

CS 380 - GPU and GPGPU Programming

Lecture 17: GPU Texturing, Pt. 3

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Reading Assignment #10 (until Nov 6)

Read (required):

- MIP-Map Level Selection for Texture Mapping

<https://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=765326>

Read (optional):

- Vulkan Tutorial

<https://vulkan-tutorial.com>



Quiz #2: Nov 9

Organization

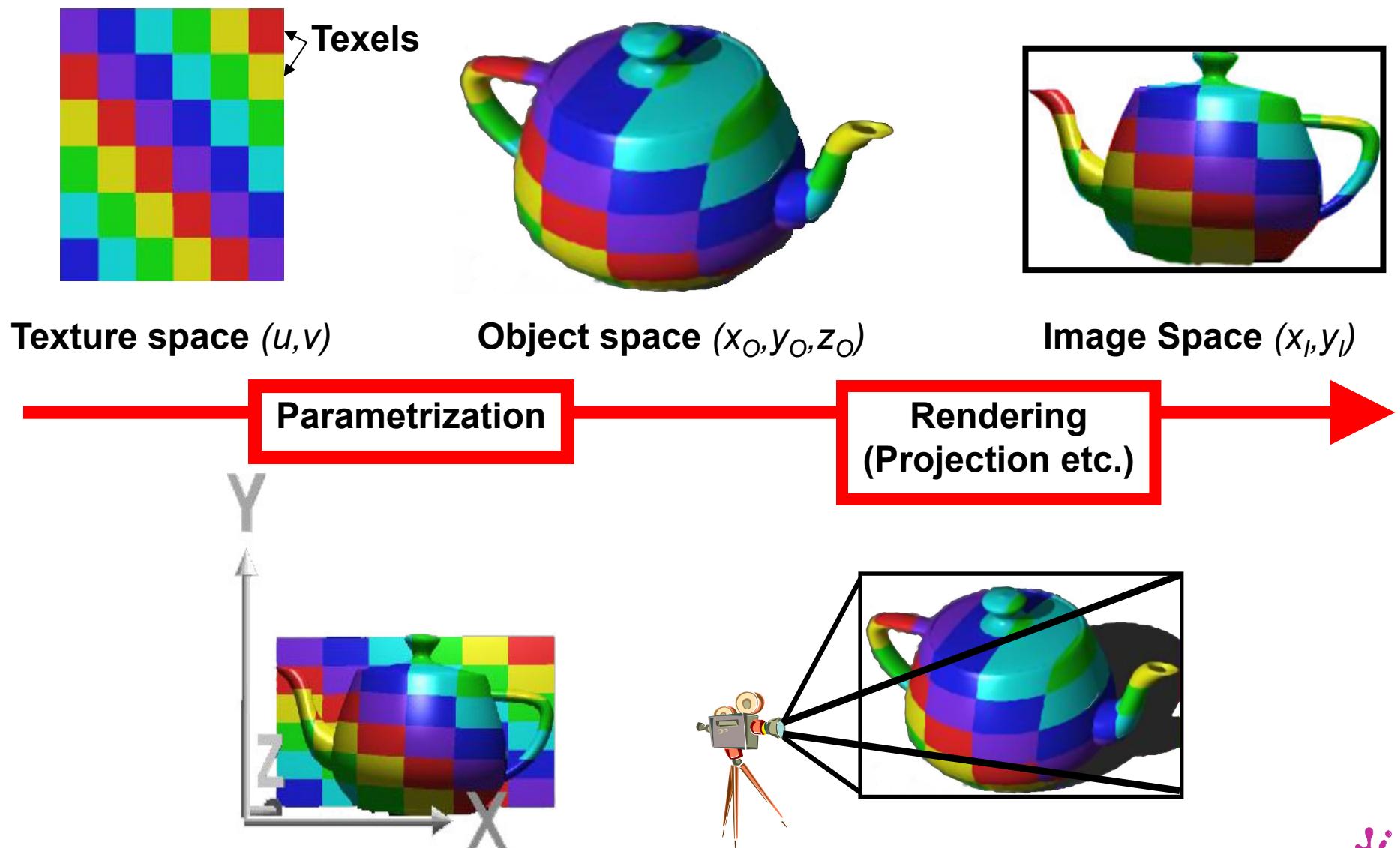
- First 30 min of lecture
- No material (book, notes, ...) allowed

Content of questions

- Lectures (both actual lectures and slides)
- Reading assignments
- Programming assignments (algorithms, methods)
- Solve short practical examples

GPU Texturing

Texturing: General Approach



Interpolation #1



Interpolation Type + Purpose #1: **Interpolation of Texture Coordinates**

(Linear / Rational-Linear Interpolation)



Homogeneous Coordinates (1)

Projective geometry

- (Real) projective spaces \mathbf{RP}^n :
Real projective line \mathbf{RP}^1 , real projective plane \mathbf{RP}^2 , ...
- A point in \mathbf{RP}^n is a line through the origin (i.e., all the scalar multiples of the same vector) in an $(n+1)$ -dimensional (real) vector space



Homogeneous coordinates of 2D projective point in \mathbf{RP}^2

- Coordinates differing only by a non-zero factor λ map to the same point
 $(\lambda x, \lambda y, \lambda)$ dividing out the λ gives $(x, y, 1)$, corresponding to (x, y) in \mathbb{R}^2
- Coordinates with last component = 0 map to “points at infinity”
 $(\lambda x, \lambda y, 0)$ division by last component not allowed; but again this is the same point if it only differs by a scalar factor, e.g., this is the same point as $(x, y, 0)$

