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# Sistemas Nebulosos

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## QUESTÃO 1: Modelagem de sistema estático monovariável

Aproximar a função  $y=x^2$

%

---

```
close all; clear; clc;  
warning('off','all');
```

```
% Geração de dados
```

```
N = 1000;  
X = (linspace(-2, 2, N)).';  
Y = (X.^2);
```

```
idx = randperm(length(Y));  
X_train = X(sort(idx(1:900)));  
Y_train = Y(sort(idx(1:900)));  
X_test = X(sort(idx(901:1000)));  
Y_test = Y(sort(idx(901:1000)));
```

# Generate FIS Using Grid Partitioning

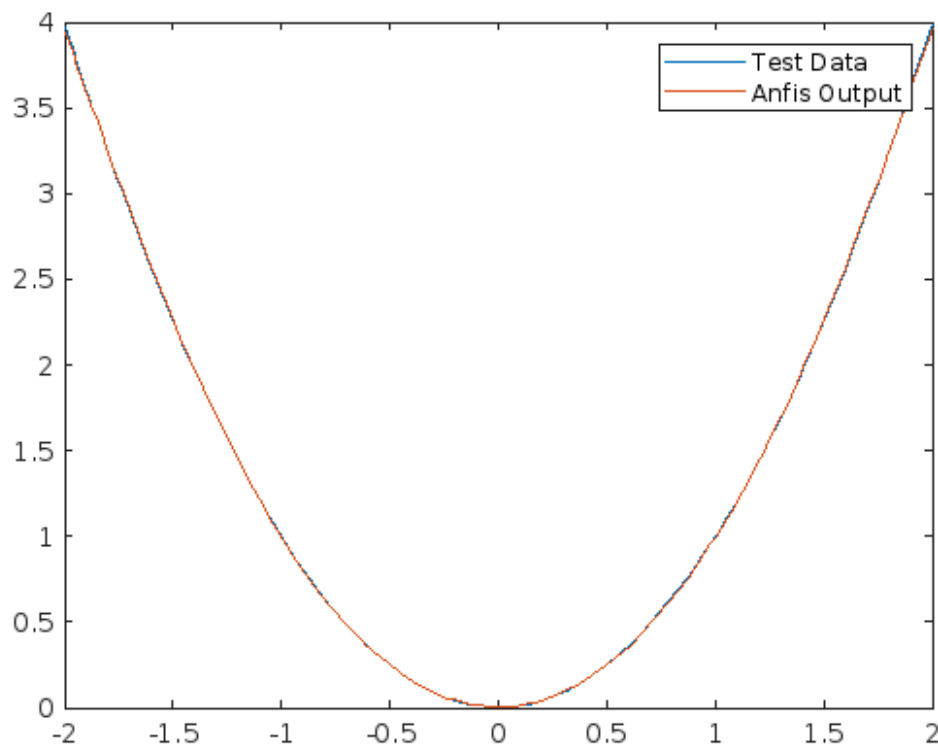
```
fig_number = 1;
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'GridPartition',2);
figure(fig_number)
plot(X_test, y_test, X_test, ys)
legend('Test Data','Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

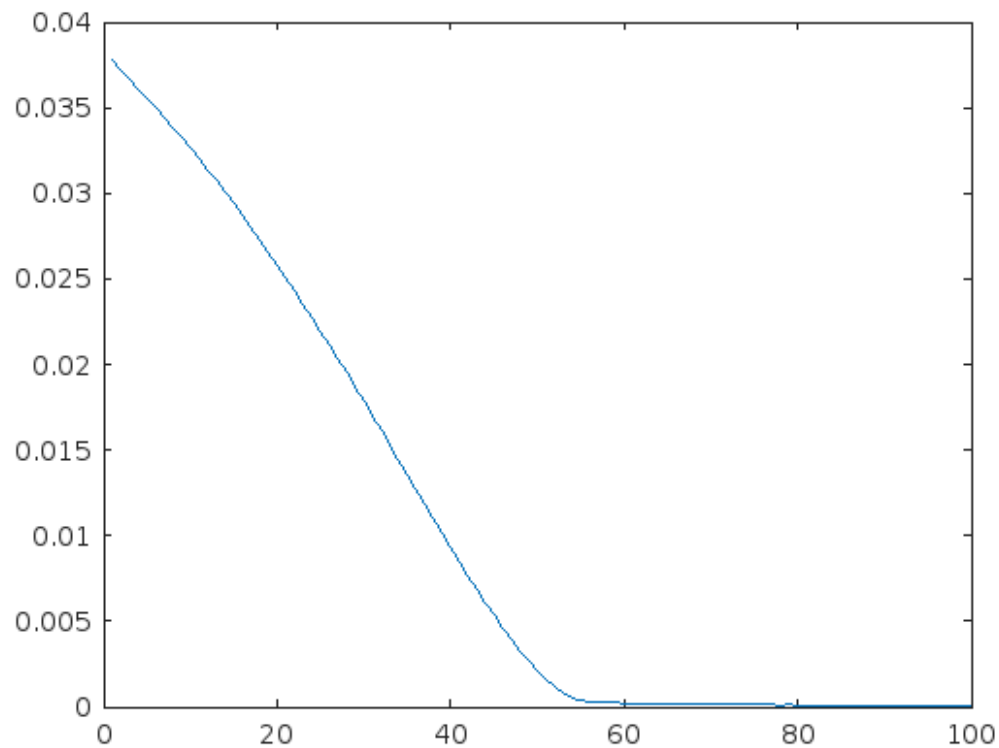
*ANFIS info:*

*Number of nodes: 12*  
*Number of linear parameters: 4*  
*Number of nonlinear parameters: 6*  
*Total number of parameters: 10*  
*Number of training data pairs: 900*  
*Number of checking data pairs: 0*  
*Number of fuzzy rules: 2*

*Minimal training RMSE = 0.0076546*

*MSE: 8.02E-05*





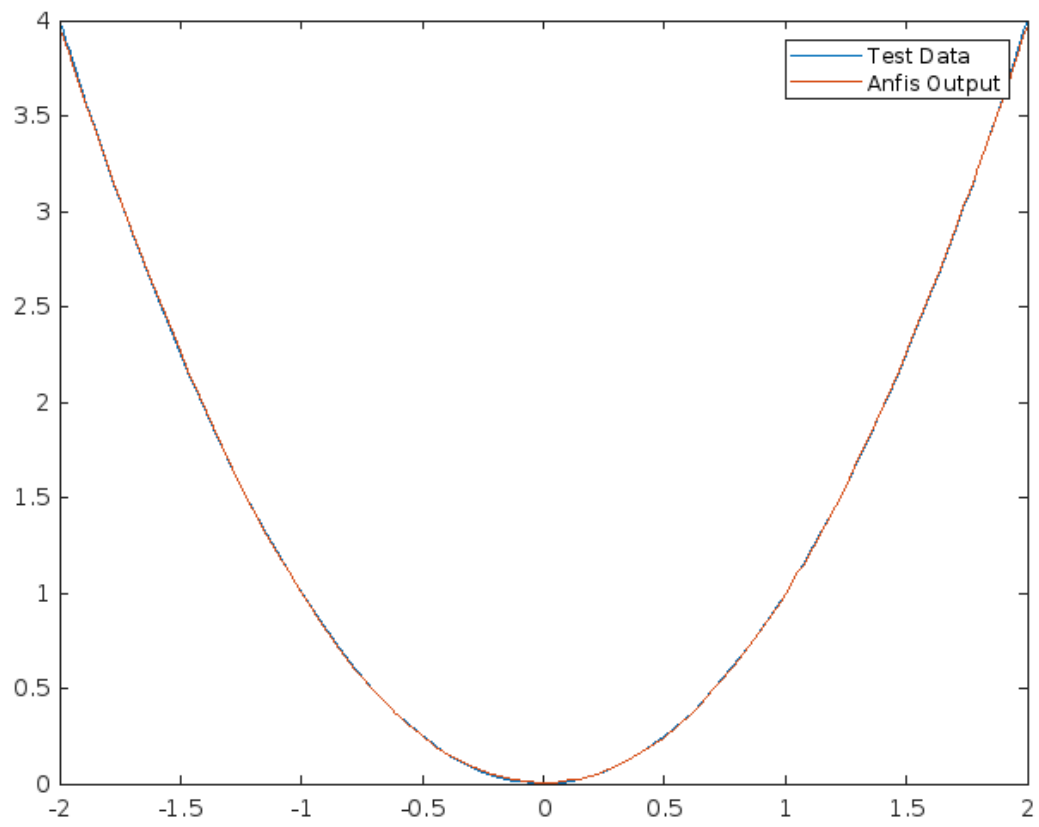
## Generate FIS Using Subtractive Clustering

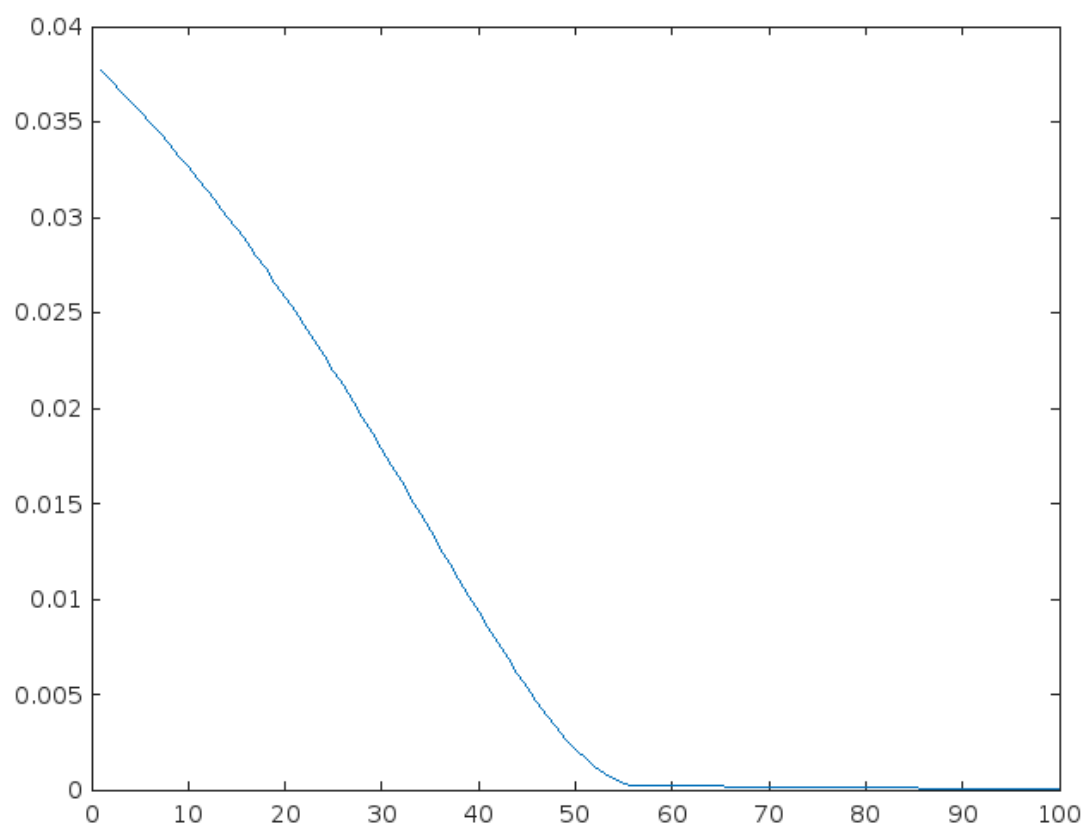
```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'SubtractiveClustering');  
figure(fig_number)  
plot(X_test, y_test, X_test, ys)  
legend('Test Data', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

