

Dynamic Tensor Rematerialization

Presenter: Steven Lyubomirsky*

Marisa Kirisame* Altan Haan* Jennifer Brennan Mike He

Jared Roesch Tianqi Chen Zachary Tatlock

*Equal contribution



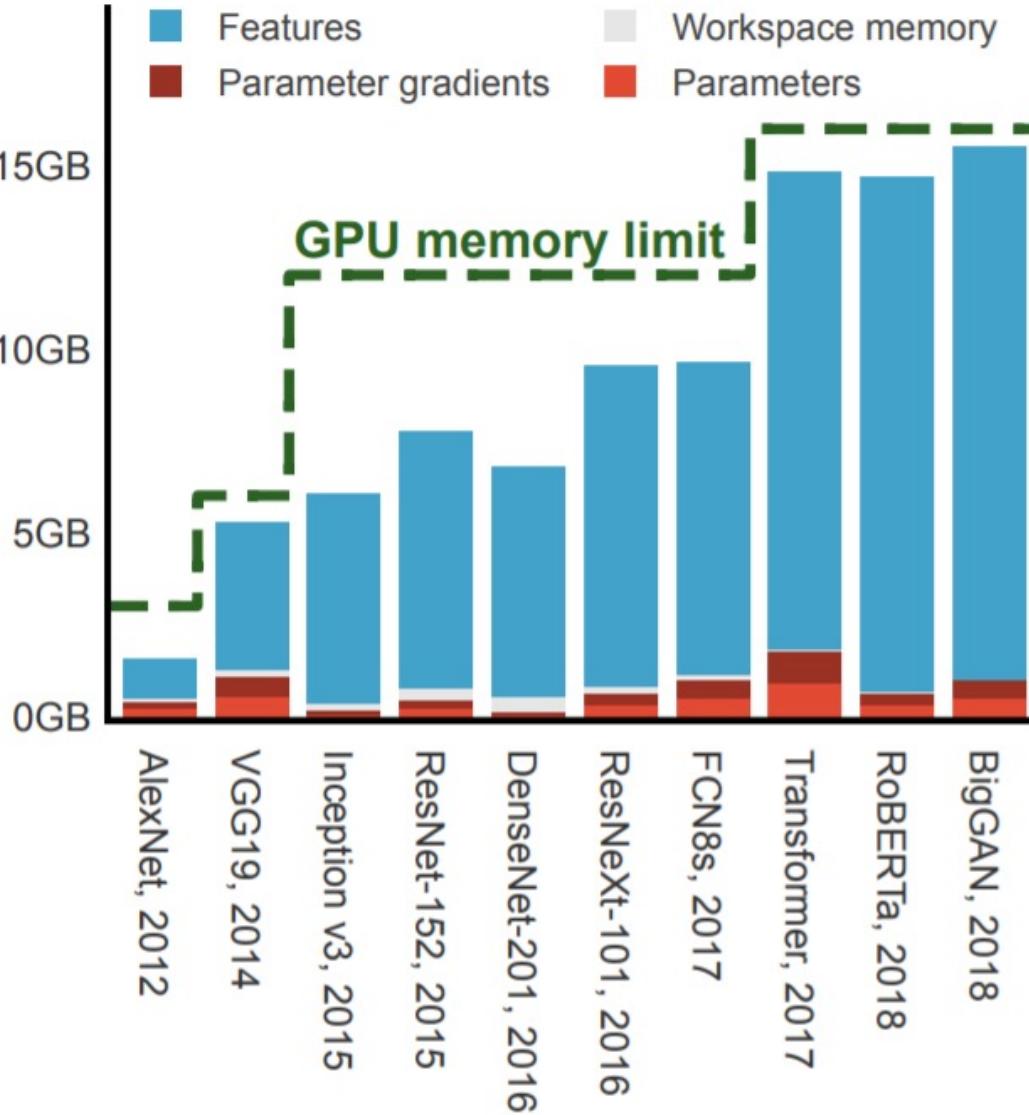
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sampl



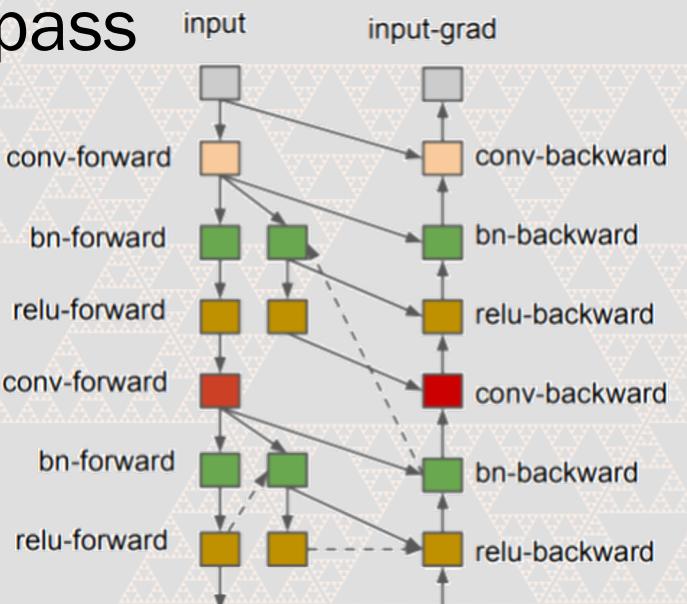
Total memory consumed



Jain et al., “Checkmate: Breaking the Memory Wall With Optimal Tensor Rematerialization” (2020)

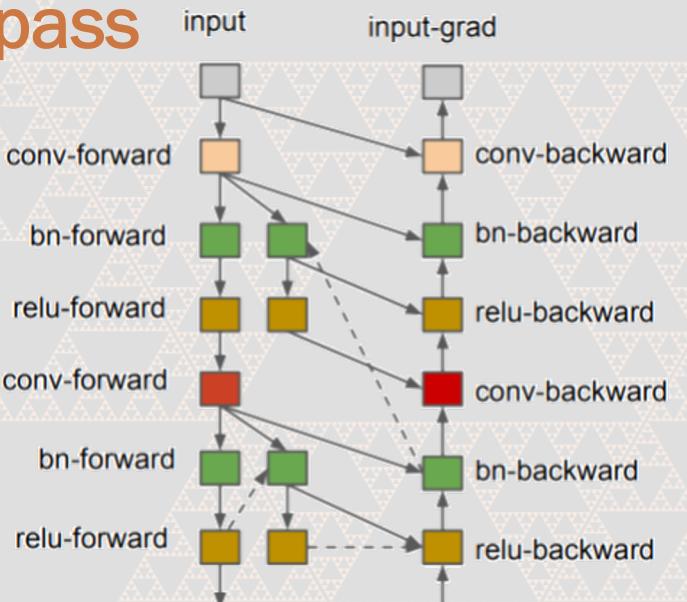
Checkpointing: Trade Time for Space

- Recompute activations instead of storing them
- Gradient Checkpointing, Chen et al. (2016)
 - Pick segments to recompute in backward pass
 - $O(\sqrt{N})$ memory for $O(N)$ extra ops
 - Many later segmenting approaches
- Checkmate, Jain et al. (2020)
 - Rematerialize individual values
 - ILP for optimal(!) planning



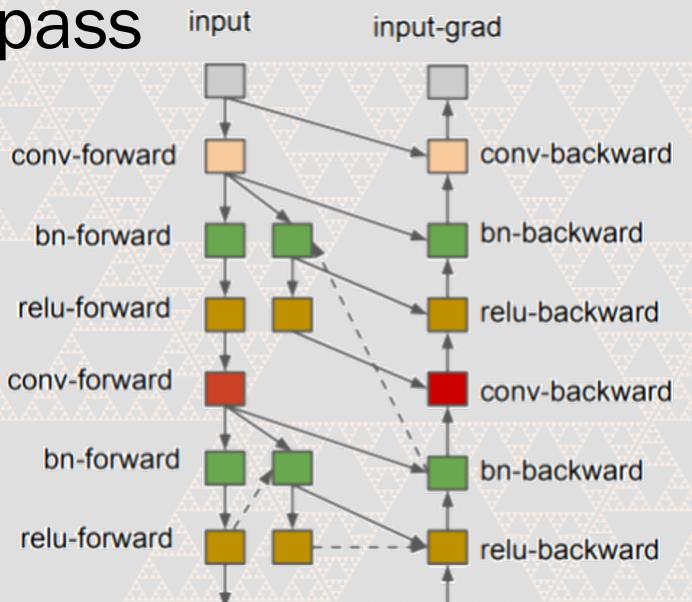
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Static Planning is Unnecessary

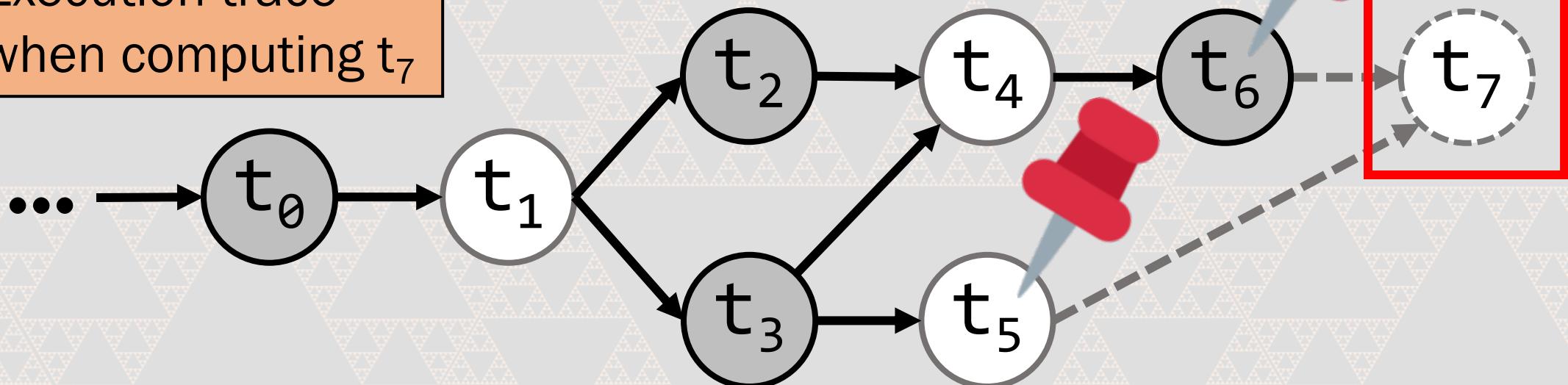
- Past approaches plan checkpoints in advance
- Require static knowledge of the model
- Planning can be expensive, limits applications
- Our contributions:
 - *Static planning is unnecessary for checkpointing*
 - Still achieve good compute-memory tradeoffs

Dynamic Tensor Rematerialization

- Cache-like approach: A runtime system
 - No static information necessary
 - Greedily allocate, evict and recompute as needed
 - Collects metadata to guide heuristics
 - Operates at a high level of abstraction
- Still competitive with static planning!

