

# **CS 380 - GPU and GPGPU Programming**

## **Lecture 21: GPU Texturing, Pt. 3**

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# Reading Assignment #12 (until Nov 24)



## Read (required):

- Look at Vulkan *sparse resources*, especially *sparse partially-resident images*
  - <https://docs.vulkan.org/spec/latest/chapters/sparsemem.html>
- Read about shadow mapping
  - [https://en.wikipedia.org/wiki/Shadow\\_mapping](https://en.wikipedia.org/wiki/Shadow_mapping)
- Look at Unreal Engine 5 virtual texturing
  - <https://dev.epicgames.com/documentation/en-us/unreal-engine/virtual-texturing-in-unreal-engine/>
- Look at Unreal Engine 5 MegaLights
  - <https://dev.epicgames.com/documentation/en-us/unreal-engine/megalights-in-unreal-engine/>

## Read (optional):

- CUDA Warp-Level Primitives
  - <https://developer.nvidia.com/blog/using-cuda-warp-level-primitives/>
- Warp-aggregated atomics
  - <https://developer.nvidia.com/blog/cuda-pro-tip-optimized-filtering-warp-aggregated-atomics/>

# Next Lectures

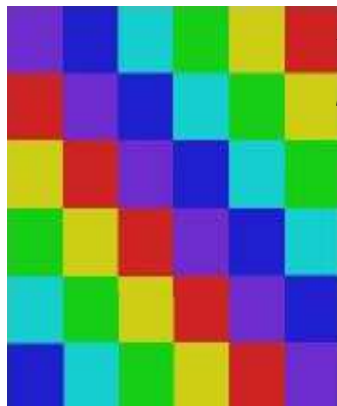


Lecture 22: Tue, Nov 18 (make-up lecture; 14:30 – 16:00, room 3131)

Lecture 23: Thu, Nov 20

# GPU Texturing

# Texturing: General Approach



Texels



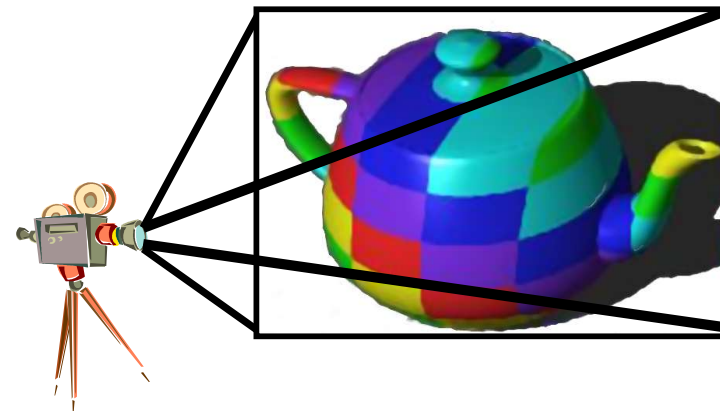
Texture space  $(u, v)$

Object space  $(x_O, y_O, z_O)$

Image Space  $(x_I, y_I)$

Parametrization

Rendering  
(Projection etc.)



