King Abdullah University of Science and Technology

KAUST

CS 380 - GPU and GPGPU Programming
Lecture 14: GPU Compute APIs, Pt. 4

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Reading Assignment #6 (until Oct 21)

Read (required):

- Programming Massively Parallel Processors book (4th edition), **Chapter 5** (*Memory architecture and data locality*)

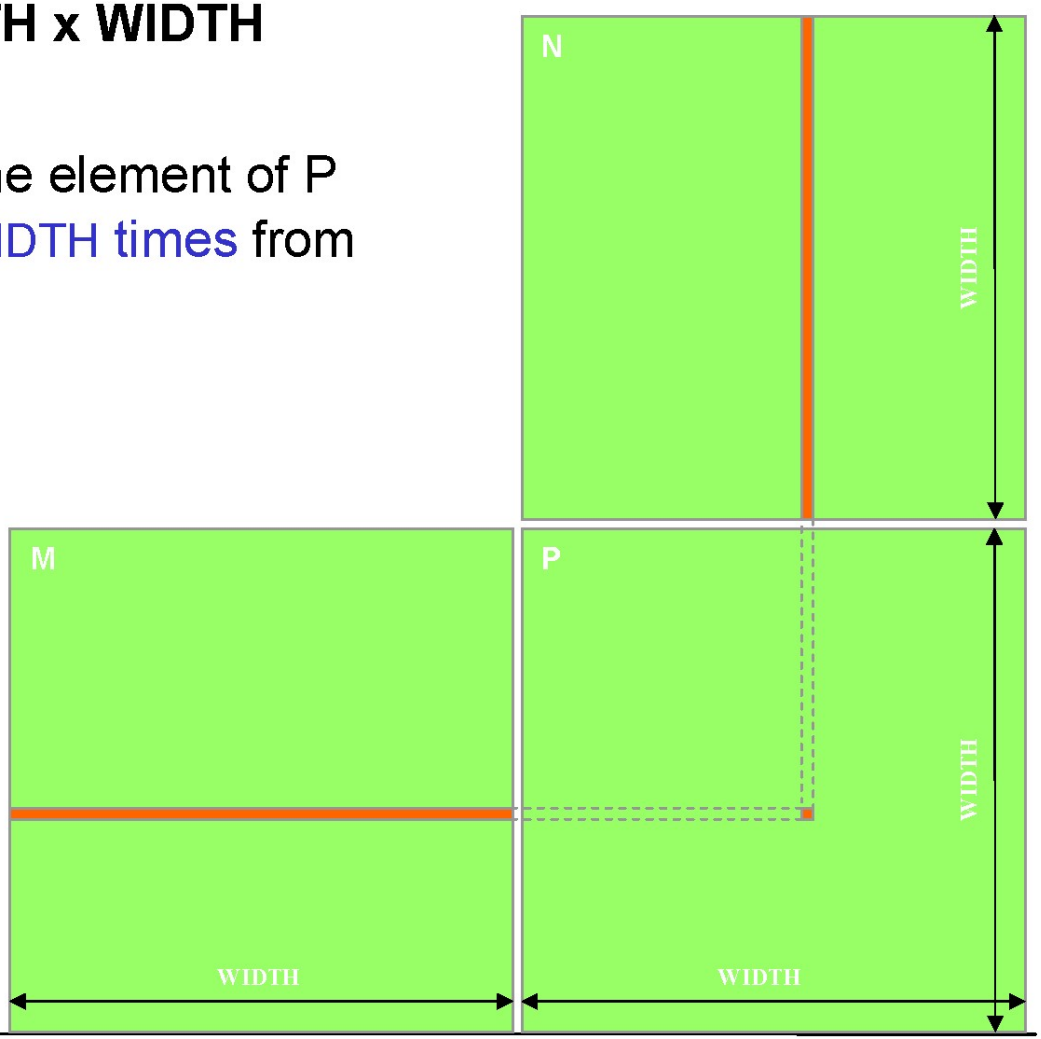
Read (optional):

- Programming Massively Parallel Processors book (4th edition), **Chapter 20** (*An introduction to CUDA streams*)
- Programming Massively Parallel Processors book (4th edition), **Chapter 21** (*CUDA dynamic parallelism*)