Rematerializing on the Fly

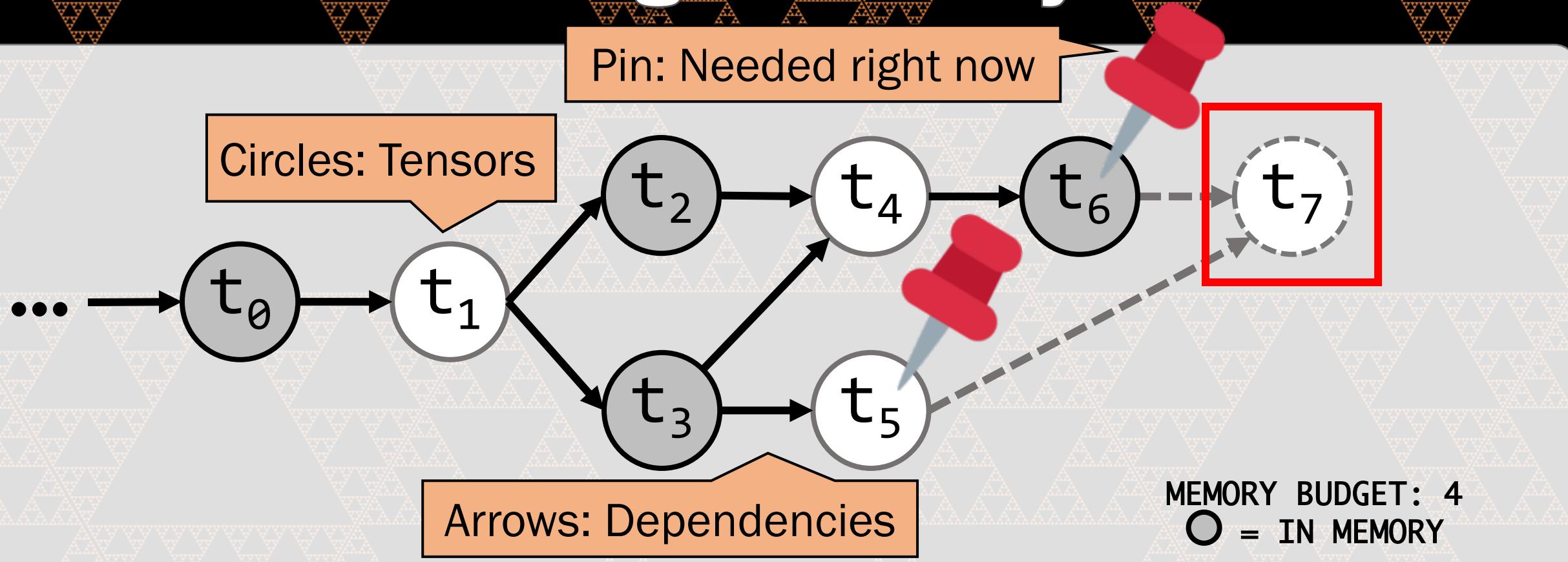
Execution trace
when computing t_7



MEMORY BUDGET: 4
○ = IN MEMORY

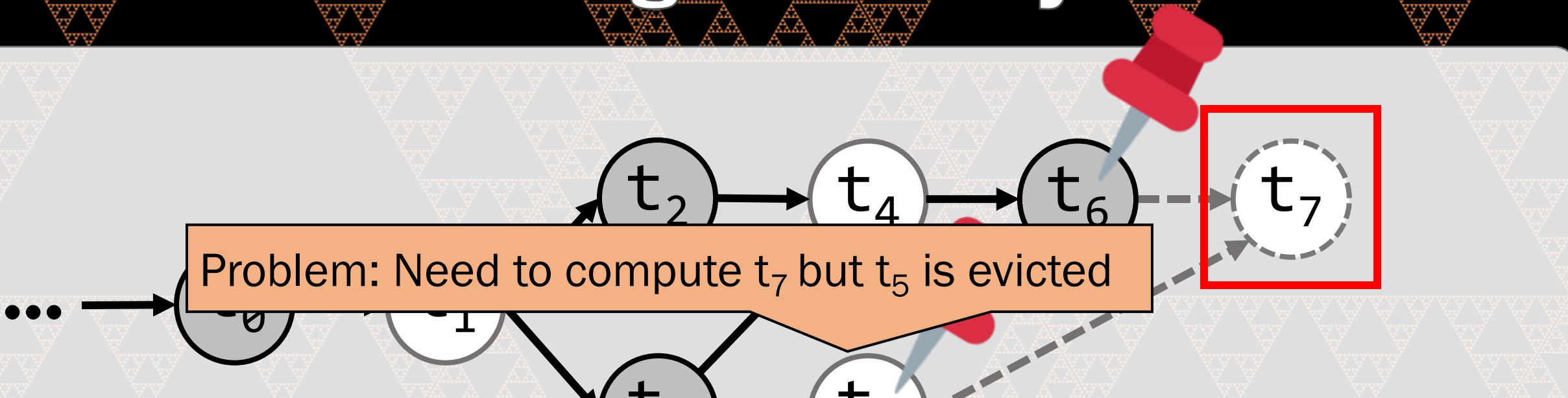
Current operation: PerformOp(op₇, [t₅, t₆])

Rematerializing on the Fly



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Rematerializing on the Fly

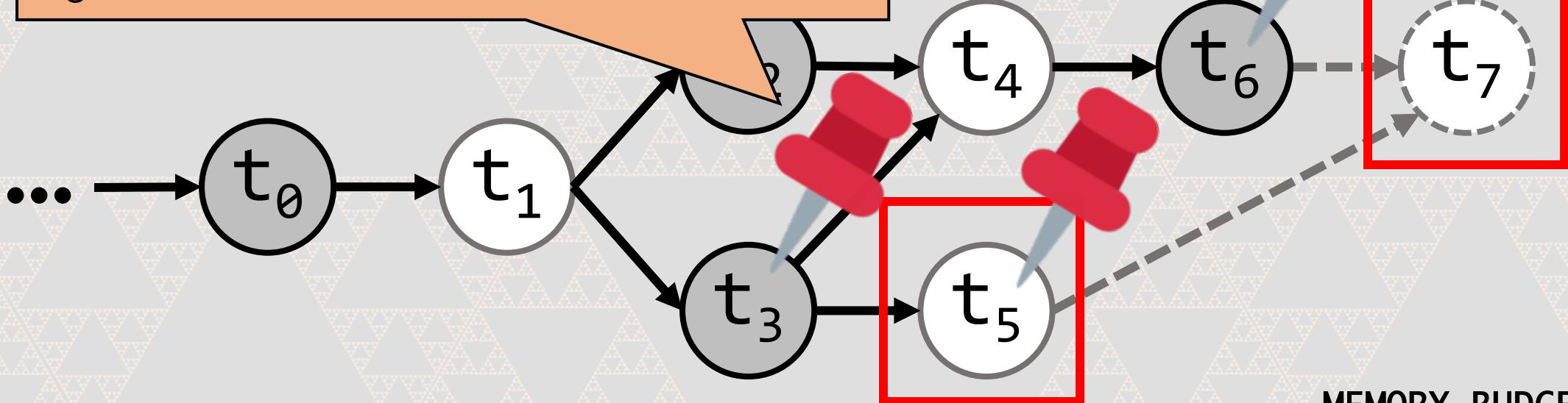


MEMORY BUDGET: 4
○ = IN MEMORY

Current operation: Rematerialize(t_5)

Rematerializing on the Fly

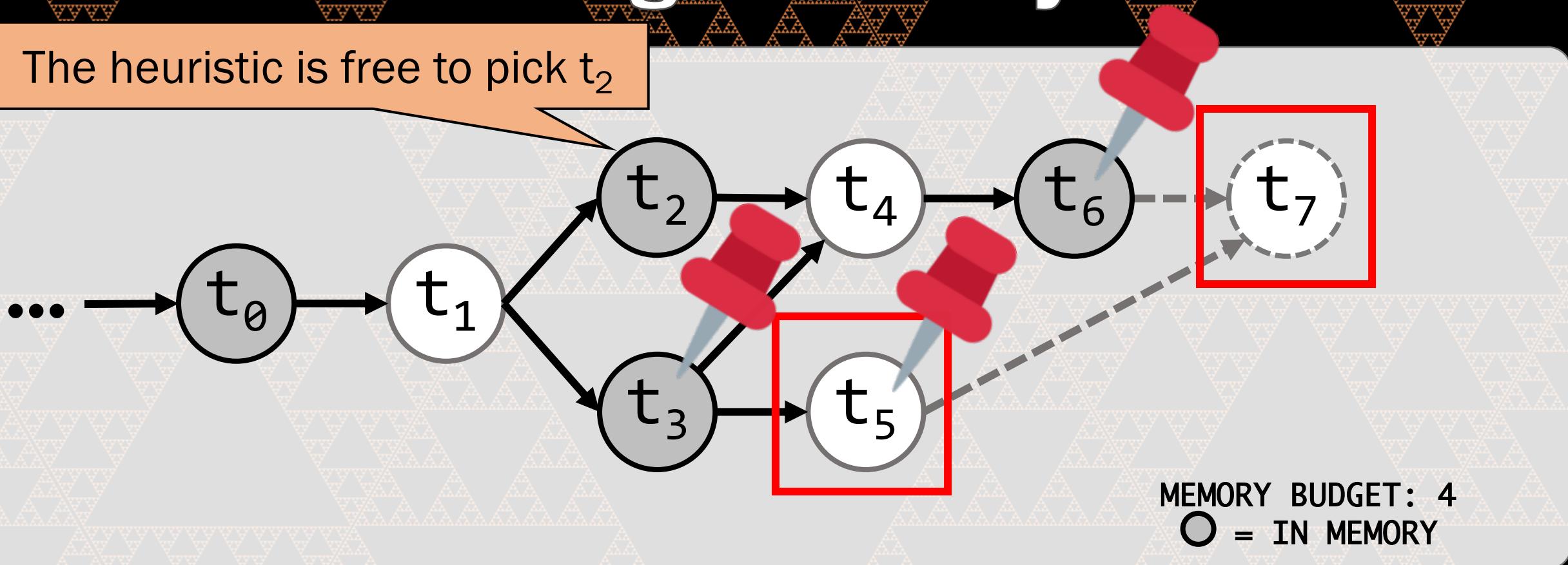
t_3 is present, but no room for result



Current operation: PerformOp(op₅, [t₃])