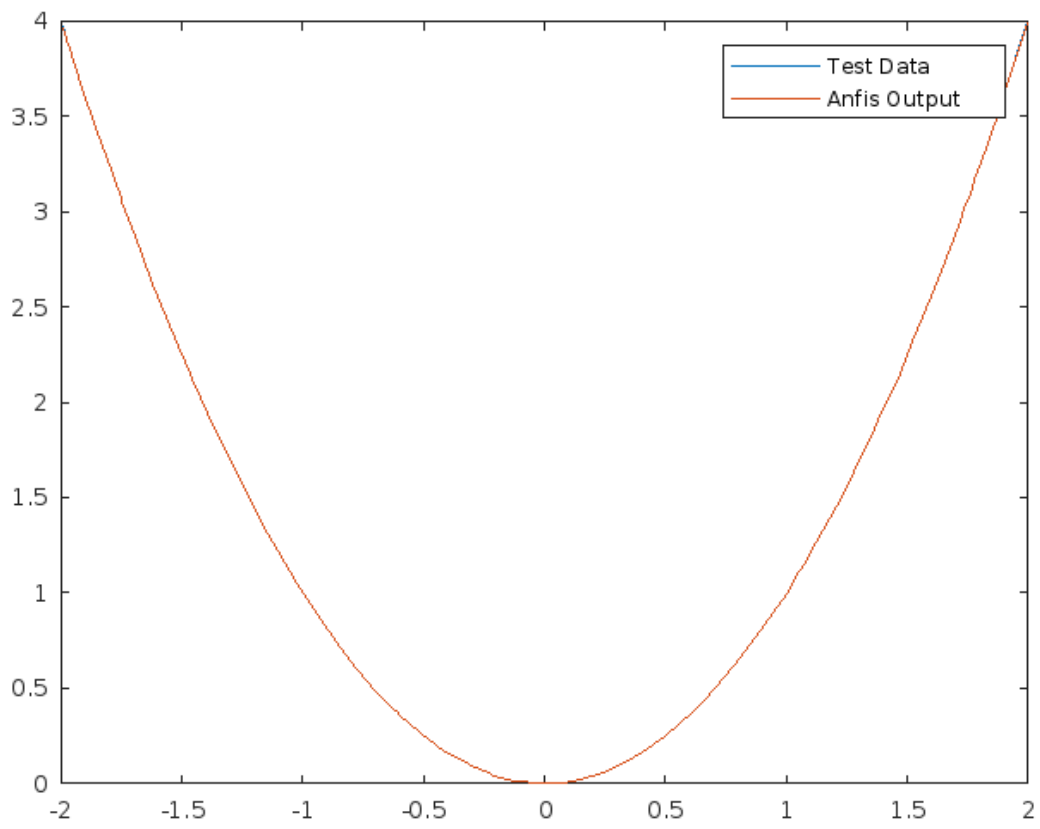
*ANFIS info:*

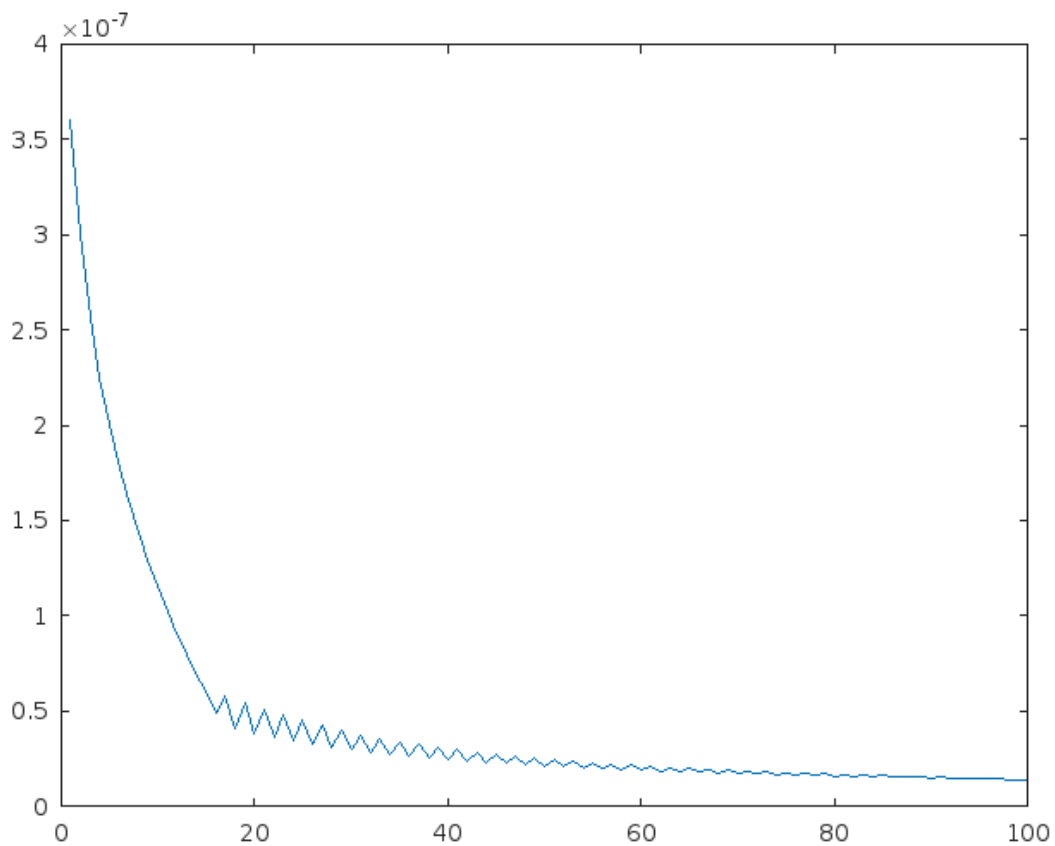
*Number of nodes: 24  
Number of linear parameters: 10  
Number of nonlinear parameters: 10  
Total number of parameters: 20  
Number of training data pairs: 900  
Number of checking data pairs: 0  
Number of fuzzy rules: 5*

*Minimal training RMSE = 0.00011831  
MSE: 1.97E-08*









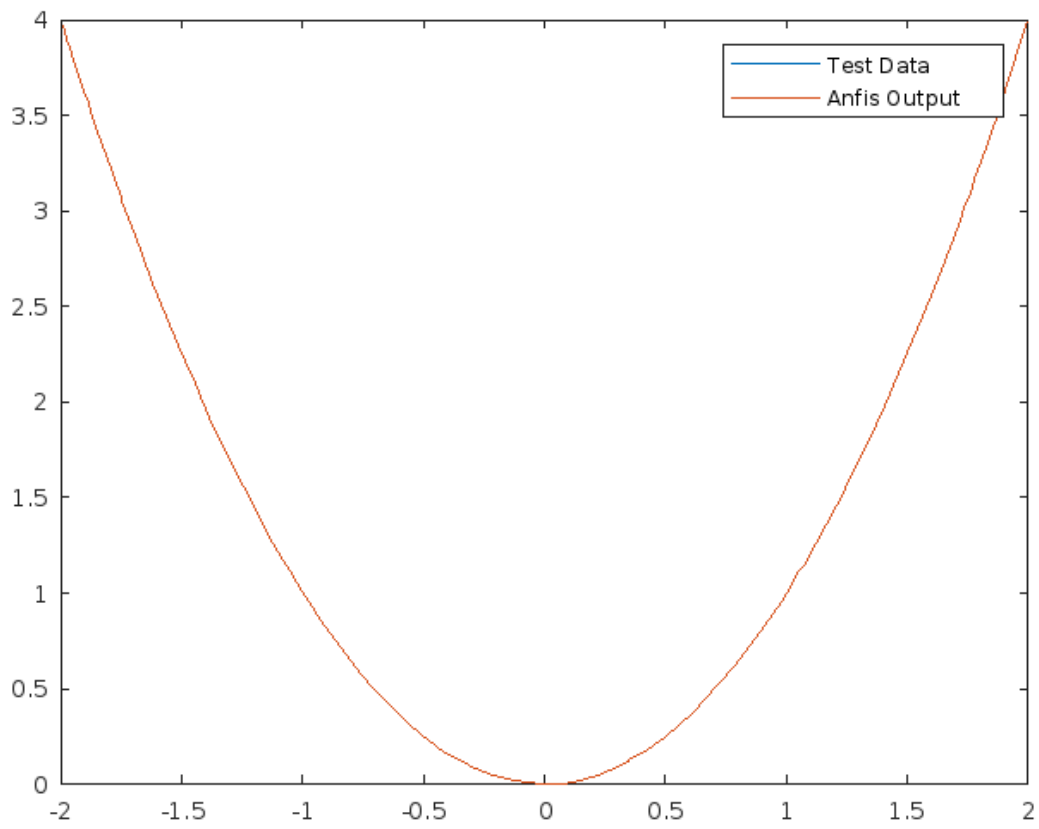
## Generate FIS Using FCM Clustering

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'FCMClustering');  
figure(fig_number)  
plot(X_test, y_test, X_test, ys)  
legend('Test Data', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

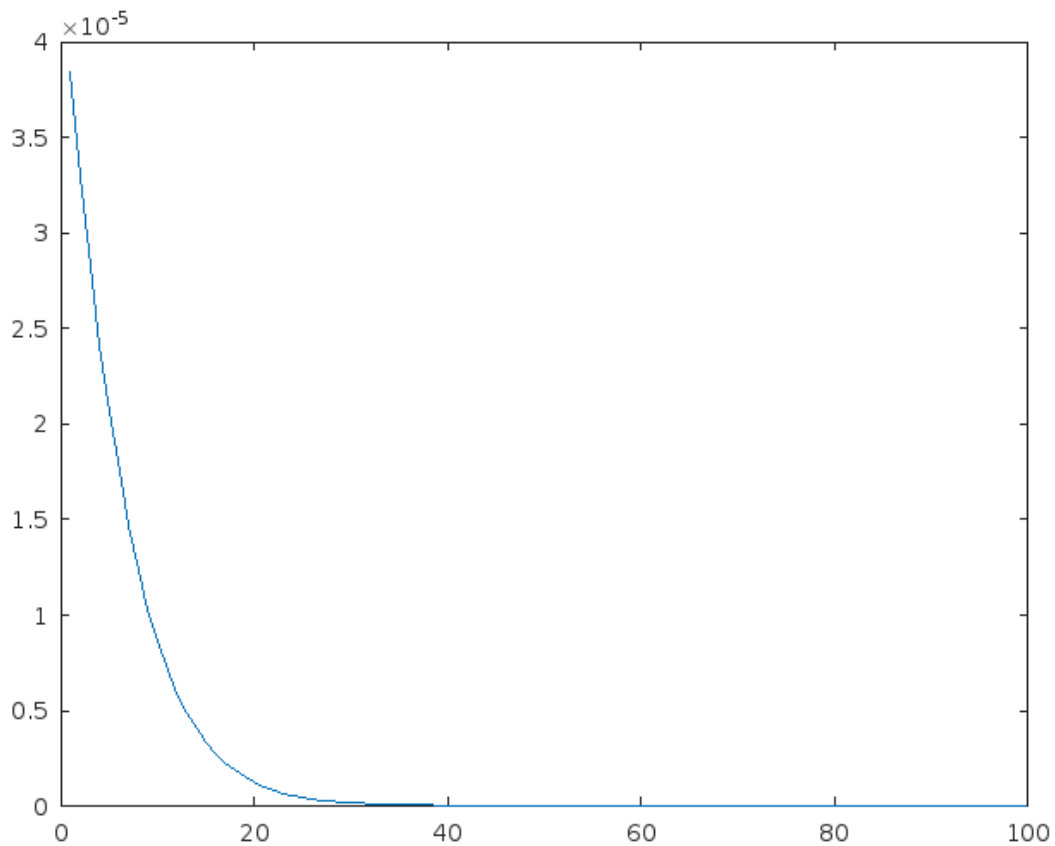
*ANFIS info:*

*Number of nodes: 24  
Number of linear parameters: 10  
Number of nonlinear parameters: 10  
Total number of parameters: 20  
Number of training data pairs: 900  
Number of checking data pairs: 0  
Number of fuzzy rules: 5*

*Minimal training RMSE = 8.23037e-05*  
*MSE: 1.04E-08*





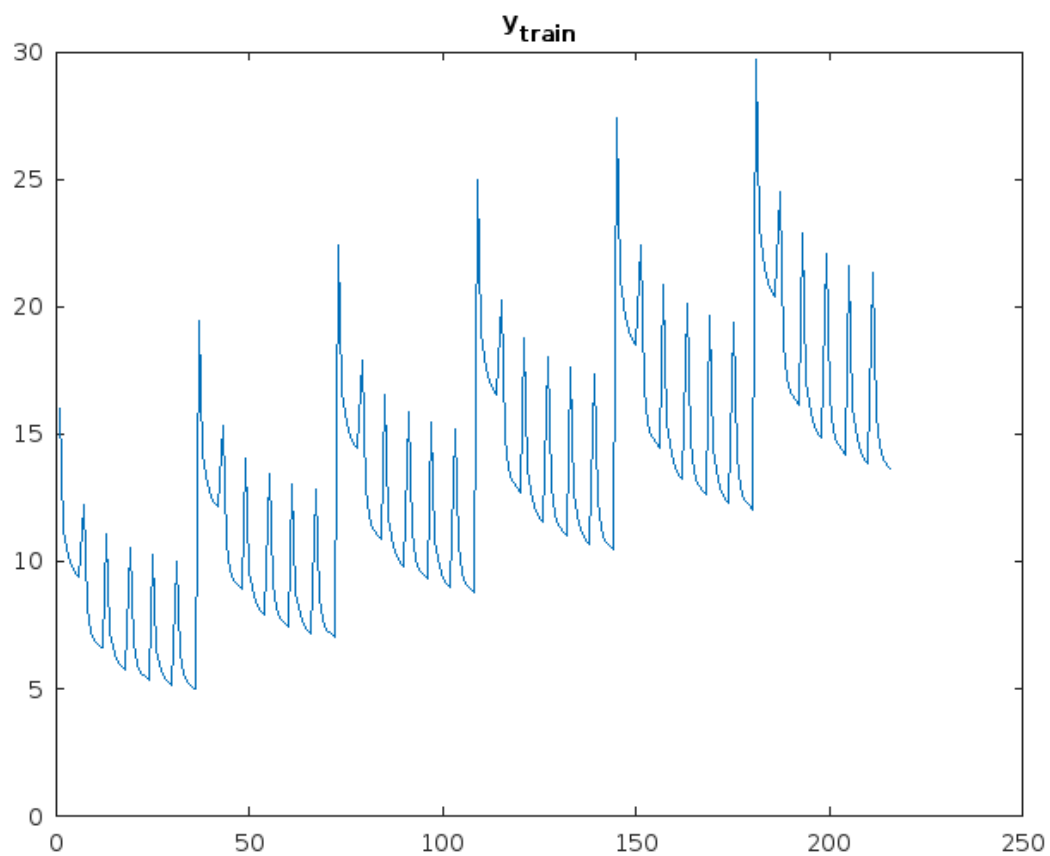


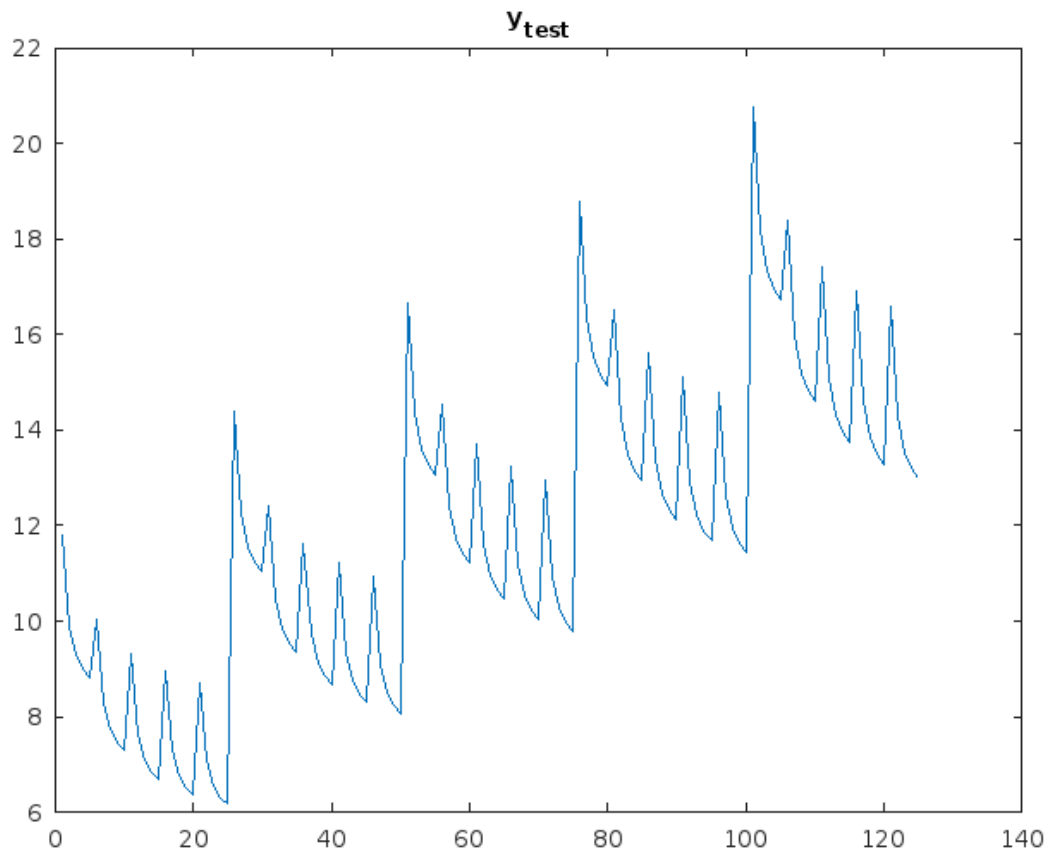
## QUESTÃO 2: Modelagem de sistema estático multivariável

