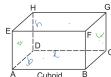




Find the volume, the total surface area and the lateral surface area of a cuboid which is 15 m long, 12 m wide and 4.5 m high.



$$V = l \times b \times h$$

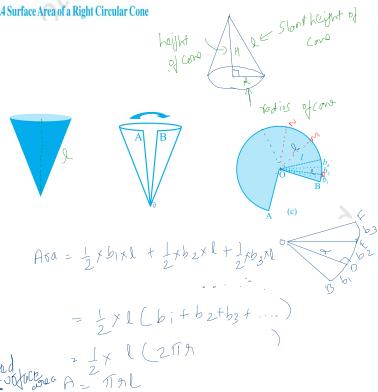
$$V = l \times b \times h = a \times a \times a = a^3$$

$$\begin{aligned} \text{Total Surface Area} &= 2(lb + bh + lh) \\ &= 2(15 \times 12 + 12 \times 4.5 + 15 \times 4.5) \\ \text{Lateral Surface Area} &= 2lh + 2bh \\ &= 2(15 \times 4.5 + 12 \times 4.5) \\ &= 2(22.5 + 27) \\ &= 90 \end{aligned}$$

$$\text{Area of front face} = [2(l+b) \times h]$$

How many bricks will be required to construct a wall 135 m long, 6 m high and 22.5 cm thick? It is being given that each brick measures (27 cm  $\times$  12.5 cm  $\times$  9 cm)?

#### 13.4 Surface Area of a Right Circular Cone

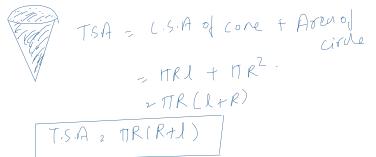


$$\text{Asa} = \frac{1}{2} \times b_1 \times l + \frac{1}{2} \times b_2 \times l + \frac{1}{2} \times b_3 \times l$$

$$= \frac{1}{2} \times l(b_1 + b_2 + b_3)$$

$$= \frac{1}{2} \times l(2\pi r)$$

Wavy bracket A =  $\pi r l$



$$\text{TSA} = \pi R(R+l)$$

1. Diameter of the base of a cone is 0.5 cm and its slant height is 10 cm. Find its curved surface area.

$$\begin{aligned} \text{LSA} &= \pi Rl \\ &= \frac{22}{7} \times \frac{0.5}{2} \times 10 \\ &= 16.5 \text{ cm}^2 \end{aligned}$$



2. Find the total surface area of a cone, if its slant height is 21 m and diameter of its base is 24 m.

$$R = 12 \text{ m}$$

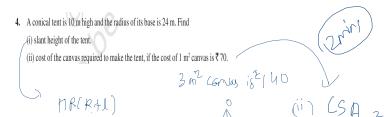
$$\text{TSA} = \pi R(R+l) = 12 \times 4.5 \text{ m}^2$$

3. Curved surface area of a cone is 308 cm<sup>2</sup> and its slant height is 14 cm. Find  
(i) radius of the base and (ii) total surface area of the cone.

$$\begin{aligned} \text{(i) CSA} &= 308 \text{ cm}^2 \quad \text{l} = 14 \text{ cm} \quad \text{(ii) } \text{TSR}(R+l) \\ 17\pi R &= 308 \\ \frac{22}{7} \times \pi \times 14 &= 308 \\ R &= 7 \text{ cm} \end{aligned}$$

4. A conical tent is 10 m high and its radius of its base is 24 m. Find

- (i) slant height of the tent.  
(ii) cost of the canvas required to make the tent, if the cost of 1 m<sup>2</sup> canvas is ₹ 70.



$$\text{L.R.A} = \pi Rl$$

$$\text{(i) LSA} = \pi Rl$$

$$\begin{aligned} \text{(i) LSA} &= \pi Rl \\ &= \frac{22}{7} \times 24 \times 26 \\ &= 13728 \text{ m}^2 \end{aligned}$$

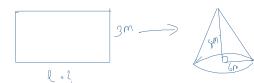
$$l^2 = (10)^2 + (24)^2$$

$$l^2 = 100 + 576$$

$$l^2 = 676 \Rightarrow l = \sqrt{676} = 26$$

$$\begin{aligned} \text{(ii) TSA} &= \pi R(R+l) \\ &= 3 \times 24 \times 140 \\ &= 8160 \text{ m}^2 \\ &= \frac{22}{7} \times 140 \times 13728 \\ &= 160 \times 13728 \end{aligned}$$

5. What length of tarpaulin 3 m wide will be required to make conical tent of height 8 m and base radius 6 m? Assume that the extra length of material that will be required for stitching margins and wastage in cutting is approximately 20 cm (Use  $\pi = 3.14$ ).