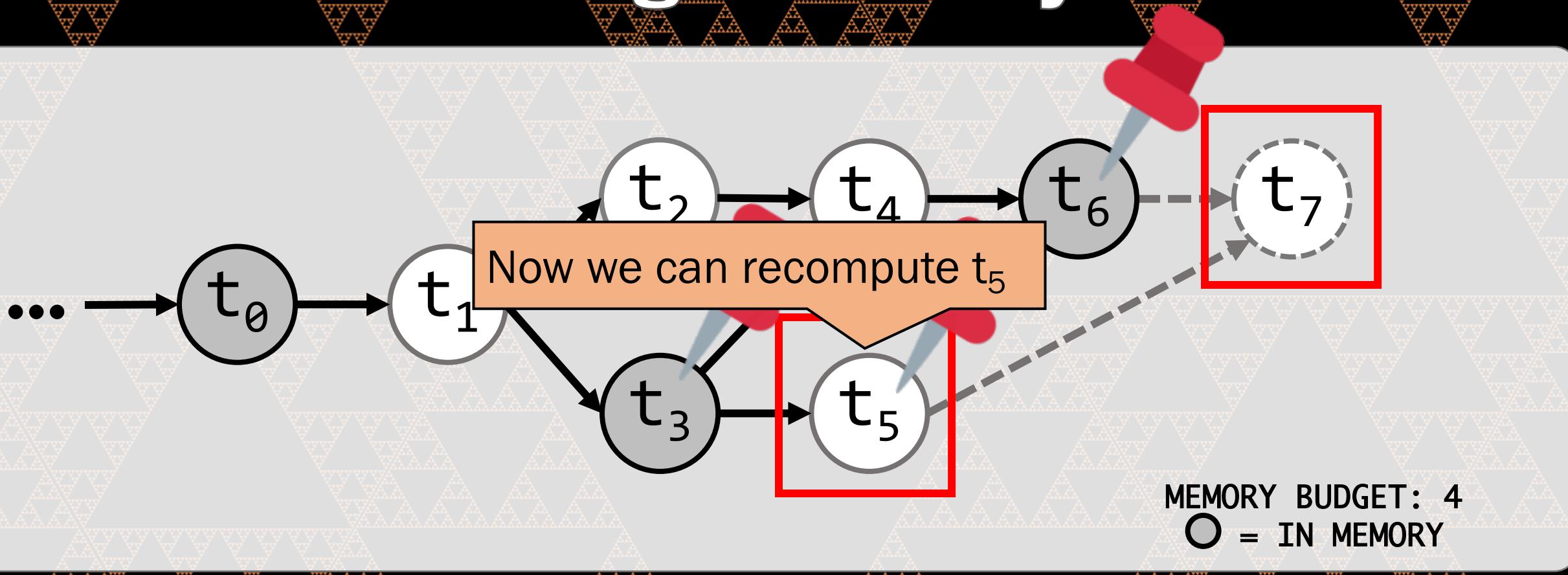
Rematerializing on the Fly

The heuristic is free to pick t_2



Current operation: PerformEviction()

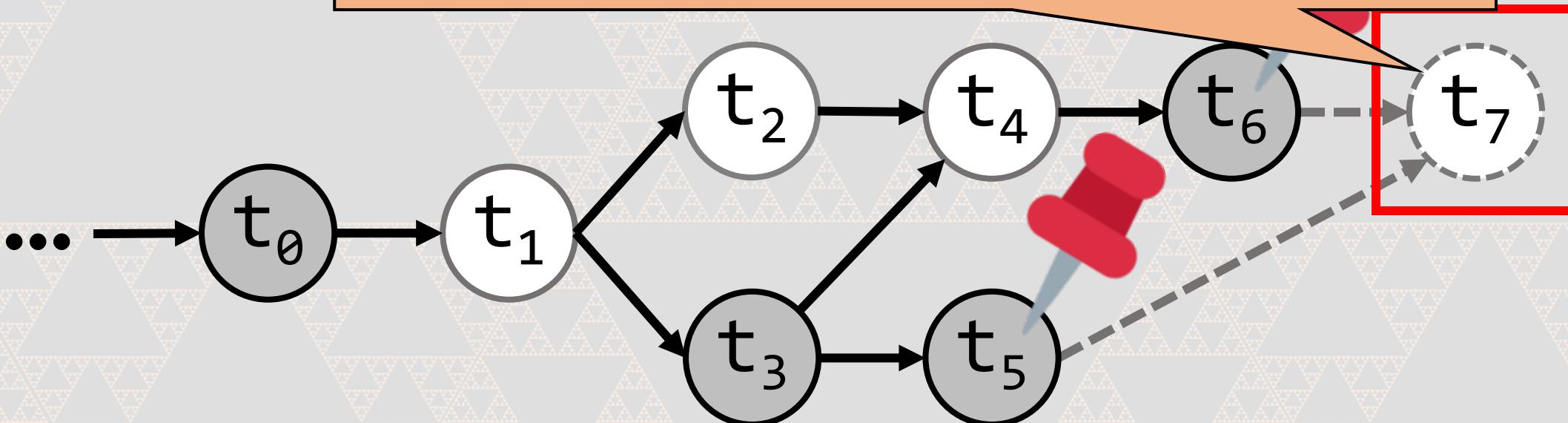
Rematerializing on the Fly



Current operation: `AllocateBuffer(t_5 .size); op5(t_3)`

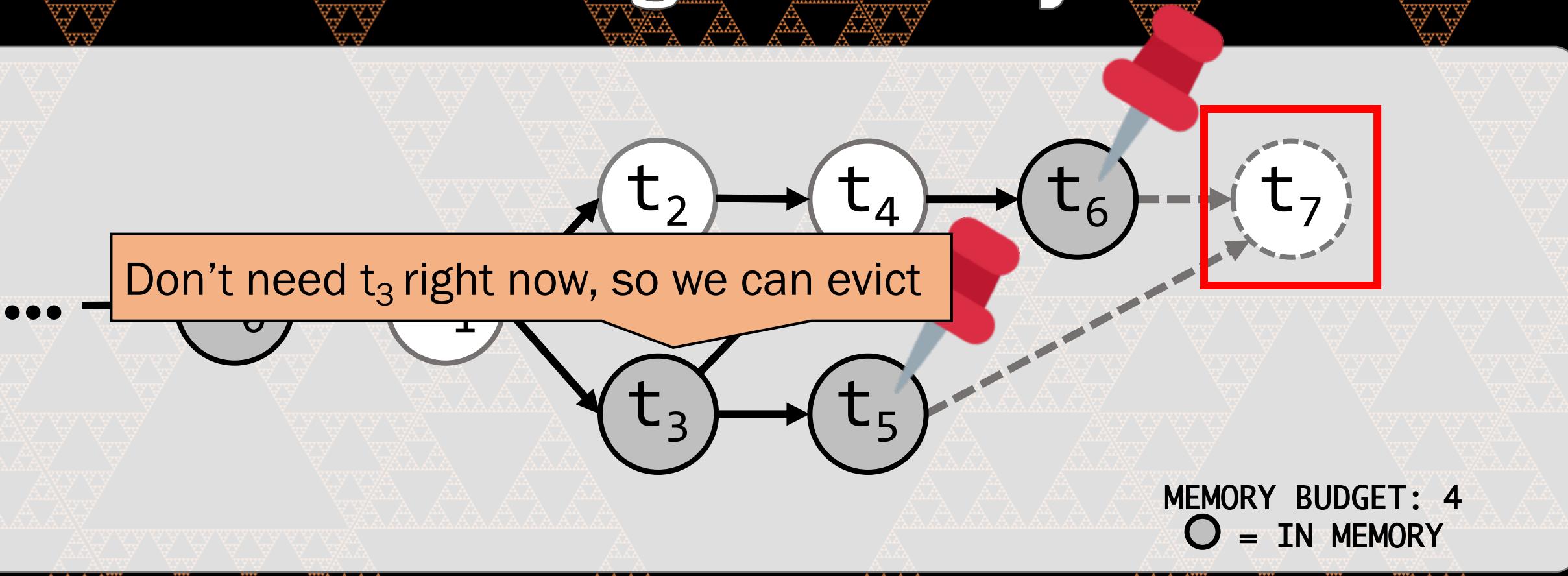
Rematerializing on the Fly

Our arguments are back—but still no room for t_7 !