Texture Mapping

2D (3D) Texture Space

| Texture Transformation

2D Object Parameters

| Parameterization

3D Object Space

| Model Transformation

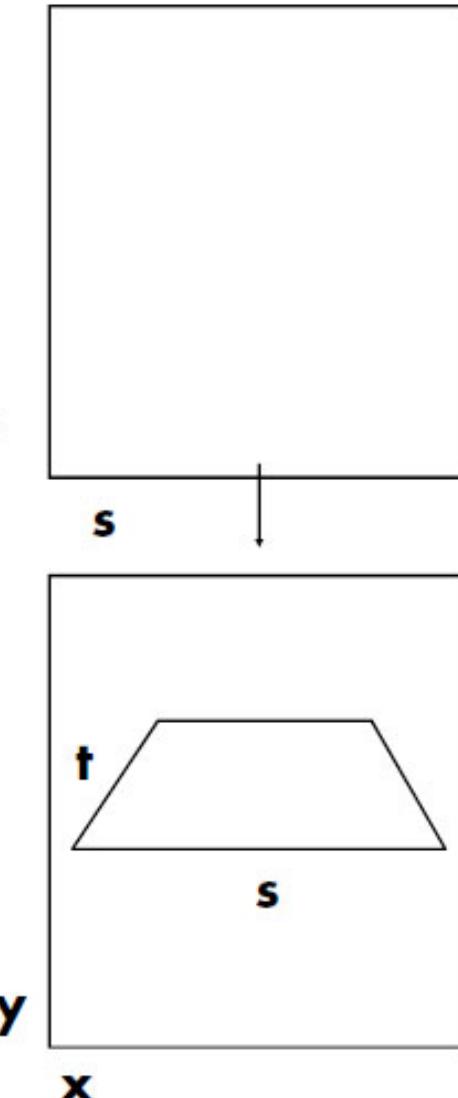
3D World Space

| Viewing Transformation

3D Camera Space

| Projection

2D Image Space



Perspective-correct linear interpolation

Only projected values interpolate correctly, so project A

- Linearly interpolate A_1/w_1 and A_2/w_2

Also interpolate $1/w_1$ and $1/w_2$

- These also interpolate linearly in screen space

Divide interpolants at each sample point to recover A

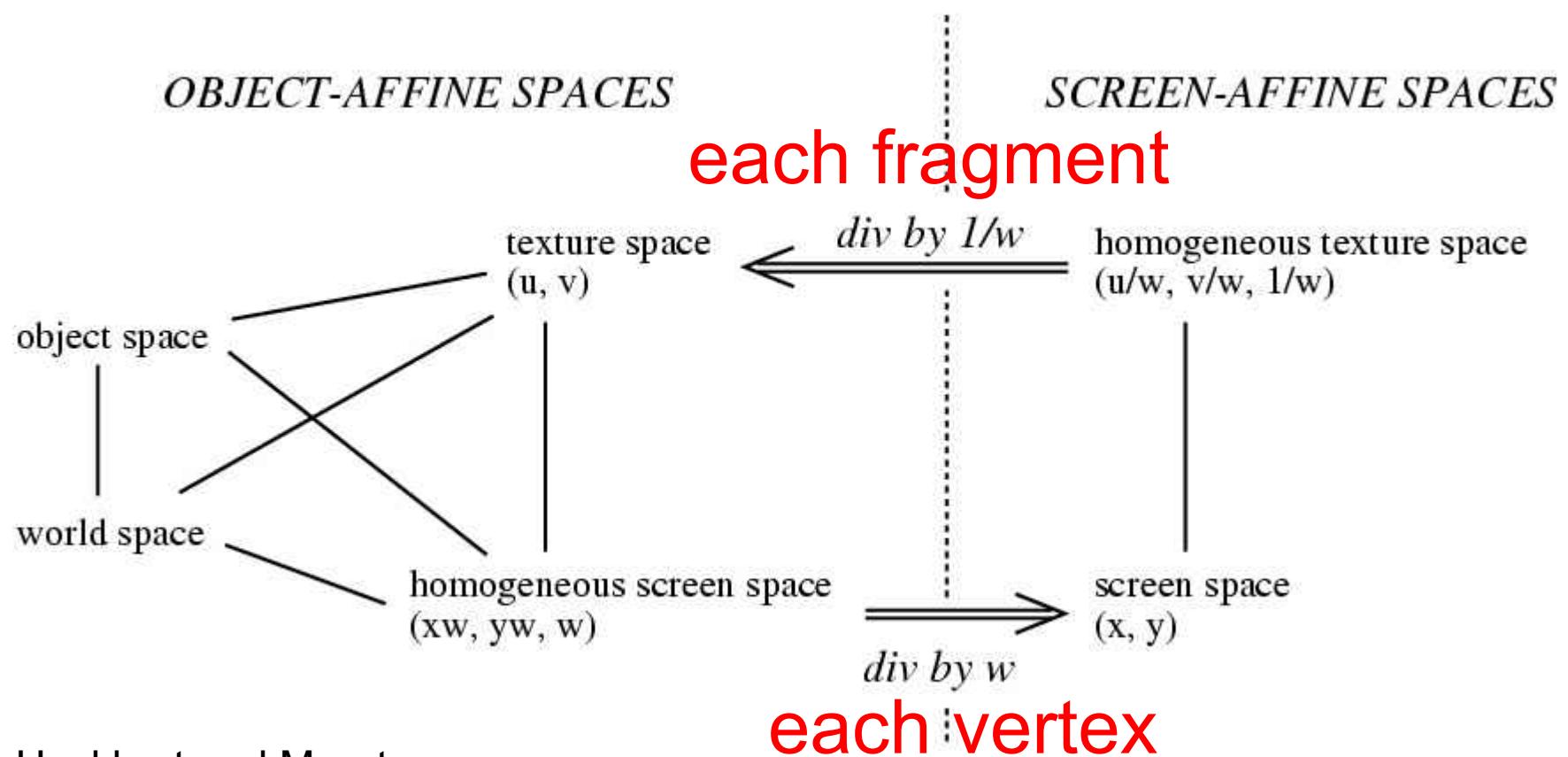
- $(A/w) / (1/w) = A$
- Division is expensive (more than add or multiply), so
 - Recover w for the sample point (reciprocate), and
 - Multiply each projected attribute by w

Barycentric triangle parameterization:

$$A = \frac{aA_1/w_1 + bA_2/w_2 + cA_3/w_3}{a/w_1 + b/w_2 + c/w_3} \quad a + b + c = 1$$

Perspective Texture Mapping

- Solution: interpolate $(s/w, t/w, 1/w)$
- $(s/w) / (1/w) = s$ etc. at every fragment