Code Example #2: Matrix Multiply

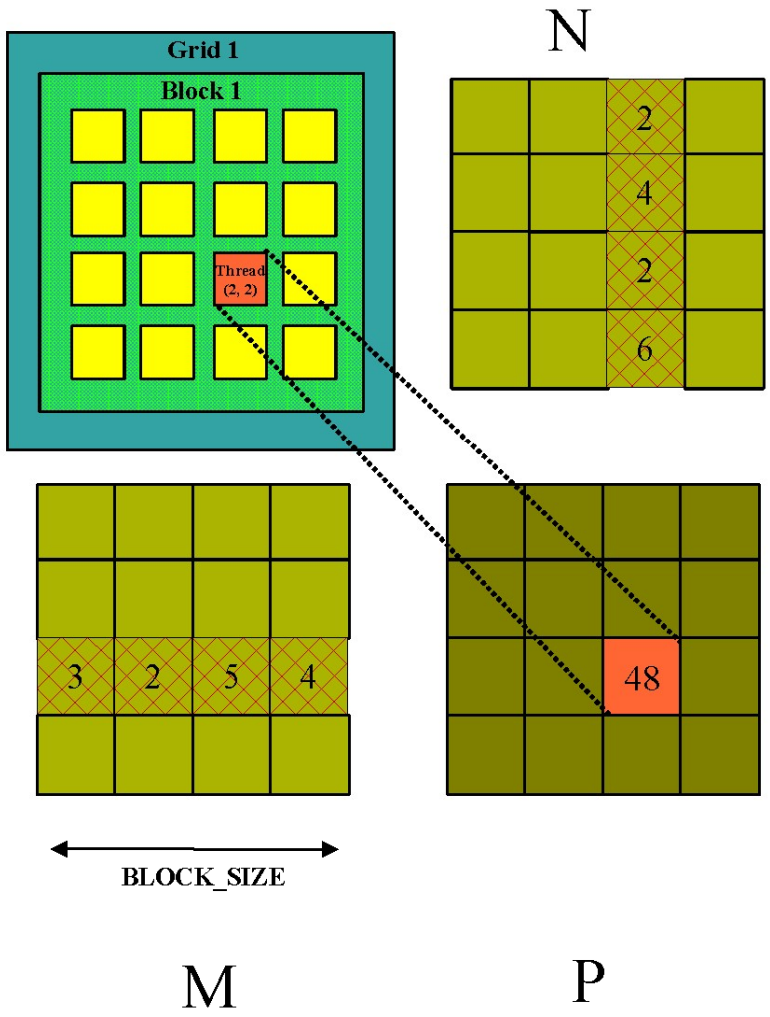
Programming Model: Square Matrix Multiplication

- **P = M * N of size WIDTH x WIDTH**
- **Without tiling:**
  - One thread handles one element of P
  - M and N are loaded WIDTH times from global memory



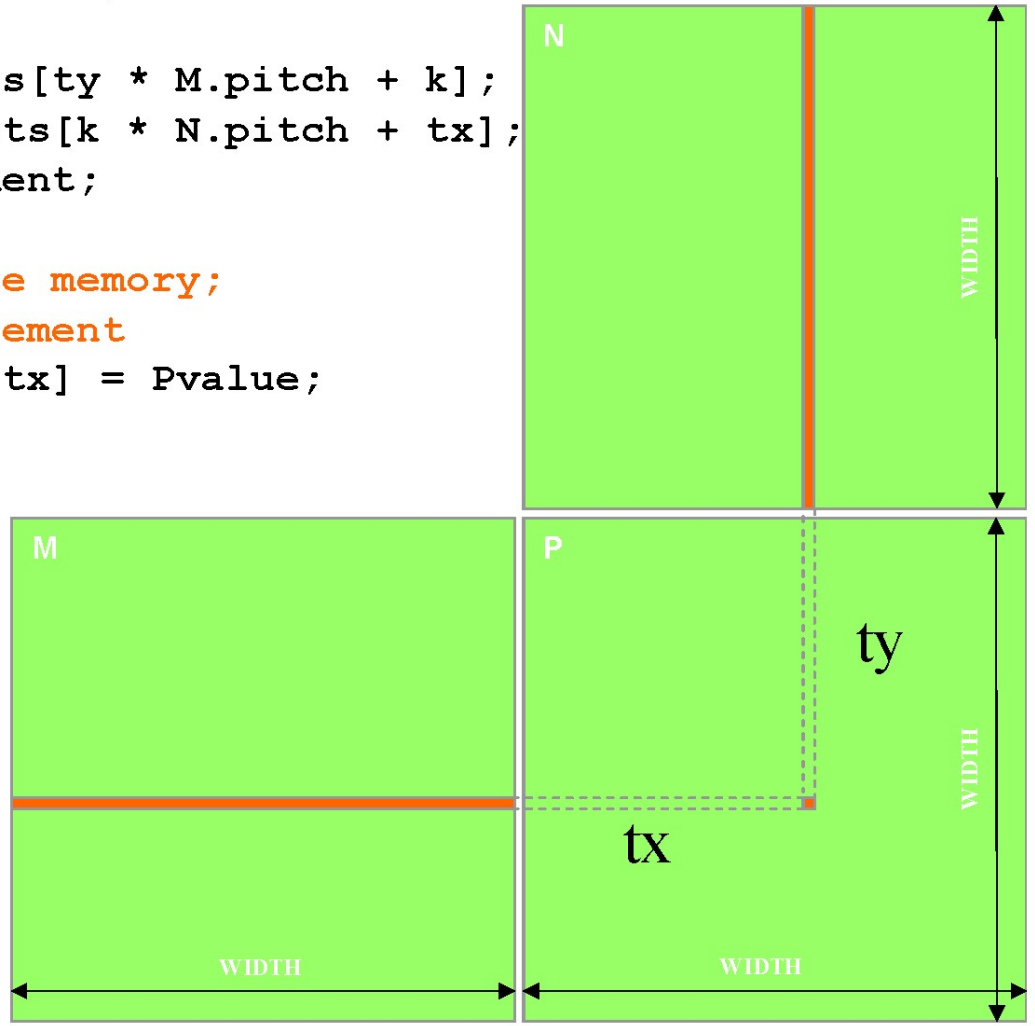
Multiply Using One Thread Block

- **One block of threads computes matrix P**
  - Each thread computes one element of P
- **Each thread**
  - Loads a row of matrix M
  - Loads a column of matrix N
  - Perform one multiply and addition for each pair of M and N elements
  - Compute to off-chip memory access ratio close to 1:1 (not very high)
- **Size of matrix limited by the number of threads allowed in a thread block**



Matrix Multiplication
Device-Side Kernel Function (cont.)