# Texture Mapping

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2D (3D) Texture Space

| Texture Transformation

2D Object Parameters

| Parameterization

3D Object Space

| Model Transformation

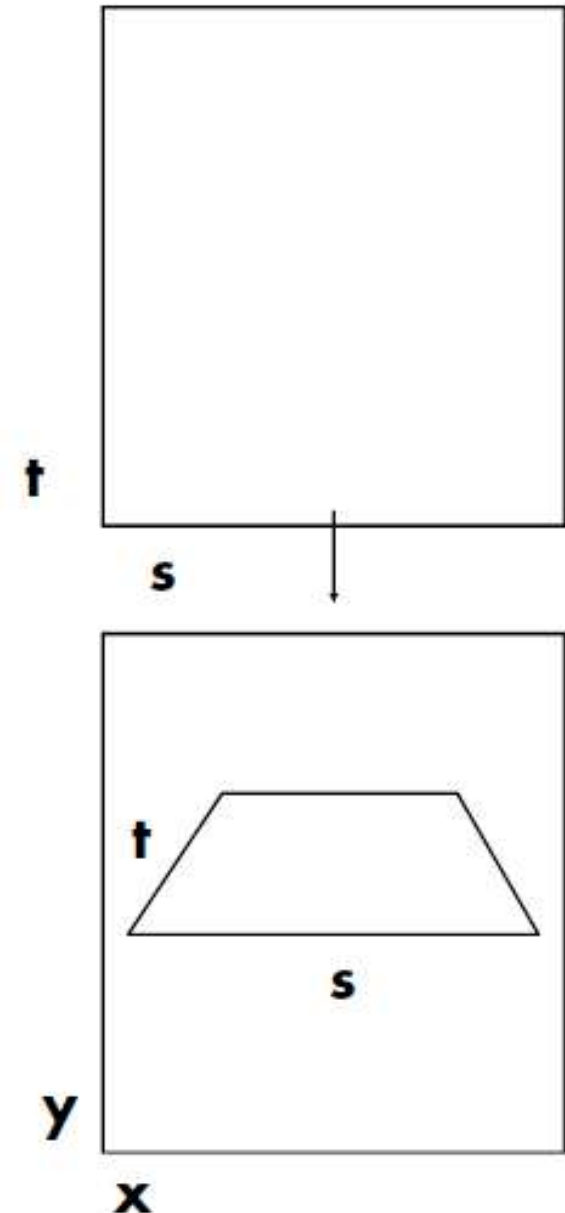
3D World Space

| Viewing Transformation

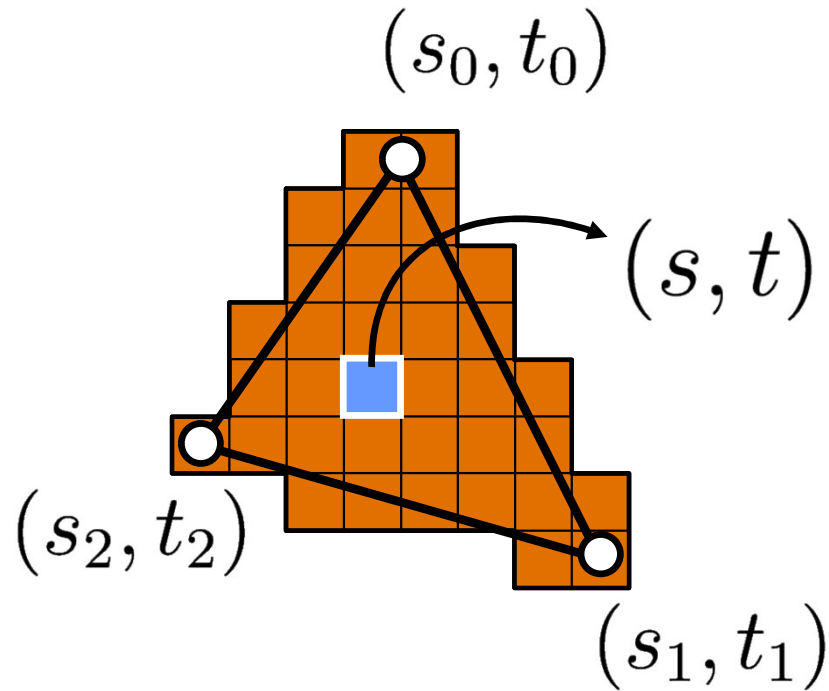
3D Camera Space