Heckbert and Moreton



Perspective-Correct Interpolation Recipe

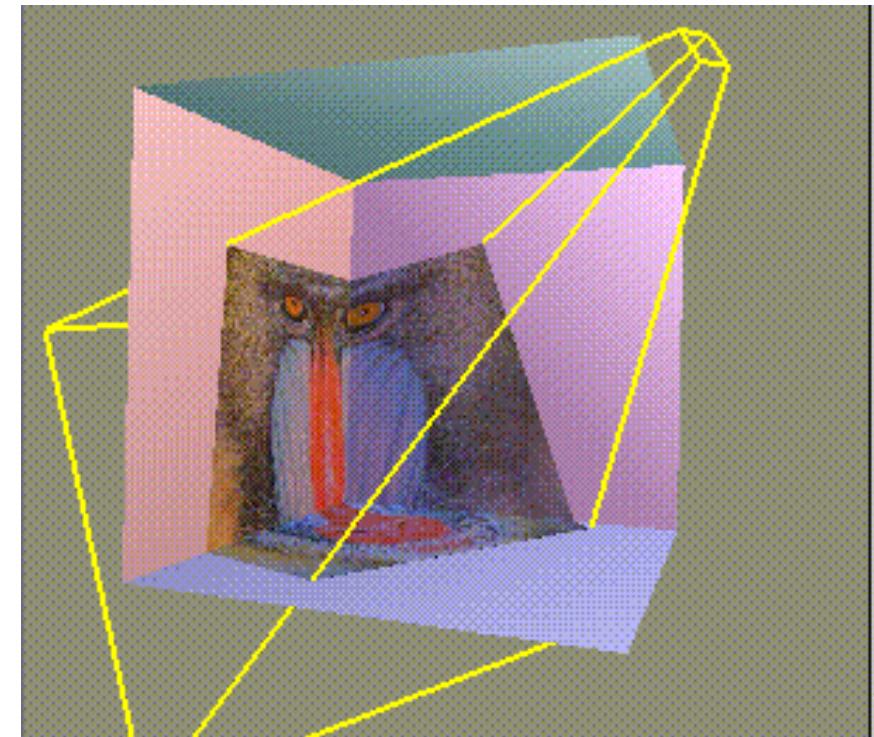


$$r_i(x, y) = \frac{r_i(x, y)/w(x, y)}{1/w(x, y)}$$

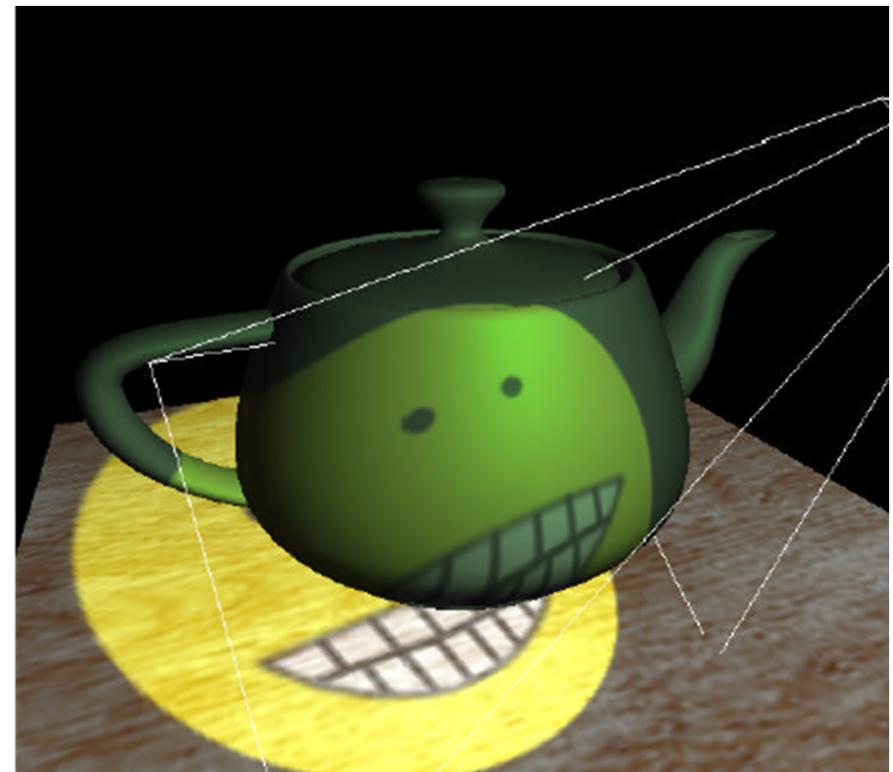
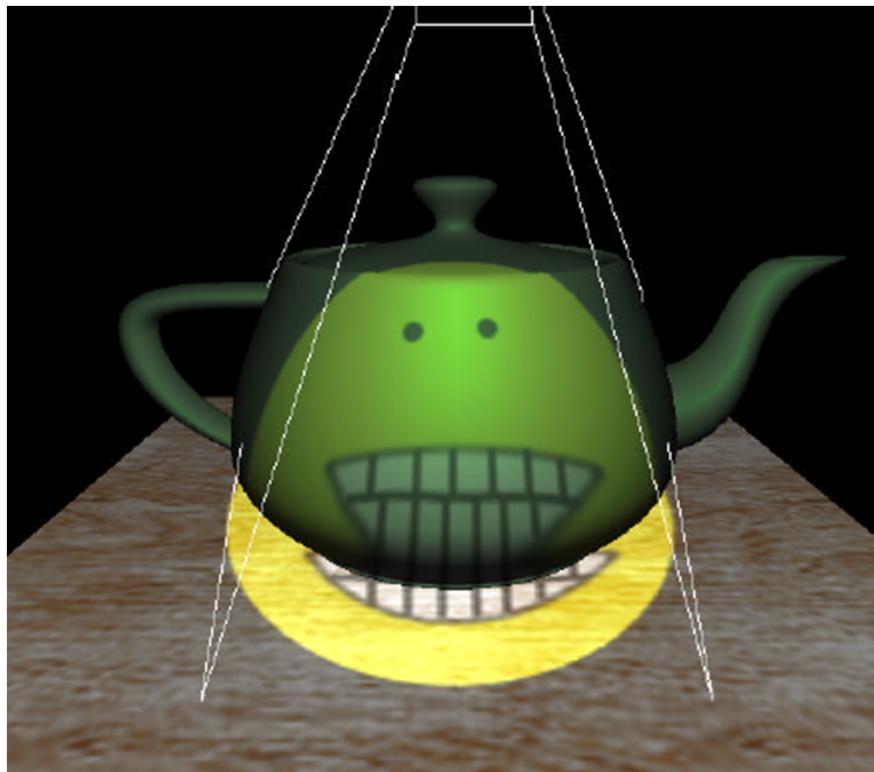
- (1) Associate a record containing the n parameters of interest (r_1, r_2, \dots, r_n) with each vertex of the polygon.
- (2) For each vertex, transform object space coordinates to homogeneous screen space using 4×4 object to screen matrix, yielding the values (xw, yw, zw, w) .
- (3) Clip the polygon against plane equations for each of the six sides of the viewing frustum, linearly interpolating all the parameters when new vertices are created.
- (4) At each vertex, divide the homogeneous screen coordinates, the parameters r_i , and the number 1 by w to construct the variable list $(x, y, z, s_1, s_2, \dots, s_{n+1})$, where $s_i = r_i/w$ for $i \leq n$, $s_{n+1} = 1/w$.
- (5) Scan convert in screen space by linear interpolation of all parameters, at each pixel computing $r_i = s_i/s_{n+1}$ for each of the n parameters; use these values for shading.

Projective Texture Mapping

- Want to simulate a beamer
 - ... or a flashlight, or a slide projector
- Precursor to shadows
- Interesting mathematics:
2 perspective projections involved!
- Easy to program!