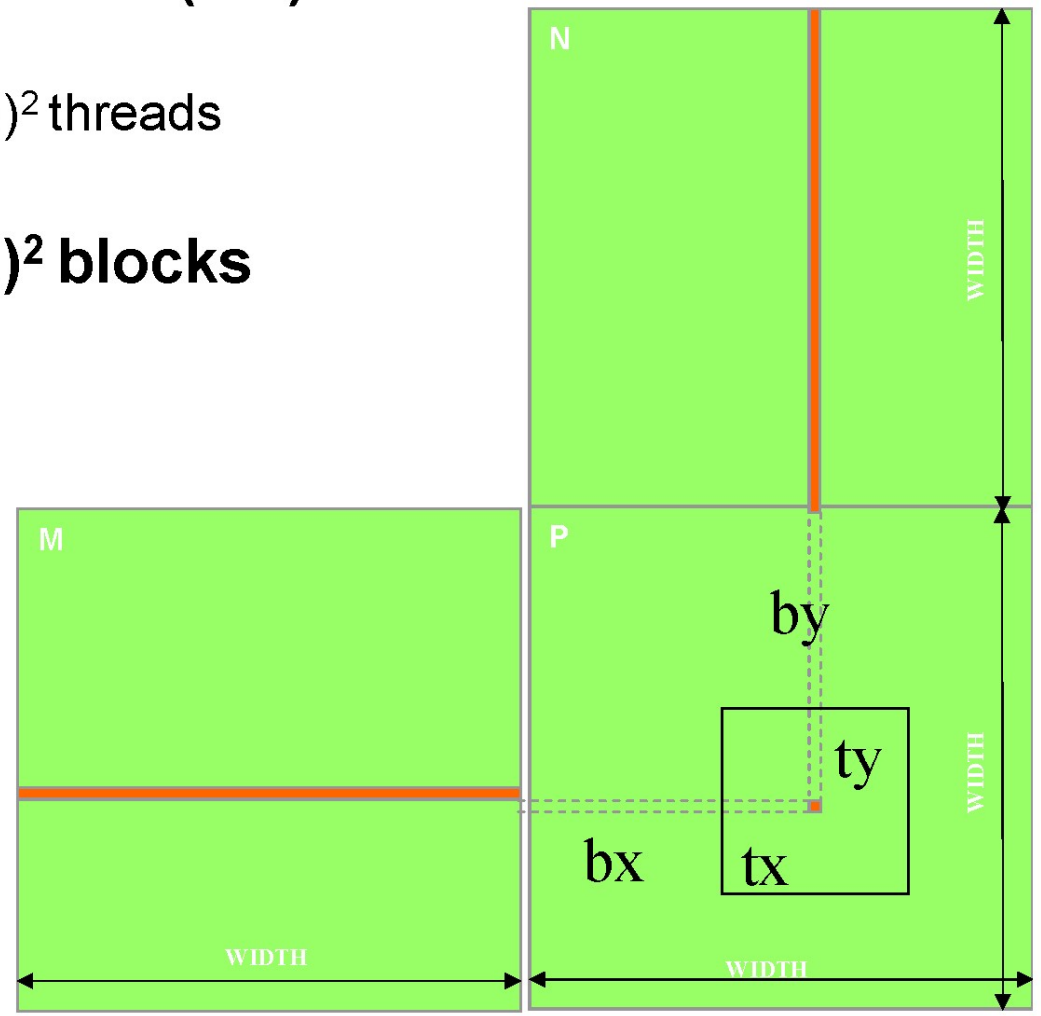
```
...
    for (int k = 0; k < M.width; ++k)
    {
      float Melement = M.elements[ty * M.pitch + k];
      float Nelement = Nd.elements[k * N.pitch + tx];
      Pvalue += Melement * Nelement;
    }
    // Write the matrix to device memory;
    // each thread writes one element
    P.elements[ty * blockDim.x+ tx] = Pvalue;
}
```



