SESSION 13 - ASSIGNMENT 13.1 _13.2_13.3 DECISION TREES

Date: 18th Feb 2019

title: "Assignment 13.1"

Use the given link below:

https://archive.ics.uci.edu/ml/machine-learning-databases/00304/

Problem- prediction of the number of comments in the upcoming 24 hours on those blogs, the train data was generated from different base times that may temporally overlap. Therefore, if you simply split the train into disjoint partitions, the underlying time intervals may overlap. Therefore, the you should use the provided, temporally disjoint train and test splits to ensure that the evaluation is fair.

ASSIGNMENT NO # 13.1

- a. Read the dataset and identify the right features.
- b. Clean dataset, impute missing values and perform exploratory data analysis.
- c. Visualize the dataset and make inferences from that.
- d. Perform any 3 hypothesis tests using columns of your choice, make conclusions.

```
author: "Vineet Bhardwaj"
date: "19 February 2019"
output:
word_document: default
html_document: default
---
"``{r setup, include=FALSE}
knitr::opts_chunk$set(echo = TRUE)
"``
"``{r}
#setting the Working directory
setwd("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedback")
getwd()
#loading all the required libraries
library(ggplot2)
library(rstan)
```

```
library(rstanarm)
library(class)
library(png)
library(grid)
library(data.table)
library(foreach)
library(MatrixModels)
library(xgboost)
library(ranger)
library(foreach)
library(e1071)
library(FNN)
library(glmnet)
#combine all files except "blogData train.csv" into one dataframe
setwd("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedback")
filenames=list.files(full.names=TRUE)
allTest=lapply(filenames,function(i){ read.csv(i, header=FALSE)})
blog.test= do.call(rbind.data.frame, allTest)
View(blog.test)
blog.full <- read.csv('C:/Users/Vineet Bhardwaj/Desktop/BlogFeedback/blogData train.csv', header = FALSE)
#Writing the combined Test Data into one file
write.csv(blog.test, "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blog.test.csv", row.names = F)
#reading the Test combined Data
blog.test <- read.csv("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blog.test.csv",header=TRUE)
View(blog.test)
#As the data doesnot have headers, after understanding the same from the link
#naming the variables in TRAIN Data
att_names <- c( paste(rep(c("comm_","links_"),each=5),
           c(".tot",".pre.1day",".pre.2day",
            ".post.1day",".pre.vsday"), sep=""))
names(blog.full) <- c( paste(c("avg", "sd", "min", "max", "med"),
               ".",rep(att_names,each=5),sep=""),
            att names,
            "pubtime", "length",
            paste("bagwords ",1:200,sep=""),
            paste("basetime_",c("Mo","Tu","We","Th","Fr","Sa","Su"),sep=""),
            paste("pubtime_",c("Mo","Tu","We","Th","Fr","Sa","Su"),sep=""),
            " parents",
            paste(c("min_","max_","avg_"),".comm.parents",sep=""),
            "comm.next24")
```

#naming the variables in TEST Data names(blog.test) <- names(blog.full)</pre>

```
# drop continous variables without variation
drop = c(8, 13, 28, 33, 38, 40, 43, 50, 278)
blog.full1 <- blog.full[, !(names(blog.full) %in% drop)]
blog.test1 <- blog.test[, !(names(blog.test) %in% drop)]
```

log-transform

blog.full1<-data.table(blog.full1)

blog.full1[, comm.next24 := log(1 + comm.next24)]

blog.test1<-data.table(blog.test1)

blog.test1[, comm.next24 := log(1 + comm.next24)]

#Saving the Train and Test Data

write.csv(blog.test1, "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Test.csv", row.names = F)
write.csv(blog.full1, "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Train.csv", row.names = F)

...

The working directory was changed to C:/Users/Vineet Bhardwaj/Desktop/BlogFeedback inside a notebook chunk. The working directory will be reset when the chunk is finished running. Use the knitr root.dir option in the setup chunk to change the working directory for notebook chunks.[1] "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedback"

```{r}

#reading the Final files after naming the headers

test<- read.csv("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Test.csv",header=TRUE) train<-read.csv("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Train.csv",header=TRUE)

#checking the headers of both the data

str(train)

```
str(test)
```

```
data.frame': 60021 obs. of 281 variables:
                       : num 10.63 43.44 1.73 27.23 4.5 ...
$ avg.comm_.tot
                                17.88 75.59 3.04 45.97 6.68 ...
$ sd.comm_.tot
                        : num
                                1 0 0 0 0 0 0 0 0 0
$ min.comm_.tot
                        : int
$ max.comm_.tot
                               259 634 9 371 18 970 191 1065 188 0 ...
                        : int
                               5 20 0 14 0.5 28 1 87 7.5 0 ...
4.018 15.999 0.733 10.784 3 ...
$ med.comm_.tot
                        : num
$ avg.comm_.pre.1day
                         num
                               10.4 44.56 1.53 24.21 4 ...
$ sd.comm_.pre.1day
                        : num
                               0 0 0 0 0 0 0 0 0
$ min.comm_.pre.1day
                        : int
                               235 473 5 228 10 725 179 491 174 0 ...
1 2 0 4 0.5 16 0 19.5 1.5 0 ...
$ max.comm_.pre.1day
                          int
$ med.comm_.pre.1day
                        : num
                                3.817 15.47 0.667 9.998 1.333 ...
$ avg.comm_.pre.2day
                        : num
                        : num
                               10.3 44.69 1.53 24.4 2.56 ...
$ sd.comm_.pre.2day
                                0 0 0 0 0 0 0 0 0
$ min.comm_.pre.2day
                          int
                               235 473 5 228 7 725 179 491 174 0 ...
$ max.comm_.pre.2day
                        : int
                               1 1 0 2 0 3 0 14 1 0 ...
9.78 40.97 1.13 22.56 2.83
                        : num
$ med.comm_.pre.2day
$ avg.comm_.post.1day :
                          num
$ sd.comm_.post.1day : num 16.07 70.31 1.82 39.76 3.67 ...
```

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1 0 0 0 0 0 0 0 0 0 0 ...
192 479 5 337 8 913 189 786 186 0 ...
min.comm_.post.1day :
                            int
max.comm_.post.1day
                            int
                                   5 18 0 10 0.5 26 0 74 5.5 0
med.comm_.post.1day
                            num
                                   0.201 0.5289 0.0667 0.7866 1.6667 ...
avg.comm_.pre.vsday
                            num
sd.comm_.pre.vsday
min.comm_.pre.vsday
                                   13.95 62.13 1.73 30.36 2.21 ...
-229 -461 -5 -156 0 -519 -178 -418 -161 0 ...
                            num
                            int
                                   217 473 4 228 6 725 170 491 174 0 ...
max.comm_.pre.vsday
                            int
med.comm_.pre.vsday
avg_links_.tot
                                   0 0 0 0 0.5
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                            num
                                   0.252 0.193 0.333 0.11 0
                            num
sd.links_.tot
                                   0.904 0.458 0.699 0.356 0 ...
                            num
min.links_.tot
                            int
                                   0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
                                   14 2 2 2 0 0 6 0 1 0
max.links_.tot
                            int
med.links_.tot
                                   0 0 0 0 0 0 0 0 0
                            num
                                   0.0944 0.0733 0.1333 0.0432 0 ...
avg.links_.pre.1day
                            num
sd.links_.pre.1day
min.links_.pre.1day
                                   0.507 0.286 0.34 0.215 0 ...
                            num
                                   0 0 0 0 0 0 0 0 0 0
                            int
max.links_.pre.1day
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                                   12 2 1 2 0 0 5 0 1 0
                            int
                                  0 0 0 0 0 0 0 0 0 0 ...
0.0919 0.0677 0.1333 0.0408 0 ...
                            num
avg.links_.pre.2day
                            num
sd.links_.pre.2day
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                                   0.504 0.278 0.34 0.21 0 ...
                                  0 0 0 0 0 0 0 0 0 0 0 ...
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max.links_.pre.2day
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max.links_.post.1day:
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0.00245 0.00564 0 0.0024 0 ...
med.links_.post.1day:
                            num
avg.links_.pre.vsday:
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                                  0.675 0.404 0.365 0.29 0 ...
-10 -2 -1 -2 0 0 -5 0 -1 0 ...
12 2 1 2 0 0 5 0 1 0 ...
sd.links_.pre.vsday
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max.links_.pre.vsday:
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35 0 2 3 0 10 0 17 1 0 ...
0 2 0 0 0 2 103 44 6 0 ...
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comm_.tot
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696 8361 2751 187 10314 6933 1961 330 6113 ...
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  [list output truncated]
```{r}
error measure
mse = function(y_hat, y) {
mse = mean((y - y_hat)^2)
return(mse)
create design matrices
train_x = model.Matrix(comm.next24 ~ . - 1, data = train, sparse = F)
train y = train$comm.next24
test_x = model.Matrix(comm.next24 ~ . - 1, data = test, sparse = F)
test_y = test$comm.next24
train_xgb = xgb.DMatrix(data = as.matrix(train_x), label = train_y)
test_xgb = xgb.DMatrix(data = as.matrix(test_x), label = test_y)
number of models
n = 5
```{r}
# fit XGBoost
pred_xgb = foreach(i = 1:n, .combine = cbind) %do% {
mdl_xgb = xgboost(data = train_xgb, nround = 500, nthread = 4, max_depth = 6, eta = 0.025, subsample = 0.7,
gamma = 3)
return(predict(mdl_xgb, test_xgb))
[1]
[2]
[3]
[4]
[5]
[6]
[7]
[8]
[9]
         train-rmse:1.123186
         train-rmse:1.105701
         train-rmse:1.088757
         train-rmse:1.072397
         train-rmse:1.056423
         train-rmse:1.041183
         train-rmse:1.026381
         train-rmse:1.011974
         train-rmse:0.998238
         train-rmse:0.984913
```

