Push Down Autonata (PDA) FA can't be used to recognize all Cr. A clam of automata anocialed Owde CALS is PDA FA have strictly finite memories whereas recognition of a CFL requires storing and an unbounded amount of information to scan a slewy from the language  $Z = \{a^nb^n\}$  we must not only check whether all as precide the first by but also count the nos of als funce on is combounded, counting cannot be done with finite memory in the memory of stade. This type of corrangement where a few of stade to the land of the containing ments where a few of stade. PA has stack leads to the generatus of a PDA PDA consists of an input- Jape ja finte conted and a stade to store and retiene the symbol. Pach move of a PDA depends on the current-state, input-symbol and top of state symbol.

Current-state, input-symbol and top of state and replacing Rach move consists of change of state and replacing top of state symbols.

Top of state symbols

Répauls model de la POR is non-de demenustre Mathematually a POD m is a 7 thether mobilion No (6,5,5,5,90, 20,5) where [-injutal of rates : 9 - finite at of dates. E - injust diphetel-To shack alphabet. F = Q is ret of final states. and s is a mapping from 9 x EU [E] x T lo a famile subsets of 9 x Ft. Interpretation of mores Helen teal- '96 PDA is in state 9, with ilp symbol a & 2 the topmost-state symbol, then pDA can enter into any state Pi and explace 2 by stains of (14 i 4m) and advance the ilp head one symbol. The more & (9 26 ) = {(p1x1) (p222) ... (bwilm) independent of the input symbol being scanned with Z on stack top, can entership: and replace Z by &i (12 i < m) states that Instantineous Description (ID) During laculton a PDA goes through a squence of conjeguration called ID consists of State is uput get to be samed

a triplet- (9, w, 8) where current stale, or is the cupulget to be read (beff most symbol of a is the current enjoyed) of is the stack content. (leftenost- symbol of & co-the current top-of stalk yould. lach move involves a charge from one ID to another the symbol and to represent a A move is defined by the following rule (P, ax, Ax) - (p, a, Pa) y 8 (p, a, A) includes (9,B) té reperents a seguence of moues Language acceptance by PDA PDA can accept a given language in 2 ways (1) Acceptance by emply stacle (2) Acceptance by Ginal state danguage crosspeed by empty stack defined as NM= { w / (90, w, 20) F (p, E, E) , | or some pin q Language cicrepted by Junal state defined as (p) = { w/(90,w,20) + (p,E) } per some u Fd Determination PDA (DPPA)

Non determination PDA (NPBA) (DPPA) PDA 2 types the are To non defermente PDA no: of choices of moues in each of nones will be 2 lypes

In the fant type of move depending on Hate of juile contail, unput symbol of top symbol on state a no: of choices are Mossible Pach choice consists of a next state for finite contain and a string of Symbols to replace the topmost states organd After selection a choice, input head is roue (E-mour) es similar to just-excep es similar to just-exceptthat input symbol not and and inputhead not advanced after the more. This type of more allows only to manyoulate the state without reading april rymbols. Deterministic PDA: (DPDA) A PDA is said to be deferministic of all the IPs in the design has to give Jornally we say a PDA m'is determinant only a single move (1) for each 9 in Q and 2 in F, whenever 8(9, E, Z) is non-empty, teur 8(q,a,2) is empty Jer all a in 5. (2) Jer no qui 9, zin fand a in ¿ v { E} does & (9,9,2) outains more than one element-

(1) Design a PDA stat accepts fexes!"
(1) Design a PDA deste
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and market of the
The central title and match the right grown to the the right grown of the title and match the right grown to the title title to the title to the title to the title title title to the title tit title tit
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Son state 9d PDA matches and proposed & for input- 1. At the and input- 1 By the and
input is comed-, severe of left postular
matches with the in put and the control
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9 2 - 1 real words remove top pale
Comput is show E)
The state of the s