Handling Arbitrary Sized Square Matrices

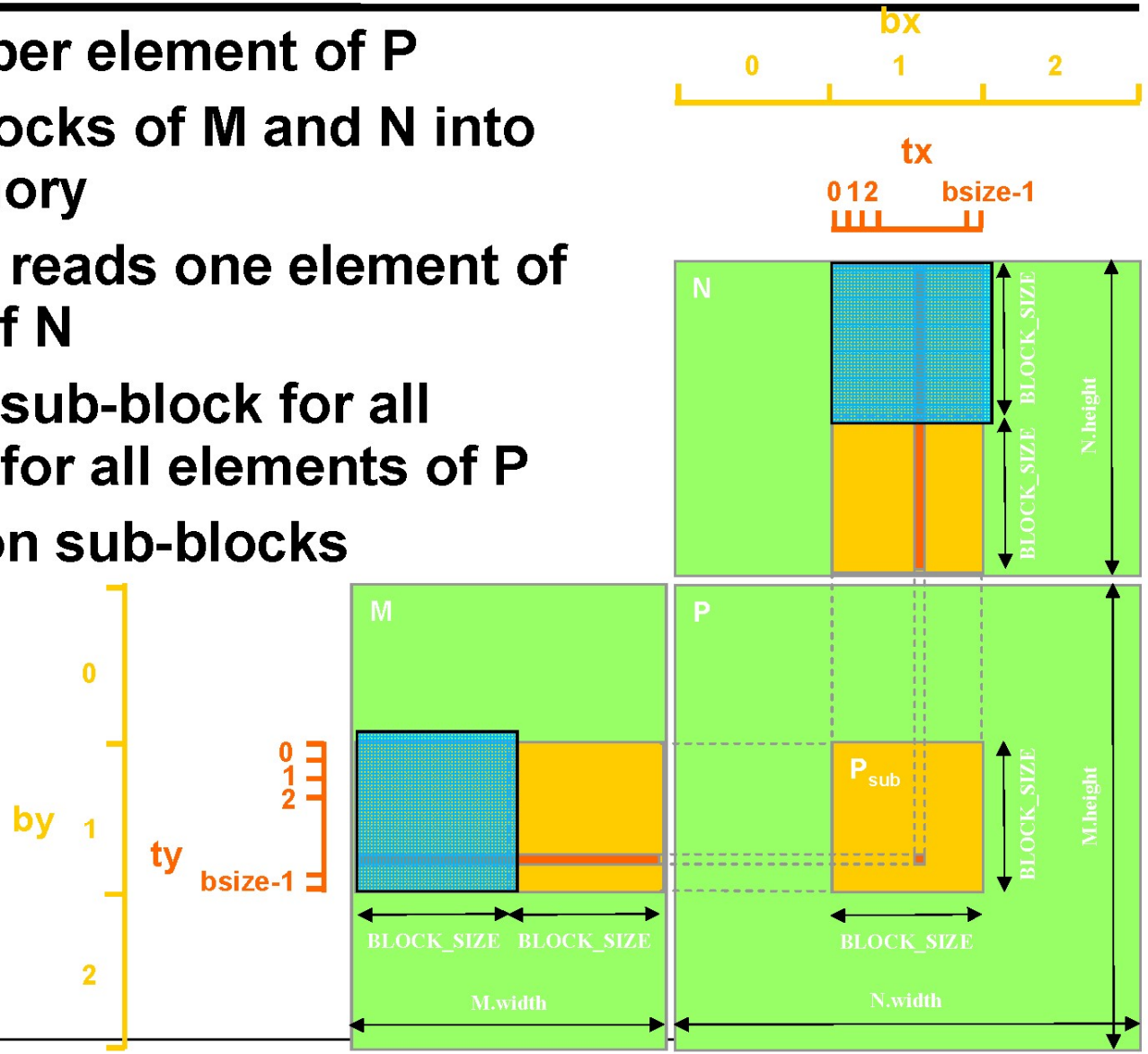
- **Have each 2D thread block to compute a $(BLOCK\_WIDTH)^2$ sub-matrix (tile) of the result matrix**
  - Each has $(BLOCK\_WIDTH)^2$ threads
- **Generate a 2D Grid of $(WIDTH/BLOCK\_WIDTH)^2$ blocks**

You still need to put a loop around the kernel call for cases where WIDTH is greater than Max grid size!



Multiply Using Several Blocks - Idea

- One thread per element of P
- Load sub-blocks of M and N into shared memory
- Each thread reads one element of M and one of N
- Reuse each sub-block for all threads, i.e. for all elements of P
- Outer loop on sub-blocks