Modelar uma função não linear de 3 entradas:

$$\text{output} = (1 + x^{0.5} + y^{-1} + z^{-1.5})^2$$

```
%  
X_train = table2array(readtable('ex2_X_train.csv'));  
y_train = table2array(readtable('ex2_y_train.csv'));  
X_test = table2array(readtable('ex2_X_test.csv'));  
y_test = table2array(readtable('ex2_y_test.csv'));  
figure(fig_number)  
plot(y_train);  
title("y_{train}");  
drawnow();  
fig_number = fig_number + 1;  
figure(fig_number)  
plot(y_test);  
title("y_{test}");  
drawnow();  
fig_number = fig_number + 1;
```





## Generate FIS Using Grid Partitioning

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'GridPartition',2);  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}','Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

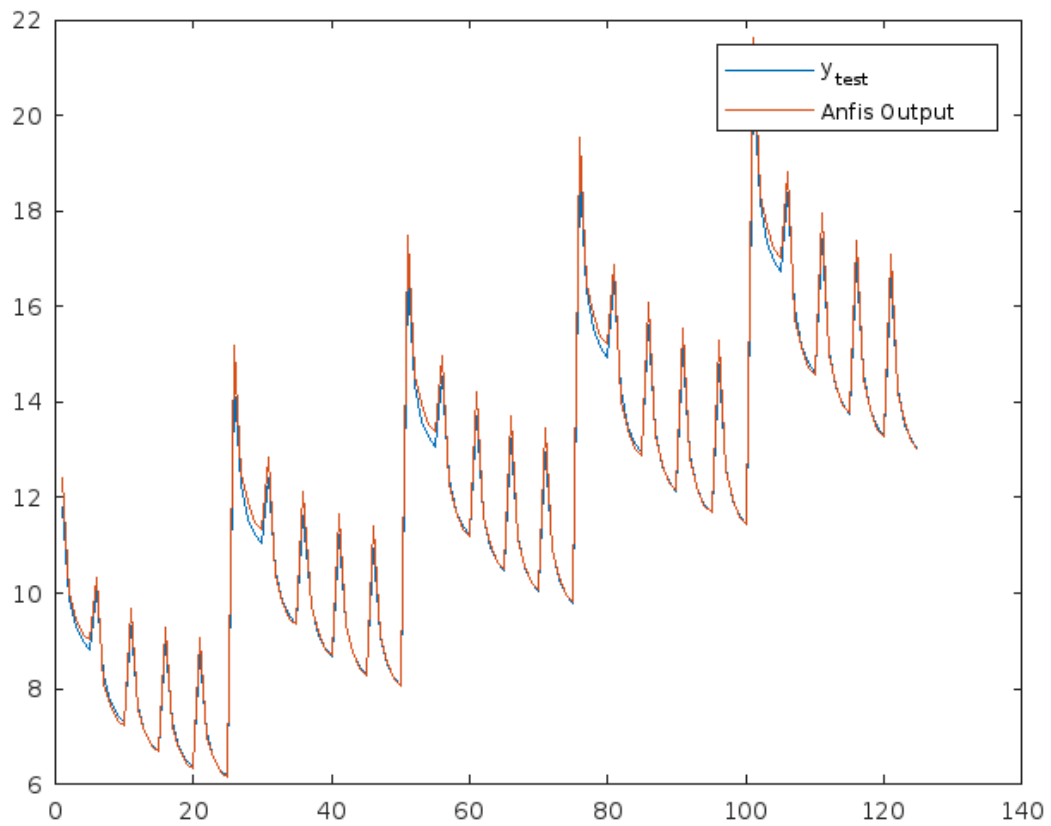
*ANFIS info:*

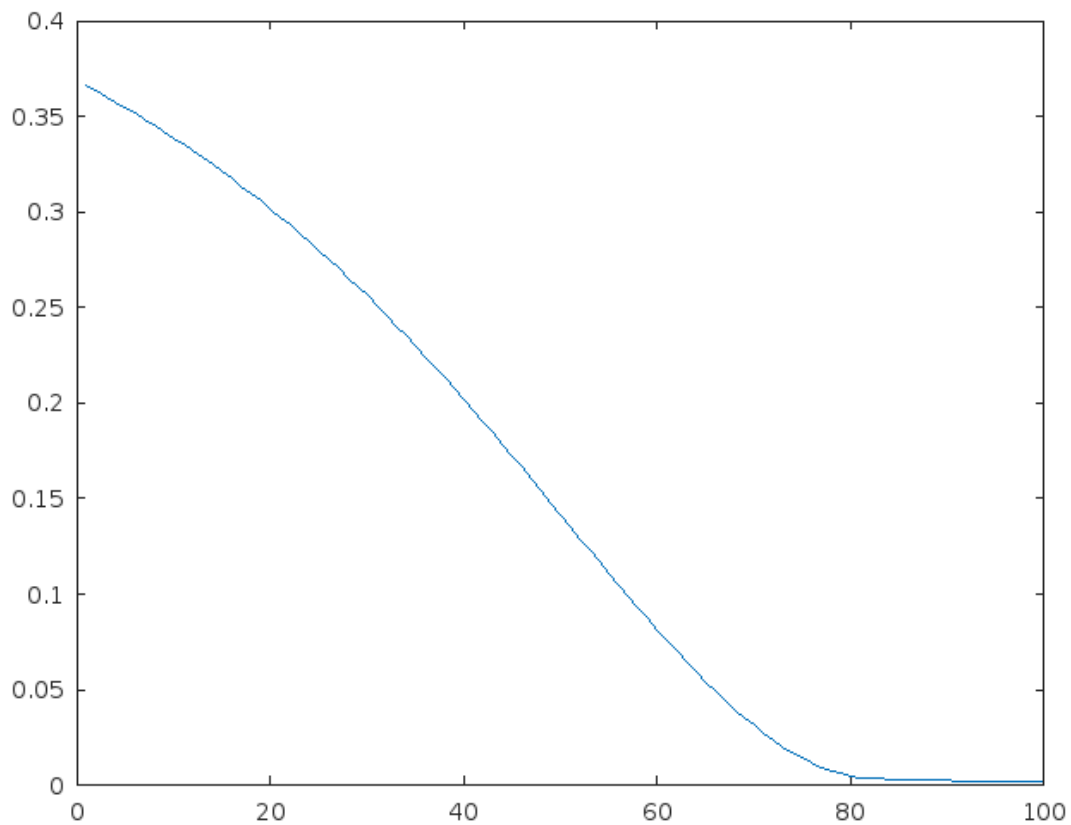
*Number of nodes: 34  
Number of linear parameters: 32  
Number of nonlinear parameters: 18  
Total number of parameters: 50  
Number of training data pairs: 216  
Number of checking data pairs: 0*

*Number of fuzzy rules: 8*

*Minimal training RMSE = 0.0412386*

*MSE: 6.95E-02*





## Generate FIS Using Subtractive Clustering

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'SubtractiveClustering');  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

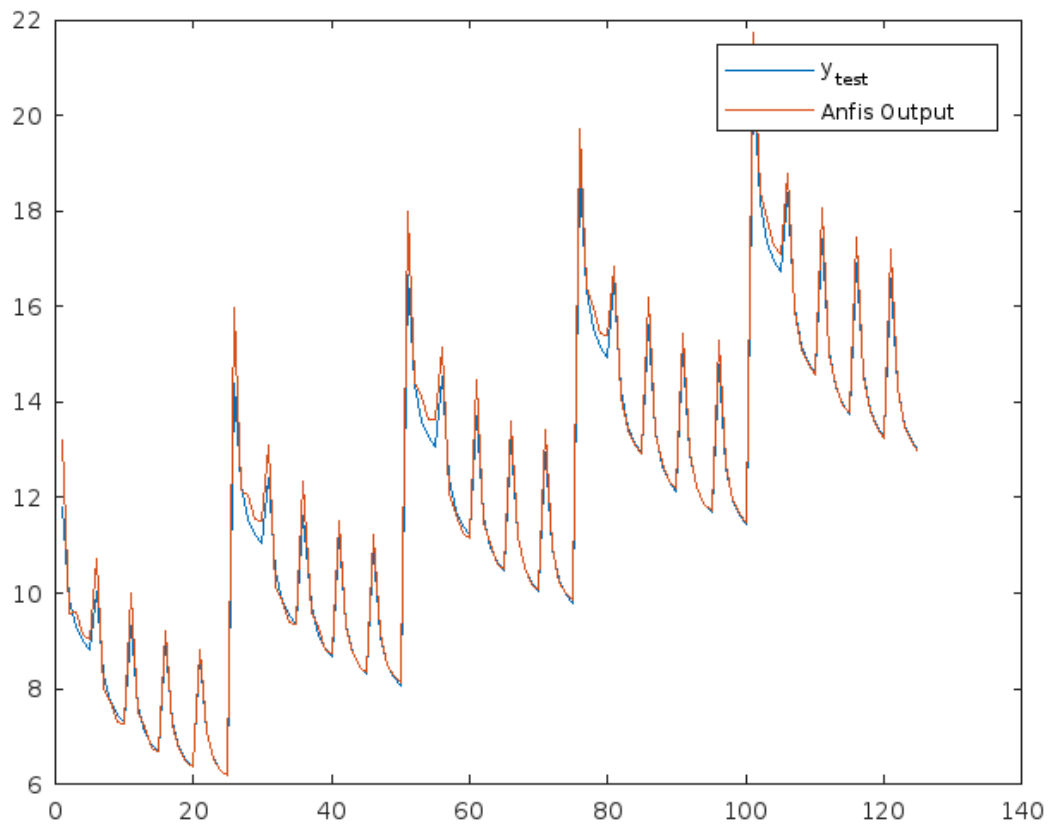
*ANFIS info:*

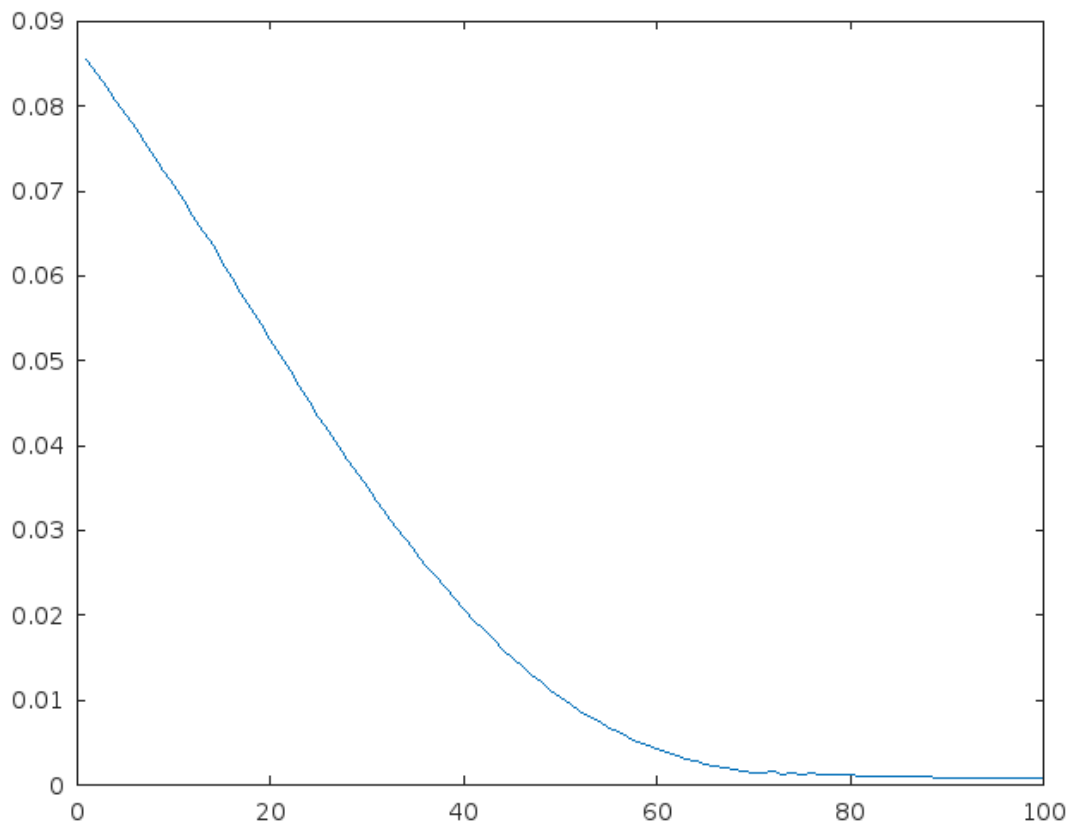
*Number of nodes: 190  
Number of linear parameters: 92  
Number of nonlinear parameters: 138  
Total number of parameters: 230  
Number of training data pairs: 216  
Number of checking data pairs: 0*

*Number of fuzzy rules: 23*

*Minimal training RMSE = 0.027412*

*MSE: 1.35E-01*





## Generate FIS Using FCM Clustering

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'FCMClustering');  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