Current operation: `AllocateBuffer(t7.size)`

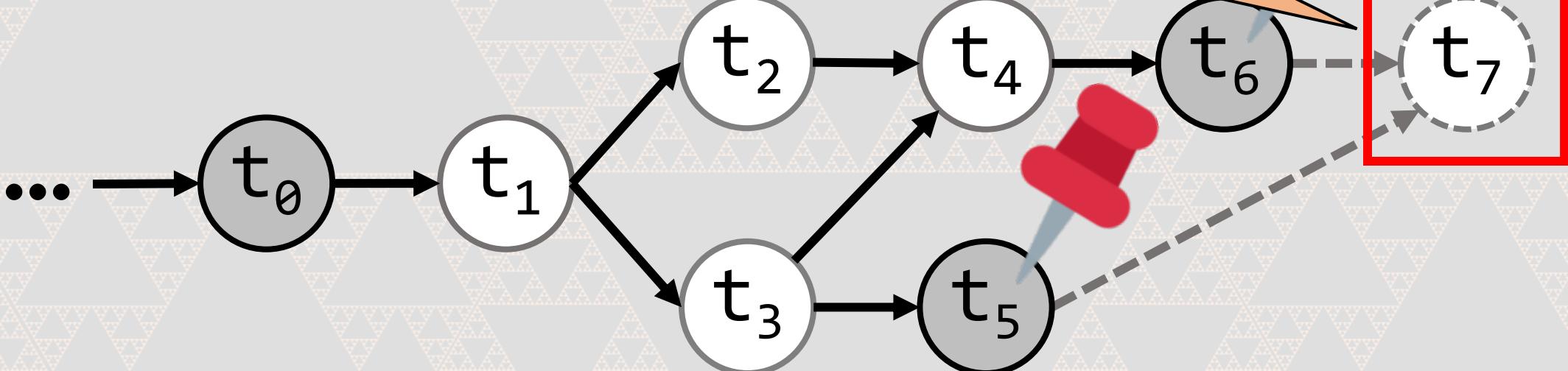
Rematerializing on the Fly



Current operation: PerformEviction()

Rematerializing on the Fly

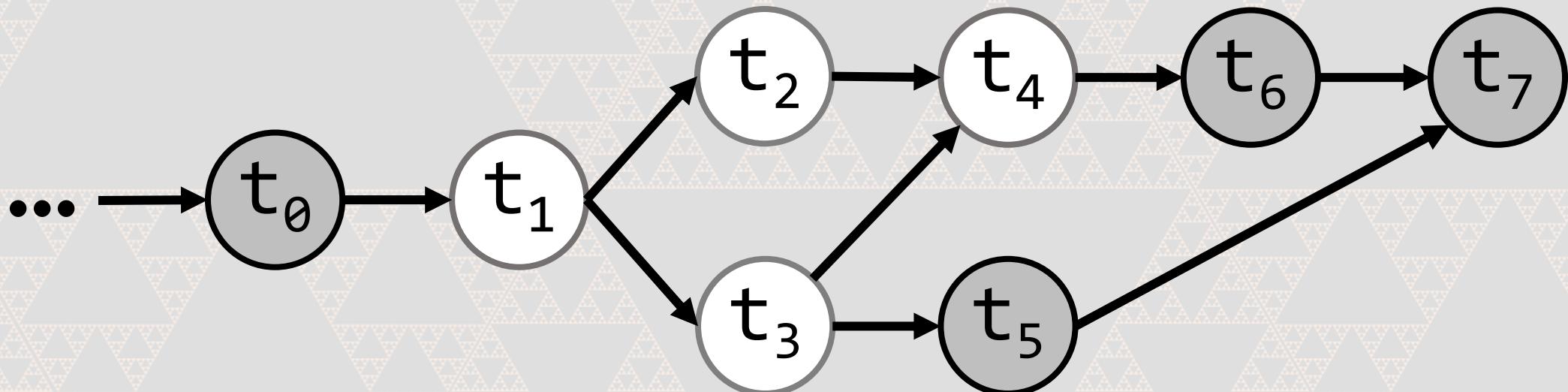
Now we can proceed



MEMORY BUDGET: 4
○ = IN MEMORY

Current operation: $op_7(t_5, t_6)$

Rematerializing on the Fly



MEMORY BUDGET: 4
○ = IN MEMORY

DTR: Just Some Callbacks

AllocateBuffer(size): Allocate if enough room, else evict until there is

PerformEviction(): Heuristic chooses a tensor to evict

Rematerialize(t): Recompute t by replaying its parent op (PerformOp)

PerformOp(op, args):

- Rematerialize evicted arguments
- Make room for result
- Update metadata

What Do Heuristics Look Like?

- Dynamic prediction of which tensor is least valuable
- Useful metadata, easy to track:
 - Cost $c(t)$: Avoid recomputing expensive tensors
 - Staleness $s(t)$: Recently used \Rightarrow likely to be used soon
 - Memory $m(t)$: Large tensors are most profitable to evict
- Resulting policy: minimize $h(t) = c(t)/(m(t) \cdot s(t))$
- Others: LRU $\left(\frac{1}{s(t)}\right)$ and largest-first $\left(\frac{1}{m(t)}\right)$

Reasoning About Tensor Cost

- True cost of a rematerialization includes recursive calls
- Recursively computing exact cost is expensive!
- We approximate evicted components via union-find
 - Keep a running sum for union-find components
 - When tensor rematerialized, map to a new component
 - Leaves “phantom connections” but is fast

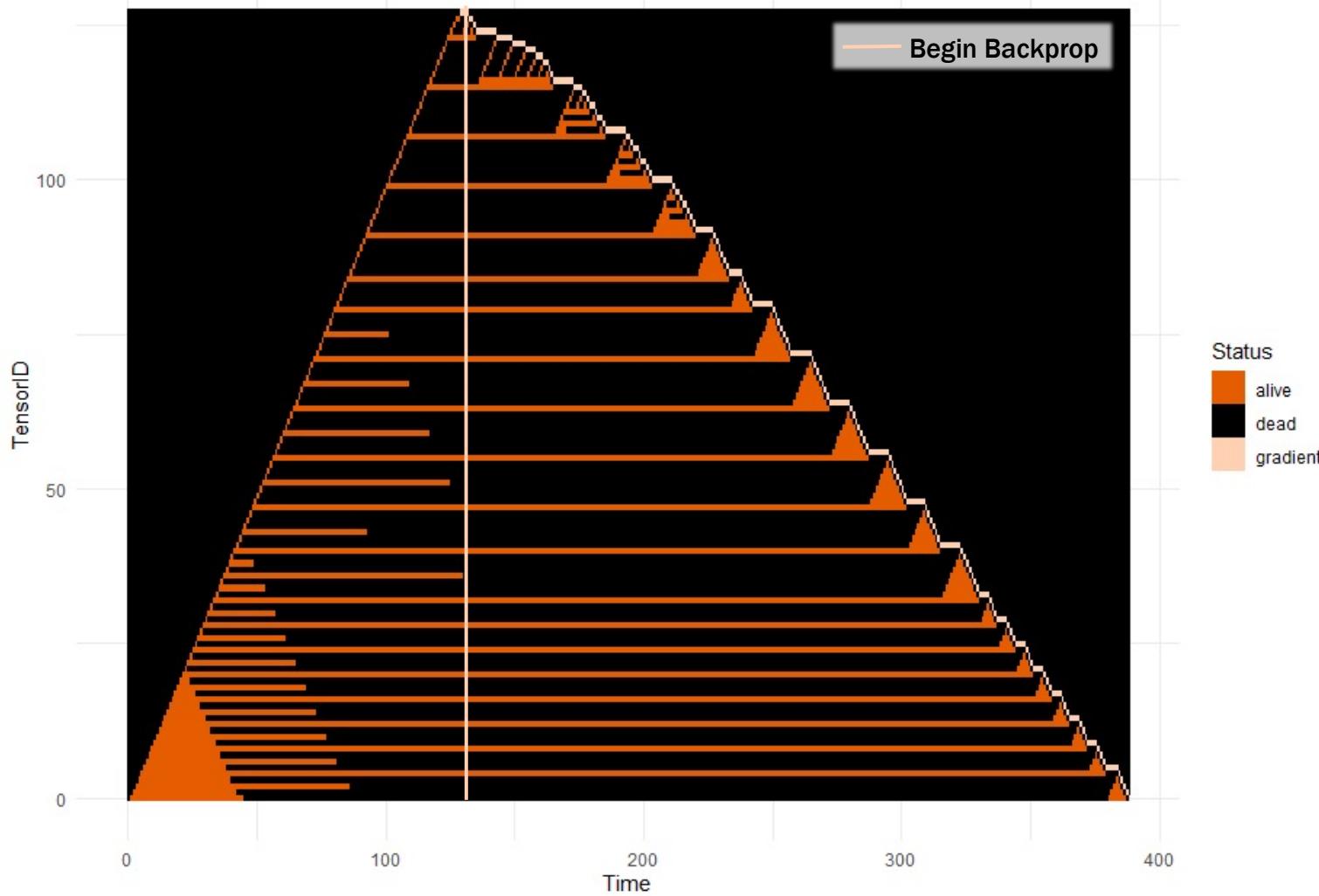
Formal Bounds

Performance on N -layer linear feedforward network:

- $\Omega(\sqrt{N})$ memory and $O(N)$ operations
- Same bound as Chen et al. (2016)
- No advance knowledge of model!

Proof (Sketch) in Pictures

Reduced (compute-memory), $2\sqrt{n}$ memory ($n=128$ layers)



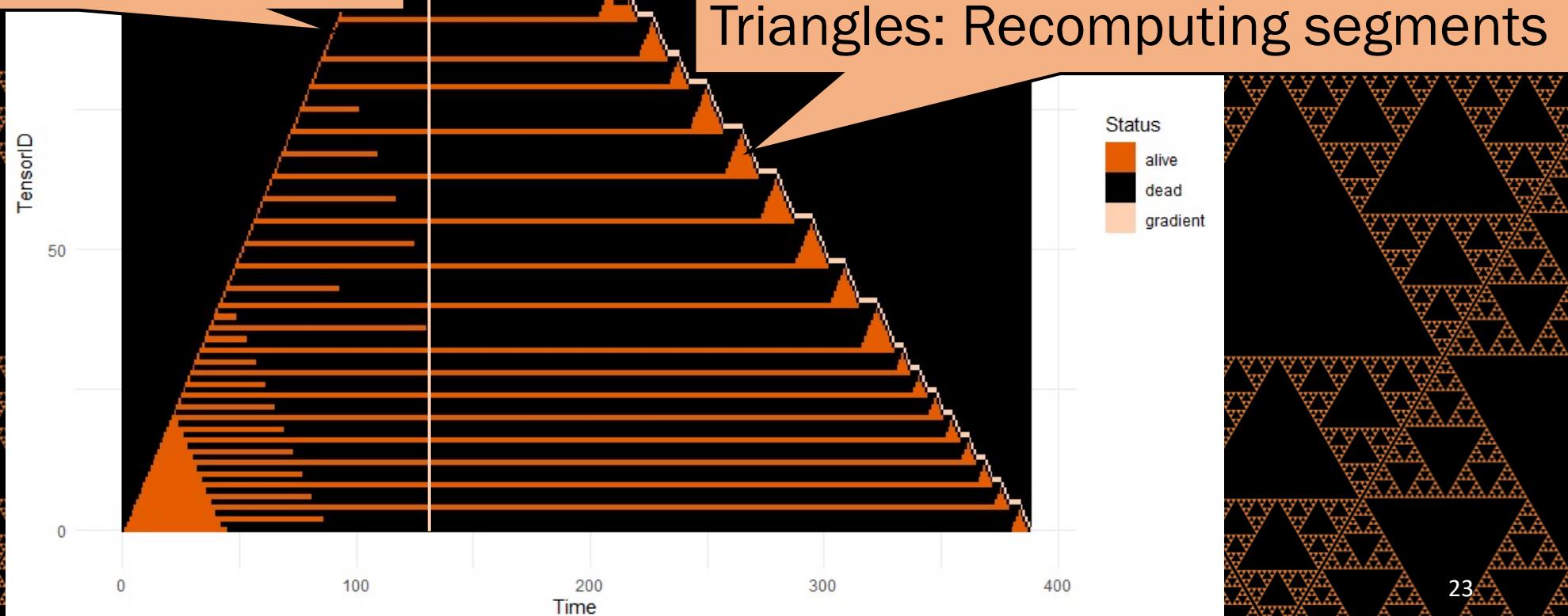
Proof (Sketch) in Pictures

Reduced (compute-memory), $2\sqrt{n}$ memory ($n=128$ layers)



Horizontal lines: Checkpoints!