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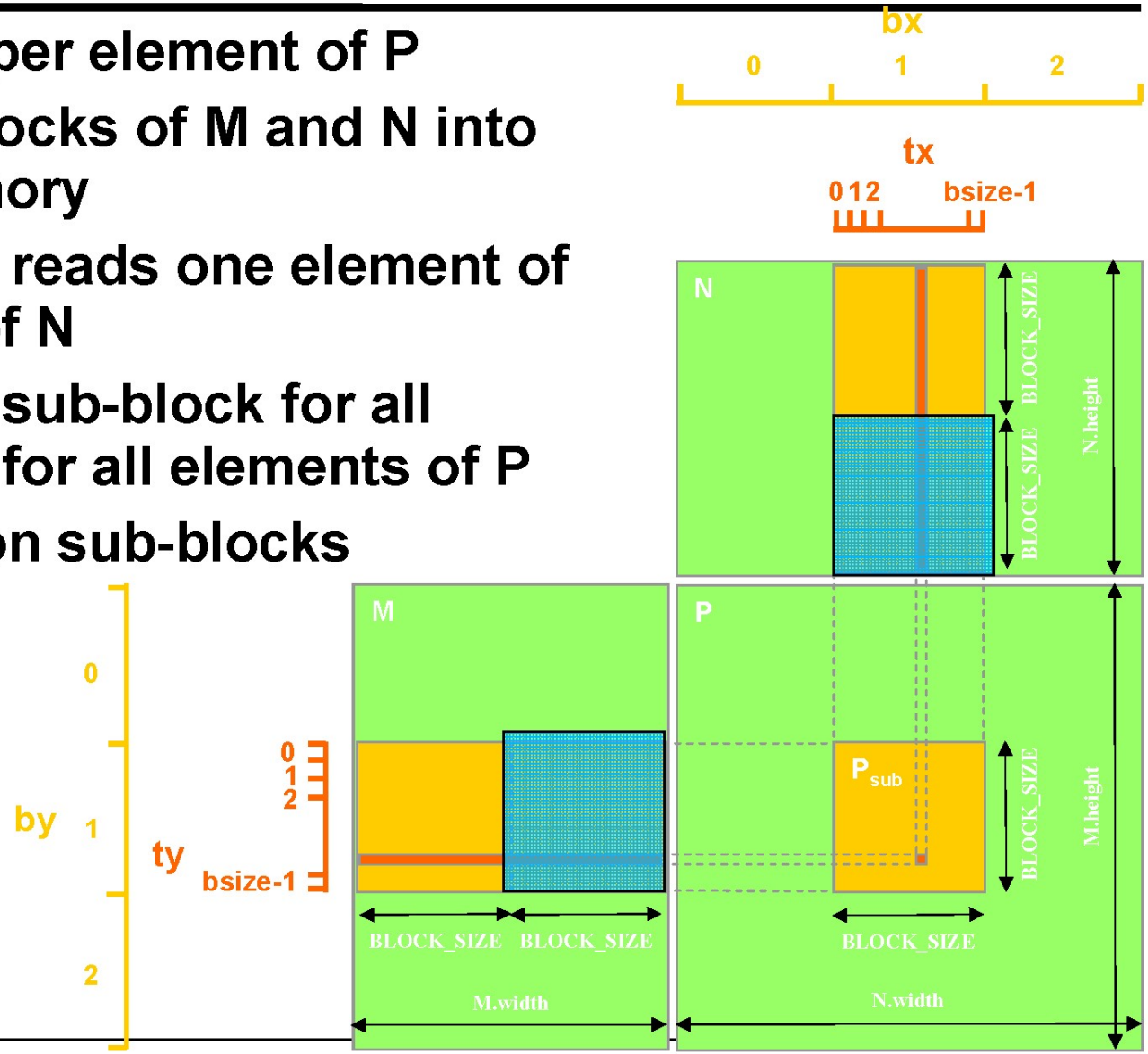


Example: Matrix Multiplication (1)

- Copy matrices to device; invoke kernel; copy result matrix back to host

```
// Matrix multiplication - Host code
// Matrix dimensions are assumed to be multiples of BLOCK_SIZE
void MatMul(const Matrix A, const Matrix B, Matrix C)
{
    // Load A and B to device memory
    Matrix d_A;
    d_A.width = d_A.stride = A.width; d_A.height = A.height;
    size_t size = A.width * A.height * sizeof(float);
    cudaMalloc((void**)&d_A.elements, size);
    cudaMemcpy(d_A.elements, A.elements, size,
               cudaMemcpyHostToDevice);
    Matrix d_B;
    d_B.width = d_B.stride = B.width; d_B.height = B.height;
    size = B.width * B.height * sizeof(float);
    cudaMalloc((void**)&d_B.elements, size);
    cudaMemcpy(d_B.elements, B.elements, size,
               cudaMemcpyHostToDevice);
```