| Projection

2D Image Space



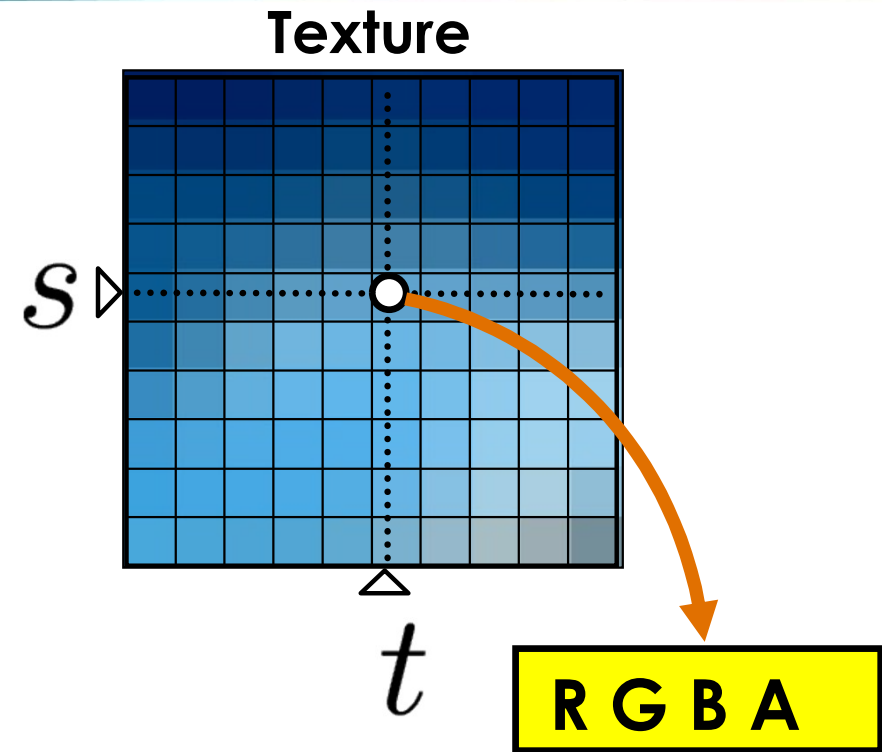
# 2D Texture Mapping



For each fragment:  
interpolate the  
texture coordinates  
(barycentric)

Or:

Use arbitrary, computed coordinates

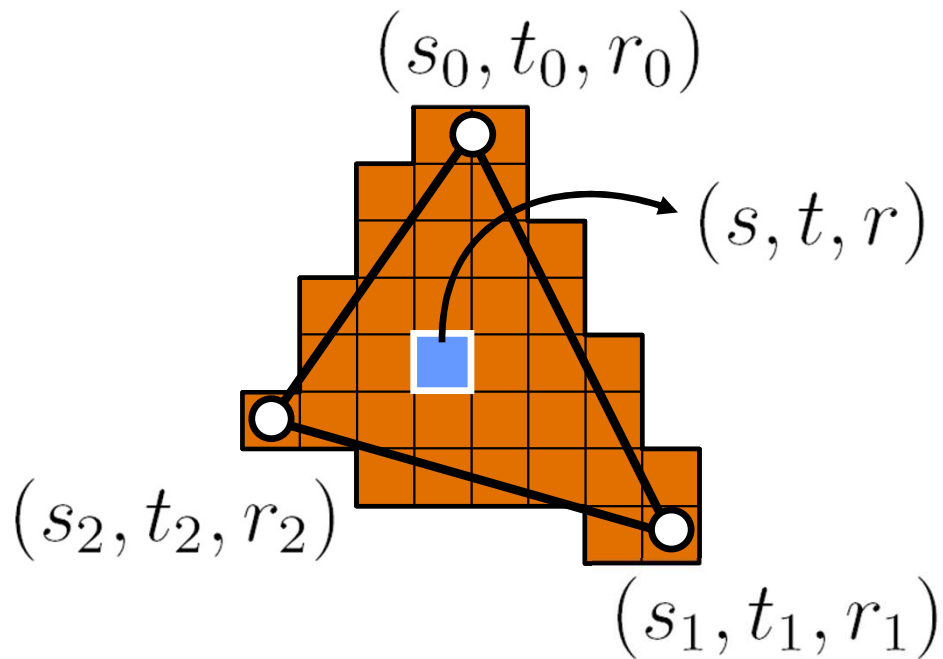


**Texture-Lookup:**  
interpolate the  
texture data  
(bi-linear)

Or:

Nearest-neighbor for “array lookup”

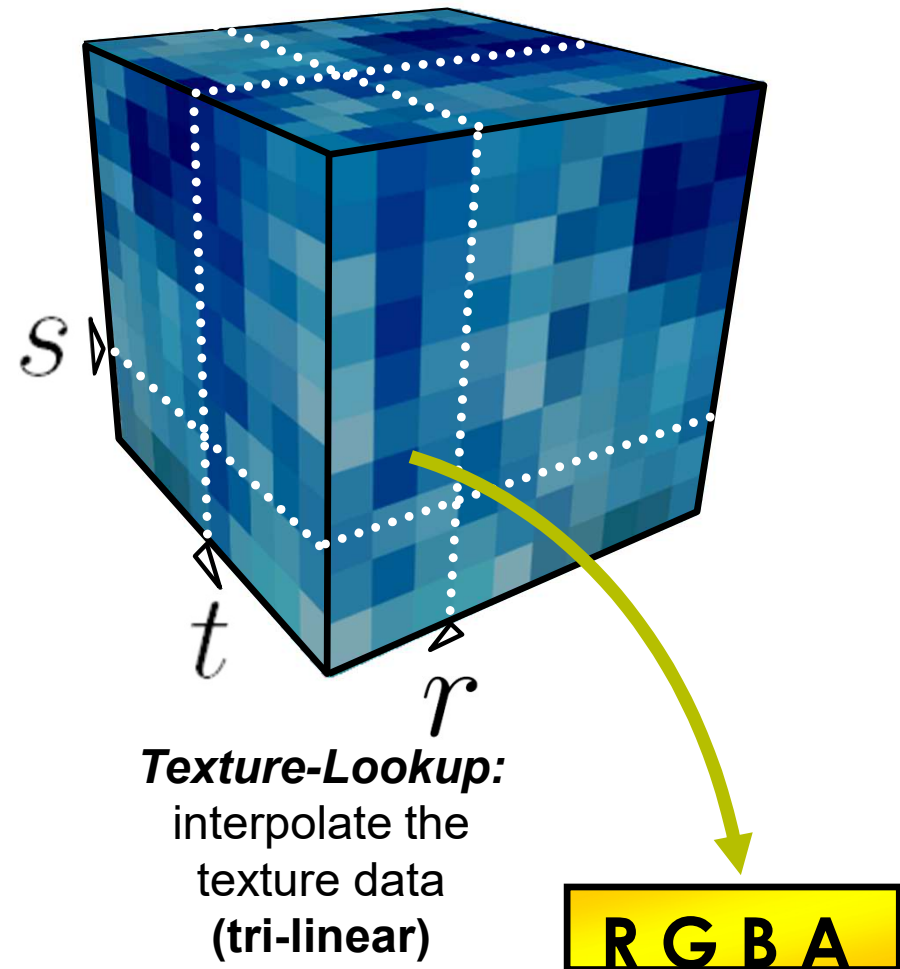
# 3D Texture Mapping



For each fragment:  
interpolate the  
texture coordinates  
(barycentric)

Or:

Use arbitrary, computed coordinates



**Texture-Lookup:**  
interpolate the  
texture data  
(tri-linear)

Or:

Nearest-neighbor for “array lookup”



# Interpolation #1



Interpolation Type + Purpose #1:

# **Interpolation of Texture Coordinates**

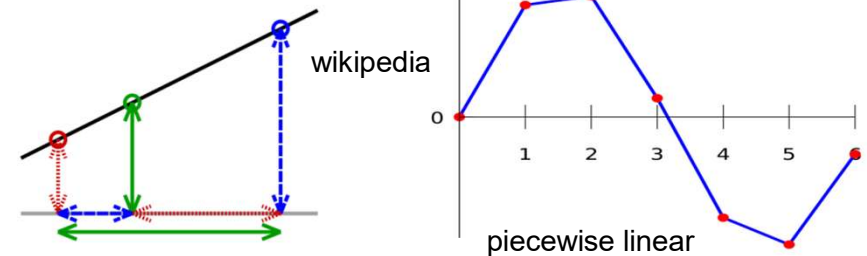
*(Linear / Rational-Linear Interpolation)*