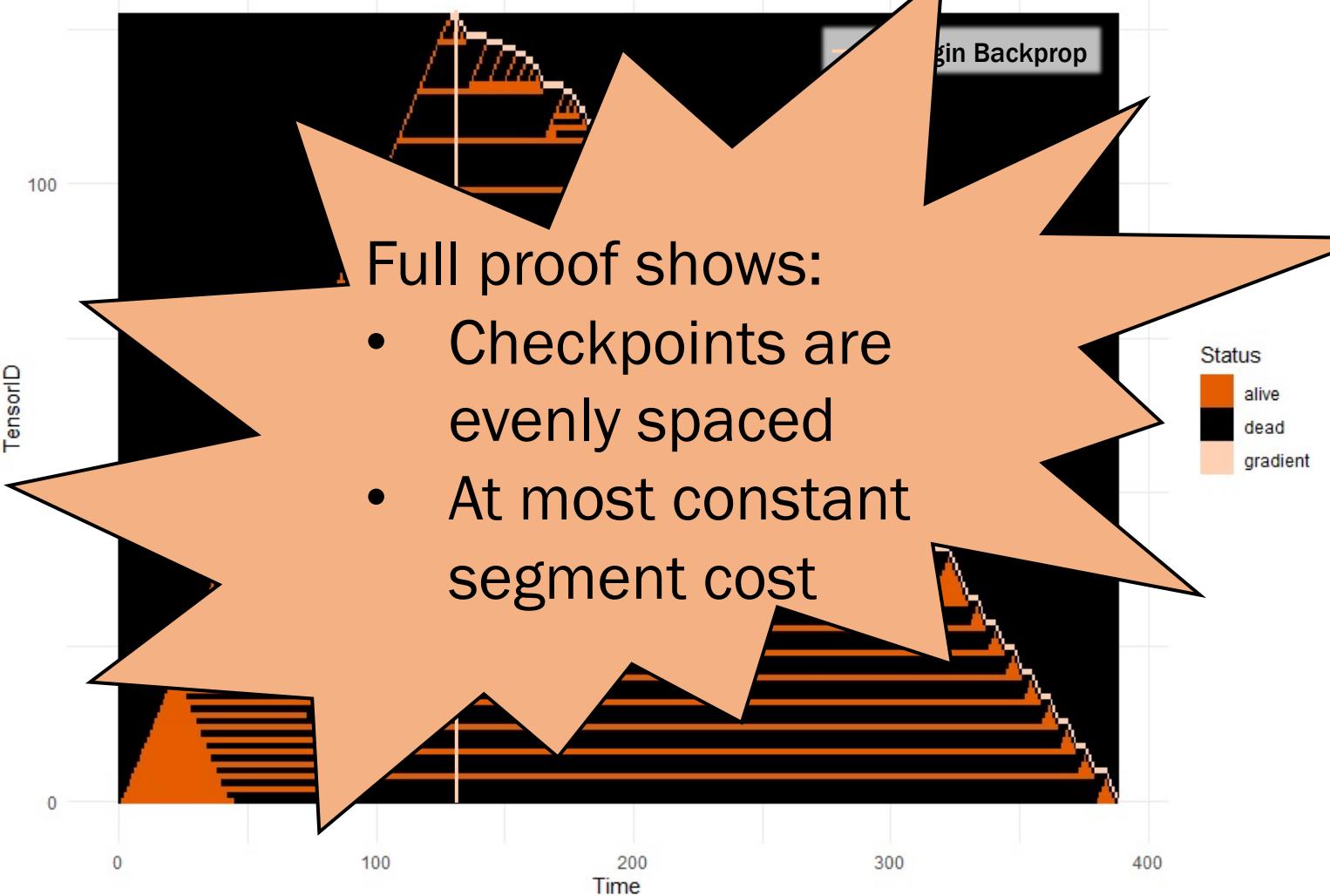
Triangles: Recomputing segments



Proof (Sketch) in Pictures

Reduced (compute-memory), $2\sqrt{n}$ memory ($n=128$ layers)

- Full proof shows:
- Checkpoints are evenly spaced
 - At most constant segment cost



Proof (Sketch) in Pictures

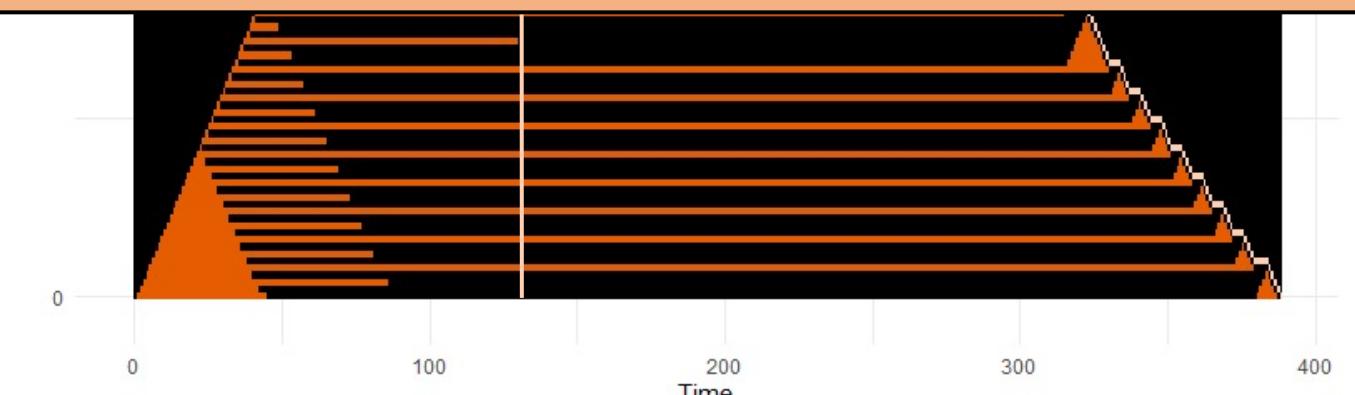
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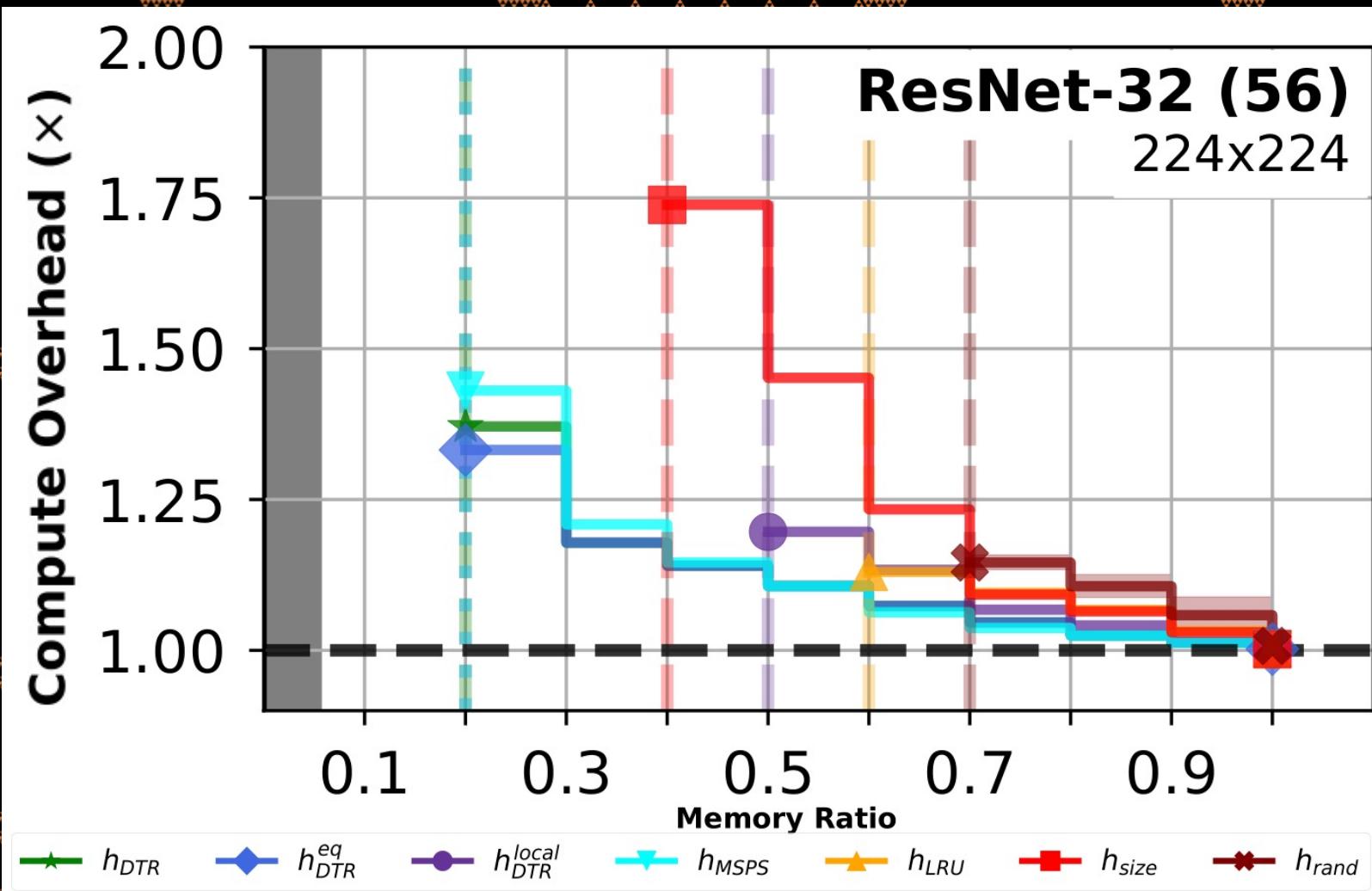
— Begin Backprop