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train-rmse:0.972034
train-rmse:0.959588
[11]
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         train-rmse:0.913737
         train-rmse:0.903260
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         train-rmse:0.893045
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         train-rmse:0.873720
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         train-rmse:0.856106
         train-rmse:0.847699
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         train-rmse:0.831753
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         train-rmse:0.824216
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         train-rmse:0.796772
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         train-rmse:0.790452
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         train-rmse:0.767387
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         train-rmse:0.762091
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         train-rmse:0.742876
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         train-rmse:0.664358
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         train-rmse:0.651007
[80]
         train-rmse:0.649865
[81]
         train-rmse:0.648709
         train-rmse:0.647565
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[83]
[84]
[85]
         train-rmse:0.646556
         train-rmse:0.645484
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         train-rmse:0.638272
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         train-rmse:0.637431
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         train-rmse:0.636689
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         train-rmse:0.635924
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         train-rmse:0.635252
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         train-rmse:0.634550
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         train-rmse:0.633897
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         train-rmse:0.631266
[103]
         train-rmse:0.630622
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         train-rmse:0.629997
         train-rmse:0.629475
Γ105<sup>-</sup>
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         train-rmse:0.628889
[107
         train-rmse:0.628356
[108]
         train-rmse:0.627734
[109]
         train-rmse:0.627164
Γ110<sup>-</sup>
         train-rmse:0.626648
[111]
         train-rmse:0.626169
[112<sup>-</sup>
         train-rmse:0.625696
[113]
         train-rmse:0.625198
[114<sup>-</sup>
         train-rmse:0.624718
[115]
         train-rmse:0.624216
[116]
         train-rmse:0.623752
[117]
         train-rmse:0.623234
[118]
         train-rmse:0.622800
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         train-rmse:0.622407
[120]
         train-rmse:0.621962
[121]
         train-rmse:0.621454
Ī122<sup>⁼</sup>
         train-rmse:0.621036
[123]
         train-rmse:0.620704
[124]
         train-rmse:0.620250
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         train-rmse:0.619885
[126]
         train-rmse:0.619455
[127<sup>-</sup>
         train-rmse:0.619091
[128]
         train-rmse:0.618616
Ī129<sup>⁼</sup>
         train-rmse:0.618210
[130]
         train-rmse:0.617725
[131]
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[132]
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[133]
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[135]
         train-rmse:0.616271
         train-rmse:0.615904
Γ136<sup>-</sup>
         train-rmse:0.615585
[137]
         train-rmse:0.615193
[138]
         train-rmse:0.614904
Ī139<sup>⁼</sup>
         train-rmse:0.614427
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         train-rmse:0.614048
[141<sup>-</sup>
         train-rmse:0.613779
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[143]
         train-rmse:0.613158
[144]
         train-rmse:0.612857
[145]
         train-rmse:0.612606
[146<sup>-</sup>
         train-rmse:0.612363
[147<sup>-</sup>
         train-rmse:0.612108
[148]
         train-rmse:0.611830
         train-rmse:0.611612
Γ149<sup>-</sup>
[150]
         train-rmse:0.611342
[151]
[152]
         train-rmse:0.611107
         train-rmse:0.610801
[153]
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         train-rmse:0.610227
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[155]
[156]
         train-rmse:0.609939
         train-rmse:0.609673
[157<sup>-</sup>
         train-rmse:0.609422
[158]
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         train-rmse:0.608735
[161]
         train-rmse:0.608487
[162]
         train-rmse:0.608289
[163]
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Γ164<sup>-</sup>
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         train-rmse:0.579193
[385]
         train-rmse:0.579123
[386]
         train-rmse:0.579053
```

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[387]
         train-rmse:0.579007
[388]
         train-rmse:0.578952
โ389โ
         train-rmse:0.578880
์ 390 โ
         train-rmse:0.578778
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         train-rmse:0.578680
Ī392⁼
         train-rmse:0.578608
[393]
         train-rmse:0.578508
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         train-rmse:0.578449
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         train-rmse:0.578336
「396<sup>™</sup>
         train-rmse:0.578268
         train-rmse:0.578132
Ī397<sup>⁼</sup>
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         train-rmse:0.578105
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         train-rmse:0.578098
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         train-rmse:0.578021
[401<sup>-</sup>
         train-rmse:0.577895
         train-rmse:0.577745
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[403]
         train-rmse:0.577635
Ī404⁼
         train-rmse:0.577542
[405]
         train-rmse:0.577443
Γ406⁻
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         train-rmse:0.577173
Ī407⁼
[408]
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Γ̄409<sup>-</sup>
         train-rmse:0.577064
[410]
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         train-rmse:0.576884
train-rmse:0.576849
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[412]
[413]
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[414<sup>-</sup>
         train-rmse:0.576703
[415]
         train-rmse:0.576577
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         train-rmse:0.576454
[417]
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Γ418⁻
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[419]
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[420]
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[422]
         train-rmse:0.576026
Γ423⁻
         train-rmse:0.576003
         train-rmse:0.575942
Ī424Ī
[425]
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         train-rmse:0.575779
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Γ428⁻
         train-rmse:0.575584
[429]
         train-rmse:0.575519
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         train-rmse:0.575475
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train-rmse:0.574736
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[439]
Γ440⁻
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[442]
Ī443<sup>⁼</sup>
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Ī447]
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Ī448⁼
         train-rmse:0.574041
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         train-rmse:0.573907
Γ450⁻
         train-rmse:0.573830
[451]
         train-rmse:0.573812
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         train-rmse:0.573695
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         train-rmse:0.573660
[454]
         train-rmse:0.573568
[455]
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         train-rmse:0.573527
         train-rmse:0.573506
[457]
         train-rmse:0.573425
Γ458Ί
         train-rmse:0.573277
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train-rmse:0.573205
train-rmse:0.573094
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           train-rmse:0.573014
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           train-rmse:0.572956
[463]
           train-rmse:0.572911
Γ464]
           train-rmse:0.572830
[465]
           train-rmse:0.572690
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           train-rmse:0.572498
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           train-rmse:0.572385
Γ468Ί
           train-rmse:0.572342
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[470]
           train-rmse:0.572163
 [471]
           train-rmse:0.572155
 [472]
           train-rmse:0.572082
 [473<sup>-</sup>
           train-rmse:0.571992
 [474]
           train-rmse:0.571893
[475]
           train-rmse:0.571832
 [476]
           train-rmse:0.571772
[477]
           train-rmse:0.571739
 [478]
           train-rmse:0.571655
 479<sup>-</sup>
           train-rmse:0.571593
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           train-rmse:0.571573
[481]
           train-rmse:0.571557
[482]
           train-rmse:0.571543
 [483]
           train-rmse:0.571490
[484]
           train-rmse:0.571446
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           train-rmse:0.571112
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           train-rmse:0.571070
 489]
           train-rmse:0.571020
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           train-rmse:0.571003
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           train-rmse:0.570843
[492]
           train-rmse:0.570798
 [493]
           train-rmse:0.570772
[494]
           train-rmse:0.570674
Γ495Ί
           train-rmse:0.570557
           train-rmse:0.570512
 496]
Γ497⁻
           train-rmse:0.570416
Γ498∃
           train-rmse:0.570368
 [499]
           train-rmse:0.570193
Г500Ī
           train-rmse:0.570069
```{r}
fit random forest
pred rf = foreach(i = 1:n, .combine = cbind) %do% {
 mdl rf = ranger(comm.next24 ~ ., data = train, num.trees = 1000, mtry = 120, write.forest = T)
 return(predict(mdl_rf, test)$predictions)
Growing trees.. Progress: 5%. Estimated remaining time: 10 minutes, 40 seconds.
Growing trees.. Progress: 10%. Estimated remaining time: 9 minutes, 45 seconds.
Growing trees.. Progress: 15%. Estimated remaining time: 8 minutes, 59 seconds. Growing trees.. Progress: 20%. Estimated remaining time: 8 minutes, 31 seconds.
Growing trees.. Progress: 25%. Estimated remaining time: 8 minutes, 2 seconds.
Growing trees.. Progress: 30%. Estimated remaining time: 7 minutes, 29 seconds. Growing trees.. Progress: 35%. Estimated remaining time: 6 minutes, 57 seconds. Growing trees.. Progress: 35%. Estimated remaining time: 6 minutes, 27 seconds.
Growing trees.. Progress: 44%. Estimated remaining time: 5 minutes, 57 seconds.
Growing trees.. Progress: 49%. Estimated remaining time: 5 minutes, 23 seconds. Growing trees.. Progress: 54%. Estimated remaining time: 4 minutes, 53 seconds.
Growing trees.. Progress: 59%. Estimated remaining time: 4 minutes, 24 seconds.
Growing trees. Progress: 64%. Estimated remaining time: 3 minutes, 51 seconds. Growing trees. Progress: 69%. Estimated remaining time: 3 minutes, 50 seconds. Growing trees. Progress: 74%. Estimated remaining time: 2 minutes, 49 seconds.
Growing trees.. Progress: 79%. Estimated remaining time: 2 minutes, 18 seconds.
```