Area of the tarpaulin = Area of cone

$$\begin{aligned} \text{(i) } 3 &= \pi Rl \\ &= \pi \times 6 \times 8 \\ &= 3.14 \times 6 \times 8 \\ &= 3.14 \times 6 \times 10 \\ l &= \frac{3.14 \times 6 \times 10}{3} = 62.8 \text{ m} \end{aligned}$$

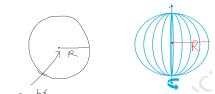
$$\begin{aligned} l &= 62.8 \text{ m} + 0.2 \text{ m} \\ &= 63 \text{ m} \end{aligned}$$

8. A bus stop is barricaded from the remaining part of the road, by using 50 hollow cones made of recycled cardboard. Each cone has a base diameter of 40 cm and height 1 m. If the outer side of each of the cones is to be painted and the cost of painting is ₹ 12 per m<sup>2</sup>, what will be the cost of painting all these cones? (Use  $\pi = 3.14$  and take  $\sqrt{104} = 10.2$ )

$$\begin{aligned} \text{CSA} &= \pi Rl \\ &= 3.14 \times 0.2 \times 1.02 \\ &= \text{_____ m}^2 \\ \text{Cost of painting one cone} &= 12 \times \text{_____} \\ \text{Cost of painting 50 cones} &= 50 \times \text{_____} \end{aligned}$$

$$\begin{aligned} &= \sqrt{(104)^2 - 0^2} \\ &= \sqrt{10400} \\ &= 104 \text{ cm} \end{aligned}$$

Circle and sphere  
20 20



$$\text{Area} = \pi R^2$$



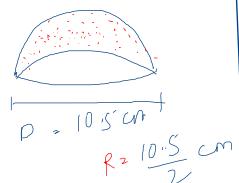
$$\begin{aligned}\text{Surface area of sphere} &= 4 \times \text{Area of Circle} \\ &= 4 \times \pi R^2\end{aligned}$$

$$\begin{aligned}\text{CSA of hemisphere} &= \frac{1}{2} \times (\text{Surface area of Sphere}) \\ &= \frac{1}{2} \times 4\pi R^2 \\ &= 2\pi R^2 \\ \text{T.S.A of hemisphere} &= \text{CSA} + \text{Area of base} \\ &= 2\pi R^2 + \pi R^2 \\ &= 3\pi R^2\end{aligned}$$

5. A hemispherical bowl made of brass has inner diameter 10.5 cm. Find the cost of tin-plating it on the inside at the rate of ₹ 16 per  $100 \text{ cm}^2$ .

$$\begin{aligned}\text{CSA of hemisphere} &= 2\pi R^2 \\ &= 2 \times 22 \times \left(\frac{10.5}{2}\right)^2 \\ &\approx 173.25 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}100 \text{ cm}^2 &\rightarrow R_1 \text{ } 16 \\ 173.25 \text{ cm}^2 &\rightarrow \frac{173.25}{100} \times 16 = 27.72\end{aligned}$$



7. 15/16

7. The diameter of the moon is approximately one fourth of the diameter of the earth.  
Find the ratio of their surface areas.

$$\begin{aligned}\text{Moon} &\quad \text{Earth} \\ D_m &= \frac{1}{4} D_e \\ 2 \times R_m &= \frac{1}{4} \times 2 \times R_e \\ R_m &= \frac{1}{4} R_e \\ \frac{\text{Area}_m}{\text{Area}_e} &= \frac{4\pi R_m^2}{4\pi R_e^2} \\ &= \frac{(R_m)^2}{(R_e)^2} \\ &= \frac{\left(\frac{1}{4} R_e\right)^2}{R_e^2} = \frac{1}{16} R_e^2 \\ &\underline{\underline{1:16}}\end{aligned}$$

8. A hemispherical bowl is made of steel 0.25 cm thick. The inner radius of the bowl is 5 cm. Find the outer curved surface area of the bowl.



$$R = 5 + 0.25 \text{ cm} \\ = 5.25 \text{ cm}$$

$$\begin{aligned}\text{Outer CSA} &= 2\pi R^2 \\ &= 2 \times 22 \times (5.25)^2 \\ &\approx 173.25 \text{ cm}^2\end{aligned}$$



9. A right circular cylinder just encloses a sphere of radius r over height H. Find

- (i) surface area of the sphere,  
(ii) curved surface area of the cylinder,  
(iii) ratio of the areas obtained in (i) and (ii).