A formal dexception as given as Pon m= ({9,1928, {0,1,03, {R,B,G}, \$19,15,8,9} & defined = (91,BR S(9,1,0,R) 8(91,018) =(91,88 8(91,0,6) = (9, 3BG) = (9,2,8)= (9,2,8)8 (9,1, C,R) 8 (9,12,518) 8 (912626) = (91, GR) 8 (917 178) = (91,768) 5(917128 = (91766) 8(91,71,6) = (92, E) 8(92,0,3) 8 (92) 1,6) = (92,E) 8 (92,8,8) = (92,6) Trainition table for &  $\overline{C}$ Top of skele State 0 symbol (9,1,GR) 9,27R 91,BR) 8,00B) A1, 38) 94 (91, 35) PDA 01010 Consider a ster 9,701clo, P) + (9,1,1clo, BR) F. (912010, GBR) F (9200, BR) F (920, BR) +(9,2, E, R) +(92,2) E

1- Sweet we Oth
Denigo a NPDAIILE recognize & - sweet we (0+1) There are 2 choices of mouses the machine wild middle of stein is reached.
There are 2 choices of modes is reached.  on in 90 state until middle of stein is reached.  There are with middle of them Menters to middle stem in ocard, then Menters to middle stem in ocard, then Up symbols.
there well middle of steins to the
on in go state is ocad, then the symbols
91 middle II march remaining of June
(A) 1 1111 (A) 1 (
contents of state and black go, R. P.
92 d thus of stack contents of stack contents of stack contents of stack of 13, 5R, B, 63, 5, 90, R, \$3
= C3 12/1/3/
( ) ( ) ( ) ( ) ( )
12 S (90) OIR) = (70) BR)
(226(92.12R) = (90.6R)
(3) & (90,01B) = 1(90,BB) 3(71)E)
(4) 8 (90,0,6) = (90BG)
(901.8) = (90.68)
(6) $S(90,156) = \{90,660, 91,20\}$
(7) 8(91,0,B) = (9,7E)
(7) SC 9150/B) (915C)
(8) $\mathcal{E}(q_1, 1, 6) = (q_1, \epsilon)$
(9) 8 (90, E, R) = (9, 15E)
(10) 8(91,2,R) =(9,1,E)
State symbol 0 1 (9.5)
(90, BR) (90, GR) (915E).
90 A 160, BA HIST (20, 68)
(go, BG) (Qo, GG), -
The Audi
(9, 8 (9, 5) (9, 5) (-)
1 CS ( - (D128)

Cowridu a stay. 011110 11 19 01 (90,011110, R) 90, 11110, BR (90,1110,6BR) - (91,110,BR) (10,110,66BR) -> (1,10,6BR) (90,10,666BR) 7 (91,0,66BR) (91,0; BR) (90,0) show GBR) 90, E, BGGGGBR) Construct a PDA to megrije all palendiomes over Mn is same as work with a slight difference Any palindrones is of form work or wowker or wowk or w PDA has to charge from got go wethout changing the state Bust as medpoint const to dekumed, DDA is given a choice to ahouge over from go to 91 Jon each 0001.

go include the fell chayes in the above probles S(20,0,R) = {(90,BR), (9,0R)} S(90,1,R) = {(90,6R),(9,0R)} 8 (90,0,8) = { (9,88), (9,8), (1,5)} S(90,0,6) = {(90,86), (91,9)} S(90,1,B) = \( (90, BB), (91,B) 3. 8 (90,100) = { (90,66) 2(9106) 2(9108)}. [ (90,6R) (91,8) { (90,6R) (91,8) } [ (90,6R) (91,8) ] [ (90,6B) (91,8) ] [ (90,6B) (91,8) ] [ (90,6B) (91,8) (91,8) ] [ (90,6B) (91,8) (91,8) [ (90,6B) (91,8) [ (9158) 91 eg (90,00100, R) =7 (21,0100, R) (90,0.100,BR) -7 (91,000, BR) (90,100,BBR) 791,100,R) 90,00, 68ER (91,00, BBR) (90,0,8688) (9,0,688) (9,20,888) (9,20,888) (9,20,888) (9,20,888) Accept -