```
Growing trees.. Progress: 83%. Estimated remaining time: 1 minute, 46 seconds. Growing trees.. Progress: 88%. Estimated remaining time: 1 minute, 14 seconds. Growing trees.. Progress: 93%. Estimated remaining time: 43 seconds.
Growing trees.. Progress: 98%. Estimated remaining time: 11 seconds. Growing trees.. Progress: 5%. Estimated remaining time: 10 minutes, 28 seconds. Growing trees.. Progress: 9%. Estimated remaining time: 9 minutes, 57 seconds.
Growing trees. Progress: 9%. Estimated remaining time: 9 minutes, 37 seconds. Growing trees. Progress: 14%. Estimated remaining time: 9 minutes, 21 seconds. Growing trees. Progress: 19%. Estimated remaining time: 8 minutes, 50 seconds. Growing trees. Progress: 24%. Estimated remaining time: 8 minutes, 17 seconds.
Growing trees. Progress: 29%. Estimated remaining time: 7 minutes, 42 seconds.
Growing trees.. Progress: 34%. Estimated remaining time: 7 minutes, 10 seconds. Growing trees.. Progress: 39%. Estimated remaining time: 6 minutes, 39 seconds. Growing trees.. Progress: 44%. Estimated remaining time: 6 minutes, 6 seconds.
Growing trees.. Progress: 48%. Estimated remaining time: 5 minutes, 34 seconds. Growing trees.. Progress: 53%. Estimated remaining time: 5 minutes, 4 seconds. Growing trees.. Progress: 58%. Estimated remaining time: 4 minutes, 32 seconds.
Growing trees.. Progress: 63%. Estimated remaining time: 3 minutes, 57 seconds.
Growing trees. Progress: 68%. Estimated remaining time: 3 minutes, 25 seconds. Growing trees. Progress: 73%. Estimated remaining time: 2 minutes, 54 seconds. Growing trees. Progress: 78%. Estimated remaining time: 2 minutes, 53 seconds. Growing trees. Progress: 82% Estimated remaining time: 1 minutes, 53 seconds.
Growing trees. Progress: 83%. Estimated remaining time: 1 minute, 52 seconds. Growing trees. Progress: 88%. Estimated remaining time: 1 minute, 18 seconds. Growing trees. Progress: 93%. Estimated remaining time: 45 seconds.
Growing trees.. Progress: 98%. Estimated remaining time: 14 seconds.
Growing trees.. Progress: 5%. Estimated remaining time: 10 minutes, 57 seconds. Growing trees.. Progress: 10%. Estimated remaining time: 9 minutes, 50 seconds.
Growing trees.. Progress: 14%. Estimated remaining time: 9 minutes, 21 seconds.
Growing trees. Progress: 19%. Estimated remaining time: 8 minutes, 48 seconds. Growing trees. Progress: 24%. Estimated remaining time: 8 minutes, 49 seconds. Growing trees. Progress: 24%. Estimated remaining time: 8 minutes, 19 seconds. Growing trees. Progress: 29%. Estimated remaining time: 7 minutes, 46 seconds.
Growing trees.. Progress: 33%. Estimated remaining time: 7 minutes, 14 seconds. Growing trees.. Progress: 38%. Estimated remaining time: 6 minutes, 44 seconds. Growing trees.. Progress: 43%. Estimated remaining time: 6 minutes, 12 seconds.
Growing trees. Progress: 48%. Estimated remaining time: 5 minutes, 39 seconds. Growing trees. Progress: 53%. Estimated remaining time: 5 minutes, 8 seconds. Growing trees. Progress: 58%. Estimated remaining time: 4 minutes, 35 seconds.
Growing trees.. Progress: 63%. Estimated remaining time: 4 minutes, 4 seconds.
Growing trees.. Progress: 67%. Estimated remaining time: 3 minutes, 33 seconds.
Growing trees.. Progress: 72%. Estimated remaining time: 3 minutes, 1 seconds. Growing trees.. Progress: 77%. Estimated remaining time: 2 minutes, 29 seconds.
Growing trees.. Progress: 82%. Estimated remaining time: 1 minute, 57 seconds. Growing trees.. Progress: 87%. Estimated remaining time: 1 minute, 26 seconds. Growing trees.. Progress: 92%. Estimated remaining time: 54 seconds.
Growing trees.. Progress: 97%. Estimated remaining time: 21 seconds.
Growing trees.. Progress: 5%. Estimated remaining time: 10 minutes, 14 seconds. Growing trees.. Progress: 10%. Estimated remaining time: 9 minutes, 43 seconds. Growing trees.. Progress: 14%. Estimated remaining time: 9 minutes, 18 seconds.
Growing trees.. Progress: 19%. Estimated remaining time: 8 minutes, 13 seconds. Growing trees.. Progress: 24%. Estimated remaining time: 8 minutes, 50 seconds. Growing trees.. Progress: 24%. Estimated remaining time: 8 minutes, 17 seconds. Growing trees.. Progress: 29%. Estimated remaining time: 7 minutes, 47 seconds.
Growing trees. Progress: 34%. Estimated remaining time: 7 minutes, 10 seconds.
Growing trees.. Progress: 39%. Estimated remaining time: 6 minutes, 39 seconds. Growing trees.. Progress: 43%. Estimated remaining time: 6 minutes, 10 seconds.
Growing trees. Progress: 48%. Estimated remaining time: 5 minutes, 38 seconds.
Growing trees. Progress: 40%. Estimated remaining time: 3 minutes, 36 seconds. Growing trees. Progress: 53%. Estimated remaining time: 5 minutes, 7 seconds. Growing trees. Progress: 57%. Estimated remaining time: 4 minutes, 37 seconds. Growing trees. Progress: 62%. Estimated remaining time: 4 minutes, 7 seconds.
Growing trees. Progress: 02%. Estimated remaining time: 3 minutes, 34 seconds.
Growing trees.. Progress: 72%. Estimated remaining time: 3 minutes, 4 seconds. Growing trees.. Progress: 77%. Estimated remaining time: 2 minutes, 31 seconds. Growing trees.. Progress: 82%. Estimated remaining time: 2 minutes, 1 seconds.
Growing trees.. Progress: 86%. Estimated remaining time: 1 minute, 35 seconds. Growing trees.. Progress: 90%. Estimated remaining time: 1 minute, 4 seconds. Growing trees.. Progress: 95%. Estimated remaining time: 33 seconds.
Growing trees.. Progress: 100%. Estimated remaining time: 1 seconds. Growing trees.. Progress: 5%. Estimated remaining time: 10 minutes, 59 seconds. Growing trees.. Progress: 10%. Estimated remaining time: 9 minutes, 58 seconds.
Growing trees.. Progress: 15%. Estimated remaining time: 9 minutes, 12 seconds.
Growing trees.. Progress: 20%. Estimated remaining time: 8 minutes, 34 seconds. Growing trees.. Progress: 25%. Estimated remaining time: 8 minutes, 1 seconds. Growing trees.. Progress: 30%. Estimated remaining time: 7 minutes, 29 seconds. Growing trees.. Progress: 35%. Estimated remaining time: 6 minutes, 54 seconds.
```