Projective Texture Mapping



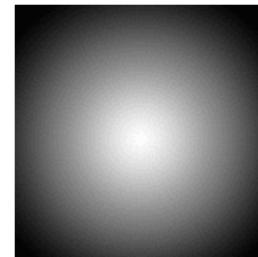
Projective Shadows in Doom 3



- What about **homogeneous** texture coords?
- Need to do perspective divide also for projector!
 - $(s, t, q) \rightarrow (s/q, t/q)$ for every fragment
- How does OpenGL do that?
 - Needs to be perspective correct as well!
 - Trick: interpolate $(s/w, t/w, r/w, q/w)$
 - $(s/w) / (q/w) = s/q$ etc. at every fragment
- Remember: s, t, r, q are equivalent to x, y, z, w in projector space! $\rightarrow r/q = \text{projector depth!}$



- Apply multiple textures in one pass
- *Integral* part of programmable shading
 - e.g. diffuse texture map + gloss map
 - e.g. diffuse texture map + light map
- Performance issues
 - How many textures are free?
 - How many are available

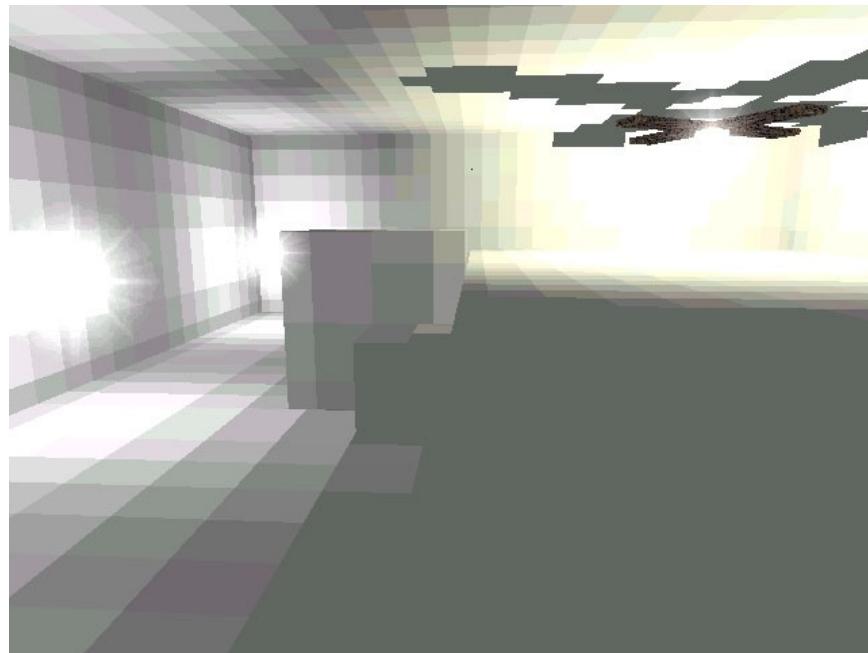


Example: Light Mapping

- Used in virtually every commercial game
- Precalculate diffuse lighting on static objects
 - Only low resolution necessary
 - Diffuse lighting is view independent!
- Advantages:
 - No runtime lighting necessary
 - VERY fast!
 - Can take global effects (shadows, color bleeds) into account



Light Mapping



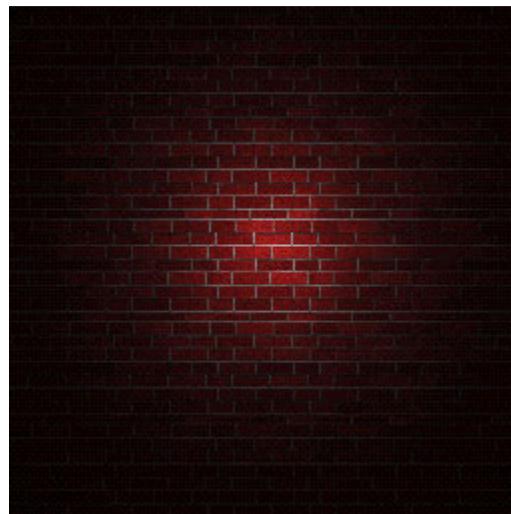
Original LM texels



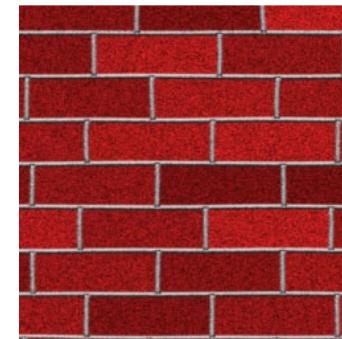
Bilinear Filtering



■ Why premultiplication is bad...



Full Size Texture
(with Lightmap)



Tiled Surface Texture
plus Lightmap

→ use tileable surface textures and low resolution lightmaps



Light Mapping



Original scene



Light-mapped



Example: Light Mapping

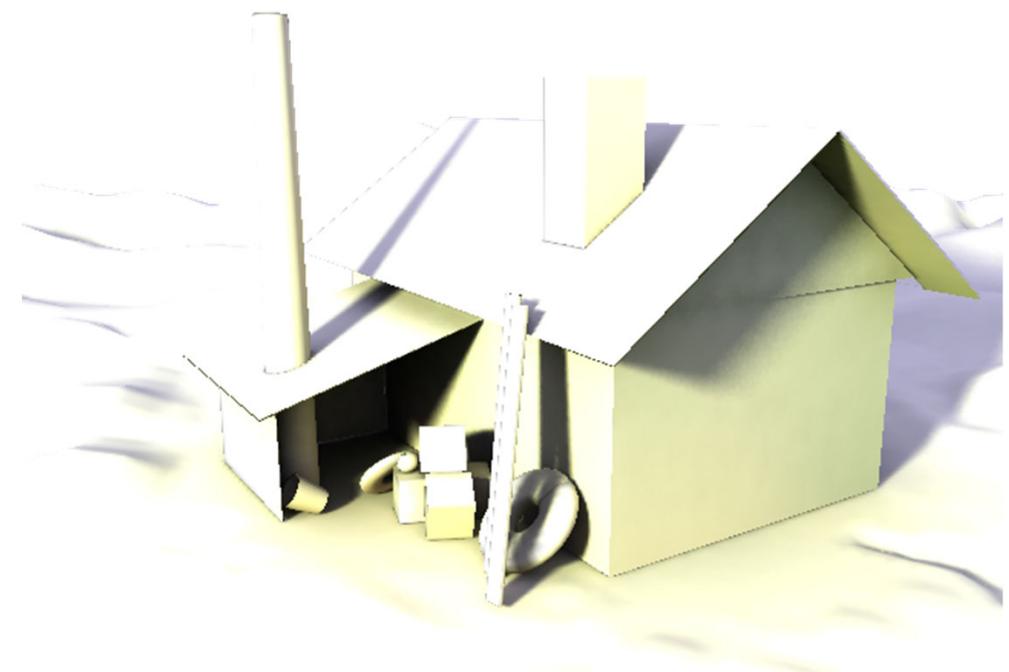
- Precomputation based on non-realtime methods
 - Radiosity
 - Ray tracing
 - Monte Carlo Integration
 - Path tracing
 - Photon mapping