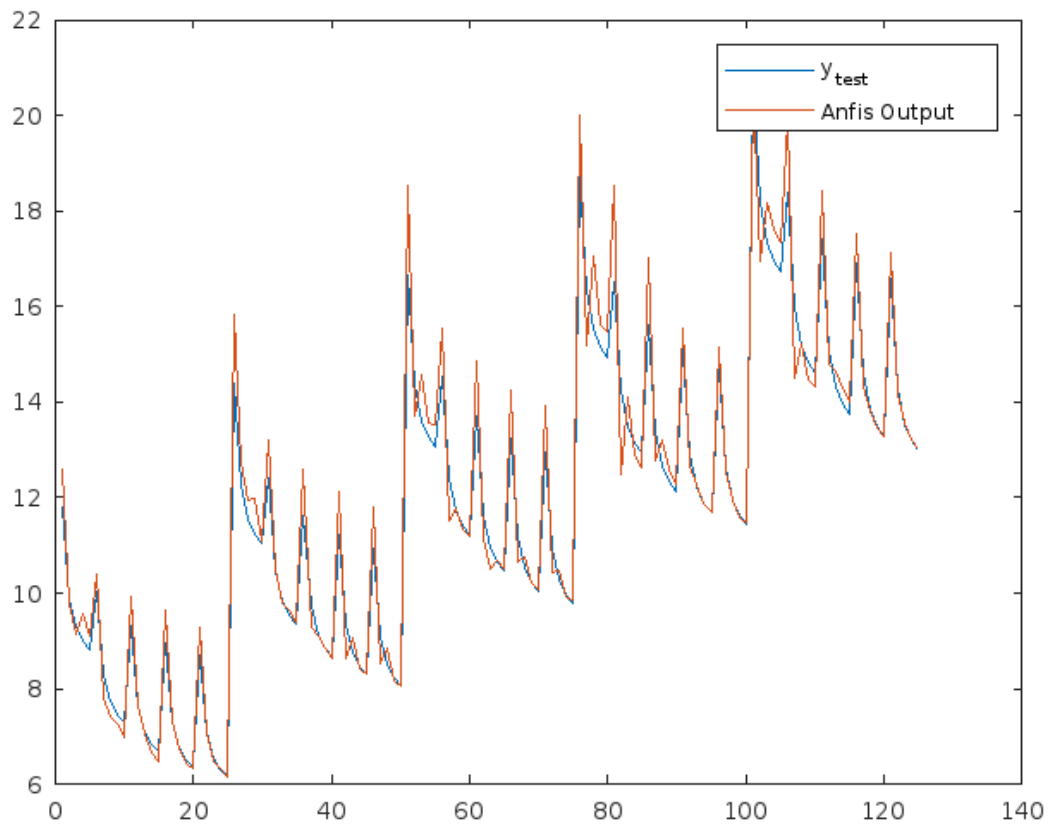
*ANFIS info:*

*Number of nodes: 190  
Number of linear parameters: 92  
Number of nonlinear parameters: 138  
Total number of parameters: 230  
Number of training data pairs: 216  
Number of checking data pairs: 0*

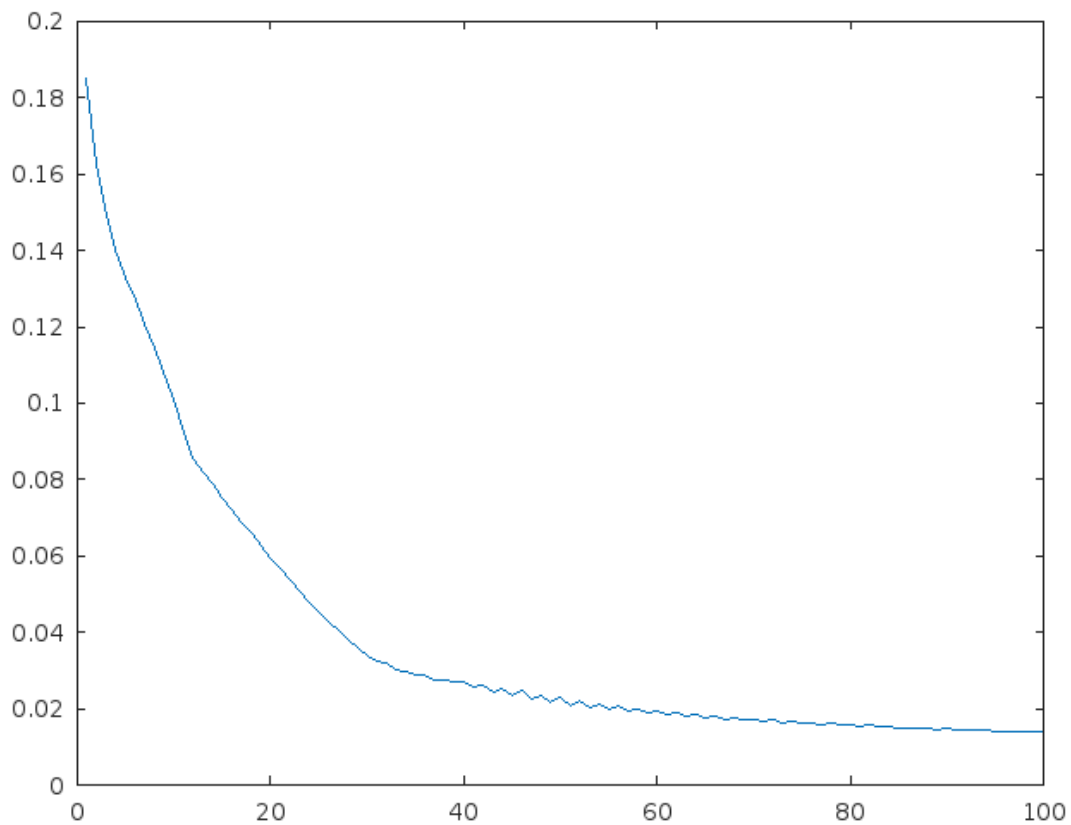
*Number of fuzzy rules: 23*

*Minimal training RMSE = 0.117529*

*MSE: 3.86E-01*

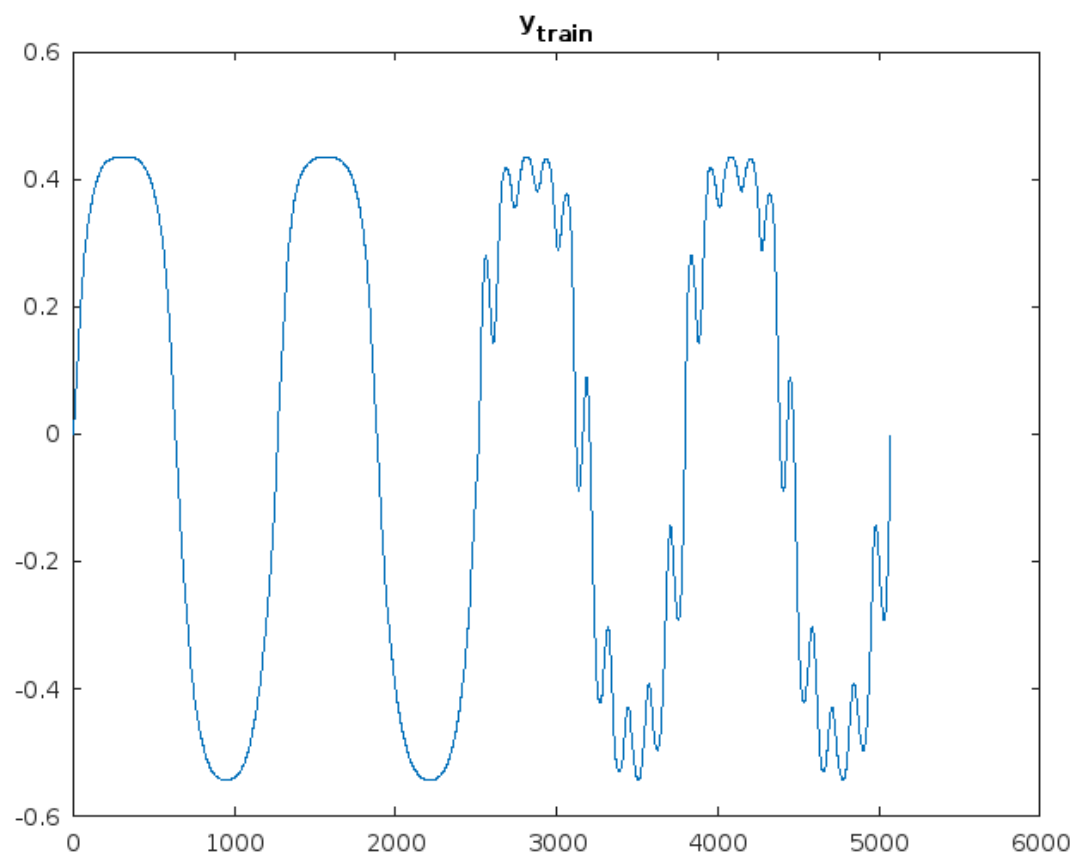


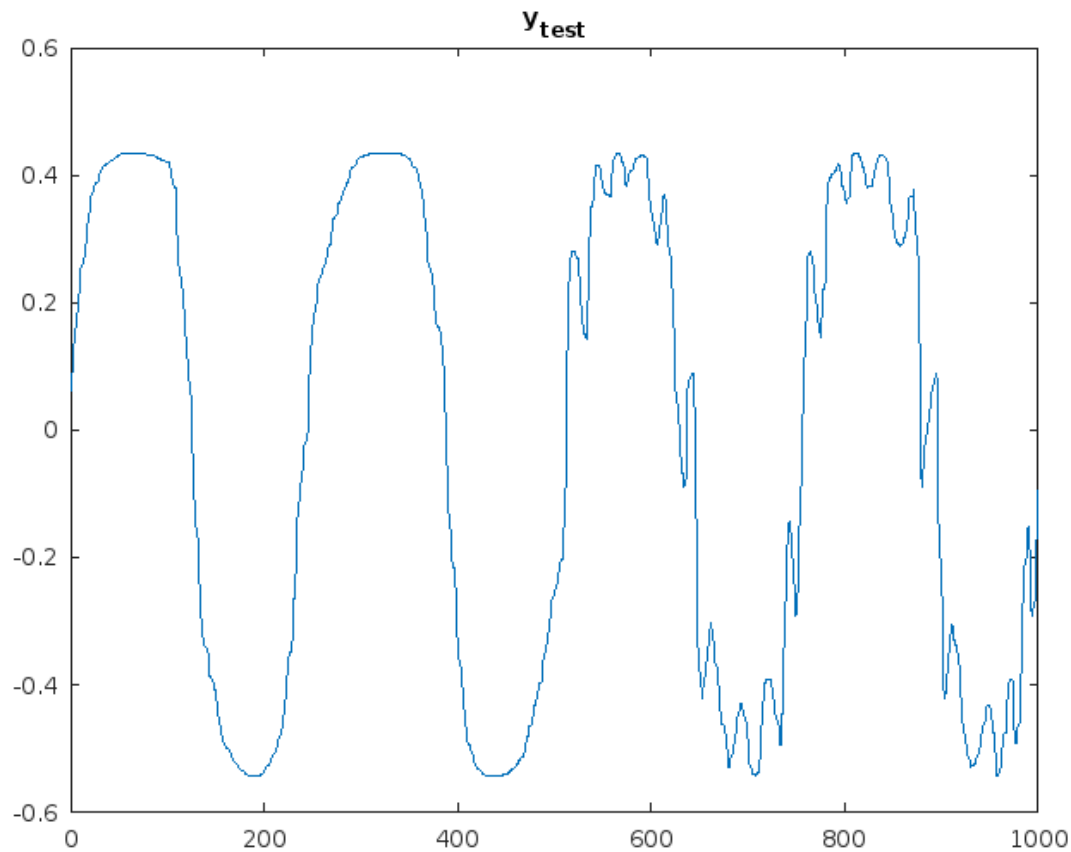




## QUESTÃO 3: Modelo de sistema dinâmico

```
%  
X_train = table2array(readtable('ex3_X_train.csv'));  
y_train = table2array(readtable('ex3_y_train.csv'));  
X_test = table2array(readtable('ex3_X_test.csv'));  
y_test = table2array(readtable('ex3_y_test.csv'));  
figure(fig_number)  
plot(y_train);  
title("y_{train}");  
drawnow();  
fig_number = fig_number + 1;  
figure(fig_number)  
plot(y_test);  
title("y_{test}");  
drawnow();  
fig_number = fig_number + 1;
```





## Generate FIS Using Grid Partitioning

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'GridPartition', 2);  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