```
Growing trees.. Progress: 40%. Estimated remaining time: 6 minutes, 24 seconds.
Growing trees.. Progress: 45%. Estimated remaining time:
 5 minutes, 48 seconds.
Growing trees.. Progress: 50%. Estimated remaining time: 5 minutes, 17 seconds.
Growing trees.. Progress: 55%. Estimated remaining time: 4 minutes, 44 seconds.
Growing trees.. Progress: 60%. Estimated remaining time: 4 minutes, 13 seconds. Growing trees.. Progress: 65%. Estimated remaining time: 3 minutes, 40 seconds.
Growing trees.. Progress: 70%. Estimated remaining time: 3 minutes, 8 seconds.
Growing trees.. Progress: 75%. Estimated remaining time: 2 minutes, 35 seconds. Growing trees.. Progress: 81%. Estimated remaining time: 2 minutes, 2 seconds. Growing trees.. Progress: 86%. Estimated remaining time: 1 minute, 30 seconds.
Growing trees.. Progress: 91%. Estimated remaining time: 56 seconds. Growing trees.. Progress: 96%. Estimated remaining time: 26 seconds.
```{r}
# weighted average
weighted_average = mse(rowMeans(pred_rf) * 0.25 + rowMeans(pred_xgb) * 0.75, test_y)
weighted_average
View(pred_rf)
View(pred_xgb)
[1] 0.2620389
```{r}
Stacked Generalization
#test<- read.csv("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Test.csv",header=TRUE)
#train<-read.csv("C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/blogData_Train.csv",header=TRUE)
train<-data.table(train)
test<-data.table(test)
error measure
mse = function(y_hat, y) {
 mse = mean((y - y_hat)^2)
 return(mse)
create design matrices
train_y = train$comm.next24
train_y
test_y = test$comm.next24
test_y
test_x = model.Matrix(comm.next24 ~ . - 1, data = test, sparse = F)
test x sparse = model.Matrix(comm.next24 ~ . - 1, data = test, sparse = T)
test_xgb = xgb.DMatrix(data = as.matrix(test_x), label = test_y)
divide training set into k folds
k = 5
```

## cv\_index = 1:nrow(train)

cv\_index\_split = split(cv\_index, cut(seq\_along(cv\_index), k, labels = FALSE))

```
[1] 0.6931472 0.0000000 0.0000000 0.6931472 3.3322045 0.0000000 0.0000000 3.3322045 2.3025851
2.3025851 0.0000000 0.0000000 1.0986123 0.0000000
[15] 2.6390573 2.7725887 1.3862944 2.7725887 2.6390573 0.6931472 3.0910425 0.6931472 3.0910425 0.6931472 1.3862944 1.3862944 1.3862944 1.3862944 [29] 1.0986123 1.0986123 1.7917595 1.7917595 0.0000000 0.0000000 3.0910425 0.0000000 0.0000000
1.3862944 0.0000000 0.0000000 0.0000000 1.0986123
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 [57] 0.0000000 0.0000000 2.0794415 1.3862944 0.6931472 0.6931472 0.6931472 1.0986123 1.0986123
0.0000000 0.0000000 1.7917595 2.8903718 1.7917595 [71] 0.0000000 1.0986123 0.0000000 0.6931472 0.0000000 0.6931472 0.0000000
3.6109179 0.6931472 1.0986123 2.5649494 2.3025851

[85] 2.1972246 2.3025851 2.1972246 1.6094379 2.1972246 0.6931472 0.6931472 1.3862944 1.3862944 1.0986123 1.0986123 0.6931472 0.6931472 1.3862944
 [99] 1.3862944 1.0986123 1.0986123 1.3862944 1.3862944 3.2958369 1.0986123 0.6931472 1.7917595
0.6931472 1.3862944 1.0986123 1.3862944 3.2188758
[113] 3.2188758 1.0986123 1.0986123 1.3862944 0.6931472 4.2766661 0.0000000 0.0000000 1.6094379 1.7917595 1.7917595 1.7917595 1.6094379 1.6094379 [127] 1.6094379 1.9459101 1.9459101 1.9459101 3.8286414 3.8286414 2.1972246 2.1972246 0.0000000
1.6094379 0.6931472 0.0000000 0.0000000 1.9459101
[183] 1.0986123 0.0000000 0.0000000 1.9459101 0.0000000 0.0000000 0.0000000 1.0986123 0.6931472 0.6931472 0.0000000 0.0000000 0.0000000 0.6931472
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[239] 2.3025851 2.3025851 0.0000000 0.0000000 1.3862944 1.3862944 0.6931472
0.6931472 0.6931472 0.6931472 1.3862944 0.0000000
0.6931472 0.6931472 1.3862944 1.3862944 1.3862944
 [295] 1.6094379 1.6094379 1.3862944 1.3862944 0.0000000 0.0000000 1.0986123 1.0986123 1.0986123
2.4849066 2.4849066 1.3862944 1.3862944 1.3862944
 [309] 1.0986123 1.0986123 0.0000000 0.0000000 0.0000000 1.0986123 1.0986123 1.3862944 1.3862944
0.6931472 0.6931472 0.0000000 0.0000000 2.3025851
[323] 2.3025851 2.3025851 2.0794415 2.0794415 2.3025851 1.0986123 3.6109179 3.6109179 1.0986123 1.0986123 2.3978953 2.1972246 1.0986123
 [337] 2.1972246 0.0000000 1.0986123 0.0000000 1.0986123 1.0986123 2.3025851 2.3025851 2.1972246
2.0794415 2.0794415 2.1972246 0.0000000 1.7917595
[351] 1.7917595 0.0000000 0.0000000 0.6931472 0.6931472 0.0000000 0.6931472 0.0000000
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 [365] 4.0253517 2.7080502 2.7080502 0.0000000 0.0000000 2.1972246 1.6094379 0.6931472 2.4849066
1.0986123 0.0000000 1.6094379 1.0986123 0.6931472
[407] 2.1972246 2.1972246 2.3978953 0.6931472 0.0000000 0.0000000 0.0000000 2.3978953 0.6931472
0.0000000 1.6094379 0.0000000 1.6094379 0.0000000
[435] 2.9957323 0.6931472 1.6094379 0.6931472 1.6094379 2.3025851 2.3025851 0.0000000 0.0000000
1.9459101 1.9459101 0.6931472 0.6931472 0.6931472
 [449] 0.6931472 1.0986123 1.0986123 1.3862944 1.3862944 4.0943446 4.0943446 0.0000000 0.0000000
2.9444390 2.9444390 1.6094379 0.0000000 0.0000000
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[463] 1.6094379 2.0794415 1.9459101 1.9459101 1.6094379 2.0794415 0.0000000 0.0000000 1.6094379 1.7917595 1.3862944 1.7917595 1.3862944 1.9459101
 [477] 1.9459101 4.8283137 4.8283137 4.8283137 4.8283137 4.0253517 4.0253517 4.0253517 4.0253517
3.0910425 3.0910425 3.0910425 3.0910425 2.3025851
[491] 2.3025851 0.6931472 0.6931472 0.6931472 3.4657359 3.4657359 2.0794415 2.0794415
1.3862944 1.3862944 1.0986123 1.0986123 0.0000000