Light Mapping



Lightmap



mapped



Light Mapping



Original scene

Light-mapped



Interpolation #2



Interpolation Type + Purpose #2: **Interpolation of Samples in Texture Space**

(Multi-Linear Interpolation)

Types of Textures

- Spatial layout
 - Cartesian grids: 1D, 2D, 3D, 2D_ARRAY, ...
 - Cube maps, ...
- Formats (too many), e.g. OpenGL
 - GL_LUMINANCE16_ALPHA16
 - GL_RGB8, GL_RGBA8, ...: integer texture formats
 - GL_RGB16F, GL_RGBA32F, ...: float texture formats
 - compressed formats, high dynamic range formats, ...
- External (CPU) format vs. internal (GPU) format
 - OpenGL driver converts from external to internal



Magnification (Bi-linear Filtering Example)



Original image



Nearest neighbor

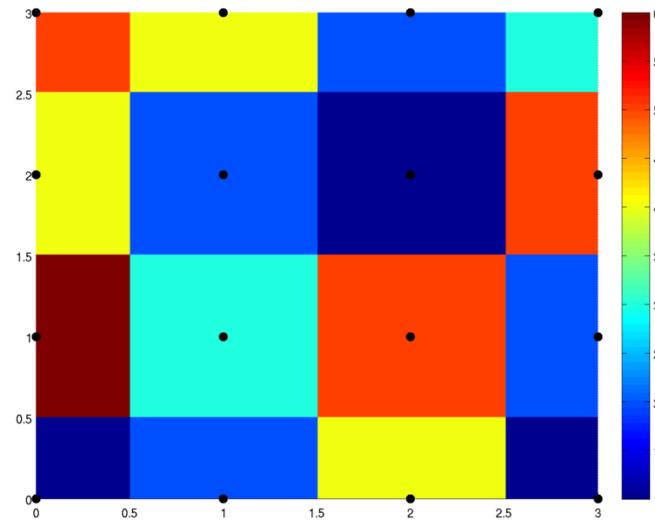


Bi-linear filtering

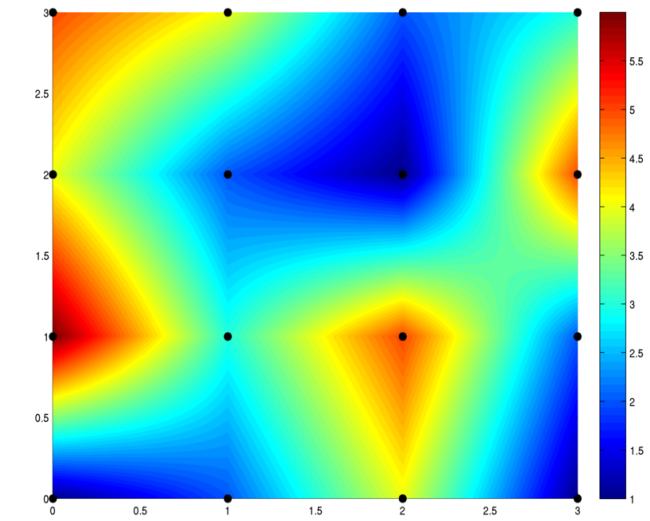




Nearest-Neighbor vs. Bi-Linear Interpolation

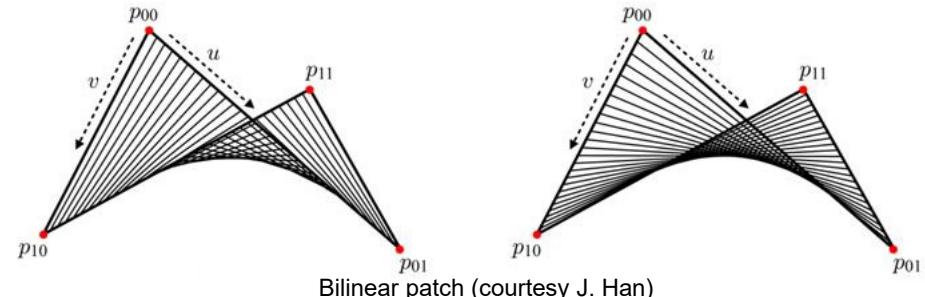


nearest-neighbor



wikipedia

bi-linear

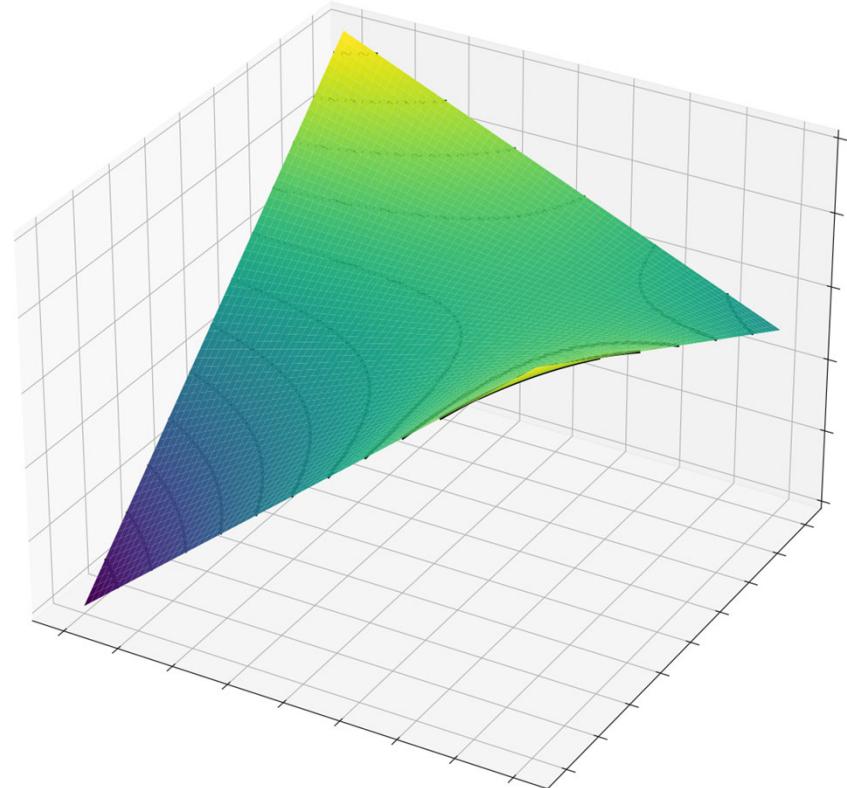
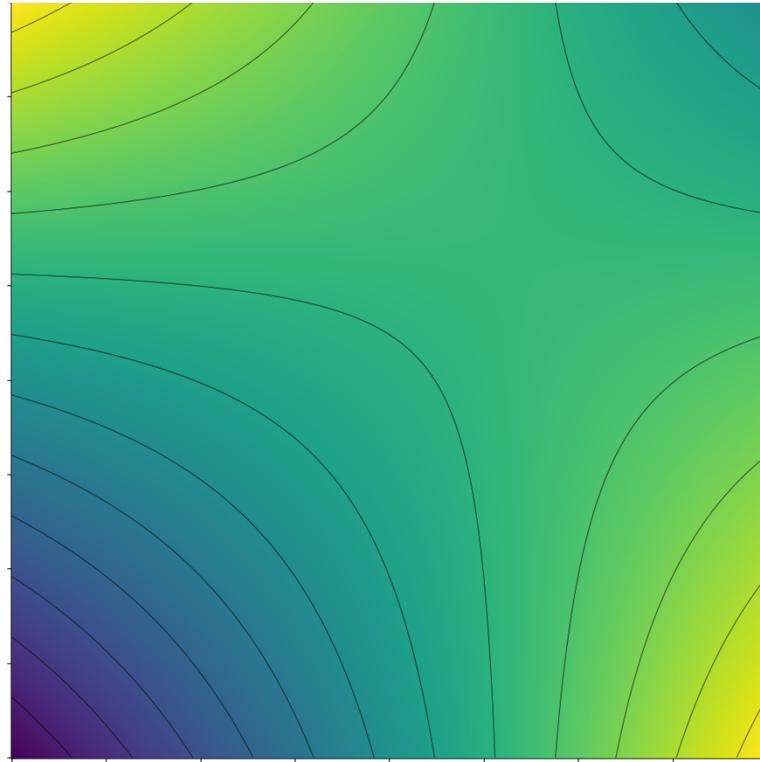