Also a “no-free-lunch” proof:

- Adversarial input exists for every heuristic
- Hence our empirical exploration

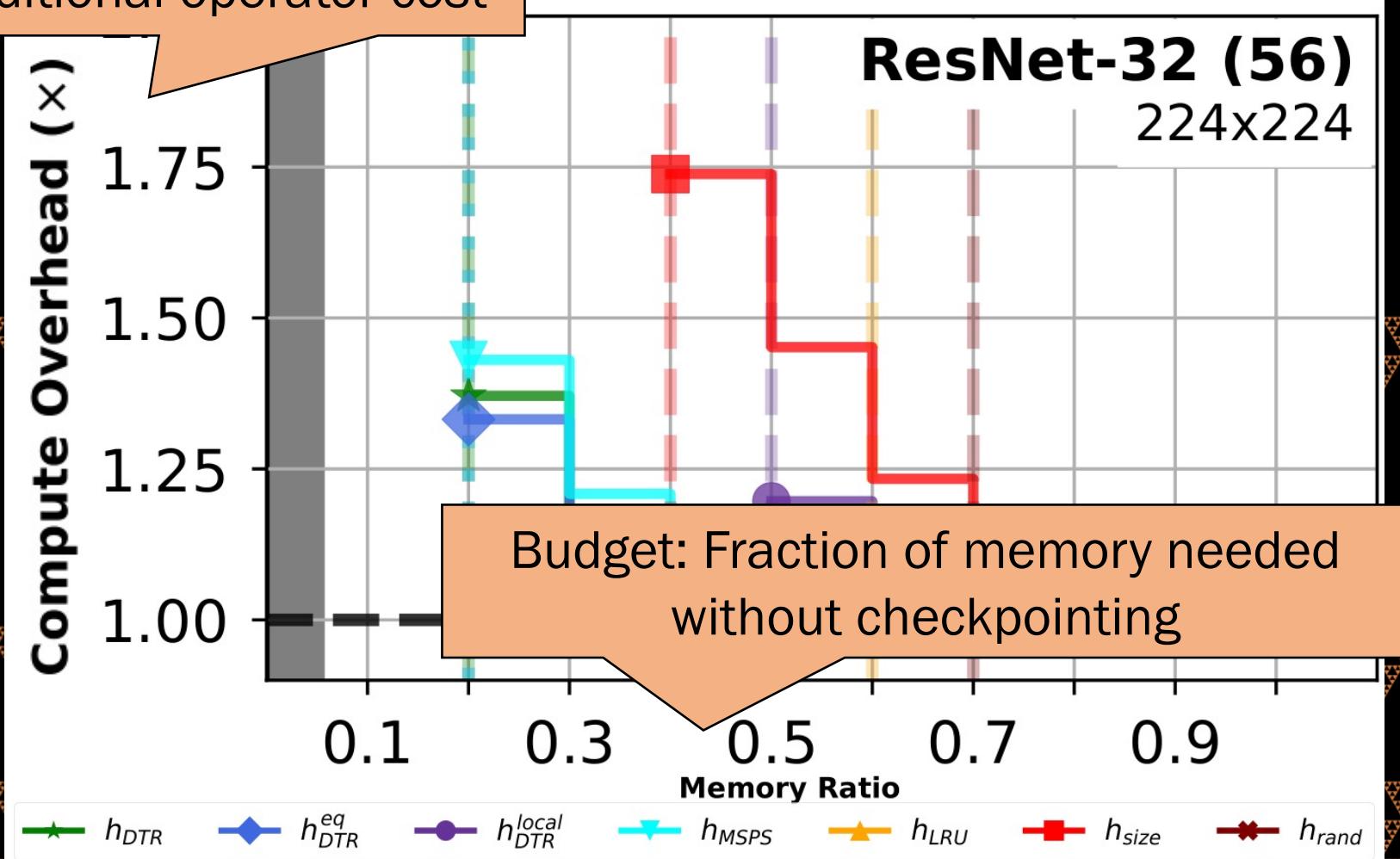


Comparison of Heuristics (Simulated)

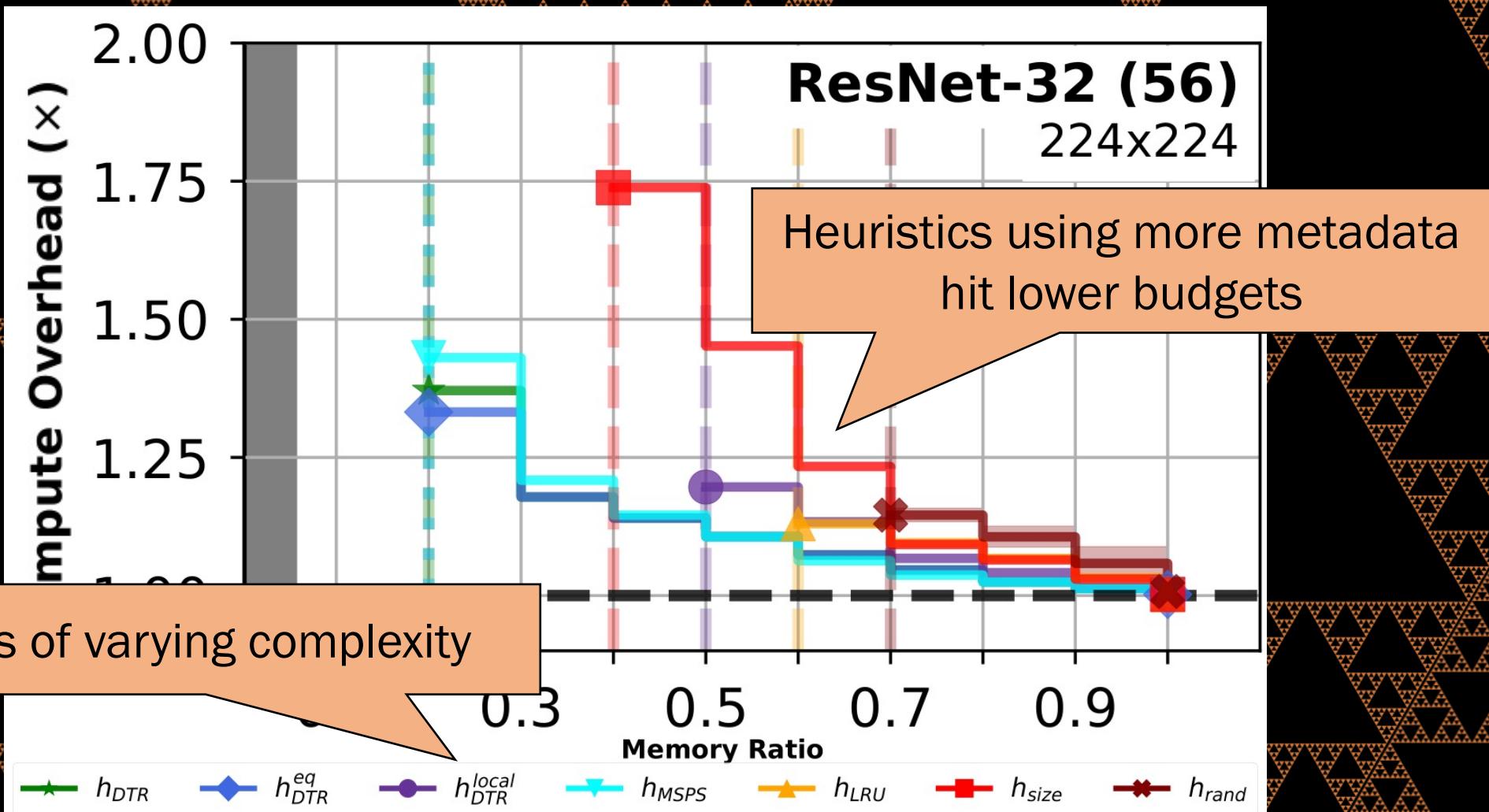


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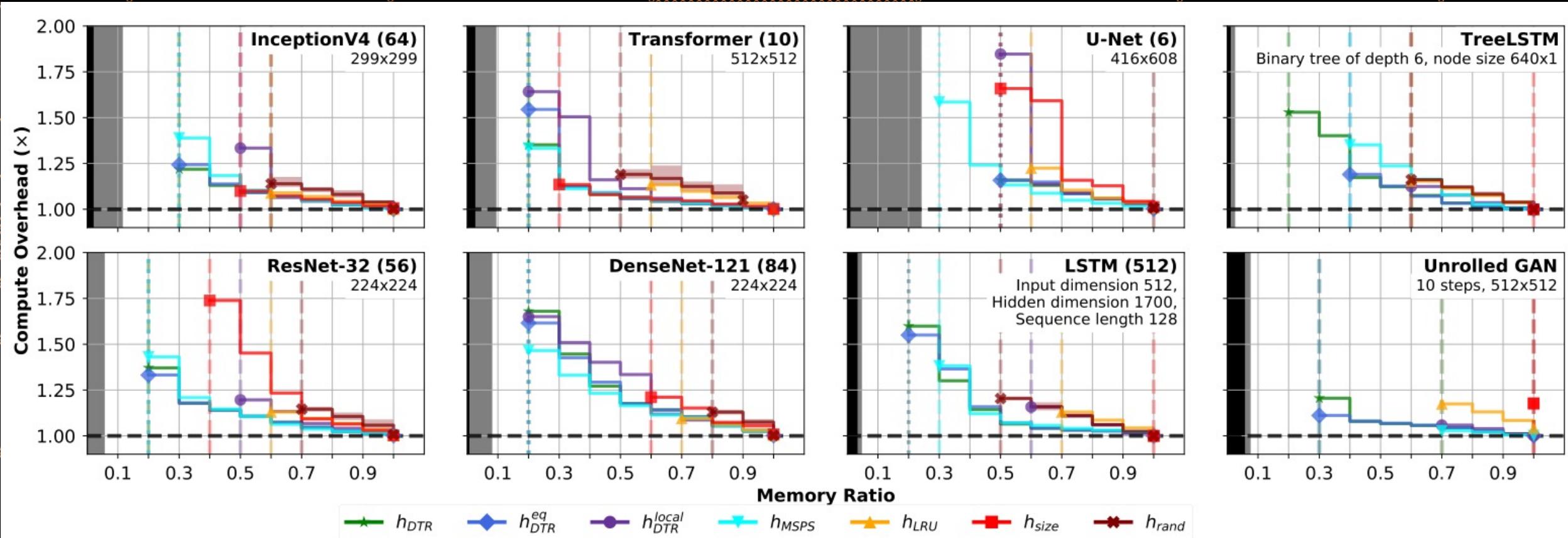
Overhead: Additional operator cost