[505] 0.00000000 2.1972246 2.1972246 1.6094379 1.6094379 2.3025851 2.3025851 2.3025851
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[533] 3.4657359 2.3978953 2.6390573 2.6390573 2.5649494 2.5649494 2.5649494 1.7917595 1.7917595 1.3862944 1.3862944 3.6888795 3.7135721 1.9459101 1.9459101 3.7135721 3.7135721
2.8332133 2.8332133 2.9444390 1.7917595 [561] 0.6931472 0.0000000 1.7917595 1.0986123 2.1972246 2.7725887 2.3025851 0.6931472 0.6931472
0.6931472 0.6931472 1.0986123 1.0986123 2.3978953
 [575] 2.3978953 2.3978953 1.9459101 1.9459101 0.6931472 0.6931472 0.6931472 3.1354942
3.1354942 0.6931472 0.6931472 1.0986123 1.0986123
 [589] 0.6931472 0.6931472 1.9459101 0.0000000 0.0000000 1.9459101 1.9459101 1.9459101 1.0986123
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[603] 1.0986123 1.0986123 1.0986123 1.0986123 0.0000000 0.0000000 2.7080502 0.6931472 2.7080502 0.6931472 1.7917595 0.0000000 1.7917595 0.0000000
[645] 0.6931472 0.6931472 0.6931472 0.0000000 0.0000000 0.0000000 3.6635616 1.3862944
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[659] 3.2188758 2.3978953 0.6931472 0.6931472 0.0000000 0.0000000 0.0000000 3.1354942
3.1354942 0.0000000 0.0000000 1.3862944 1.3862944
 [673] 3.2580965 3.7376696 2.7080502 1.0986123 1.0986123 0.0000000 0.0000000 0.6931472 0.0000000
[687] 0.0000000 1.0986123 1.0986123 0.0000000 0.0000000 0.0000000 1.0986123 1.0986123 1.0986123 0.0000000 1.0986123 1.0986123 0.0000000
 [701] 1.0986123 3.4965076 3.4965076 0.0000000 3.4965076 2.3978953 2.3978953 2.3978953 1.0986123
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 [743] 1.6094379 1.6094379 1.6094379 1.6094379 1.6094379 0.0000000 0.0000000 0.0000000 0.6931472
0.6931472 0.6931472 1.0986123 1.0986123 1.0986123
 [757] 0.0000000 0.0000000 0.0000000 1.0986123 1.0986123 2.0794415 2.0794415 2.0794415
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 [813] 0.0000000 0.6931472 0.6931472 0.6931472 0.6931472 0.6931472 0.6931472 0.6931472 0.6931472
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 [883] 0.0000000 1.3862944 0.0000000 1.3862944 0.0000000 0.0000000 0.6931472 0.0000000 0.6931472
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 [911] 1.0986123 1.0986123 0.6931472 0.6931472 1.0986123 0.0000000 0.6931472 0.6931472 0.0000000
0.0000000 0.6931472 1.0986123 0.6931472 0.6931472 0.6931472 0.6931472 0.0000000 2.5649494 2.5649494
[939] 0.0000000 1.6094379 0.0000000 0.0000000 1.6094379 0.0000000 1.6094379 0.0000000 0.0000000
0.0000000 1.3862944 1.3862944 0.6931472 [953] 0.6931472 0.6931472 3.1780538 0.6931472 3.1780538
1.0986123 2.7080502 2.7080502 1.0986123 2.7080502
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[967] 1.0986123 2.7080502 1.7917595 1.7917595 0.0000000 1.7917595 0.0000000 0.0000000 1.7917595
0.000000 0.0000000 0.0000000 0.0000000
0.0000000 1.0986123 0.0000000 0.0000000 0.0000000
 [reached getOption("max.print") -- omitted 51397 entries]
[1] 1.6094379 0.0000000 0.6931472 1.7917595 0.0000000 4.9416424 0.6931472 1.7917595 1.0986123
0.0000000 0.0000000 0.6931472 0.0000000 1.7917595
 6931472 0.0000000 0.0000000 1.0986123 0.0000000
0.\bar{0}00\bar{0}000 0.0000000 0.0000000 0.0000000 2.1972246
 57] 1.0986123 0.0000000 0.0000000 1.0986123 0.0000000 0.6931472 0.0000000 0.0000000 1.3862944
0.000000 3.3672958 1.6094379 5.9989366 0.0000000
 [71] 0.0000000 0.0000000 0.0000000 2.4849066 0.0000000 2.9444390 1.6094379 0.0000000 0.0000000
0.\bar{0}00\bar{0}000 0.0000000 0.0000000 0.0000000 2.5649494
 [99] 0.0000000 0.0000000 0.6931472 0.0000000 0.0000000 1.9459101 0.0000000 0.0000000 0.0000000
 .0000000 0.0000000 0.0000000 1.9459101 0.0000000
[113] 0.0000000 0.0000000 0.6931472 0.6931472 0.0000000 0.0000000 0.0000000 1.3862944 1.6094379 0.0000000 4.1108739 0.0000000 1.3862944 0.0000000
[127] 0.0000000 0.0000000 0.0000000 1.0986123 1.0986123 0.0000000 0.0000000 1.6094379 0.0000000 0.0000000 0.0000000 1.0986123 0.6931472
[141] 0.6931472 0.0000000 0.0000000 0.0000000 1.0986123 0.0000000 1.9459101 0.0000000
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0.6931472 3.2580965 0.0000000 0.0000000 0.0000000
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 [253] 0.0000000 0.0000000 0.0000000 0.6931472 0.0000000 0.0000000 0.0000000 0.6931472 1.0986123
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 [295] 0.0000000 0.0000000 1.3862944 1.7917595 0.0000000 2.3978953 0.0000000 1.0986123 0.0000000
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[323] 1.3862944 0.0000000 4.7095302 0.0000000 0.0000000 2.5649494 0.0000000 0.0000000
0.0000000 0.0000000 0.0000000 0.0000000 1.0986123
[337] \ \ 0.6931472 \ \ 0.0000000 \ \ 0.0000000 \ \ 3.4011974 \ \ 0.0000000 \ \ 0.0000000 \ \ 1.9459101 \ \ 0.6931472 \ \ 0.0000000
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[351] 0.0000000 0.0000000 0.0000000 1.9459101 0.0000000 0.0000000 0.0000000 2.5649494 0.0000000
0.0000000 3.0910425 0.0000000 0.0000000 0.0000000
[379] 0.0000000 0.0000000 1.3862944 0.0000000 0.0000000 0.0000000 3.9889840 0.0000000 0.0000000
1.0986123 1.6094379 0.00000000 0.00000000 0.00000000 [393] 0.00000000 1.0986123 0.6931472 1.9459101 0.0000000 2.1972246 0.0000000 0.0000000 0.00000000
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[435] 0.0000000 0.6931472 0.0000000 0.0000000 0.0000000 1.0986123 1.6094379 0.0000000 2.0794415
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```