Construct a PDA for language

La f w E { a, b} + / m(w) = n\_b(w) such / late

La f w E { a, b} + / m(w) = n\_b(w) Whenever a is read dinte push D to skele then when b is read pop a out of the then when a corrend pop B. m=(8903, (9,6), {A,B, 203, 5,203,4). where S defined as: 8(90, 8, 20) = (90, 8) S(90, a, 20) = (90, A20) (90, alab, 20)  $\begin{array}{lll}
S(90, b, 20) &= (90, 820) \\
S(90, a, A) &= (90, AA) \\
S(90, b, B) &= (90, BB) \\
S(90, a, B) &= (90, BB) \\
S(90, a, B) &= (90, E) \\
S(90, b, A) &= (90, E) \\
S(90, B) &= (90, E) \\$ Design a PDA to recognize the language 1- fanbolo 213 Here m=({90,9,3,(0,6) (A,0020),8,90,20,4) where of defined as  $\begin{array}{ll}
\delta(q_0, a, z_0) &= (q_0, A z_0) \\
8(q_0, a, A) &= (q_0, AA) \\
8(q_0, b, A) &= (q_1, E) \\
8(q_1, b, A) &= (q_1, E) \\
6(q_1, b, A) &= (q_1, E)
\end{array}$ 8(91,2,20) = (91,2)

Here cohen a is read push A to stack.

When b is read after A push pop A .

When when all the strings are read stack contains 20 pop 20 and make the stack empty contains 20 pop 20 and make the stack empty

eg (90, 9961,20) + (90, 966, A20) when all is read. 1- (20, 66, AAZO) 1-(21,6, AZO) + (21, E, Zo) + (21, E, E). (b) Constant a PDA, to secognize  $\lambda = \{a^n, b^m c^{m+n} | n, m z \}$ Here stack symbol A used to count no. of a's & b's. In state 8tate 90, PDA pushes A Fr each Qu. 9h state 91 PDA scans bb + pashes one A Ja each b. Dn reading C,

PDA goes to 92 state while poping of fone A

9n 92, I reads c of pops of one A for

each c. At .nd y all As are or hausted, PDA goes to final state 22 maling slade confty m = ({90,9,192, =3, {a,6,63, (A,20), 8,90,20, 8 \$ 3 step 705 a 167 E nied as (2252) - 94 34 defined as (2252) 8 (90, 9, 20) = (90, A 20) 8 (90, a, A) = (90, AA) (90, b, 20) = (20, A 20) 8 (q0, b, A) = (21, AA) = (21)AA) 8 (917 b, A) = (92, E)-8 (91, c) A) 8 (qu, c, A) = (.92, E) ~ 8 (92, 5, 20) = (92, 8)/6 por (a for signing)

Scanned with CamScanner

eg : (90, bbccc, 720) + (90, bbccc, A20) 1100 1 (91) becc, nA20) + (21) ccc, AAA20), F (92, CC) AA20) F (92, C, A20)

- (92, E, 20) F (92, E, E)

Acceptto recognize d={aibick|j=i+k, 1 Construct a PDA Lece 2 stack symbols 1 + 1 ened : 2abbbe Symbol A aned to count no: of a's.

B is aned to count excess no: of b's. In state 90, PDA pushes A dor cach 9 In state 911 as long as A is in stack sPDA pops off one A for each b. cohen A's are

pops off one A for each b.

exhamted, PDA stacks pushing one B for each b.

On encounting In 92 it rope off one B for each C At end when B's are exhausted and 20 is exposed, it gosto state makes state empty and rea accepts L. m = ( {90,91,923, {a,b,c3, {A,B,20},8,90,20,43 where & defined as 8(90,9,20) =(90,120) S (90, a, A) = (90, AA) S (90, b, 20) = (91, B 20) 8 (90, b, A) = (91, 2E) 8 (91, b, A) = (91, 2E)