# Linear Interpolation / Convex Combinations



Linear interpolation in 1D:

$$f(\alpha) = (1 - \alpha)v_1 + \alpha v_2$$



Line embedded in 2D (linear interpolation of vertex coordinates/attributes):

$$f(\alpha_1, \alpha_2) = \alpha_1 v_1 + \alpha_2 v_2$$

$$\alpha_1 + \alpha_2 = 1$$

$$f(\alpha) = v_1 + \alpha(v_2 - v_1)$$

$$\alpha = \alpha_2$$

Line segment:  $\alpha_1, \alpha_2 \geq 0$  ( $\rightarrow$  convex combination)

Compare to line parameterization  
with parameter  $t$ :

$$v(t) = v_1 + t(v_2 - v_1)$$

# Linear Interpolation / Convex Combinations



**Linear** combination ( $n$ -dim. space):

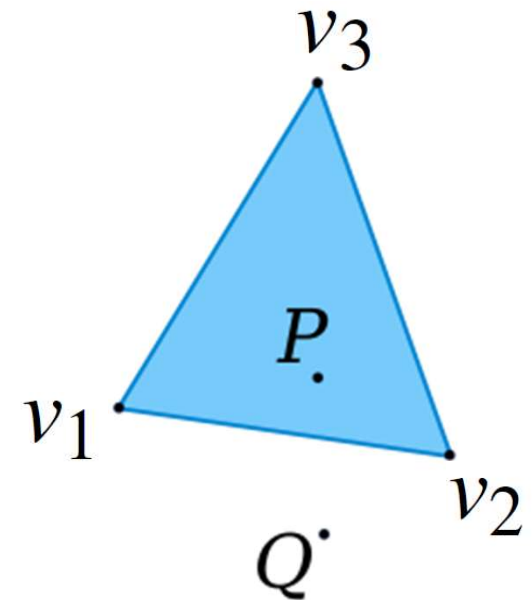
$$\alpha_1 v_1 + \alpha_2 v_2 + \dots + \alpha_n v_n = \sum_{i=1}^n \alpha_i v_i$$

**Affine** combination: Restrict to  $(n-1)$ -dim. subspace:

$$\alpha_1 + \alpha_2 + \dots + \alpha_n = \sum_{i=1}^n \alpha_i = 1$$

**Convex** combination:  $\alpha_i \geq 0$

(restrict to simplex in subspace)



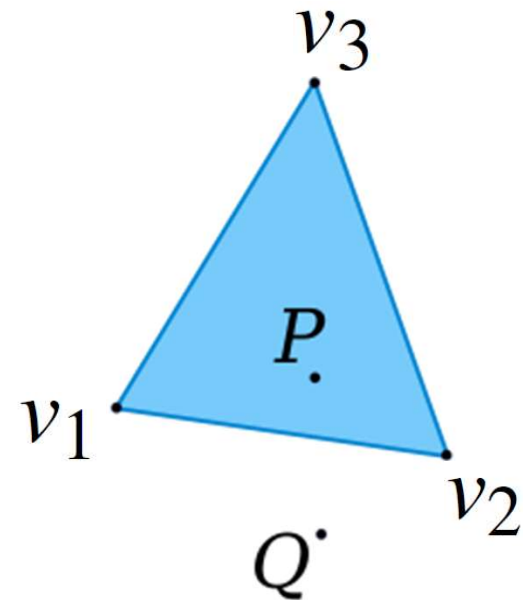
# Linear Interpolation / Convex Combinations



$$\alpha_1 v_1 + \alpha_2 v_2 + \dots + \alpha_n v_n = \sum_{i=1}^n \alpha_i v_i$$
$$\alpha_1 + \alpha_2 + \dots + \alpha_n = \sum_{i=1}^n \alpha_i = 1$$