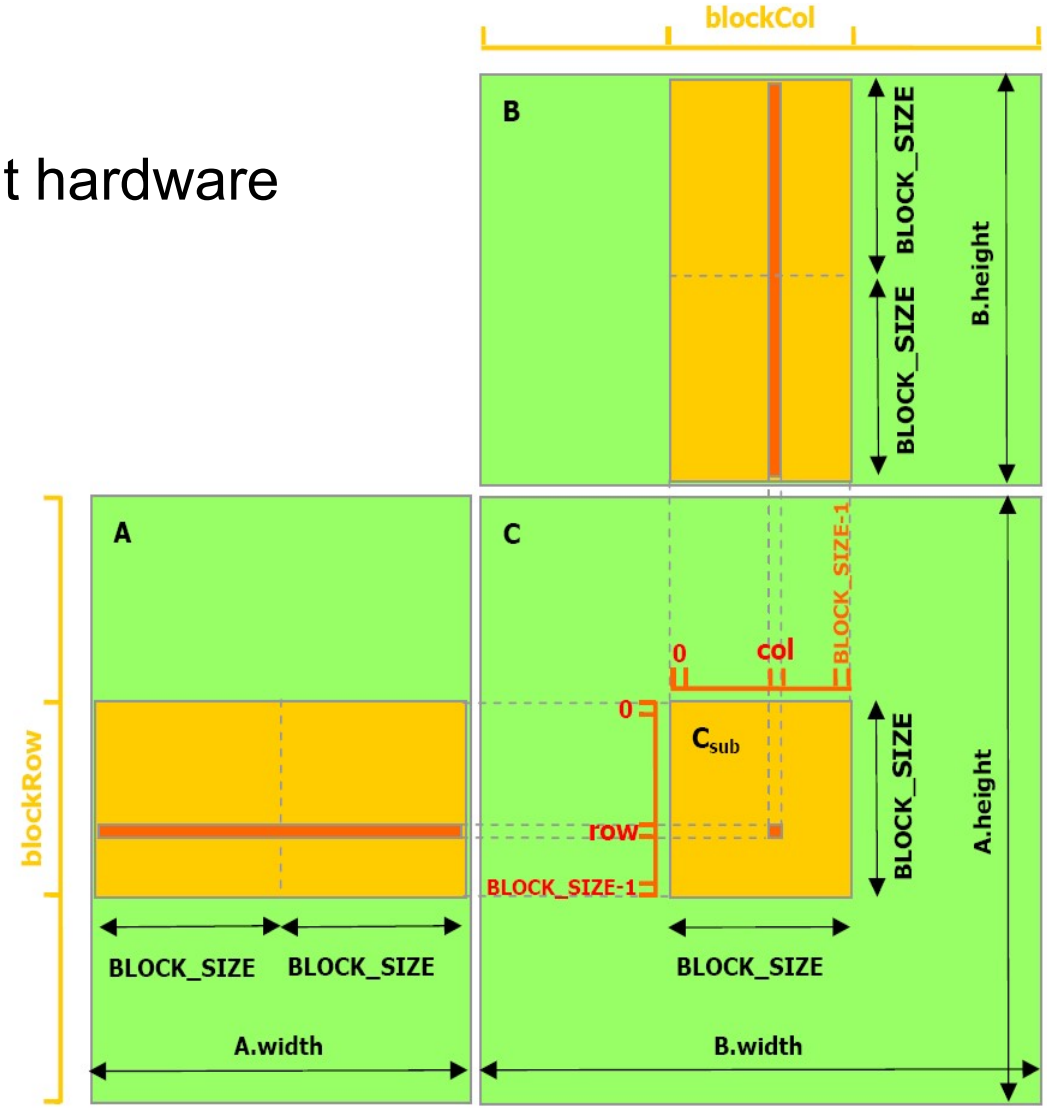
Example: Matrix Multiplication (2)

```
    // Allocate C in device memory
    Matrix d_C;
    d_C.width = d_C.stride = C.width; d_C.height = C.height;
    size = C.width * C.height * sizeof(float);
    cudaMalloc((void**)&d_C.elements, size);

    // Invoke kernel
    dim3 dimBlock(BLOCK_SIZE, BLOCK_SIZE);
    dim3 dimGrid(B.width / dimBlock.x, A.height / dimBlock.y);
    MatMulKernel<<<dimGrid, dimBlock>>>(d_A, d_B, d_C);

    // Read C from device memory
    cudaMemcpy(C.elements, d_C.elements, size,
               cudaMemcpyDeviceToHost);

    // Free device memory
    cudaFree(d_A.elements);
    cudaFree(d_B.elements);
    cudaFree(d_C.elements);
}
```

Example: Matrix Multiplication (3)

- Multiply matrix block-wise
- Set BLOCK_SIZE for efficient hardware use, e.g., to 16 on cc. 1.x or 16 or 32 on cc. 2.x +

- Maximize parallelism
  - Launch as many threads per block as block elements
  - Each thread fetches one element of block
  - Perform row * column dot products in parallel



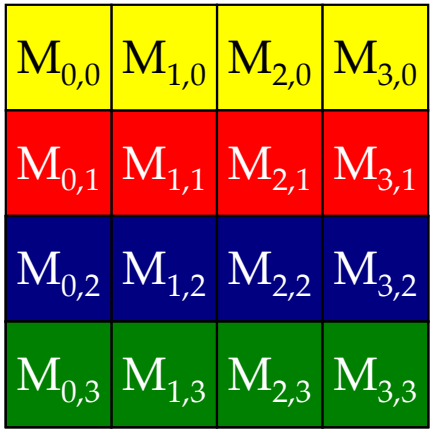
Example: Matrix Multiplication (4)

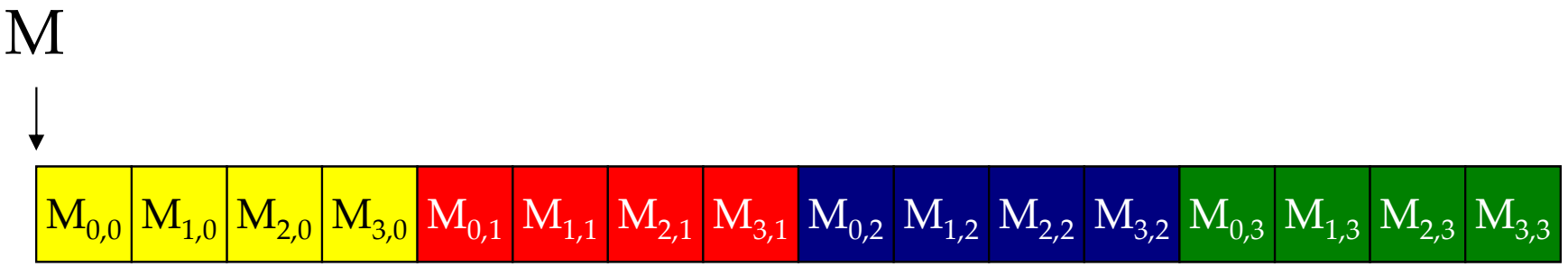
```
__global__ void MatrixMul( float *matA, float *matB, float *matC, int w )
{
      __shared__ float blockA[ BLOCK_SIZE ][ BLOCK_SIZE ];
      __shared__ float blockB[ BLOCK_SIZE ][ BLOCK_SIZE ];

      int bx = blockIdx.x; int tx = threadIdx.x;
      int by = blockIdx.y; int ty = threadIdx.y;

      int col = bx * BLOCK_SIZE + tx;
      int row = by * BLOCK_SIZE + ty;

      float out = 0.0f;
      for ( int m = 0; m < w / BLOCK_SIZE; m++ ) {

          blockA[ ty ][ tx ] = matA[ row * w +   m * BLOCK_SIZE + tx       ];
          blockB[ ty ][ tx ] = matB[ col     + ( m * BLOCK_SIZE + ty ) * w ];
          __syncthreads();

          for ( int k = 0; k < BLOCK_SIZE; k++ ) {
              out += blockA[ ty ][ k ] * blockB[ k ][ tx ];
          }
          __syncthreads();
      }

      matC[ row * w + col ] = out;
}
```