$$2\pi rH$$

$$\begin{aligned}\text{CSA of cylinder} &= 2\pi rH = 2\pi r(2r) \\ \text{Ratio} &= \frac{\pi r^2}{2\pi r^2} = \frac{1}{2} \underline{\underline{1:2}}\end{aligned}$$

### Volume of a Right circular Cone

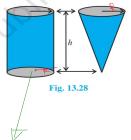


Fig. 13.28



$$\text{Vol of a cylinder} = \pi R^2 H$$

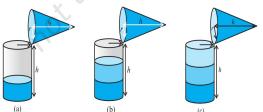


Fig. 13.29

$$\text{Volume of a Cone} = \frac{1}{3} \pi r^2 h$$

$r$  is the base radius and  $h$  is the height of the cone.

Assume  $\pi = \frac{22}{7}$  unless stated otherwise.

1. Find the volume of the right circular cone with
  - (i) radius 6 cm, height 7 cm
  - (ii) radius 3.5 cm, height 12 cm
2. Find the capacity in litres of a conical vessel with
  - (i) radius 7 cm, slant height 25 cm
  - (ii) height 12 cm, slant height 13 cm

$$R = 7 \text{ cm} \quad l = 25 \text{ cm}$$

Is having  
Slant height  
Dihedral angle  
Vs?

3. The height of a cone is 15 cm. If its volume is  $1570 \text{ cm}^3$ , find the radius of the base.  
(Use  $\pi = 3.14$ )

$$V = \frac{1}{3} \pi R^2 h$$

$$1570 = \frac{1}{3} \times 3.14 \times R^2 \times 15$$

$$1570 = 15.7 \pi R^2$$

$$1570 = 15.7 \times 3.14 \times R^2$$

$$1570 = 48.98 R^2$$

$$R^2 = \frac{1570}{48.98}$$

$$R^2 = 32$$

$$R = \sqrt{32} \approx 5.66 \text{ cm}$$



$$l^2 = h^2 + r^2$$

$$h = \sqrt{l^2 - r^2}$$

$$l^2 = h^2 + r^2$$

$$h^2 = l^2 - r^2$$

$$h = \sqrt{l^2 - r^2}$$

$$h^2 = l^2 - r^2$$

$$h = \sqrt{l^2 - r^2}$$

$$h^2 = l^2 - r^2$$

$$h = \sqrt{l^2 - r^2}$$

4. If the volume of a right circular cone of height 9 cm is  $48\pi \text{ cm}^3$ , find the diameter of its base.

$$\text{Vol} = \frac{1}{3} \pi R^2 H$$

$$48\pi = \frac{1}{3} \pi R^2 \times 9$$

$$48 = \frac{1}{3} R^2 \times 9$$

$$48 = 3R^2$$

$$R^2 = 16$$

$$R = 4 \text{ cm}$$

5. A conical pit of top diameter 3.5 m is 12 m deep. What is its capacity in kilolitres?

$$D = 3.5 \text{ m} \quad R = \frac{3.5}{2} \text{ m}$$

$$\text{Vol} = \frac{1}{3} \pi R^2 H$$

$$= \frac{1}{3} \times 3.14 \times \left(\frac{3.5}{2}\right)^2 \times 12$$

$$= 38.5 \text{ m}^3$$

$$1 \text{ m}^3 = 1 \text{ kl}$$

$$38.5 \text{ m}^3 = 38.5 \text{ kl}$$

6. A heap of wheat is in the form of a cone whose diameter is 10.5 m and height is 3 m. Find its volume. The heap is to be covered by canvas to protect it from rain. Find the area of the canvas required.

$$V = \frac{1}{3} \pi R^2 H$$

$$= \frac{1}{3} \pi \times 5.25^2 \times 3$$

$$= 84.75 \text{ m}^3$$

$$\text{CSA} = \pi R l$$



6. The volume of a right circular cone is  $9856 \text{ cm}^3$ . If the diameter of the base is 28 cm, find
  - (i) height of the cone
  - (ii) slant height of the cone
  - (iii) curved surface area of the cone

$$(i) D = 28 \text{ cm} \quad R = 14 \text{ cm}$$

$$V = \frac{1}{3} \pi R^2 H$$

$$9856 = \frac{1}{3} \times 3.14 \times 14^2 \times H$$

$$H = 18 \text{ cm}$$

$$(ii) l^2 = h^2 + r^2$$

$$= (14)^2 + (18)^2$$

$$l = \sqrt{280+324}$$

$$= \sqrt{604}$$

$$l = 24.5 \text{ cm}$$

$$(iii) \text{CSA} = \pi R l$$

$$= \frac{22}{7} \times 14 \times 24.5$$

$$= 220 \text{ cm}^2$$

7. A right triangle ABC with sides 5 cm, 12 cm and 13 cm is revolved about the side 12 cm.

Find the volume of the solid so obtained.