Re-parameterize to get affine coordinates:

$$\begin{aligned}\alpha_1 v_1 + \alpha_2 v_2 + \alpha_3 v_3 &= \\ \tilde{\alpha}_1 (v_2 - v_1) + \tilde{\alpha}_2 (v_3 - v_1) + v_1 & \\ \tilde{\alpha}_1 &= \alpha_2 \\ \tilde{\alpha}_2 &= \alpha_3\end{aligned}$$



# Linear Interpolation / Convex Combinations



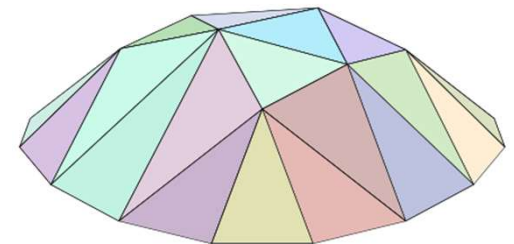
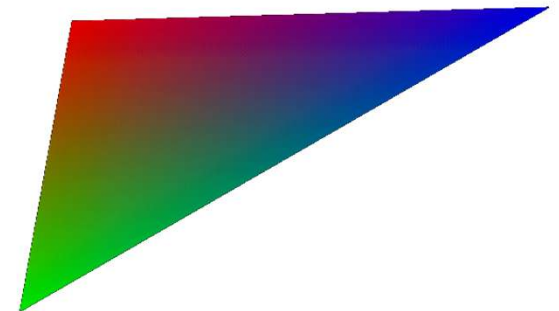
The weights  $\alpha_i$  are the (normalized) barycentric coordinates

→ linear attribute interpolation in simplex

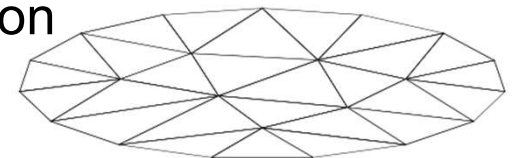
$$\alpha_1 v_1 + \alpha_2 v_2 + \dots + \alpha_n v_n = \sum_{i=1}^n \alpha_i v_i$$

$$\alpha_1 + \alpha_2 + \dots + \alpha_n = \sum_{i=1}^n \alpha_i = 1$$
$$\alpha_i \geq 0$$

attribute interpolation



spatial position  
interpolation



wikipedia

# Homogeneous Coordinates (1)



## Projective geometry

- (Real) projective spaces  $\mathbb{RP}^n$ :  
Real projective line  $\mathbb{RP}^1$ , real projective plane  $\mathbb{RP}^2$ , ...
- A point in  $\mathbb{RP}^n$  is a line through the origin (i.e., all the scalar multiples of the same vector) in an  $(n+1)$ -dimensional (real) vector space



## Homogeneous coordinates of 2D projective point in $\mathbb{RP}^2$

- Coordinates differing only by a non-zero factor  $\lambda$  map to the same point  
 $(\lambda x, \lambda y, \lambda)$       dividing out the  $\lambda$  gives  $(x, y, 1)$ , corresponding to  $(x, y)$  in  $\mathbb{R}^2$
- Coordinates with last component = 0 map to “points at infinity”  
 $(\lambda x, \lambda y, 0)$       division by last component not allowed; but again this is the same point if it only differs by a scalar factor, e.g., this is the same point as  $(x, y, 0)$

# Homogeneous Coordinates (2)



## Examples of usage

- Translation (with translation vector  $\vec{b}$ )
- Affine transformations (linear transformation + translation)

$$\vec{y} = A\vec{x} + \vec{b}.$$

- With homogeneous coordinates:

$$\begin{bmatrix} \vec{y} \\ 1 \end{bmatrix} = \left[ \begin{array}{ccc|c} & A & & \vec{b} \\ 0 & \dots & 0 & 1 \end{array} \right] \begin{bmatrix} \vec{x} \\ 1 \end{bmatrix}$$