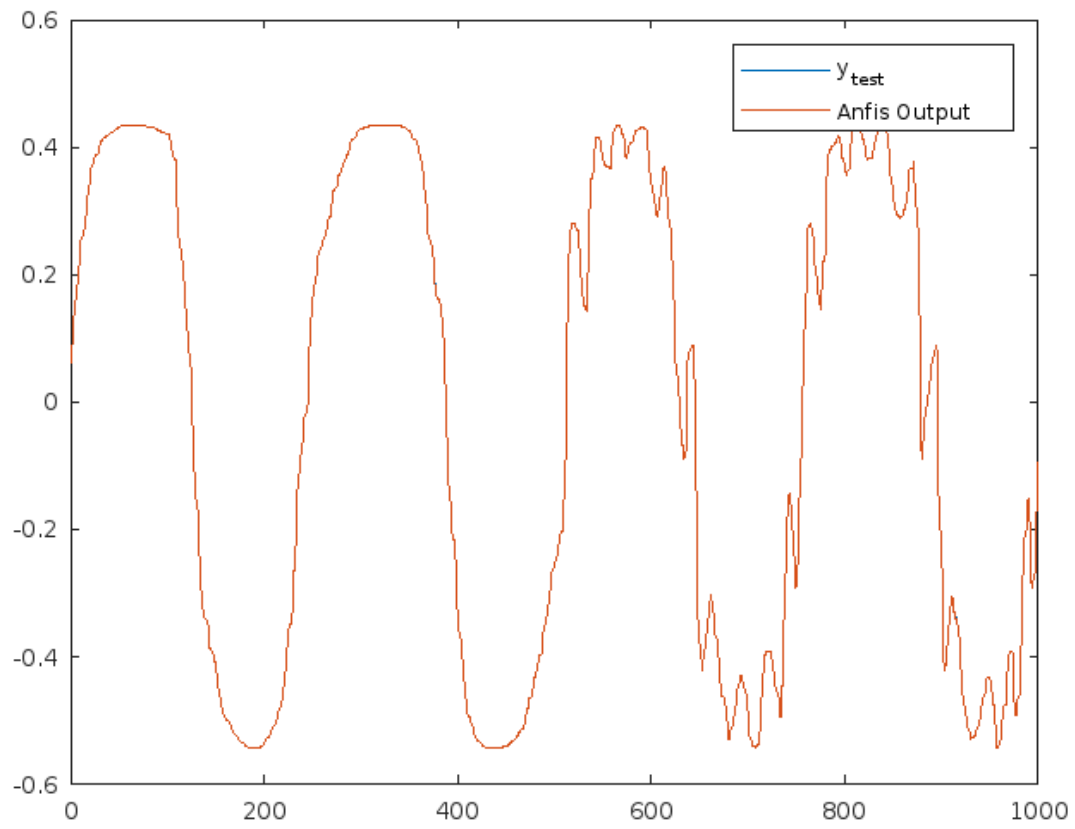
*ANFIS info:*

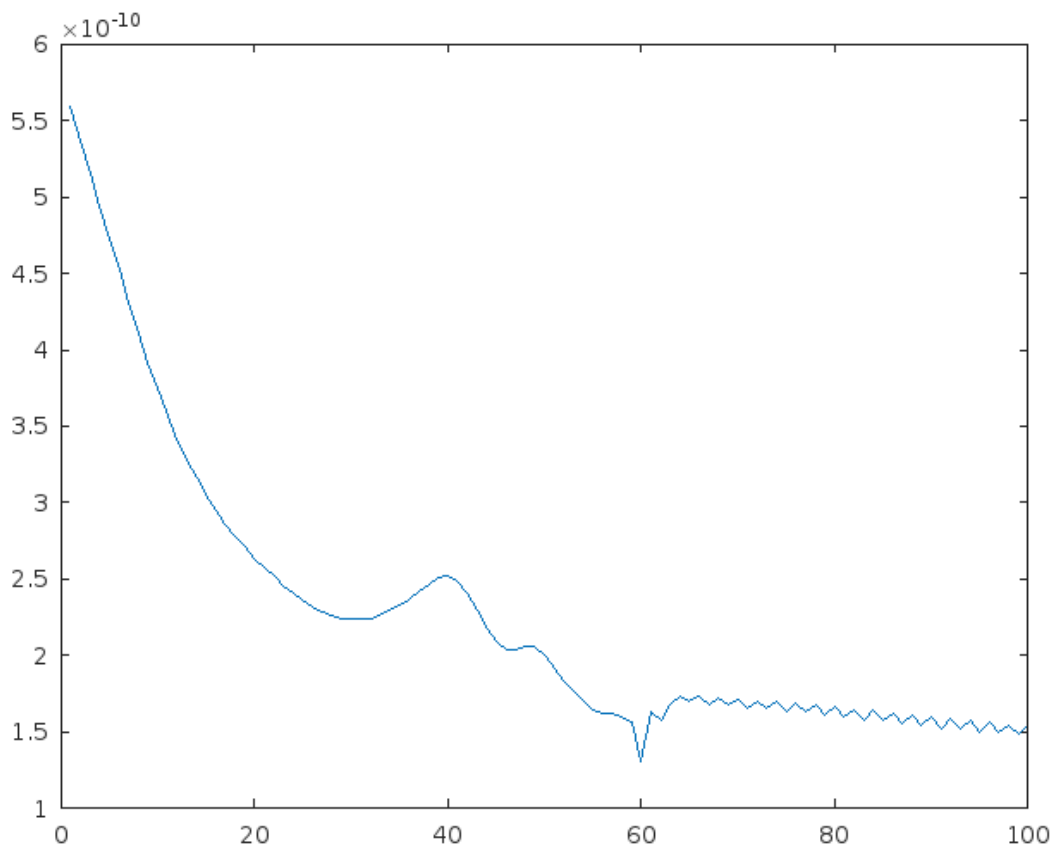
*Number of nodes: 92  
Number of linear parameters: 192  
Number of nonlinear parameters: 30  
Total number of parameters: 222  
Number of training data pairs: 5074  
Number of checking data pairs: 0*

*Number of fuzzy rules: 32*

*Minimal training RMSE = 1.13997e-05*

*MSE: 1.19E-10*





## Generate FIS Using Subtractive Clustering

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'SubtractiveClustering');  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

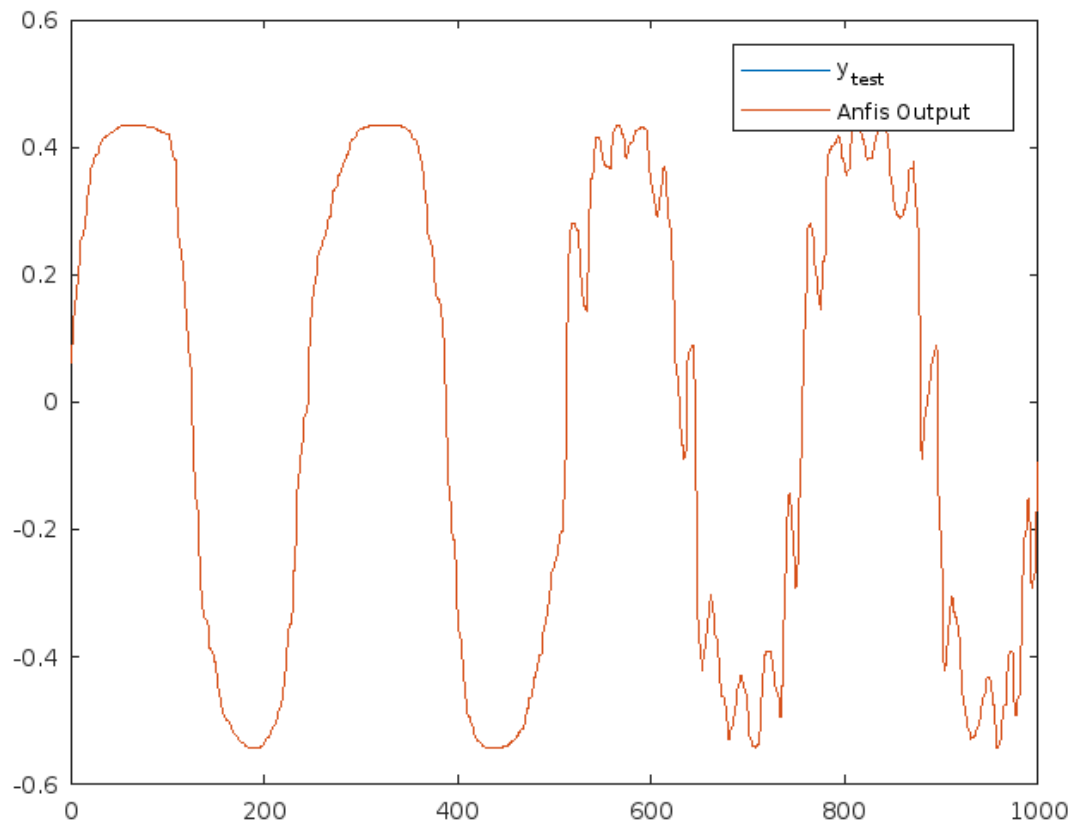
*ANFIS info:*

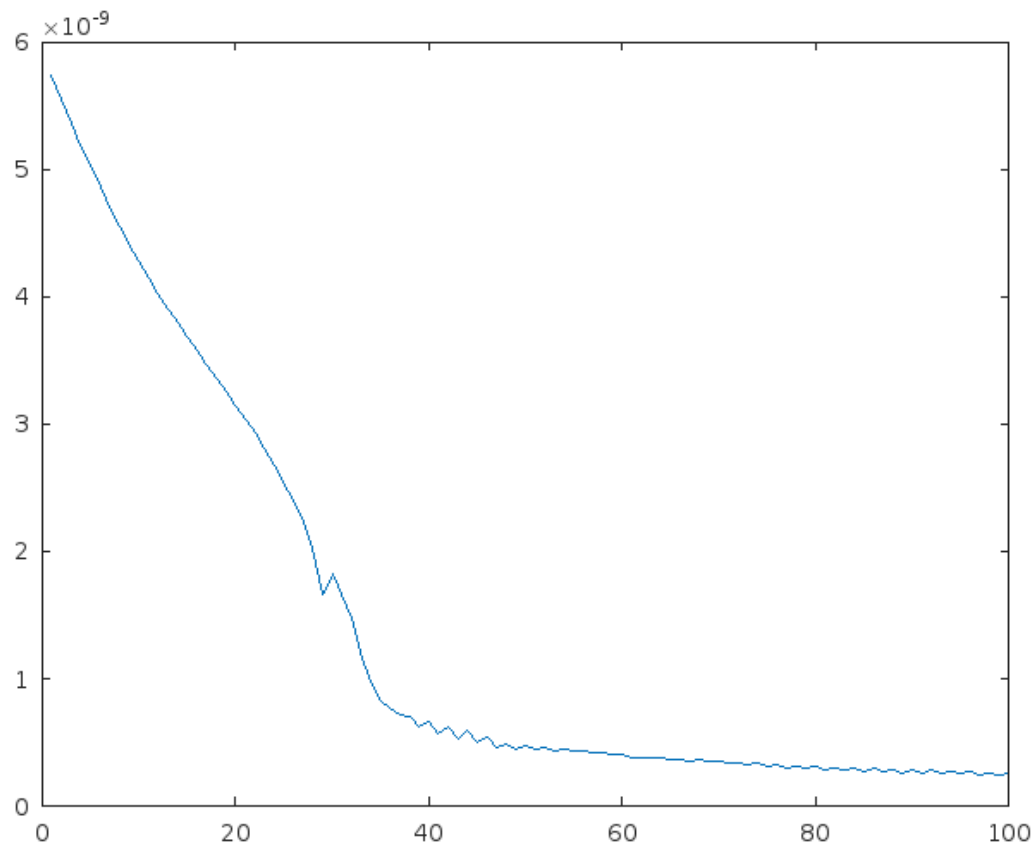
*Number of nodes: 68  
Number of linear parameters: 30  
Number of nonlinear parameters: 50  
Total number of parameters: 80  
Number of training data pairs: 5074  
Number of checking data pairs: 0*