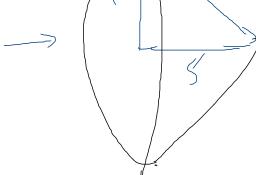
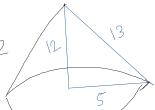
$$\text{Vol} = \frac{1}{3} \pi R^2 h$$

$$= \frac{1}{3} \pi \times 5^2 \times 12$$

$$= \frac{1}{3} \pi \times 100 \text{ cm}^3$$

$$= 100 \pi \text{ cm}^3$$

$$= 100 \times 3.14 \text{ cm}^3$$



8. If the triangle ABC in the Question 7 above is revolved about the side 5 cm, then find the volume of the solid so obtained. Find also the ratio of the volumes of the two solids obtained in Questions 7 and 8.

$$\text{Vol} = \frac{1}{3} \pi R^2 H$$

$$= \frac{1}{3} \pi \times 12^2 \times 5 \text{ cm}^3$$

$$= 240 \pi \text{ cm}^3$$

$$= 240 \times 3.14 \text{ cm}^3$$

$$= 753.6 \text{ cm}^3$$

$$\text{Ratio} = \frac{753.6}{100\pi}$$

$$= \frac{753.6}{100 \times 3.14}$$

$$= \frac{753.6}{314}$$

$$= \frac{24}{8}$$

$$= 3 : 12$$

### 13.9 Volume of a Sphere



$$\text{Volume of sphere} = \frac{4}{3}\pi r^3$$

$$\text{Volume of hemisphere} = \frac{2}{3}\pi r^3 + \frac{2}{3}\pi r^2 h$$

$$\text{Given } R = 0.63 \text{ m}$$

$$V = \frac{4}{3}\pi R^3$$

$$= \frac{4}{3}\pi \times 22 \times (0.63)^3$$

$$= \frac{4}{3}\pi \times 22 \times \frac{21}{100} \times \frac{63}{100} \times \frac{13}{100}$$

$$= \frac{1}{1000} \times 6.00$$

$$\text{Given } D = 0.21 \text{ m}$$

$$R = \frac{D}{2} = \frac{0.21}{2} \text{ m}$$

$$V = \frac{4}{3}\pi R^3 = \frac{4}{3}\pi \times \frac{21}{2} \times \left(\frac{0.21}{2}\right)^3$$

$$= \frac{4}{3}\pi \times \frac{21}{2} \times \frac{21}{100} \times \frac{21}{100} \times \frac{21}{100}$$

$$= \frac{11 \times 21 \times 21}{100 \times 100 \times 100}$$

$$= \frac{4933}{1000000} \text{ m}^3$$

$$= 0.004933 \text{ m}^3$$

3. The diameter of a metallic ball is 4.2 cm. What is the mass of the ball, if the density of the metal is 8.9 g per cm<sup>3</sup>?

$$D = 4.2 \text{ cm}$$

$$R = 2.1 \text{ cm}$$

$$V = \frac{4}{3}\pi R^3$$

$$= \frac{4}{3}\pi \times \frac{21}{2} \times (2.1)^3$$

$$= \frac{4}{3}\pi \times \frac{21}{2} \times \frac{21}{10} \times (2.1)^3$$

$$= \frac{22 \times 4 \times 21 \times 21}{1000}$$

$$= 3.9808 \text{ cm}^3$$

$$m = 8.9 \text{ g}$$

$$m = 8.9 \times 3.9808 \text{ g}$$

$$= 35.69 \text{ g}$$

4. The diameter of the moon is approximately one-fourth of the diameter of the earth. What fraction of the volume of the earth is the volume of the moon?

$$D_m = \frac{1}{4} D_e$$

$$\frac{V_m}{V_e} = \frac{\frac{4}{3}\pi R_m^3}{\frac{4}{3}\pi R_e^3}$$

$$R_m = \frac{1}{4} R_e \quad \text{(1)}$$

$$\frac{V_m}{V_e} = \frac{R_m^3}{(R_e)^3}$$

$$V_m = \frac{1}{64} V_e$$

$$V_e > \frac{4}{3}\pi R_e^3$$

$$\frac{V_e}{V_m} = \frac{64}{1}$$

$$\frac{V_e}{V_m} = \frac{R_e^3}{(R_m)^3} = \frac{R_e^3}{(\frac{1}{4}R_e)^3} = \frac{R_e^3}{\frac{1}{64}R_e^3} = 64$$