Caveat: for brevity, this code assumes matrix sizes are a multiple of the block size (either because they really are, or because padding is used; otherwise guard code would need to be added)

What About Memory Performance? (more to come later…)

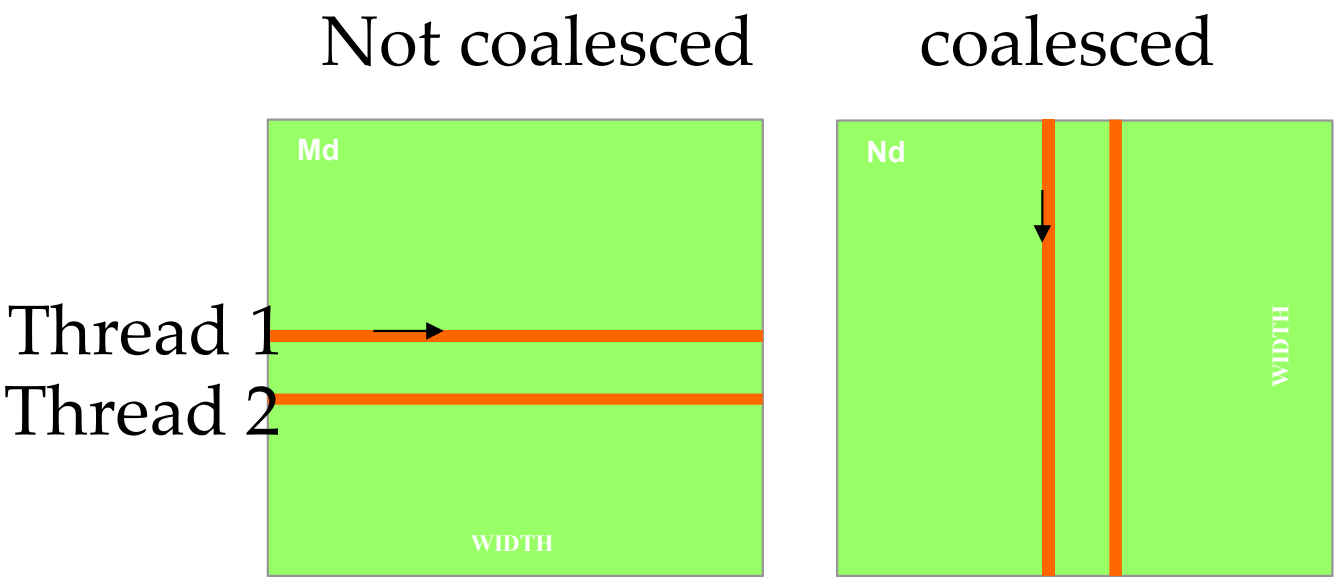
Memory Layout of a Matrix in C





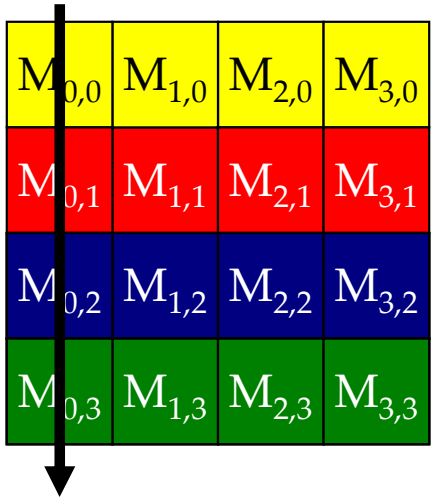
Memory Coalescing

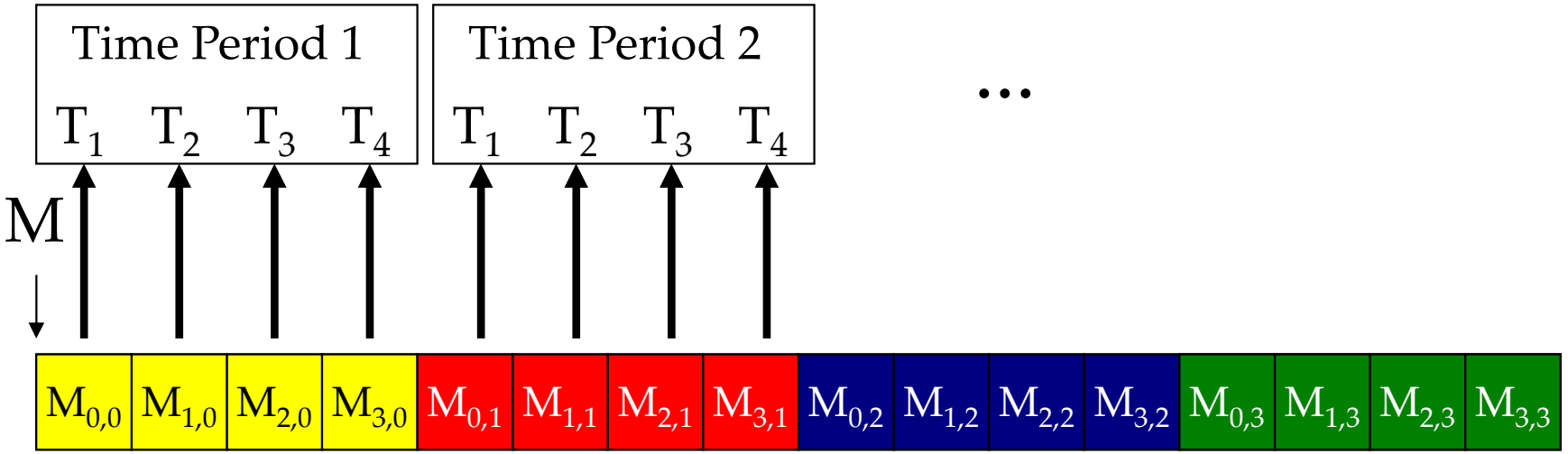