Bi-Linear Interpolation

Consider area between 2x2 adjacent samples (e.g., pixel centers)

Example #2: 1 at top-left and bottom-right, 0 at bottom-left, 0.5 at top-right





Bi-Linear Interpolation

Consider area between 2x2 adjacent samples (e.g., pixel centers):

Given any (fractional) position

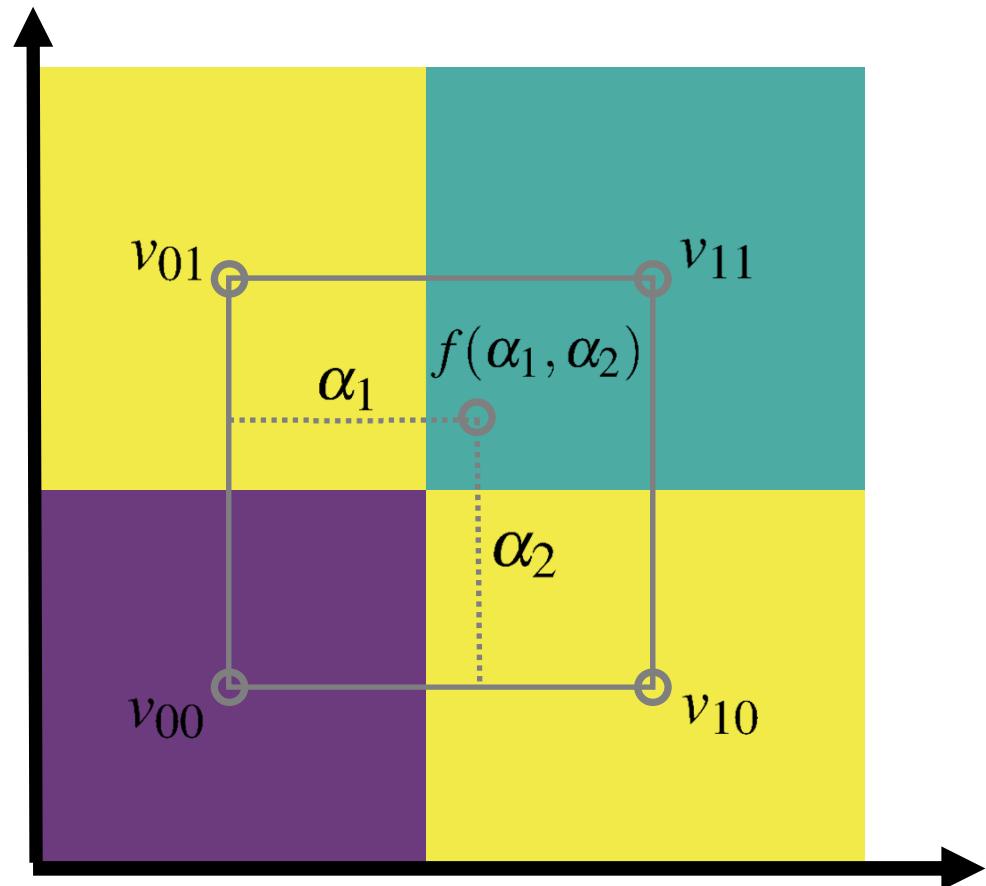
$$\alpha_1 := x_1 - \lfloor x_1 \rfloor \quad \alpha_1 \in [0.0, 1.0]$$

$$\alpha_2 := x_2 - \lfloor x_2 \rfloor \quad \alpha_2 \in [0.0, 1.0]$$

and 2x2 sample values

$$\begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix}$$

Compute: $f(\alpha_1, \alpha_2)$





Bi-Linear Interpolation

Consider area between 2x2 adjacent samples (e.g., pixel centers):