5. How many litres of milk can a hemispherical bowl of diameter 10.5 cm hold?

$$V = \frac{2}{3}\pi R^2$$

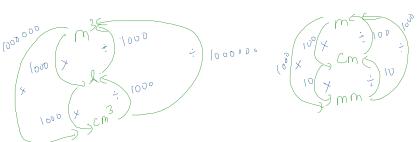
$$= \frac{2}{3}\pi \times \frac{10.5}{2}^2$$

$$= \frac{2}{3}\pi \times 5.25^2$$

$$= \frac{2}{3}\pi \times 27.5625$$

$$= \frac{55.125}{3}\pi$$

$$= 56.7 \text{ cm}^3$$



6. A hemispherical tank is made up of an iron sheet 1 cm thick. If the inner radius is 1 m, find the volume of the iron used to make the tank.

$$\text{Inner radius (r)} = 1 \text{ m}$$

$$\text{Outer radius (R)} = r + t$$

$$= 1 + 0.01 \text{ m}$$

$$R = 1.01 \text{ m}$$

$$\text{Volume of iron used} = \frac{2}{3}\pi R^3 - \frac{2}{3}\pi r^3$$

$$= \frac{2}{3}\pi (R^3 - r^3)$$

$$= \frac{2}{3}\pi ((1.01)^3 - (1)^3)$$

$$= \frac{2}{3}\pi (1.030301 - 1)$$

$$= \frac{2}{3}\pi \times 0.030301$$

7. Find the volume of a sphere whose surface area is 154 cm<sup>2</sup>.

$$V = \frac{4}{3}\pi R^3$$

$$A = 4\pi r^2$$

$$154 = 4\pi r^2$$

$$154 = 4\pi \times \frac{R^2}{4}$$

$$154 = \pi R^2$$

$$\frac{154}{\pi} = R^2$$

8. A dome of a building is in the form of a hemisphere. From inside, if the cost of white-washing is ₹ 20 per square meter, find the (i) inside surface area of the dome. (ii) volume of the air inside the dome.

Total cost of white-washing = ₹ 4989.60

$$\text{Area} = \pi r^2$$

$$20 \times \pi r^2 = 4989.60$$

$$\pi r^2 = \frac{4989.60}{20}$$

$$r^2 = \frac{4989.60}{20\pi}$$

$$r^2 = \frac{4989.60}{62.832}$$

$$r^2 = 79.48$$

$$r = \sqrt{79.48} = 8.91 \text{ m}$$

$$\text{Volume} = \frac{4}{3}\pi r^3$$

$$= \frac{4}{3}\pi \times 8.91^3$$

$$= 898.5 \text{ m}^3$$

$$(i) V = \frac{2}{3}\pi R^2$$

$$A = 2\pi R^2$$

$$20 \times \pi R^2 = 2 \times 22 \times \frac{7}{22} \times R^2$$

$$20 \times 7 \times R^2 = 2 \times 22 \times 7 \times R^2$$

$$20 \times 7 \times R^2 = 2 \times 22 \times 7 \times \frac{567}{100}$$

$$20 \times 7 \times R^2 = 567 \times 7$$

$$R^2 = \frac{567 \times 7}{20 \times 22 \times 7} = \frac{567}{100}$$

$$R^2 = 5.67$$

$$R = \sqrt{\frac{567}{100}} = \frac{23.7}{10} = 2.37 \text{ m}$$

9. Twenty seven solid iron spheres, each of radius 'r' and surface area S are melted to form a sphere with surface area 9S. Find the (i) radius 'r'' of the new sphere. (ii) ratio of S and S'.

$$\text{Volume of small 27 spheres} = \text{Volume of new sphere}$$

$$(i) 27 \times \frac{4}{3}\pi r^3 = \frac{4}{3}\pi r'^3$$

$$27 \times \frac{4}{3}\pi r^3 = (3r)^3$$

$$27r^3 = 27r^3$$

$$3r = r'$$

$$(ii) S = 4\pi r^2$$

$$S' = 4\pi (r')^2$$

$$S' = 4\pi (3r)^2$$

$$S' = 36\pi r^2$$

$$S : S' = 1 : 36$$

10. A capsule of medicine is in the shape of a sphere of diameter 3.5 mm. How much medicine (in ml) would be required to fill this capsule?

$$V = \frac{4}{3}\pi R^3$$

$$= \frac{4}{3}\pi \times \frac{3.5}{2}^3$$

$$= \frac{4}{3}\pi \times 1.75^3$$

$$= \frac{4}{3}\pi \times 5.0625$$

$$= 21.26 \text{ mm}^3$$