

## Week 1 - Crystal Binding Comprehension Check

Total points = 25 (scaled by a factor of 1/10 in the system)

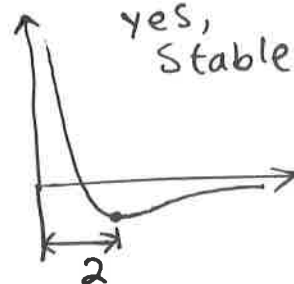
### Question 1 (5 points)

The potential energy of a diatomic molecule is given by  $U(r) = -1/r + 1/r^2$ , with  $r$  being the separation distance between the two atoms. Does this configuration lead to a stable bond? If yes, what is the bond length?

$$\frac{dU}{dr} = \frac{1}{r^2} - \frac{2}{r^3} = 0 \Rightarrow \text{critical point at } r=2$$

$$U(2) = -\frac{1}{2} + \frac{1}{4} = -\frac{1}{4} ; U(\infty) = 0$$

$$U(0) = \frac{1}{r}(-1 + \frac{1}{r}) = \frac{1}{0}(-1 + \infty) \rightarrow \infty$$



### Question 2 (8 points)

Match each of the following bond types to the interaction mechanism involved in the bonding:

1. van der Waals **C**

A. Interaction between free electrons and fixed ions

2. Covalent **D**

B. Electrostatic potential between oppositely charged ions

3. Metallic **A**

C. Dipole-dipole interaction between neutral atoms

4. Ionic **B**

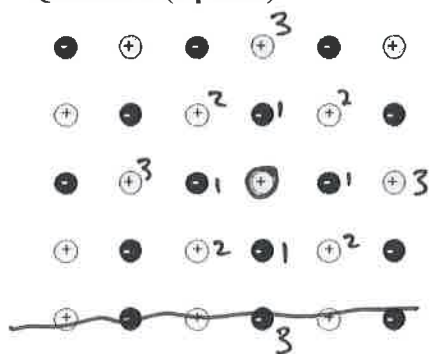
D. Sharing of electronic orbitals

### Question 3 (6 points)

The ionization energy for atom A is 4 eV. The electron affinity for atom B is 6 eV. The cohesive energy for molecule AB relative to ions  $A^+$  and  $B^-$  is 2 eV. Can free atoms A and B join together to form a molecule? Justify your answer.

$$\begin{aligned} \text{Loss} &= 4 \text{ eV ionization} \\ \text{Gain} &= 6 \text{ eV} + 2 \text{ eV} = 8 \text{ eV} \\ \text{Gain} &> \text{Loss} \Rightarrow \text{yes, they can join} \end{aligned}$$

### Question 4 (6 points)



Assume that in this figure the gray and black circles represent oppositely charged ions. Calculate the first three terms in the Madelung's constant.

$$\alpha = \frac{4}{1} - \frac{4}{\sqrt{2}} - \frac{4}{2}$$

1<sup>st</sup>                  2<sup>nd</sup>                  3<sup>rd</sup>