Given any (fractional) position

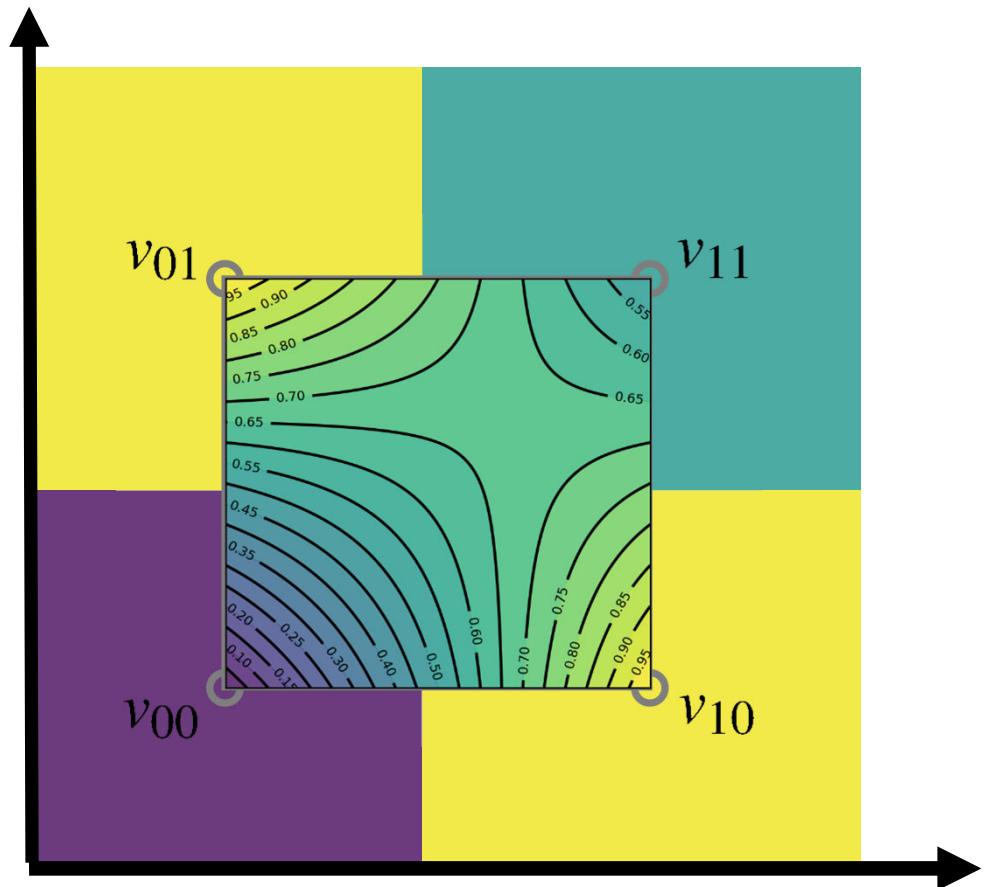
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$$\alpha_2 := x_2 - \lfloor x_2 \rfloor \quad \alpha_2 \in [0.0, 1.0]$$

and 2x2 sample values

$$\begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix}$$

Compute: $f(\alpha_1, \alpha_2)$





Bi-Linear Interpolation

Weights in 2x2 format:

$$\begin{bmatrix} \alpha_2 \\ (1 - \alpha_2) \end{bmatrix} \begin{bmatrix} (1 - \alpha_1) & \alpha_1 \end{bmatrix} = \begin{bmatrix} (1 - \alpha_1)\alpha_2 & \alpha_1\alpha_2 \\ (1 - \alpha_1)(1 - \alpha_2) & \alpha_1(1 - \alpha_2) \end{bmatrix}$$

Interpolate function at (fractional) position (α_1, α_2) :

$$f(\alpha_1, \alpha_2) = [\alpha_2 \quad (1 - \alpha_2)] \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \alpha_1) \\ \alpha_1 \end{bmatrix}$$



Bi-Linear Interpolation

Interpolate function at (fractional) position (α_1, α_2) :

$$\begin{aligned} f(\alpha_1, \alpha_2) &= [\alpha_2 \quad (1 - \alpha_2)] \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \alpha_1) \\ \alpha_1 \end{bmatrix} \\ &= [\alpha_2 \quad (1 - \alpha_2)] \begin{bmatrix} (1 - \alpha_1)v_{01} + \alpha_1 v_{11} \\ (1 - \alpha_1)v_{00} + \alpha_1 v_{10} \end{bmatrix} \\ &= [\alpha_2 v_{01} + (1 - \alpha_2)v_{00} \quad \alpha_2 v_{11} + (1 - \alpha_2)v_{10}] \begin{bmatrix} (1 - \alpha_1) \\ \alpha_1 \end{bmatrix} \end{aligned}$$



Bi-Linear Interpolation

Interpolate function at (fractional) position (α_1, α_2) :

$$\begin{aligned} f(\alpha_1, \alpha_2) &= [\alpha_2 \quad (1 - \alpha_2)] \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \alpha_1) \\ \alpha_1 \end{bmatrix} \\ &= (1 - \alpha_1)(1 - \alpha_2)v_{00} + \alpha_1(1 - \alpha_2)v_{10} + (1 - \alpha_1)\alpha_2v_{01} + \alpha_1\alpha_2v_{11} \\ &= v_{00} + \alpha_1(v_{10} - v_{00}) + \alpha_2(v_{01} - v_{00}) + \alpha_1\alpha_2(v_{00} + v_{11} - v_{10} - v_{01}) \end{aligned}$$