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 \begin{tabular}{l} 463] $2.6390573 & 0.0000000 & 0.0000000 & 0.6931472 & 0.0000000 & 0.0000000 & 0.6931472 & 0.0000000 \\ 0.0000000 & 1.7917595 & 0.0000000 & 0.6931472 & 0.6931472 \\ [477] $0.0000000 & 0.0000000 & 1.9459101 & 0.0000000 & 0.0000000 & 0.0000000 & 0.0000000 \\ \hline \end{tabular} \begin{tabular}{l} 0.0000000 & 0.0000000 & 0.0000000 & 0.0000000 & 0.0000000 \\ 0.0000000 & 0.0000000 & 1.3862944 & 0.0000000 \\ \hline \end{tabular} \begin{tabular}{l} 0.0000000 & 0.0000000 & 0.0000000 & 0.0000000 \\ 0.0000000 & 0.0000000 & 1.3862944 & 0.0000000 \\ \hline \end{tabular} \begin{tabular}{l} 0.0000000 & 0.0000000 & 0.0000000 \\ 0.0000000 & 0.0000000 & 0.0000000 \\ \hline \end{tabular}
0.0000000 0.6931472 4.5538769 0.0000000 0.0000000
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[561] 0.0000000 0.6931472 1.9459101 0.0000000 0.0000000 0.0000000 0.6931472 0.6931472 0.0000000 0.0000000 2.8903718 0.6931472 0.0000000 1.7917595
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[603] 1.0986123 0.6931472 0.0000000 0.0000000 1.0986123 0.0000000 2.5649494 0.0000000
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[617] 1.6094379 0.0000000 0.0000000 3.3672958 0.0000000 0.0000000 0.6931472 0.0000000 0.6931472 0.0000000 0.0000000 0.6931472 0.0000000
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[673] 0.0000000 0.6931472 1.9459101 2.8903718 0.0000000 0.0000000 0.6931472 0.0000000 0.0000000 0.0000000 3.7612001 0.0000000 0.0000000
[687] 0.0000000 0.0000000 1.0986123 0.0000000 0.0000000 0.0000000 4.0430513 0.0000000 0.0000000 0.0000000 2.0794415 0.0000000 1.7917595
0.0000000 0.0000000 0.0000000 0.0000000 0.6931472
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 [869] 0.0000000 0.0000000 1.6094379 0.0000000 0.0000000 0.0000000 0.6931472 0.6931472 0.0000000
0.6931472 0.6931472 0.0000000 0.0000000 0.0000000
0.0000000 1.6094379 0.0000000 0.0000000 0.0000000
```

```
meta features from kNN
library(Matrix)
meta_knn_test = rep(0, nrow(test))
meta_knn_train = foreach(i = 1:k, .combine = c) %do% {
split the raining set into two disjoint sets
train_index = setdiff(1:nrow(train), cv_index_split[[i]])
train set1 = model.Matrix(comm.next24 ~ . - 1, data = train[train index], sparse = T)
train_set2 = model.Matrix(comm.next24 ~ . - 1, data = train[cv_index_split[[i]]], sparse = T)
 # level 0 prediction
meta pred = knn.reg(train set1, train set2, train[train index]$comm.next24, k = 19)$pred
meta knn test = meta knn test + knn.reg(train set1, test x sparse, train[train index]$comm.next24, k =
19)$pred / k
 return(meta pred)
```{r}
# meta features from LASSO
meta glm test = rep(0, nrow(test))
meta glm train = foreach(i = 1:k, .combine = c) %do% {
# split the raining set into two disjoint sets
train_index = setdiff(1:nrow(train), cv_index_split[[i]])
train set1 = model.Matrix(comm.next24 ~ . - 1, data = train[train index], sparse = T)
train_set2 = model.Matrix(comm.next24 ~ . - 1, data = train[cv_index_split[[i]]], sparse = T)
# level 0 prediction
temp_glm = cv.glmnet(train_set1, train[train_index]$comm.next24, family = "gaussian", alpha = 1)
meta_pred = predict(temp_glm, newx = train_set2)
meta_glm_test = meta_glm_test + predict(temp_glm, newx = test_x_sparse) / k
return(meta pred)
```{r}
meta features from SVM
meta_svm_test = rep(0, nrow(test))
meta_svm_train = foreach(i = 1:k, .combine = c) %do% {
split the raining set into two disjoint sets
train_index = setdiff(1:nrow(train), cv_index_split[[i]])
train_set1 = train[train_index]
train set2 = train[cv index split[[i]]]
 # level 0 prediction
```

```
temp_svm = svm(comm.next24 ~ comm_.pre.1day + comm_.pre.vsday + pubtime + comm_.tot +
comm .post.1day + avg.comm .pre.vsday +
 avg.comm_.pre.1day + med.comm_.pre.1day, data = train_set1,
 kernel = "radial", cost = 2, gamma = 0.25)
 meta_pred = predict(temp_svm, train_set2)
 meta sym test = meta sym test + predict(temp sym, test) / k
 return(meta pred)
 ``{r}
meta features from random forest
meta rf test = rep(0, nrow(test))
meta rf train = foreach(i = 1:k, .combine = c) %do% {
 # split the raining set into two disjoint sets
 train_index = setdiff(1:nrow(train), cv_index_split[[i]])
 train_set1 = train[train_index]
 train_set2 = train[cv_index_split[[i]]]
 # level 0 prediction
 temp rf = ranger(comm.next24 ~ ., data = train set1, num.trees = 500, mtry = 120, write.forest = T)
 meta_pred = predict(temp_rf, train_set2)$predictions
 meta rf test = meta rf test + predict(temp rf, test)$predictions / k
 return(meta pred)
Growing trees.. Progress: 12%. Estimated remaining time: 3 minutes, 51 seconds.
Growing trees.. Progress: 24%. Estimated remaining time: 3 minutes, 16 seconds.
Growing trees.. Progress: 36%. Estimated remaining time: 2 minutes, 42 seconds. Growing trees.. Progress: 49%. Estimated remaining time: 2 minutes, 11 seconds. Growing trees.. Progress: 62%. Estimated remaining time: 1 minute, 34 seconds.
Growing trees.. Progress: 76%. Estimated remaining time: 1 minute, 0 seconds.
Growing trees.. Progress:
Growing trees.. Progress:
 89%. Estimated remaining time: 27 seconds.
 13%. Estimated remaining time: 3 minutes, 40 seconds.
Growing trees.. Progress: 27%. Estimated remaining time: 2 minutes, 51 seconds. Growing trees.. Progress: 40%. Estimated remaining time: 2 minutes, 24 seconds. Growing trees.. Progress: 53%. Estimated remaining time: 1 minute, 52 seconds.
Growing trees.. Progress: 66%. Estimated remaining time: 1 minute, 21 seconds.
Growing trees.. Progress: 79%. Estimated remaining time: 50 seconds.
Growing trees.. Progress:
 93%.
 Estimated remaining time:
 16 seconds.
Growing trees.. Progress: 13%. Estimated remaining time: 3 minutes, 40 seconds.
Growing trees.. Progress: 27%. Estimated remaining time: 2 minutes, 54 seconds. Growing trees.. Progress: 42%. Estimated remaining time: 2 minutes, 16 seconds. Growing trees.. Progress: 55%. Estimated remaining time: 1 minute, 46 seconds.
Growing trees.. Progress: 68%. Estimated remaining time: 1 minute, 15 seconds.
Growing trees.. Progress:
 82%. Estimated remaining time: 42 seconds.
Growing trees.. Progress:
 95%.
 Estimated remaining time:
 11 seconds.
Growing trees.. Progress: 12%.
 Estimated remaining time: 3 minutes, 47 seconds.
Growing trees.. Progress: 25%.
 Estimated remaining time: 3 minutes, 4 seconds.
Growing trees.. Progress:
 37%. Estimated remaining time: 2
 minutes, 41 seconds.
Growing trees.. Progress: 49%.
 2 minutes, 12 seconds.
 Estimated remaining time:
 minute, 38 seconds.
Growing trees.. Progress: 61%. Estimated remaining time: 1
Growing trees.. Progress:
 74%. Estimated remaining time:
 1 minute,
 5 seconds.
Growing trees.. Progress:
 88%.
 30 seconds.
 Estimated remaining time:
Growing trees.. Progress: 13%. Estimated remaining time: 3 minutes, 31 seconds.
 26%. Estimated remaining time: 3 minutes, 1 seconds. 39%. Estimated remaining time: 2 minutes, 27 seconds
Growing trees.. Progress:
 39%. Estimated remaining time: 2 minutes, 27 seconds 52%. Estimated remaining time: 1 minute, 55 seconds.
Growing trees.. Progress:
 27 seconds.
Growing trees.. Progress:
Growing trees.. Progress: 65%. Estimated remaining time: 1 minute, 23 seconds.
Growing trees.. Progress: 79%. Estimated remaining time: 51 seconds. Growing trees.. Progress: 92%. Estimated remaining time: 19 seconds.
```