*Number of fuzzy rules: 5*

*Minimal training RMSE = 1.57355e-05*

*MSE: 2.35E-10*





## Generate FIS Using FCM Clustering

```
[ys, ERROR] =run_anfis(X_train, y_train, X_test, 'FCMClustering');
figure(fig_number)
plot(y_test)
hold on
plot(ys)
legend('y_{test}','Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

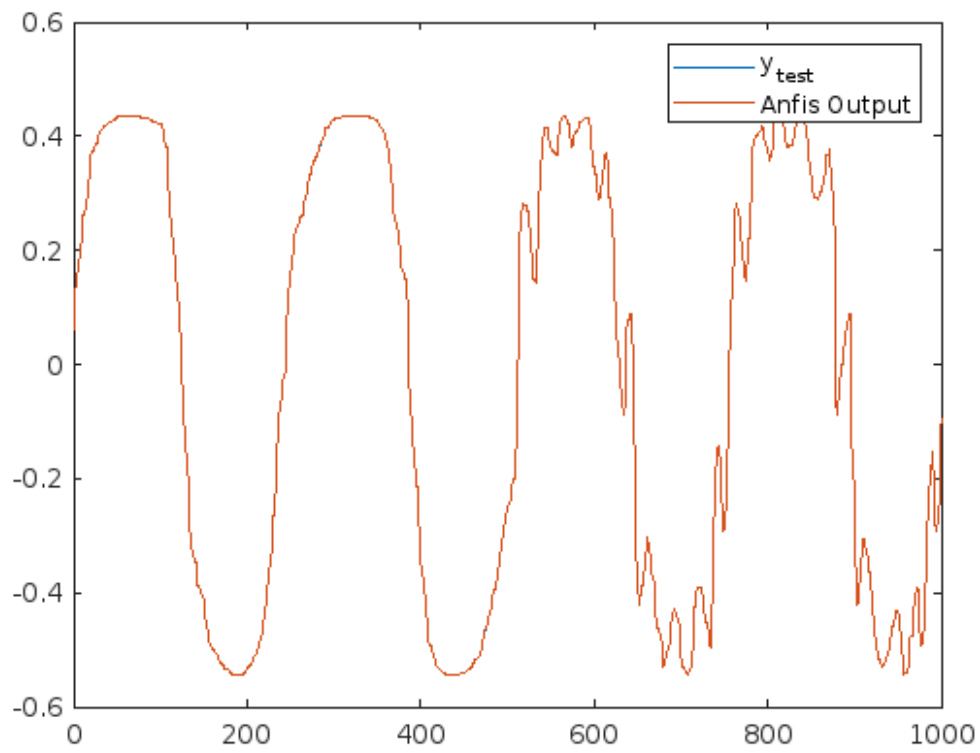
*ANFIS info:*

Number of nodes: 68  
Number of linear parameters: 30  
Number of nonlinear parameters: 50  
Total number of parameters: 80  
Number of training data pairs: 5074  
Number of checking data pairs: 0

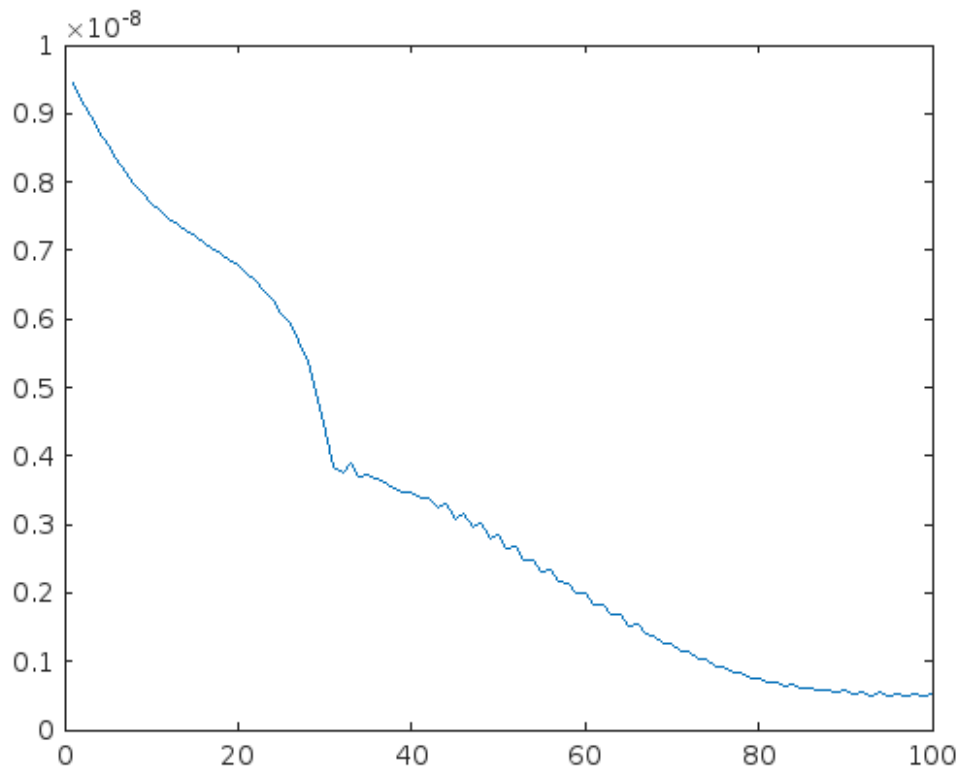
*Number of fuzzy rules: 5*

*Minimal training RMSE = 2.21524e-05*

*MSE: 4.83E-10*

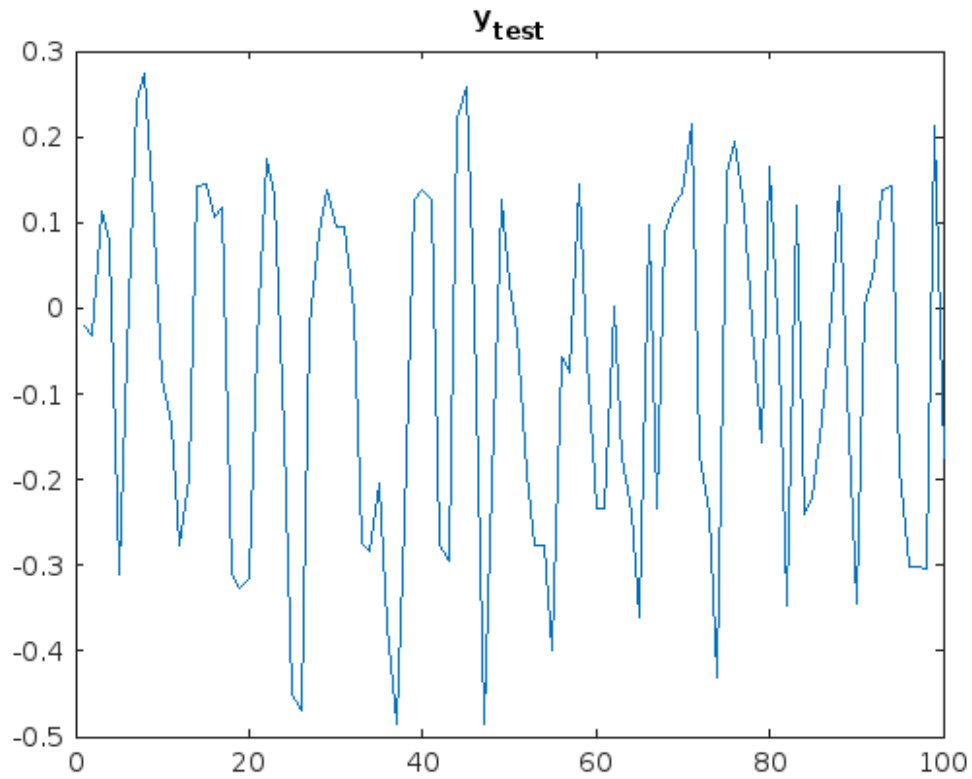
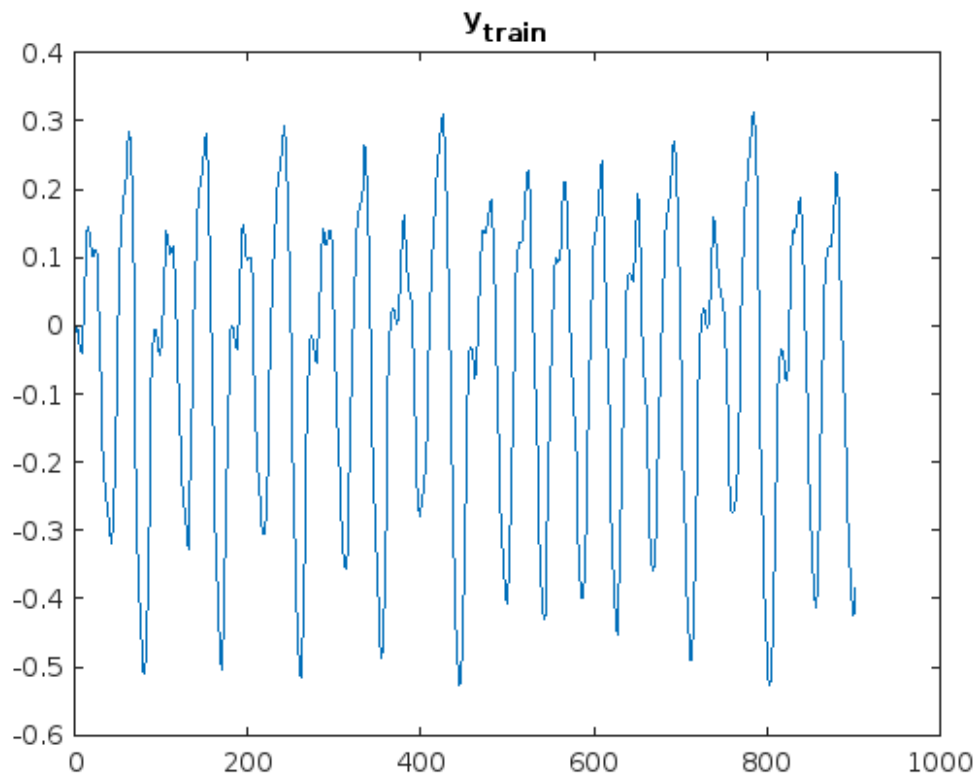






## QUESTÃO 4: Previsão de uma série temporal caótica

```
%  
X_train = table2array(readtable('ex4_X_train.csv'));  
y_train = table2array(readtable('ex4_y_train.csv'));  
X_test = table2array(readtable('ex4_X_test.csv'));  
y_test = table2array(readtable('ex4_y_test.csv'));  
figure(fig_number)  
plot(y_train);  
title("y_{train}");  
drawnow();  
fig_number = fig_number + 1;  
figure(fig_number)  
plot(y_test);  
title("y_{test}");  
drawnow();  
fig_number = fig_number + 1;
```



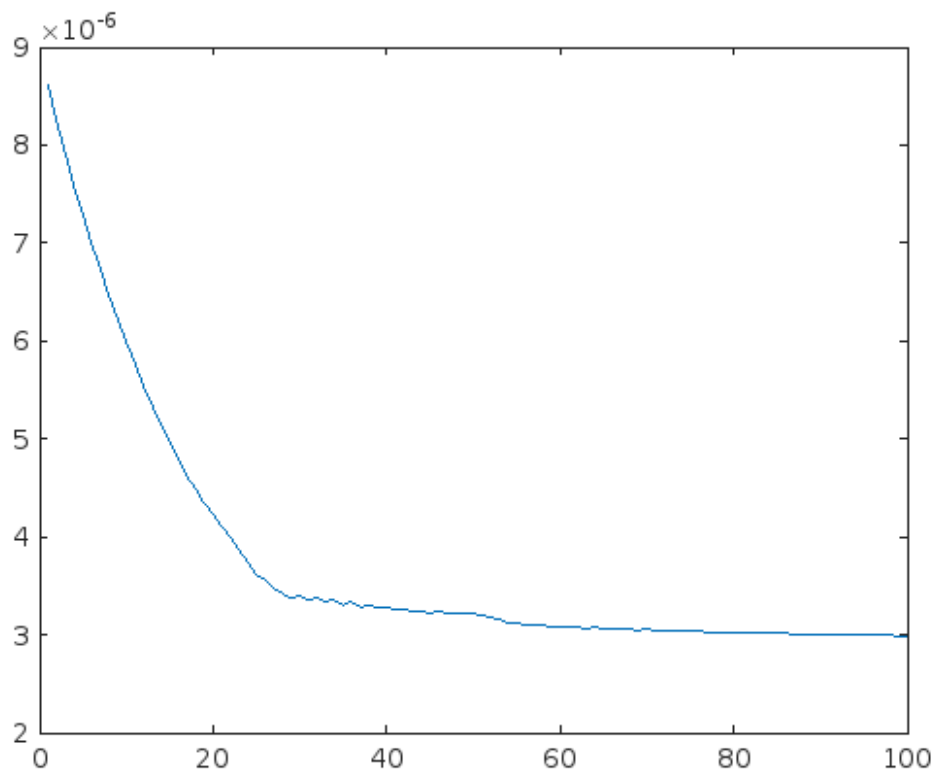
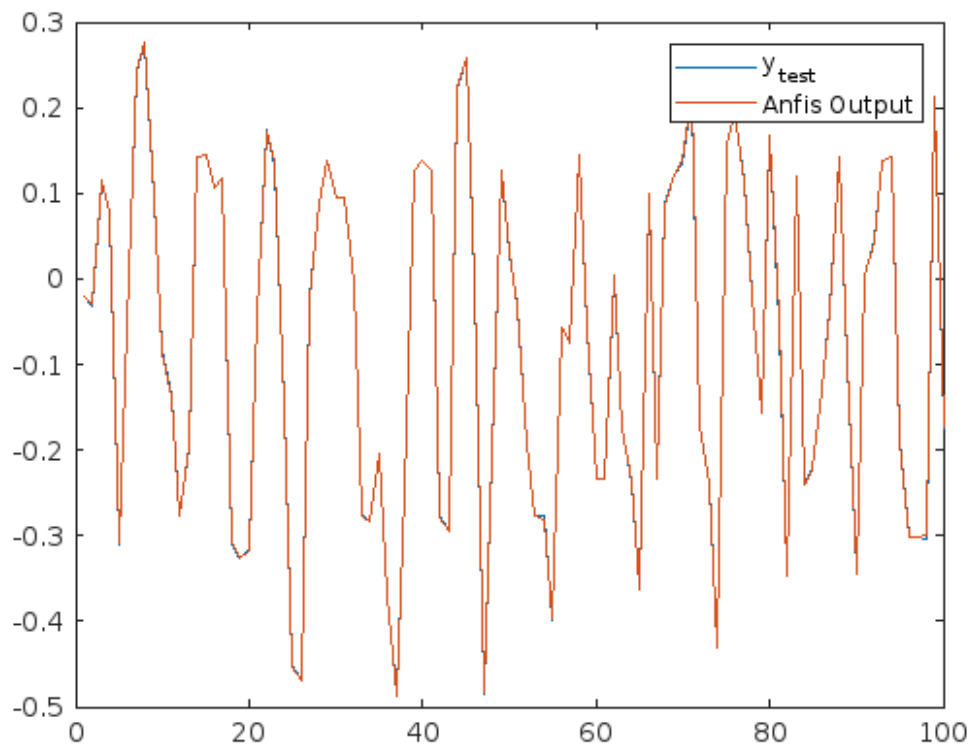
## Generate FIS Using Grid Partitioning

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'GridPartition', 2);
figure(fig_number)
plot(y_test)
hold on
plot(ys)
legend('y_{test}', 'Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

*ANFIS info:*

*Number of nodes: 55  
Number of linear parameters: 80  
Number of nonlinear parameters: 24  
Total number of parameters: 104  
Number of training data pairs: 903  
Number of checking data pairs: 0  
Number of fuzzy rules: 16*

*Minimal training RMSE = 0.00172881  
MSE: 2.15E-06*



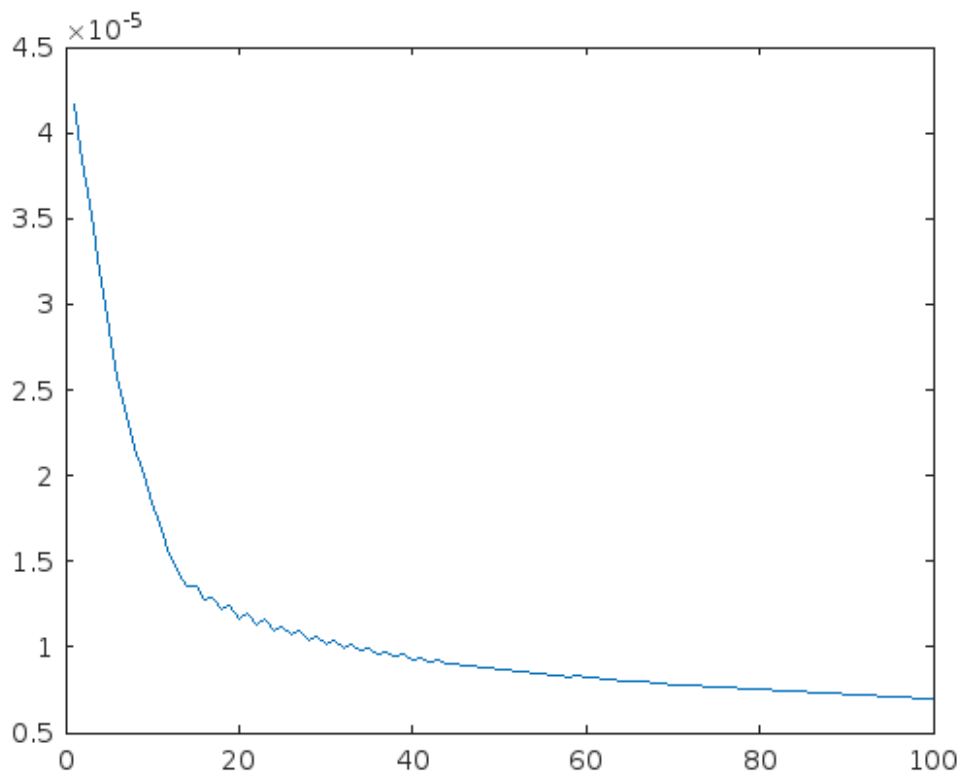
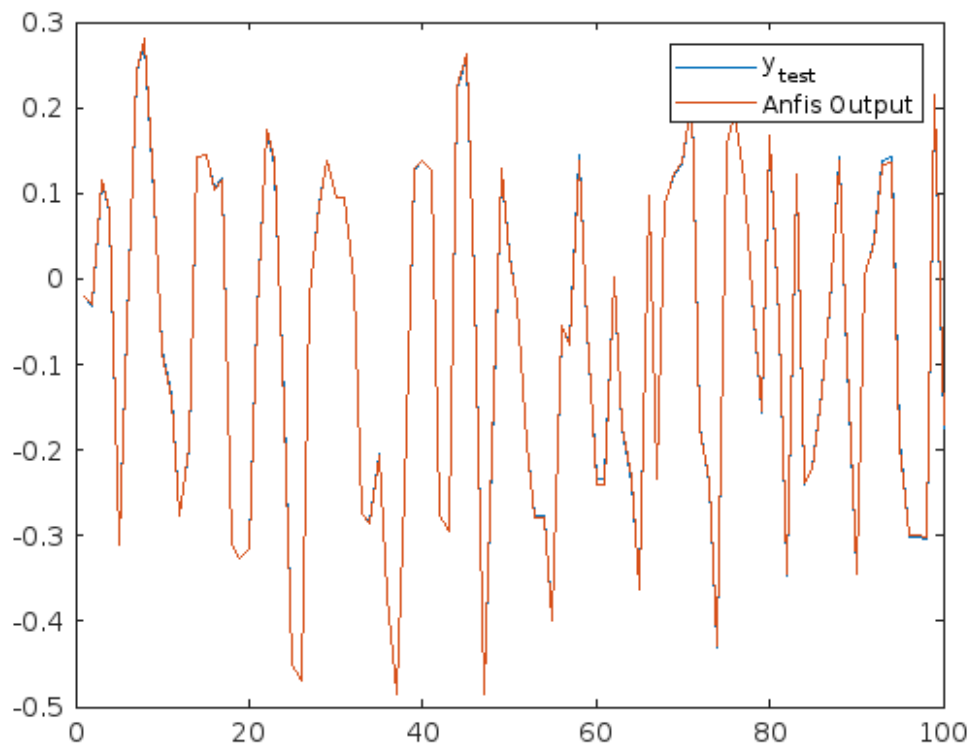
## Generate FIS Using Subtractive Clustering