Comparison of Heuristics (Simulated)

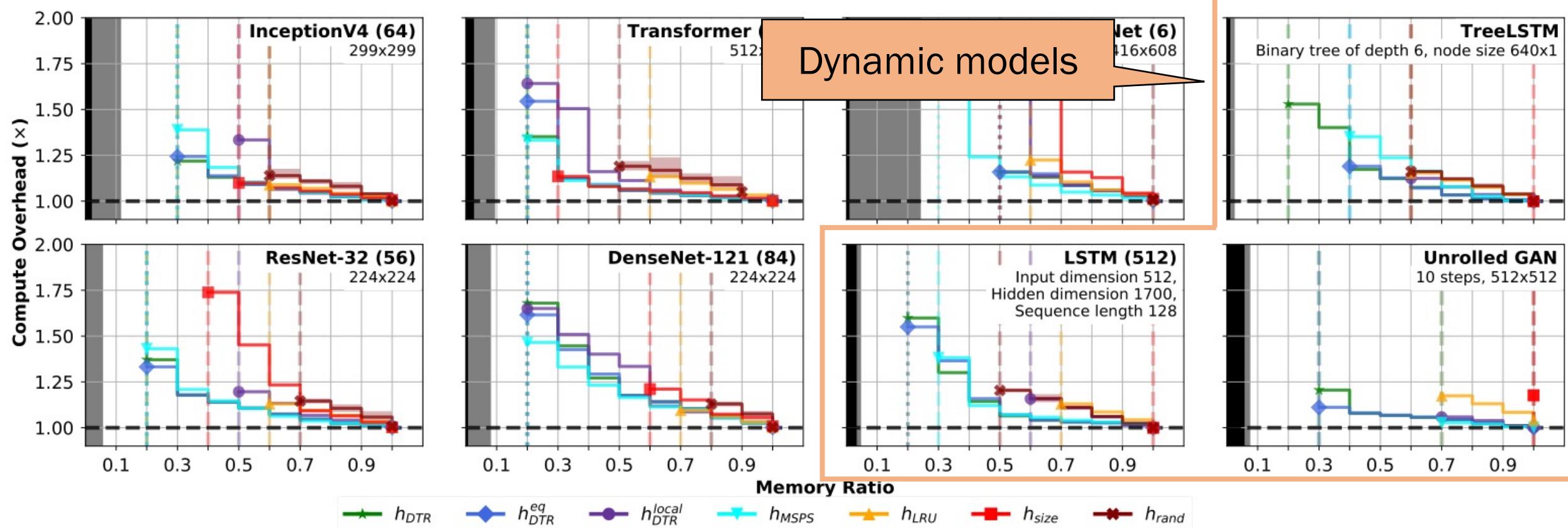


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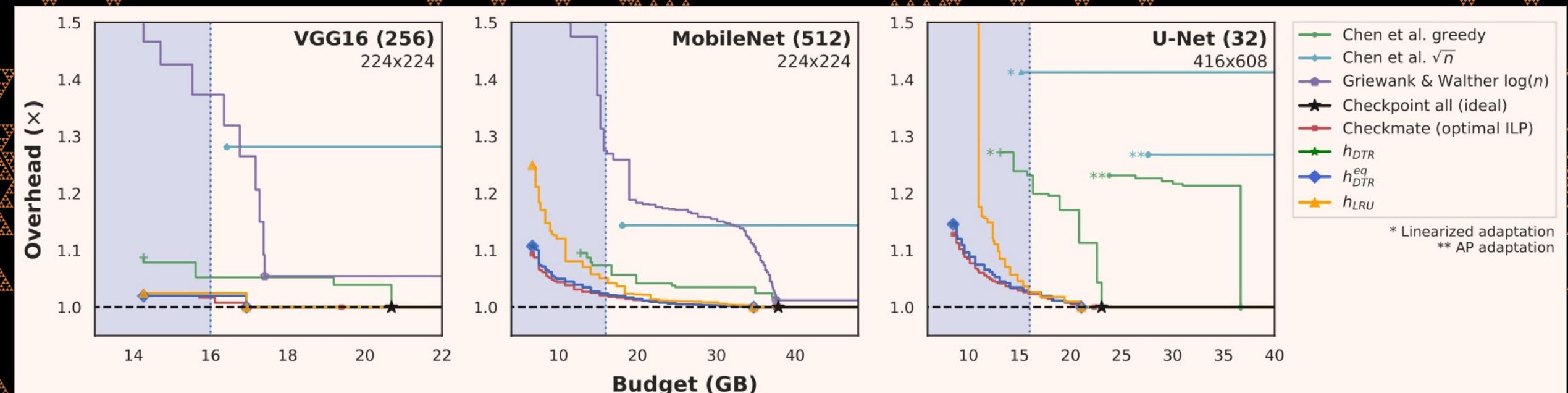
Similar trend holds across all models examined!

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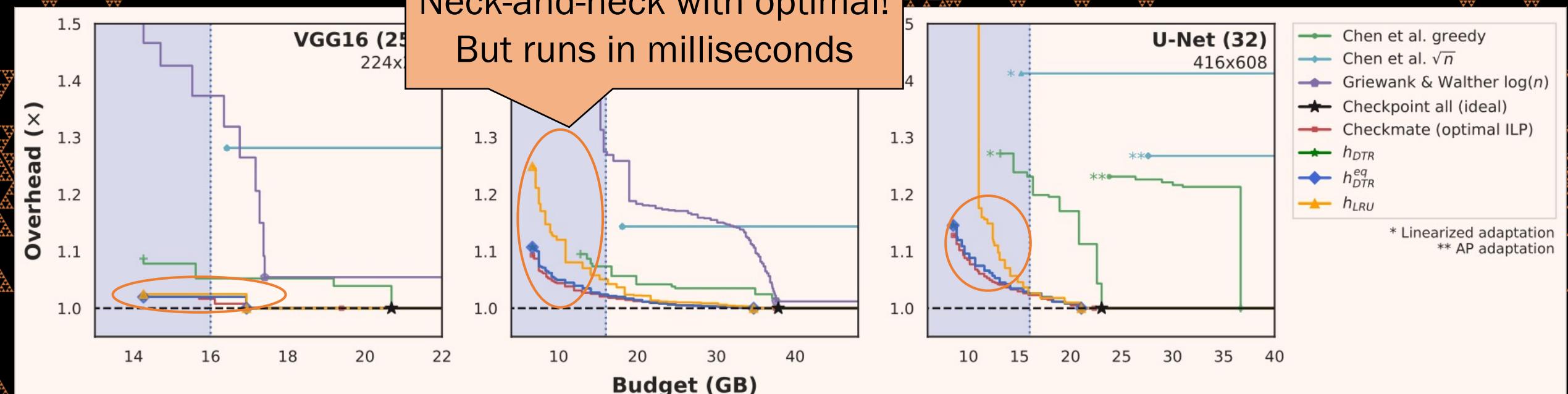
Comparison Against Static Techniques