```
```{r}
# meta features from XGBoost
meta xgb test = rep(0, nrow(test))
meta_xgb_train = foreach(i = 1:k, .combine = c) %do% {
# split the raining set into two disjoint sets
train_index = setdiff(1:nrow(train), cv_index_split[[i]])
train set1 = model.Matrix(comm.next24 ~ . - 1, data = train[train index], sparse = F)
train_set2 = model.Matrix(comm.next24 ~ . - 1, data = train[cv_index_split[[i]]], sparse = F)
# xgb data
train_set1_xgb = xgb.DMatrix(data = as.matrix(train_set1), label = train[train_index]$comm.next24)
train_set2_xgb = xgb.DMatrix(data = as.matrix(train_set2), label = train[cv_index_split[[i]]]$comm.next24)
# level 0 prediction
temp_xgb = xgboost(data = train_set1_xgb, nround = 500, nthread = 4, max_depth = 6, eta = 0.025, subsample =
0.7, gamma = 3)
meta_pred = predict(temp_xgb, train_set2_xgb)
meta_xgb_test = meta_xgb_test + predict(temp_xgb, test_xgb) / k
return(meta_pred)
[1]
[2]
[3]
[4]
[5]
[6]
[7]
[8]
[10]
[11]
         train-rmse:1.041150
         train-rmse:1.025012
         train-rmse:1.009377
         train-rmse:0.994275
         train-rmse:0.979666
         train-rmse:0.965676
         train-rmse:0.952060
         train-rmse:0.938887
         train-rmse:0.926134
         train-rmse:0.913716
         train-rmse:0.901808
         train-rmse:0.890405
[13]
         train-rmse:0.879322
         train-rmse:0.868612
         train-rmse:0.858176
[16]
[17]
         train-rmse:0.848063
         train-rmse:0.838441
         train-rmse:0.828999
19]
         train-rmse:0.819989
         train-rmse:0.811182
         train-rmse:0.802770
         train-rmse:0.794634
         train-rmse:0.786686
         train-rmse:0.779157
         train-rmse:0.771825
[26]
[27]
[28]
[29]
         train-rmse:0.764762
         train-rmse:0.757972
         train-rmse:0.751423
         train-rmse:0.745163
         train-rmse:0.739111
         train-rmse:0.733291
         train-rmse:0.727675
[33]
[34]
         train-rmse:0.722263
         train-rmse:0.716826
         train-rmse:0.711822
         train-rmse:0.706863
[36]
         train-rmse:0.702086
         train-rmse:0.697519
         train-rmse:0.693195
         train-rmse:0.688983
```