```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'SubtractiveClustering');
figure(fig_number)
plot(y_test)
hold on
plot(ys)
legend('y_{test}', 'Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

*ANFIS info:*

*Number of nodes: 107*  
*Number of linear parameters: 50*  
*Number of nonlinear parameters: 80*  
*Total number of parameters: 130*  
*Number of training data pairs: 903*  
*Number of checking data pairs: 0*  
*Number of fuzzy rules: 10*

*Minimal training RMSE = 0.00264106*  
*MSE: 7.95E-06*



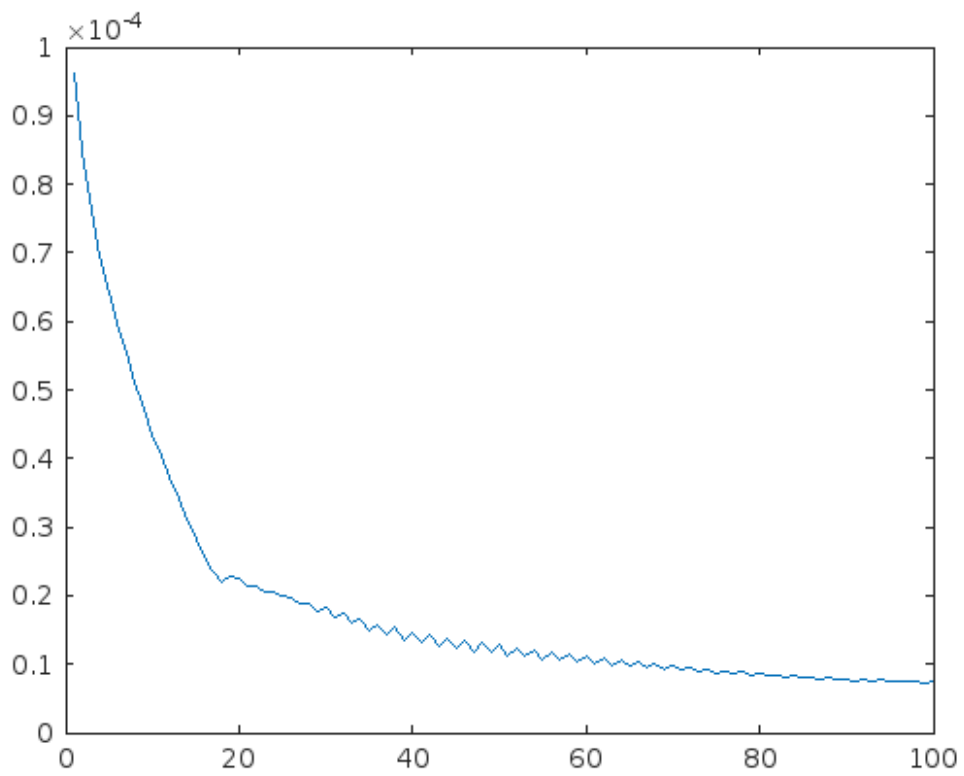
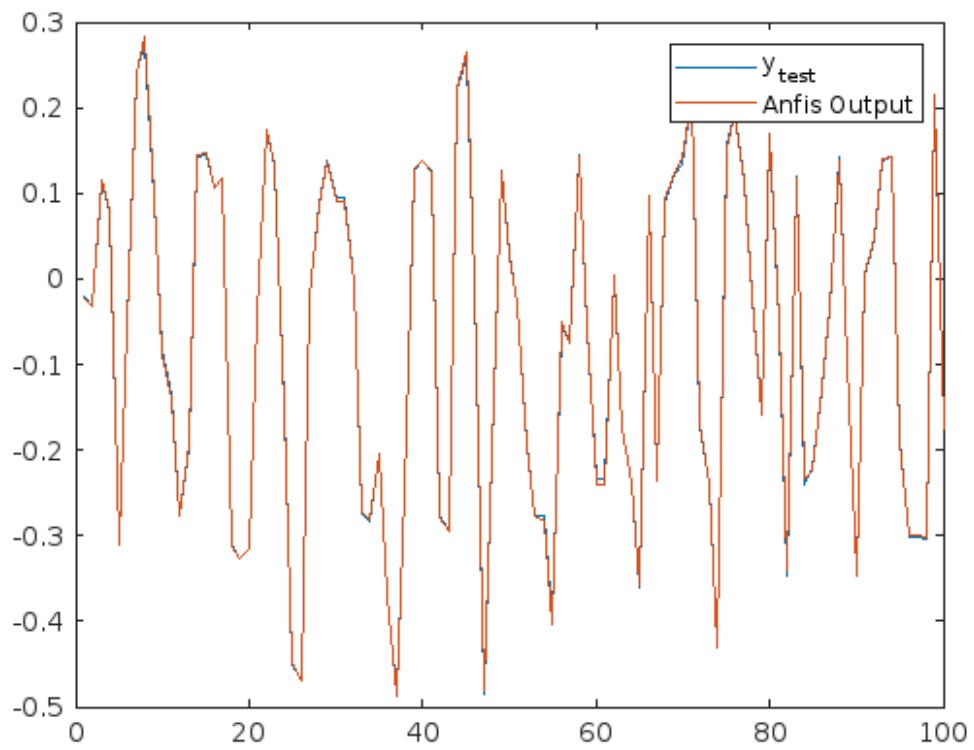
# Generate FIS Using FCM Clustering

```
[ys, ERROR] =run_anfis(X_train, y_train, X_test, 'FCMClustering');
figure(fig_number)
plot(y_test)
hold on
plot(ys)
legend('y_{test}', 'Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

*ANFIS info:*

*Number of nodes: 107*  
*Number of linear parameters: 50*  
*Number of nonlinear parameters: 80*  
*Total number of parameters: 130*  
*Number of training data pairs: 903*  
*Number of checking data pairs: 0*  
*Number of fuzzy rules: 10*

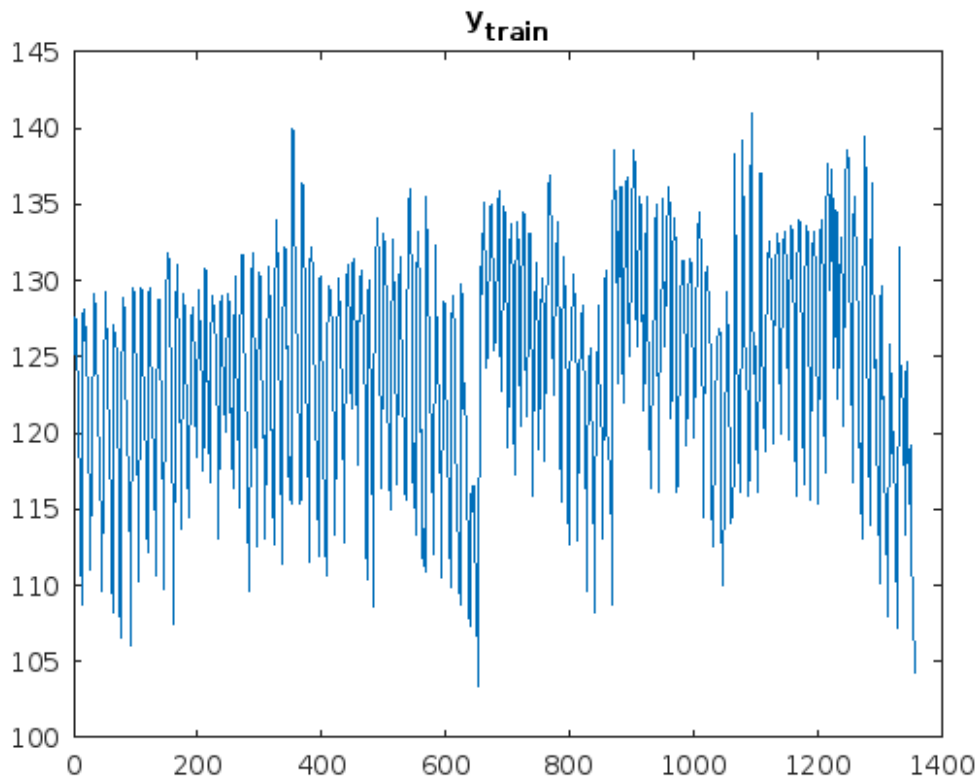
*Minimal training RMSE = 0.00270777*  
*MSE: 8.89E-06*

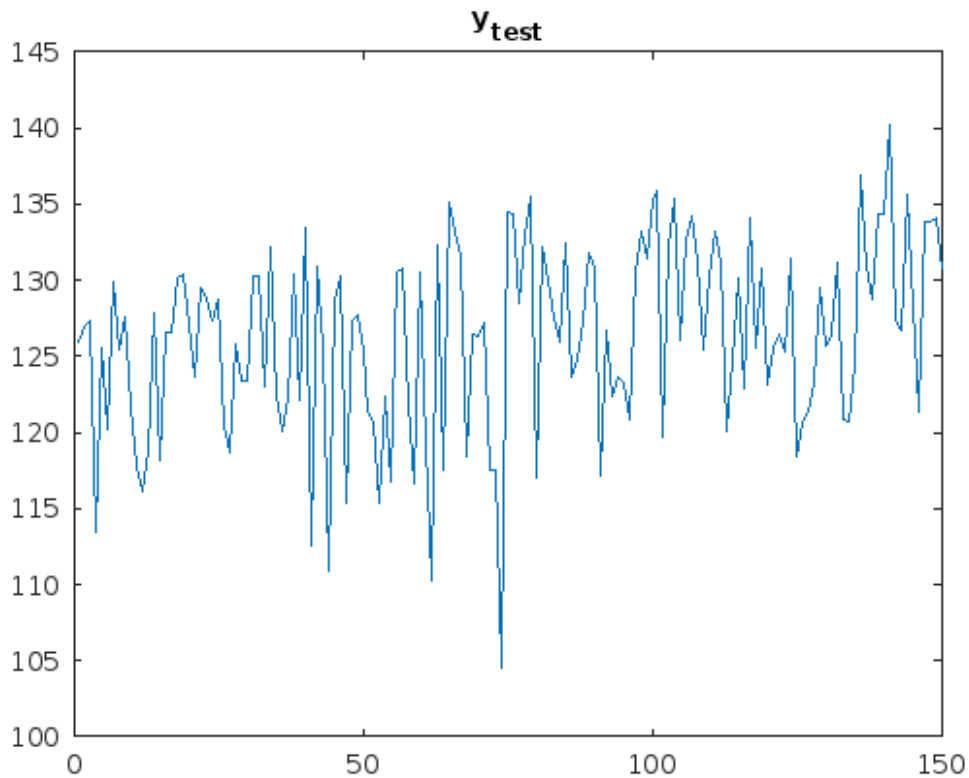




## QUESTÃO 5: Data set UCI