- When accessing global memory, peak performance utilization occurs when all threads in a half warp (full warp on Fermi) access continuous memory locations.
- Requirements relaxed on >=1.2 devices; L1 cache on Fermi!



Memory Layout of a Matrix in C

Access direction in Kernel code





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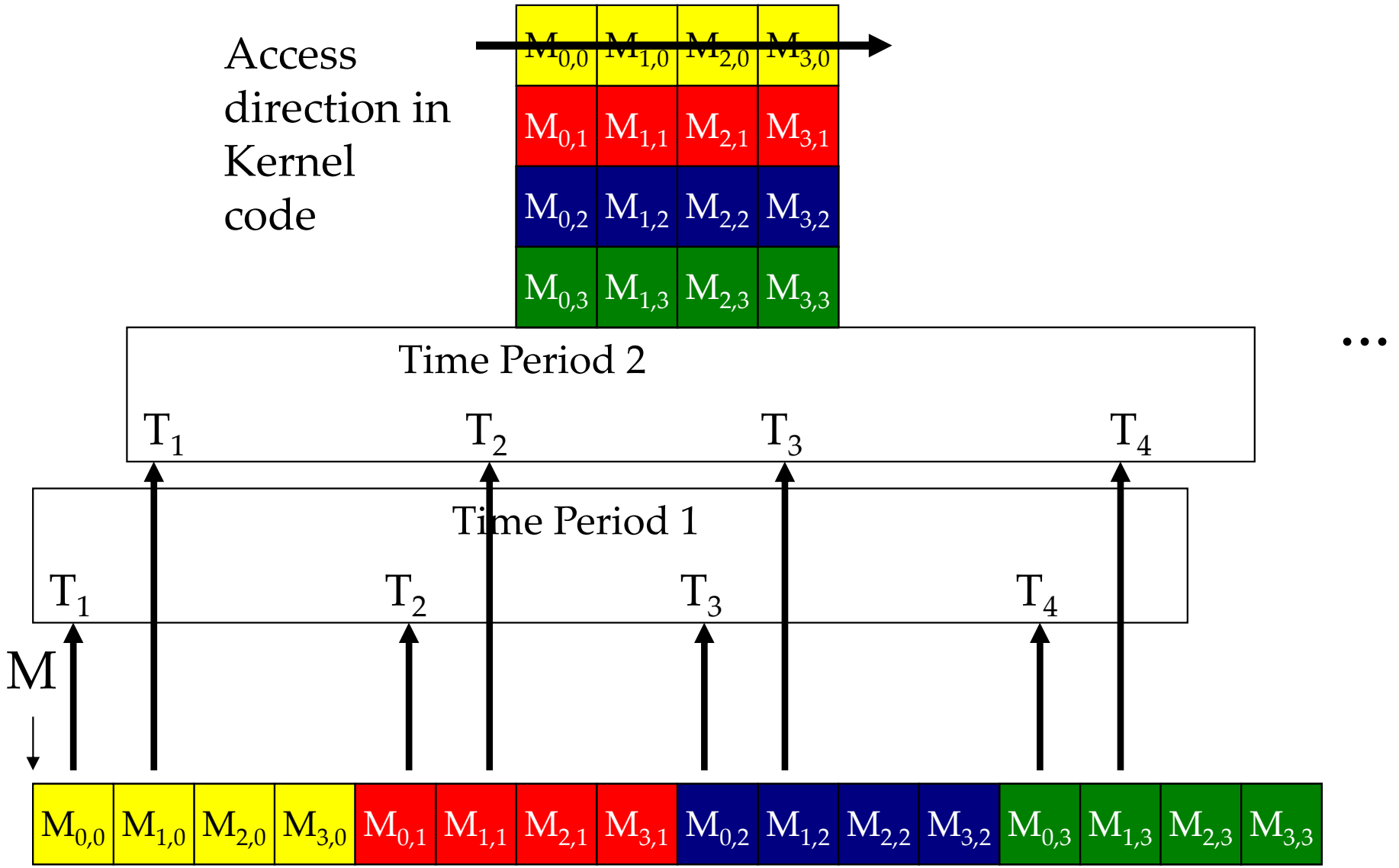

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Thank you.