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[41]
[42]
[43]
         train-rmse:0.684843
         train-rmse:0.680958
         train-rmse:0.677244
[44]
         train-rmse:0.673550
[45]
         train-rmse:0.670160
[46]
[47]
         train-rmse:0.666816
         train-rmse:0.663481
[48]
         train-rmse:0.660263
[49]
[50]
         train-rmse:0.657246
         train-rmse:0.654429
[51]
[52]
[53]
[54]
         train-rmse:0.651604
         train-rmse:0.648855
         train-rmse:0.646318
         train-rmse:0.643736
55
         train-rmse:0.641245
[56]
[57]
         train-rmse:0.638934
         train-rmse:0.636633
[58]
[59]
         train-rmse:0.634391
         train-rmse:0.632310
Г60 Ī
         train-rmse:0.630265
[61]
         train-rmse:0.628302
[62]
         train-rmse:0.626367
[63]
         train-rmse:0.624426
[64]
         train-rmse:0.622714
[65]
[66]
         train-rmse:0.620845
         train-rmse:0.619144
[67]
         train-rmse:0.617523
[68]
         train-rmse:0.615901
[69]
         train-rmse:0.614365
[70]
         train-rmse:0.612886
[71]
[72]
         train-rmse:0.611523
         train-rmse:0.610054
[73]
[74]
         train-rmse:0.608744
         train-rmse:0.607472
[75]
[76]
         train-rmse:0.606238
         train-rmse:0.605063
[77
         train-rmse: 0.603943
[78]
         train-rmse:0.602796
79
         train-rmse:0.601612
โ80โ
         train-rmse:0.600529
[81]
[82]
         train-rmse:0.599534
         train-rmse:0.598473
train-rmse:0.597468
[83]
[84]
         train-rmse:0.596508
         train-rmse:0.595550
train-rmse:0.594656
[85]
[86]
[87]
         train-rmse:0.593830
[88]
         train-rmse:0.592932
[89]
         train-rmse:0.592154
         train-rmse:0.591240
Ī90Ī
[91]
         train-rmse:0.590441
         train-rmse:0.589682
train-rmse:0.588900
[92]
[§3]
Г947
         train-rmse:0.588204
95
         train-rmse:0.587438
[96]
         train-rmse:0.586715
Ī97Ī
         train-rmse:0.586100
[98]
         train-rmse:0.585375
「99T
         train-rmse:0.584711
         train-rmse:0.584067
[100]
[101]
         train-rmse:0.583379
[102]
[103]
         train-rmse:0.582712
         train-rmse:0.582128
Γ104<sup>-</sup>
         train-rmse:0.581530
[105]
         train-rmse:0.580906
[106]
         train-rmse:0.580393
         train-rmse:0.579770
Γ107<sup>-</sup>
[108]
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[109]
         train-rmse:0.578668
train-rmse:0.578155
[110]
[111]
         train-rmse:0.577562
[112]
         train-rmse:0.577104
```

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Γ1137
          train-rmse:0.576609
[114]
[115]
          train-rmse:0.576182
          train-rmse:0.575626
          train-rmse:0.575119
[116]
[117]
          train-rmse:0.574628
Γ118<sup>-</sup>
          train-rmse:0.574106
Γ119<sup>-</sup>
          train-rmse:0.573649
          train-rmse:0.573222
train-rmse:0.572811
[120]
[121]
[122<sup>-</sup>
          train-rmse:0.572371
[123]
          train-rmse:0.571991
[124]
          train-rmse:0.571655
[125]
          train-rmse:0.571275
[126]
          train-rmse:0.570982
Γ127<sup>-</sup>
          train-rmse:0.570588
          train-rmse:0.570161
[128]
[129]
          train-rmse:0.569784
Ī130Ī
          train-rmse:0.569437
[131]
          train-rmse:0.569069
Γ1327
          train-rmse:0.568641
          train-rmse:0.568377
[133]
[134]
          train-rmse:0.568051
          train-rmse:0.567700
Γ135<sup>-</sup>
          train-rmse:0.567407
[136]
[137]
[138]
         train-rmse:0.567101
train-rmse:0.566824
[139]
          train-rmse:0.566510
Γ140<sup>-</sup>
          train-rmse:0.566280
[141]
          train-rmse:0.565974
Ī142Ī
          train-rmse:0.565706
[143]
          train-rmse:0.565449
[144<sup>-</sup>
          train-rmse:0.565203
[145
          train-rmse:0.564939
[146]
          train-rmse:0.564721
[147<sup>-</sup>
          train-rmse:0.564373
[148]
          train-rmse:0.564055
Γ149<sup>-</sup>
          train-rmse:0.563845
          train-rmse:0.563584
[150
[151]
          train-rmse:0.563398
Ī152<sup>™</sup>
          train-rmse:0.563161
[153]
          train-rmse:0.562973
[154]
          train-rmse:0.562605
[155]
          train-rmse:0.562286
[156]
          train-rmse:0.561954
Γ157<sup>-</sup>
          train-rmse:0.561632
[158]
          train-rmse:0.561382
Ī159Ī
          train-rmse:0.561128
[160]
          train-rmse:0.560854
[161]
          train-rmse:0.560646
[162]
          train-rmse:0.560427
          train-rmse:0.560226
[163]
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train-rmse:0.559812
[164
[165]
[166
          train-rmse:0.559638
          train-rmse:0.559389
[167<sup>-</sup>
          train-rmse:0.559209
[168]
[169]
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          train-rmse:0.558686
[170]
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          train-rmse:0.558163
[172]
[173]
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[174
          train-rmse:0.557699
[175]
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[176]
          train-rmse:0.557326
[177]
          train-rmse:0.556995
[178]
          train-rmse:0.556817
Ī179<sup>⁼</sup>
          train-rmse:0.556611
[180]
          train-rmse:0.556405
[181]
          train-rmse:0.556245
[182]
          train-rmse:0.556028
[183]
          train-rmse:0.555760
          train-rmse:0.555483
Γ1847
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[185]
          train-rmse:0.555329
[186]
          train-rmse:0.555156
Ī187Ī
          train-rmse:0.554925
[188]
          train-rmse:0.554755
[189]
          train-rmse:0.554526
Γ190<sup>-</sup>
          train-rmse:0.554326
[191]
          train-rmse:0.554178
[192]
          train-rmse:0.553969
[193]
          train-rmse:0.553678
「194<sup>⁻</sup>
          train-rmse:0.553496
195
          train-rmse:0.553318
[196]
          train-rmse:0.553200
Ī197Ī
          train-rmse:0.552978
[198]
          train-rmse:0.552846
[199
          train-rmse:0.552613
          train-rmse:0.552450
[200]
          train-rmse:0.552264
[201]
[202]
[203]
          train-rmse:0.552103
          train-rmse:0.551862
[204]
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205
          train-rmse:0.551535
[206]
          train-rmse:0.551312
[207]
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[208]
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         train-rmse:0.550787
train-rmse:0.550640
[211]
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[212]
[213]
[214]
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          train-rmse:0.550324
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[215]
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[217]
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          train-rmse:0.548306
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          train-rmse:0.548113
          train-rmse:0.547933
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[229]
[230]
[231]
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          train-rmse:0.547230
          train-rmse:0.547116
[232]
[233]
          train-rmse:0.546931
          train-rmse:0.546773
[234]
[235]
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Ī463Ē
         train-rmse:0.581120
Γ464]
         train-rmse:0.581087
[465]
         train-rmse:0.580976
[466]
         train-rmse:0.580908
[467]
         train-rmse:0.580825
         train-rmse:0.580738
train-rmse:0.580688
Ī468⁼
[469]
Γ470⁻
         train-rmse:0.580590
471
         train-rmse:0.580514
[472]
         train-rmse:0.580457
Ī473<sup>⁼</sup>
         train-rmse:0.580397
[474]
         train-rmse:0.580333
Γ475⁻
         train-rmse:0.580273
476
         train-rmse:0.580153
[477]
         train-rmse:0.580127
Ī478⁼
         train-rmse:0.580021
[479]
         train-rmse:0.579962
Γ480⁻
         train-rmse:0.579833
[481]
         train-rmse:0.579736
[482]
         train-rmse:0.579599
         train-rmse:0.579539
Γ483⁻
[484]
         train-rmse:0.579450
[485]
         train-rmse:0.579418
[486]
         train-rmse:0.579225
[487]
         train-rmse:0.579109
         train-rmse:0.579077
Γ488Ί
```

```
Γ4891
         train-rmse:0.579027
[490]
         train-rmse:0.578893
[491]
         train-rmse:0.578798
[492]
         train-rmse:0.578682
[493]
         train-rmse:0.578600
[494]
         train-rmse:0.578445
495]
         train-rmse:0.578327
์ 496โ
         train-rmse:0.578293
[497]
         train-rmse:0.578187
Γ498∫
         train-rmse:0.578096
499
         train-rmse:0.578039
Γ5001
         train-rmse:0.577873
```{r}
combine meta features
sg_col = c("meta_knn", "meta_glm", "meta_svm", "meta_rf", "meta_xgb", "y")
sg_col
train_y = train$comm.next24
test_y = test$comm.next24
train_sg = data.frame(meta_knn_train, meta_glm_train, meta_svm_train, meta_rf_train, meta_xgb_train, train_y)
test_sg = data.frame(meta_knn_test, meta_glm_test, meta_svm_test, meta_rf_test, meta_xgb_test, test_y)
colnames(train sg) = sg col
colnames(test_sg) = sg_col
View(test_sg)
View(train_sg)
write.csv(train_sg, "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/train_sg.csv", row.names = F)
write.csv(test_sg, "C:/Users/Vineet Bhardwaj/Desktop/BlogFeedbackNew/test_sg.csv", row.names = F)
[1] "meta_knn" "meta_glm" "meta_svm" "meta_rf" "meta_xgb" "y"
```{r}
# ensemble with elastic-net regression
train_sg_sparse = model.Matrix(y ~ . - 1, data = train_sg, sparse = T)
View(train_sg_sparse)
test_sg_sparse = model.Matrix(y ~ . - 1, data = test_sg, sparse = T)
mdl_glm = cv.glmnet(train_sg_sparse, train_y, family = "gaussian", alpha = 0.2)
summary(mdl glm)
pred_glm = predict(mdl_glm, newx = test_sg_sparse, s = "lambda.min")
mse(pred_glm, test_y)
            Length Class Mode
            85
85
lambda
                    -none- numeric
                    -none- numeric
CVM
            85
85
85
cvsd
                    -none- numeric
                    -none- numeric
-none- numeric
cvup
cvlo
nzero
            85
                    -none- numeric
name
                    -none- character
glmnet.fit 12
                    elnet list
lambda.min 1
                    -none- numeric
```

Basic testing model Model	Error
k-NN	0.638315
LASS0	0.635483
SVM	0.445464
Random Forest	0.396741
Boosting	0.382399

Weighted Average Model	Error
Best RF	0.396415
Best BST	0.382642
Mean RF	0.396803
Mean BST	0.382934
Best RF + BST	0.380572
Mean RF + BST	0.381167

Stacked Generalization

- 1. Split the training dataset in to k folds.
- 2. For i-th fold of training data, train models with each of the level-0 learners on the rest of the training data.
- 3. Make predictions using the models we trained:
 - a. make predictions on i-th fold of data.
 - b. make predictions on the test set.
- 4. Repeat 2. and 3. until we used all k folds of training data.
- 5. Generate the level-1 data using predictions we obtained:
 - a. generate level-1 training data by concatenating the predictions we made on each fold of the training data.
 - b. generate level-1 test data by averaging the predictions we made on the test
- 6. Train a level-1 generalizer using the level-1 data and the correct responses, make predictions.

Model	Error
LV-1 k-NN	0.631110
LV-1 LASSO	0.624957
LV-1 SVM	0.443895
LV-1 RF	0.393018
LV-1 BST	0.379804
Stacked	0.382274

This is an R Markdown document. Markdown is a simple formatting syntax for authoring HTML, PDF, and MS Word documents. For more details on using R Markdown see http://rmarkdown.rstudio.com.

When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
""{r cars}
summary(cars)
""
## Including Plots

You can also embed plots, for example:
""{r pressure, echo=FALSE}
plot(pressure)
```

Note that the `echo = FALSE` parameter was added to the code chunk to prevent printing of the R code that generated the plot.