```
%  
X_train = table2array(readtable('ex5_X_train.csv'));  
y_train = table2array(readtable('ex5_y_train.csv'));  
X_test = table2array(readtable('ex5_X_test.csv'));  
y_test = table2array(readtable('ex5_y_test.csv'));  
figure(fig_number)  
plot(y_train);  
title("y_{train}");  
drawnow();  
fig_number = fig_number + 1;  
figure(fig_number)  
plot(y_test);  
title("y_{test}");  
drawnow();  
fig_number = fig_number + 1;
```





## Generate FIS Using Grid Partitioning

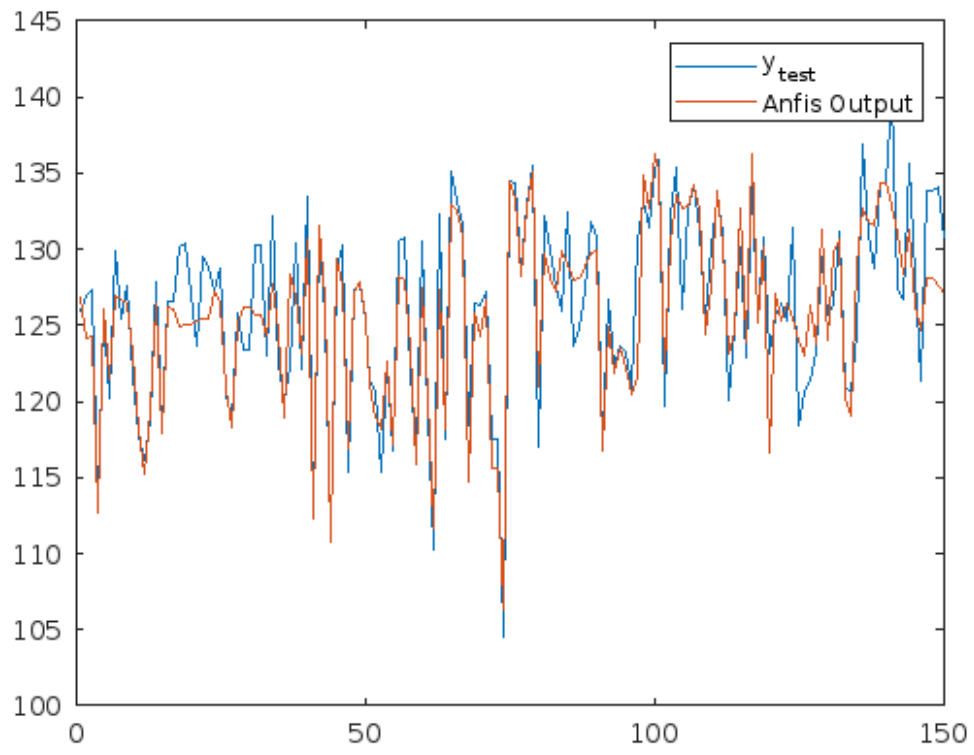
```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'GridPartition', 2);
figure(fig_number)
plot(y_test)
hold on
plot(ys)
legend('y_{test}', 'Anfis Output');
drawnow();
figure(fig_number+1)
plot(ERROR.^2)
drawnow();
fprintf('MSE: %.2E', immse(ys,y_test));
fig_number = fig_number + 2;
```

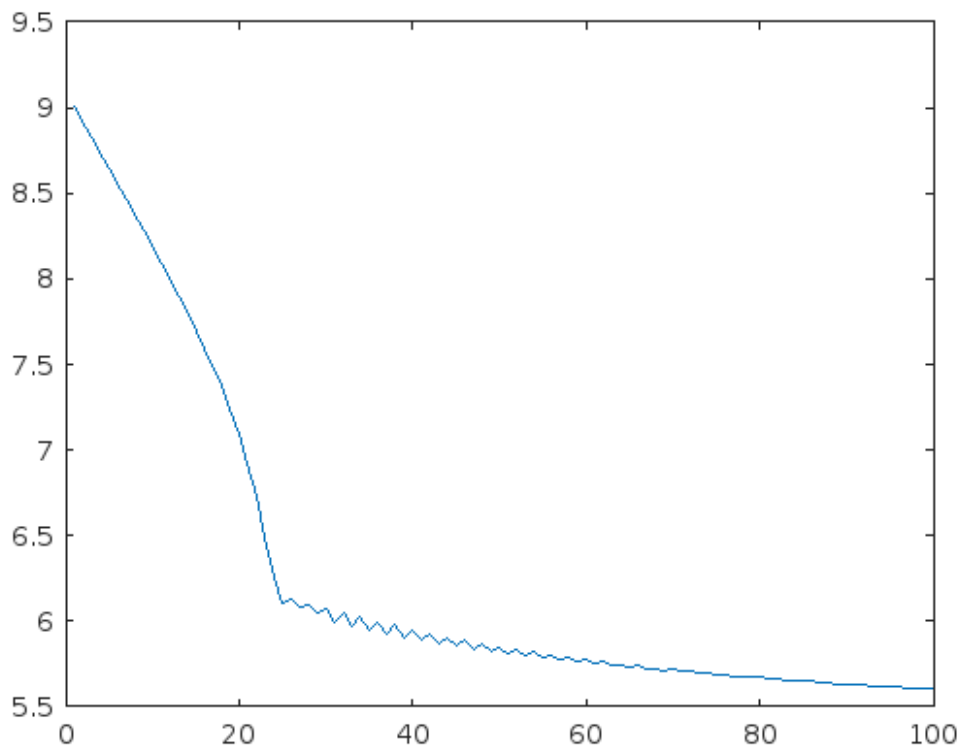
*ANFIS info:*

*Number of nodes: 92  
Number of linear parameters: 192  
Number of nonlinear parameters: 30  
Total number of parameters: 222  
Number of training data pairs: 1358  
Number of checking data pairs: 0  
Number of fuzzy rules: 32*

*Minimal training RMSE = 2.36704*

*MSE: 7.31E+00*





## Generate FIS Using Subtractive Clustering

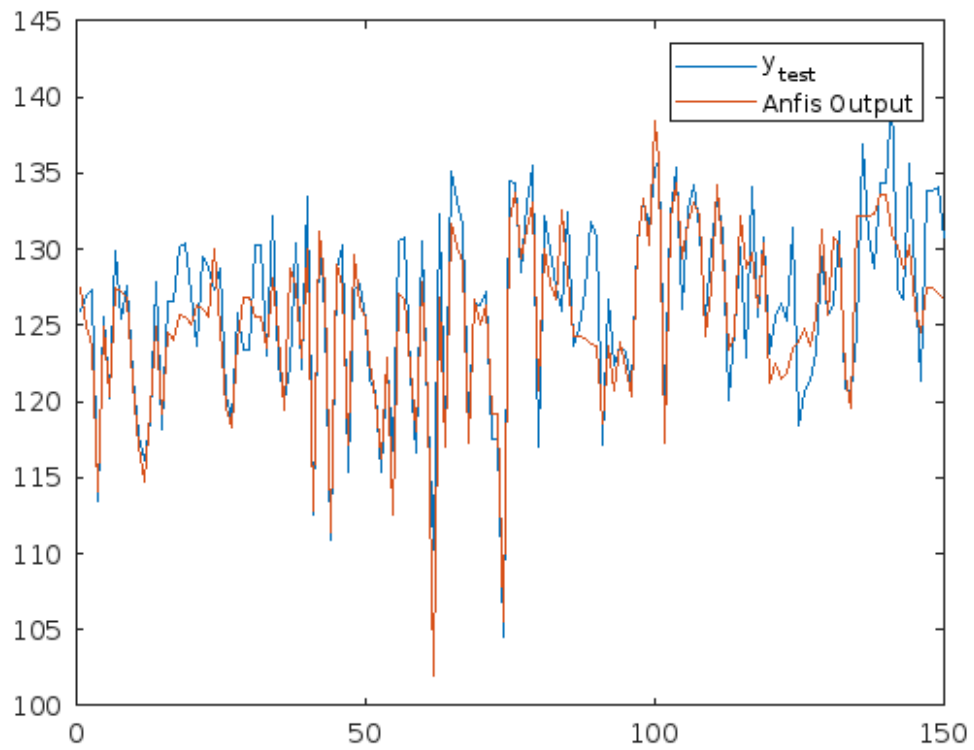
```
[ys, ERROR] = run_anfis(X_train, y_train, X_test, 'SubtractiveClustering');  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

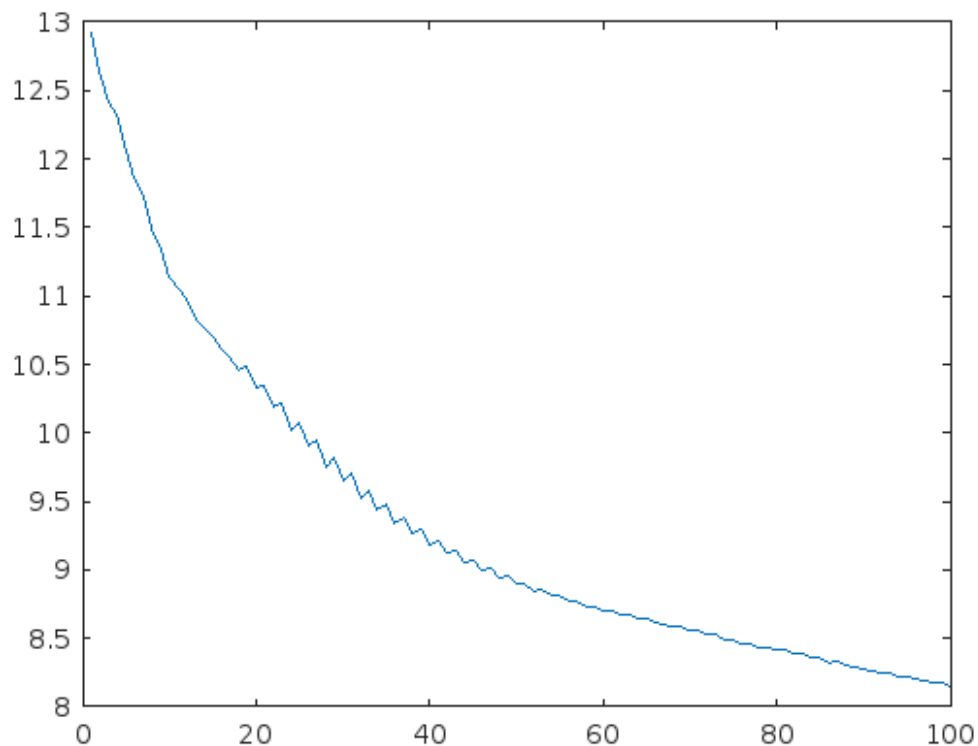
*ANFIS info:*

*Number of nodes: 200  
Number of linear parameters: 96  
Number of nonlinear parameters: 160  
Total number of parameters: 256  
Number of training data pairs: 1358  
Number of checking data pairs: 0  
Number of fuzzy rules: 16*

*Minimal training RMSE = 2.85522*

*MSE: 9.74E+00*





## Generate FIS Using FCM Clustering

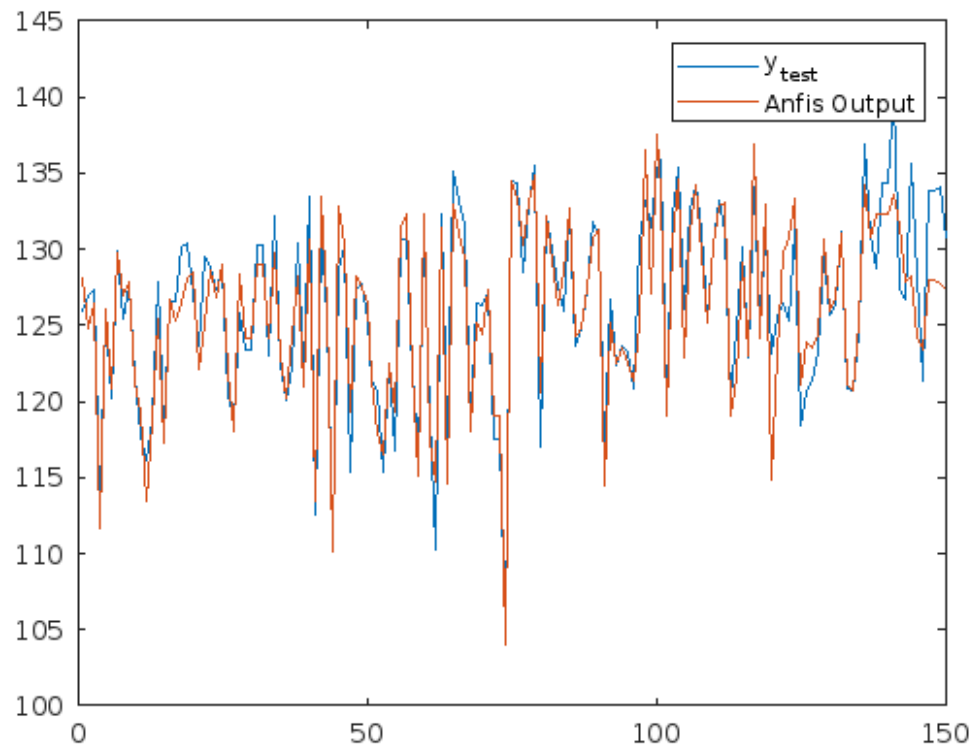
```
[ys, ERROR] =run_anfis(X_train, y_train, X_test, 'FCMClustering');  
figure(fig_number)  
plot(y_test)  
hold on  
plot(ys)  
legend('y_{test}', 'Anfis Output');  
drawnow();  
figure(fig_number+1)  
plot(ERROR.^2)  
drawnow();  
fprintf('MSE: %.2E', immse(ys,y_test));  
fig_number = fig_number + 2;
```

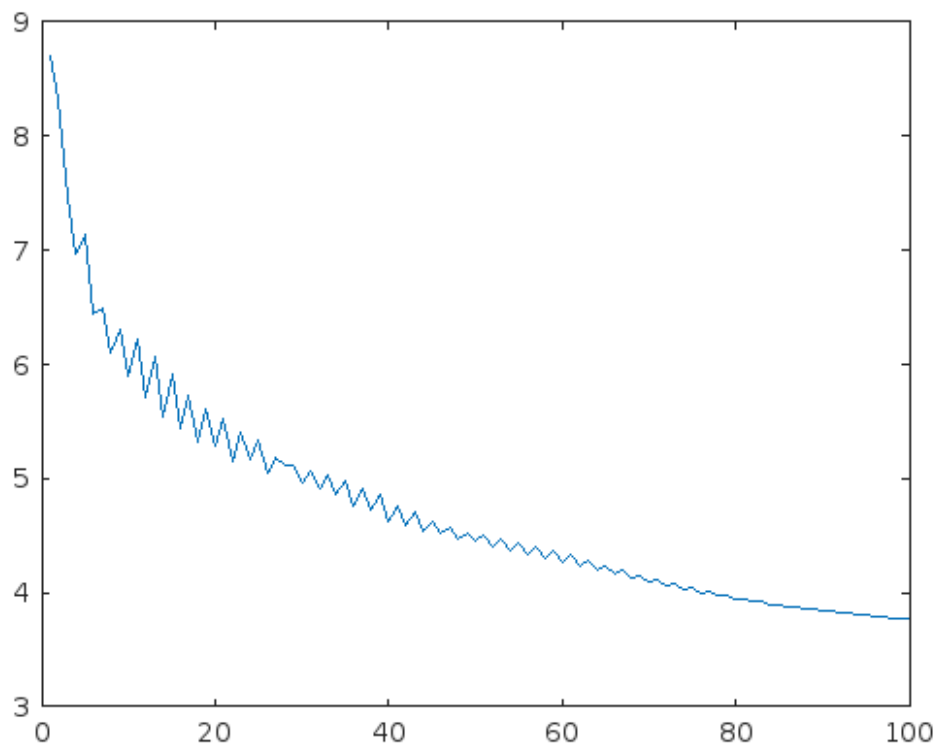
*ANFIS info:*

*Number of nodes: 200  
Number of linear parameters: 96  
Number of nonlinear parameters: 160  
Total number of parameters: 256  
Number of training data pairs: 1358  
Number of checking data pairs: 0  
Number of fuzzy rules: 16*

*Minimal training RMSE = 1.94068*

*MSE: 5.54E+00*





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