x = value
                              (assign a value to symbol x)
                                                                                                  (replace x by a in expr)
  x := expr
                                      (delayed assignment)
                                                                 expr //. x \rightarrow a
                                                                                                      (replace repeatedly)
  x = . or Clear[x]
                             (remove value assigned to x)
                                                                 lhs :> rhs /; test
                                                                                               (apply rule if test is True)
                                   (define a function f(x))
                                                                 lhs := rhs /; test
                                                                                                    (assign if test is True)
  f[x_{-}] := expr
Algebraic Calculations
  Expand [expr]
                                   (multiply out products)
                                                                 Factor [expr]
                                                                                          (reduce to a product of factors)
                                   (common denominator)
  Together [expr]
                                                                 Cancel[expr]
                                                                                                 (cancel common factors)
  Expand[expr,Trig->True]
                                      (\sin^2 x \to \sin 2x, \text{ etc.})
                                                                 Simplify [expr]
                                                                                                      (find simplist form)
                                      (\sin 2x \rightarrow \sin^2 x, \text{ etc.})
  Factor[expr,Trig->True]
                                                                 Apart [expr]
                                                                                          (write expr as a sum of terms)
  Coefficient [expr, x]
                                  (coefficient of x in expr)
                                                                 Exponent [expr, x]
                                                                                                (max power of x in expr)
  Solve [lhs==rhs, x] (solve algebraic equation for x)
                                                                 DSolve [eqn, y[x], x]
                                                                                              (solve differential equation)
                                         (reduce equations)
                                                                                                     (eliminate variable e)
  Reduce [eqn, x]
                                                                 Eliminate [eqn, e]
Linear Algebra
  \{a,b,c\}
                                            \{\{a,b\}, \{c,d\}\}
                                                                   (2 \times 2 \text{ matrix})
                                                                                                         (matrix multiply)
                               (vector)
                                                                                      n.m
  Inverse[m]
                   (inverse of matrix)
                                            Transpose [m]
                                                                      (transpose)
                                                                                      Det[m]
                                                                                                             (determinant)
  MatrixPower[m, n]
                                            MatrixExp[m]
                                                                             (e^m)
                                  (m^n)
                                                                                      LinearSolve [m, b] (solve mx = b)
  Eigenvalues[m]
                          (eigenvalues)
                                            Eigenvectors [m]
                                                                   (eigenvectors)
                                                                                      Eigensystem[m] (value & vector)
Calculus
  D[f, x]
                               (\partial f/\partial x)
                                            Integrate[f, x]
                                                                         (\int f dx)
                                                                                      Series [f, \{x, a, n\}] (expand at a)
                                            Integrate [f, {x, a, b}] (\int_a^b f dx)
                                                                                      \operatorname{Limit}[f, x \rightarrow a]
  D[f, \{x, n\}]
                            (\partial^n f/\partial x^n)
                                                                                      \begin{array}{l} \mathtt{Limit}[f,x\text{->}a] & (\lim_{x\to a}f) \\ \mathtt{Product}[f,\{i,m,n\}] & (\prod_{i=n}^mf) \end{array}
                                            Sum[f, \{i, m, n\}]
                                                                       \left(\sum_{i=m}^{n} f\right)
                                   (df)
  NIntegrate, NSum, NProduct, NSolve, NDSolve, FindRoot
                                                                               (numerical integration, summation, etc.)
Graphics
  Plot[f, {x, a, b}, option \rightarrow value]
                                                                                  (plot f as a function of x from a to b)
  Show [plot_1, plot_2, ...]
                                                                                                            (redraw plots)
                                                                 (three-dimensional plot of f as a function of x and y)
  Plot3D[f, {x, a, b}, {y, c, d}]
  ListPlot[\{\{x_1, y_1\}, \{x_2, y_2\}, \dots \}]
                                                                                                 (plot points (x_1, y_1) \dots)
  ParametricPlot[\{x, y\}, \{t, a, b\}]
                                                                                                  (plot curve (x(t), y(t)))
Plot options:
```

(draw frame)

AspectRatio (height-to-width ratio) AxesLabel->{"x", "y"} (add labels) Frame -> True

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Programming
 Module [\{a, b, \dots\}, expr_1; expr_2; ...] (a procedure/w local variables a, b, \dots, return value of last expr)
 Table [expr, \{i, max\}]
                                                               (make a list of values of expr with i from 1 to max)
 Do [expr, \{i, min, max, di\}]
                                                        (evaluate expr with i run from min to max in steps of di)
 While [test, body]
                                                                (evaluate body repetitively, so long as test is True)
 For [start, test, inc, body]
                                           (evaluate start, then repetitively evaluate body and inc, until test fails)
 If [test, then, else]
                                                              (evaluate then if test is True, and else if it is False)
 Which [test_1, value_1, test_2, ...]
                                                         (give the value associated with the first test that is True)
 Switch[expr, form_1, value_1, form_2, ...]