Simulated comparison via the Checkmate MLSys 2020 artifact

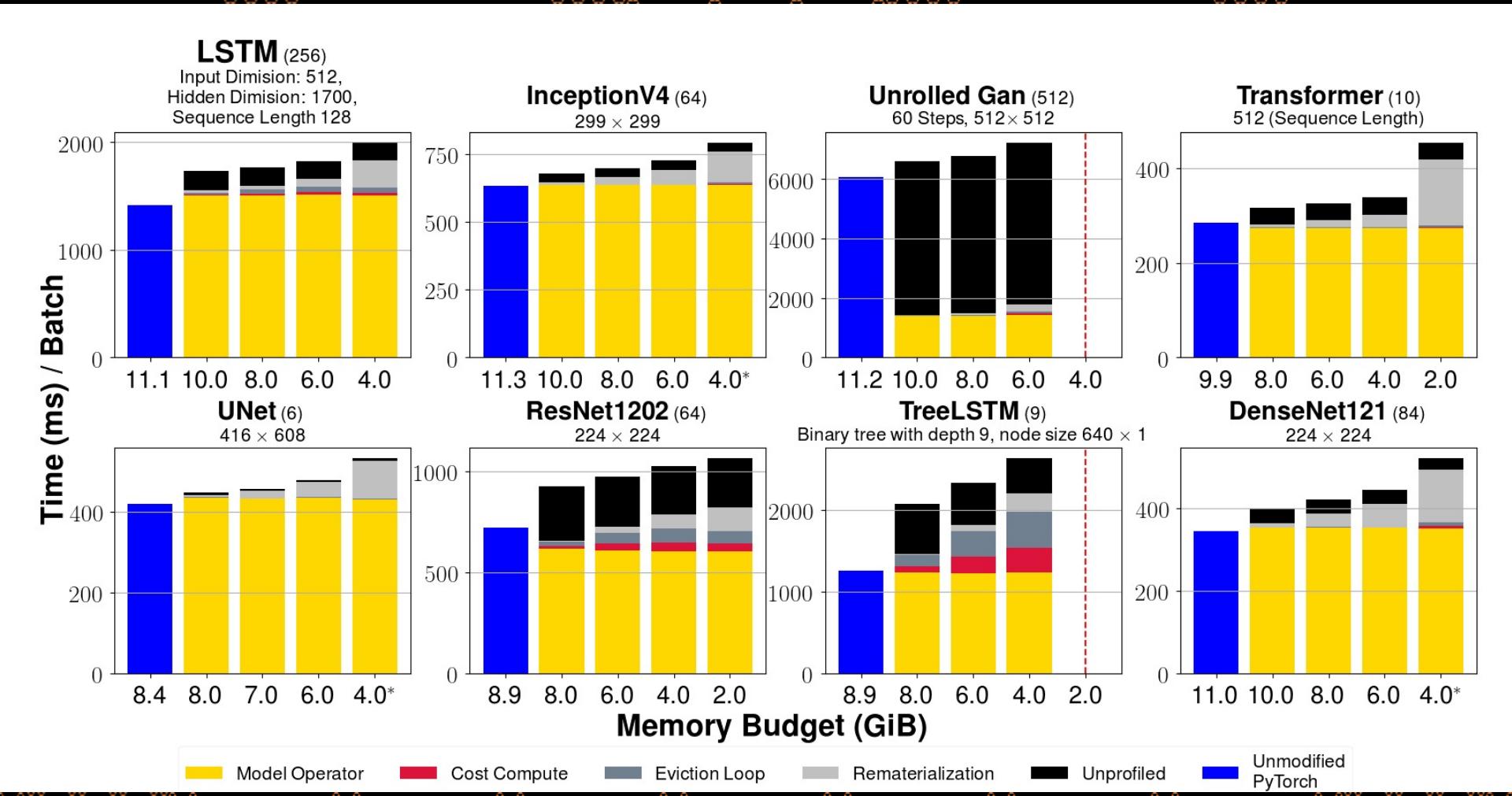
Comparison Against Static Techniques

Neck-and-neck with optimal!
But runs in milliseconds



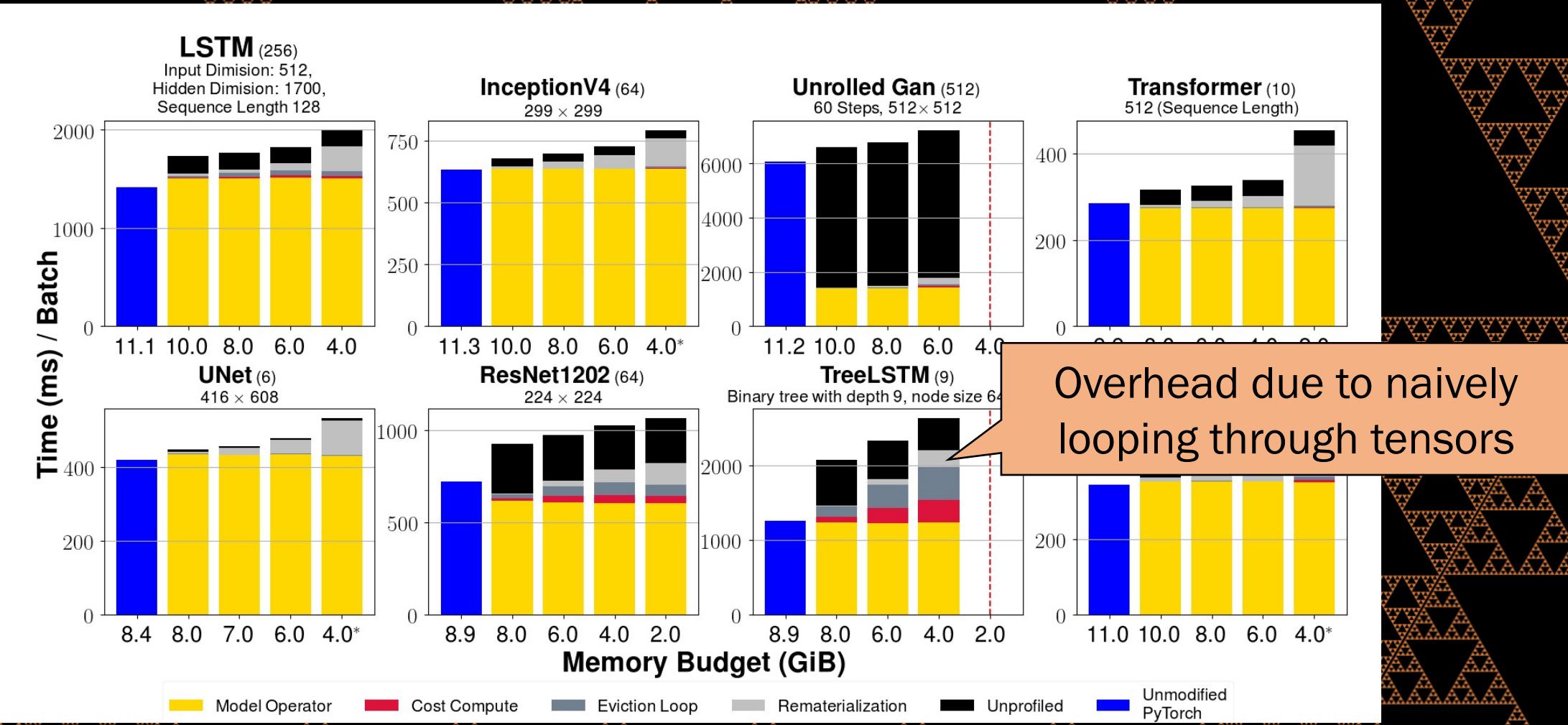
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Prototype Implementation in PyTorch



Thin wrapper over tensor operators, core logic a few hundred LOC

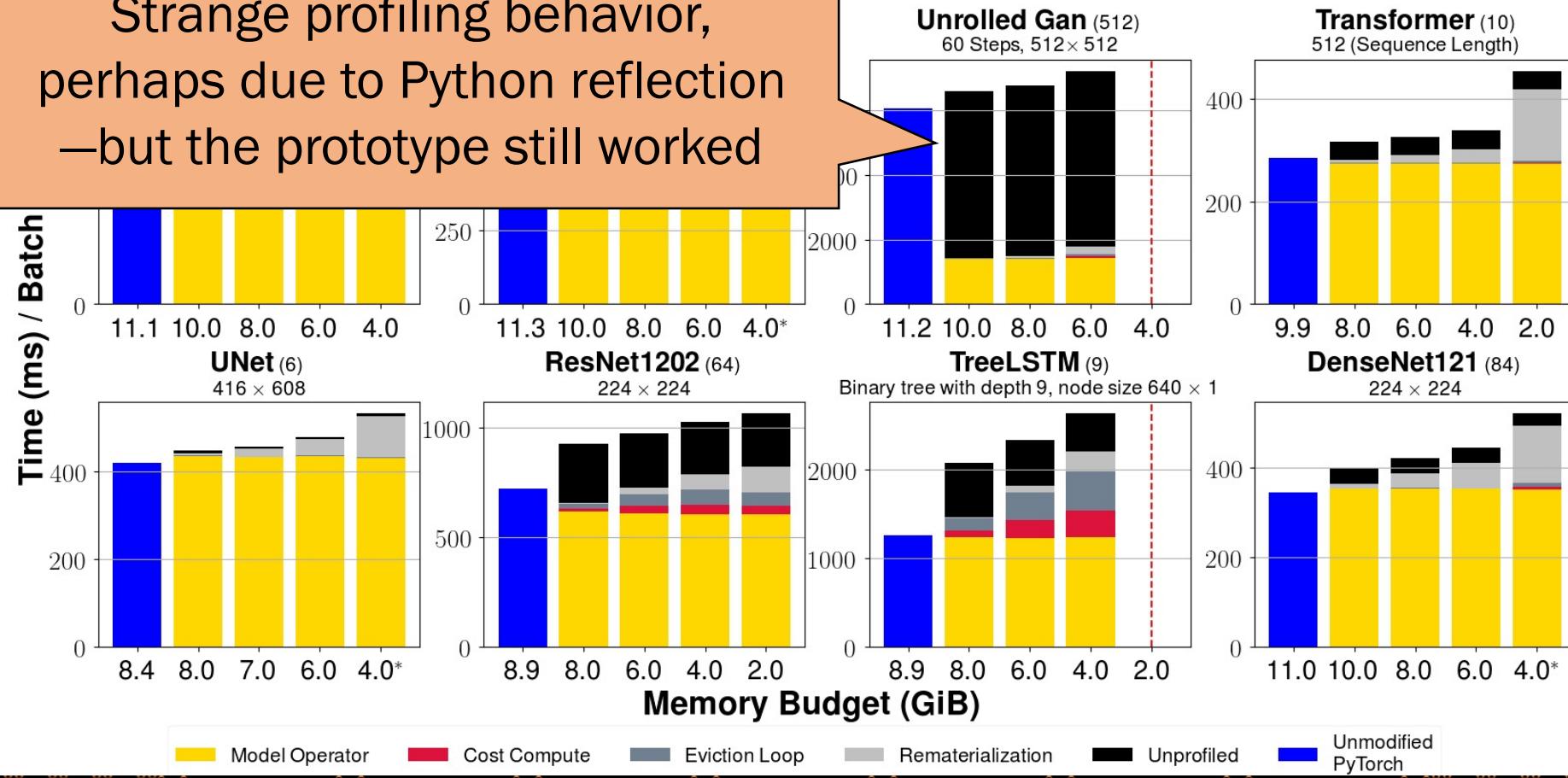
Prototype Implementation in PyTorch



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Prototype Implementation in PyTorch

Strange profiling behavior,
perhaps due to Python reflection
—but the prototype still worked



Thin wrapper over tensor operators, core logic a few hundred LOC

Conclusion

- Encouraging initial results
- Many possible avenues of future work
 - Distributed settings: DTR per GPU?
 - Combining DTR with swapping
 - Tighter integration into the memory manager
 - Learning heuristics, learn from past batches
- Check out the simulator and prototype!
<https://github.com/uwsampl/dtr-prototype>



Marisa Kirisame



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Mike He



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