- Setting the last coordinate = 1 and the last row of the matrix to  $[0, \dots, 0, 1]$  results in translation of the point  $\vec{x}$  (via addition of translation vector  $\vec{b}$ )
- The matrix above is a linear map, but because it is one dimension higher, it does not have to move the origin in the  $(n+1)$ -dimensional space for translation



# Homogeneous Coordinates (3)

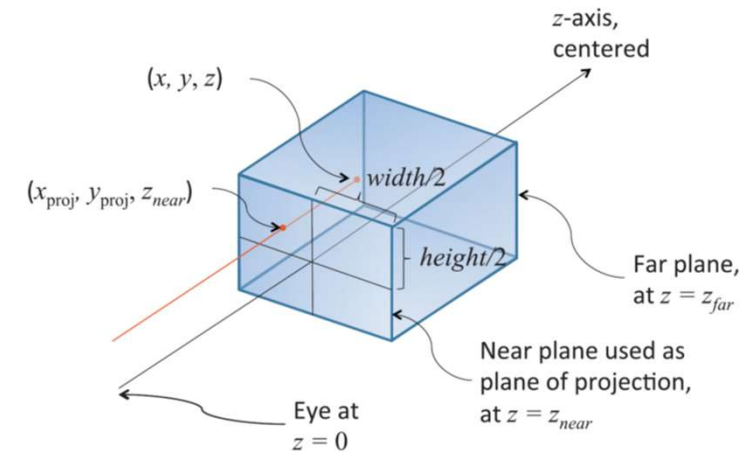


## Examples of usage

- Projection (e.g., OpenGL projection matrices)

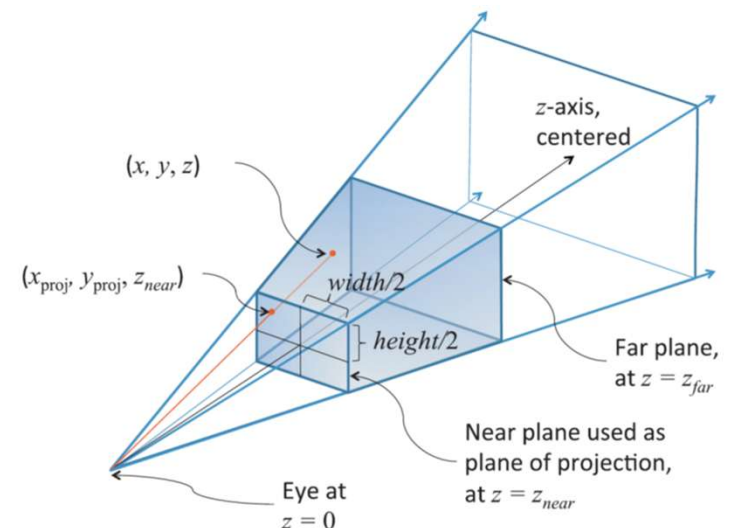
$$\begin{bmatrix} \frac{2}{\text{right} - \text{left}} & 0 & 0 & -\frac{\text{right} + \text{left}}{\text{right} - \text{left}} \\ 0 & \frac{2}{\text{top} - \text{bottom}} & 0 & -\frac{\text{top} + \text{bottom}}{\text{top} - \text{bottom}} \\ 0 & 0 & \frac{-2}{\text{far} - \text{near}} & \frac{\text{far} + \text{near}}{\text{far} - \text{near}} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

orthographic



$$\begin{bmatrix} \frac{z_{\text{near}}}{\text{width}/2} & 0.0 & \frac{\text{left} + \text{right}}{\text{width}/2} & 0.0 \\ 0.0 & \frac{z_{\text{near}}}{\text{height}/2} & \frac{\text{top} + \text{bottom}}{\text{height}/2} & 0.0 \\ 0.0 & 0.0 & \frac{z_{\text{far}} + z_{\text{near}}}{z_{\text{far}} - z_{\text{near}}} & \frac{2z_{\text{far}}z_{\text{near}}}{z_{\text{far}} - z_{\text{near}}} \\ 0.0 & 0.0 & -1.0 & 0.0 \end{bmatrix}$$

perspective



Thank you.