                                                         (give the value associated with first form matching expr)
 Function[x, body] or body &
                                                                                           (specify a pure function)
 Nest[f, x, n]
                                                                         (apply the function f nested n times to x)
 NestList[f, x, n]
                                                         (generate list \{x, f(x), f(f(x)), \ldots\} nested up to n deep)
 Fold[f, x, {a, b, c}]
                                                                                        (produce f(f(f(x,a),b),c))
 FixedPoint[f, x]
                                                (apply the function f repeated until the result no longer changes)
 Apply [f, \{a, b, c\}] or f @@ expr
                                                                                                 (produce f(a, b, c))
                                                                    (apply f to each elements, \{f(a), f(b), f(c)\})
 Map[f, \{a, b, c\}] or f /0 expr
 i++
          (post-increment)
                                       (post-decrement)
                                                                          (add di to i)
                                                                                          x \neq c \pmod{x} by c
                                                             i += di
  ++i
                               --i
                                                             i -= di
                                                                         (subtract di)
                                                                                          x \neq c  (divide x by c)
           (pre-increment)
                                         (pre-decrement)
                               f::usage="text" (info)
                (comment)
                                                             Timing [expr]
                                                                                (time)
                                                                                          MemoryInUse[] (space)
  (* text *)
Iterators in Do, Table, Sum, etc.
                                                                                     (i from 1 to max in steps of 1)
  \{max\}
                                     (iterate max times)
                                                             \{i, max\}
  \{i, min, max\}
                      (i from min to max in steps of 1)
                                                             \{i, min, max, di\}\ (i \text{ from } min \text{ to } max \text{ in steps of } di)
Logical Operators
                               !=
                                               (unequal)
                                                                            (identical)
                                                                                          =!=
                                                                                                      (not identical)
  ==
                    (equal)
  <
                (less than)
                               <=
                                           (less or equal)
                                                             p \mid \mid q
                                                                                   (or)
                                                                                          p && q
                                                                                                               (and)
  >
             (greater than)
                                       (greater or equal)
                                                                                          Xor[p,q]
                                                                                                      (exclusive or)
                                                                                 (not)
                                                             !p
List Manipulation
 Part[t, i] or t[[i]]
                                            (i-th sublist)
                                                             Position [t, form]
                                                                                         (the position form occur)
 Take [t, n]
                                       (first n elements)
                                                             Last[t]
                                                                                                  (last element in t)
 Drop[t, n]
                                  (drop first n elements)
                                                             First[t]
                                                                                                 (first element in t)
 Count[t, form]
                         (number of times form occur)
                                                             MemberQ[t, form]
                                                                                        (test whether form is in t)
 Prepend[t, e]
                                (add e at the beginning)
                                                             Insert[t, e, i]
                                                                                             (insert e at position i)
                                      (add e at the end)
                                                             Delete[t, i]
                                                                                      (delete element at position i)
 Append [t, e]
                                                             Join[t_1, t_2, \ldots]
 ReplacePart[t, e, i]
                           (replace with e at position i)
                                                                                        (concatenate lists together)
 Union [t_1, t_2, ...]
                                          (union of lists)
                                                             Intersection [t_1, t_2, \ldots]
                                                                                               (common to all lists)
 Sort[t]
                       (sort elements in standard order)
                                                             Reverse[t]
                                                                                    (reverse the order of elements)
 RotateLeft[t, n]
                             (rotate n places to the left)
                                                                                       (rotate n places to the right)
                                                             RotateRight[t, n]
Input/Output
                                                                                   (save the definition of x to file)
  << file  (read expressions from file, return last expr)
                                                             Save["file", x]
 expr >> file
                                   (write expr to a file)
                                                             Display["!psfix>file",graph]
                                                                                                    (save as PS file)
 expr>>> file
                                 (append expr to a file)
                                                             ReadList["file", type] (read objects of a given type)
  !!file
                          (display the content of a file)
                                                             PSPrint[graph]
                                                                                     (print a hardcopy of graphics)
                                        (load a package)
  <<Calculus'VectorAnalysis'
                                                             !command
                                                                                         (issue a UNIX command)
Patterns
                          (any \ expr)
                                         \mathbf{x}_{-}
                                                        (any expr named x)
                                                                                 x:pattern
                                                                                                    (match pattern)
 x_h
               (pattern with head h)
                                         pattern /; condition (conditional)
                                                                                                    (if test is True)
                                                                                 pattern?test
                  (sequence of expr)
                                                         (zero or more expr)
                                                                                                (expr \text{ with default})
                                                                                 \mathbf{x}_{-}: v
Expression in Different Formats
 FullForm[e] (full form)
                                                             FortranForm[e] (fortran)
                               \mathtt{CForm}[e]
                                               (C codes)
                                                                                          StandardForm[e] (math)
 InputForm[e]
                    (input)
                               OutputForm[e]
                                                    (out)
                                                             MatrixForm[e] (matrix)
                                                                                          TeXForm[e]
                                                                                                              (T_{F}X)
Input Editing and Help
                         (last result)
                                                                                 * (represent 0 or more characters)
                                         ?Name
                                                            (help on Name)
 %
                  (result on Out[n])
                                                      (more help on Name)
                                                                                      (1 or more lower-case letters)
 n
                                         ??Name
                                                                                 @
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Ctrl-C

(interrupt execution)

!

(shell escape)

(evaluate expr)

Shift-Enter