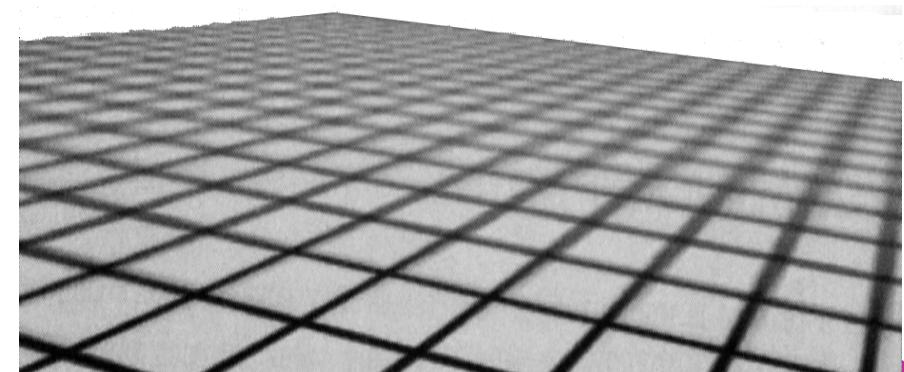
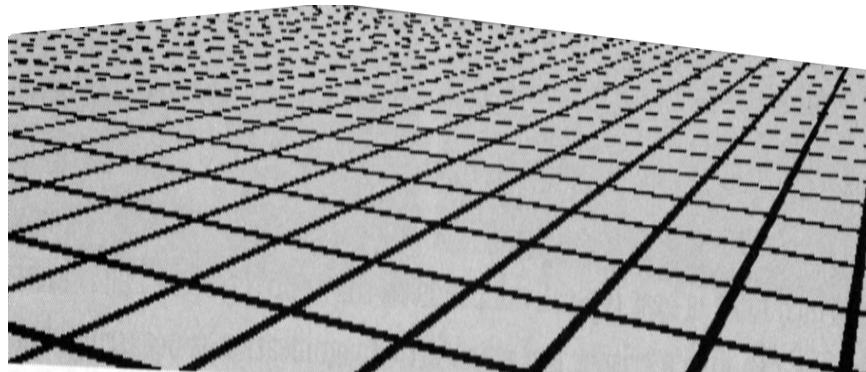
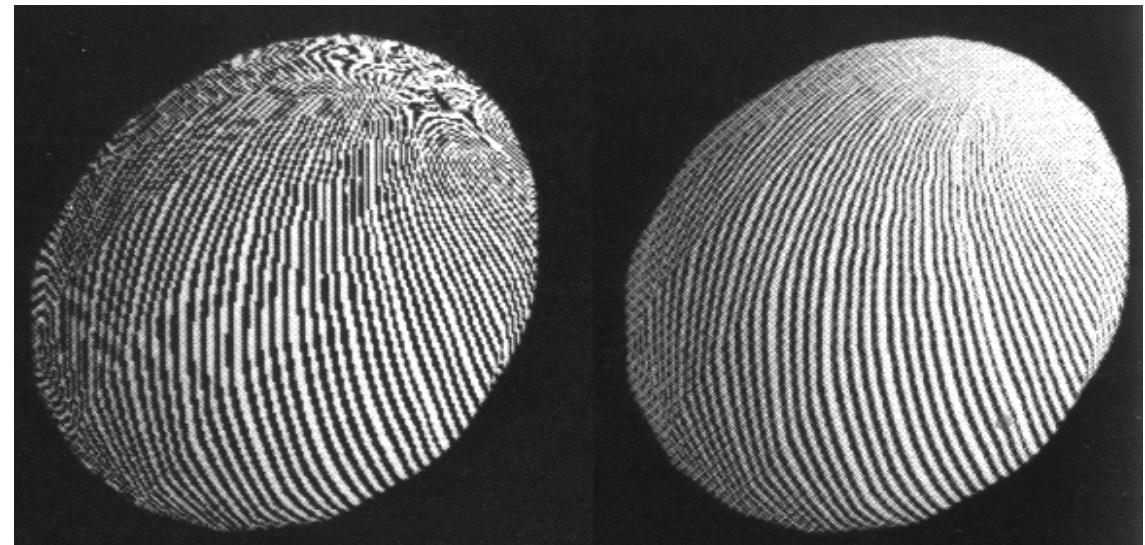
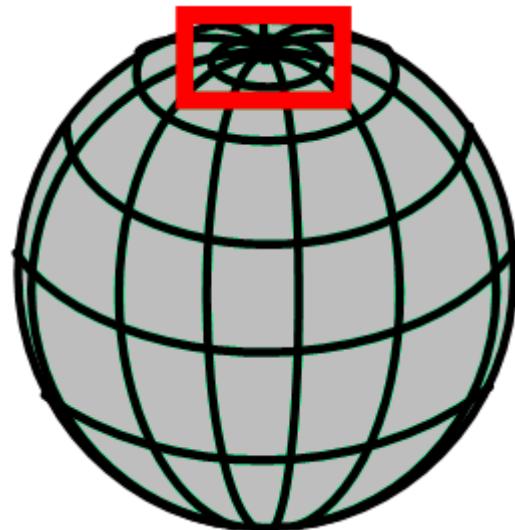
REALLY IMPORTANT:

this is a different thing (for a different purpose)
than the linear (or, in perspective, rational-linear)
interpolation of texture coordinates!!

Texture Minification

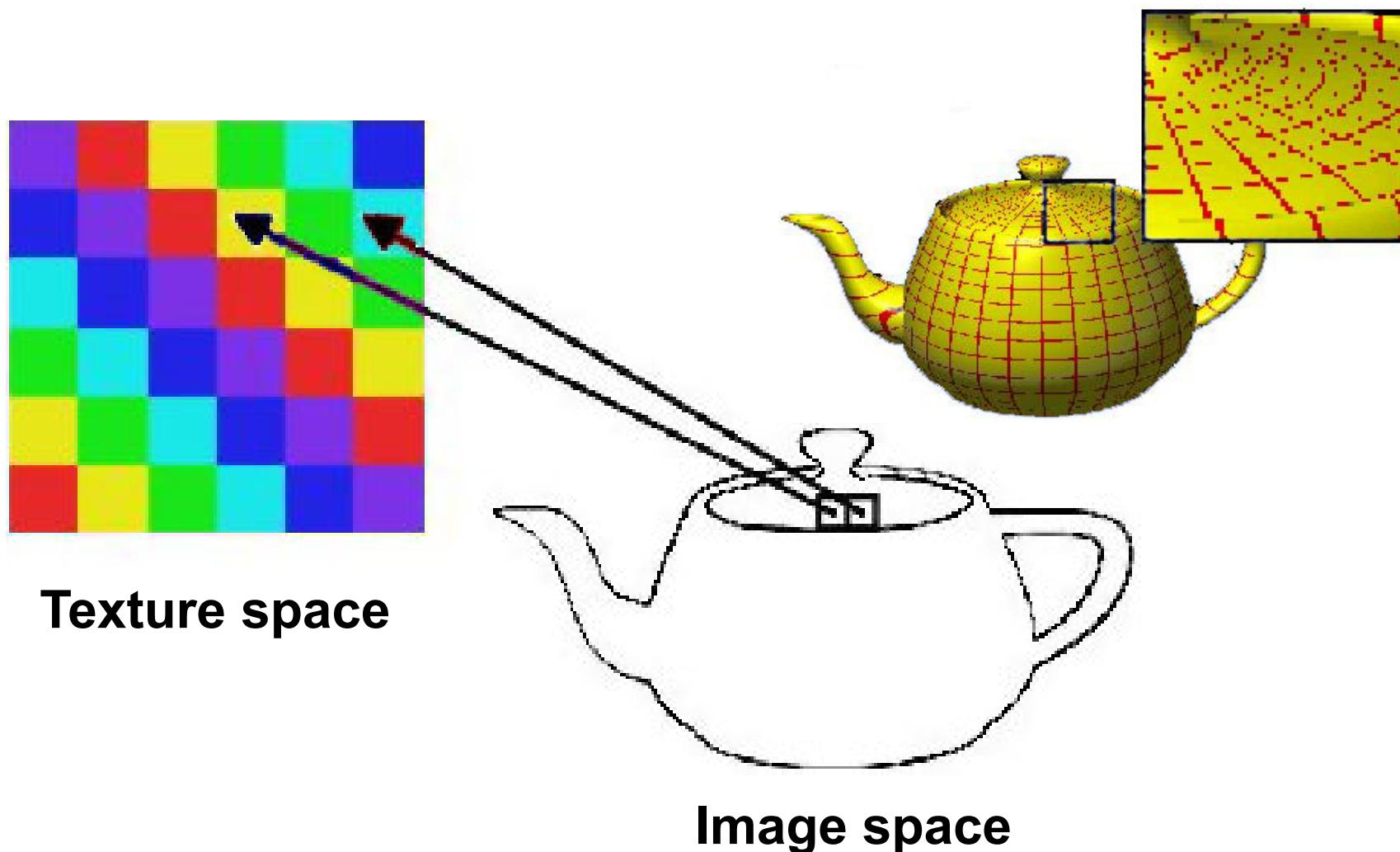
Texture Aliasing: Minification

- Problem: One pixel in image space covers many texels



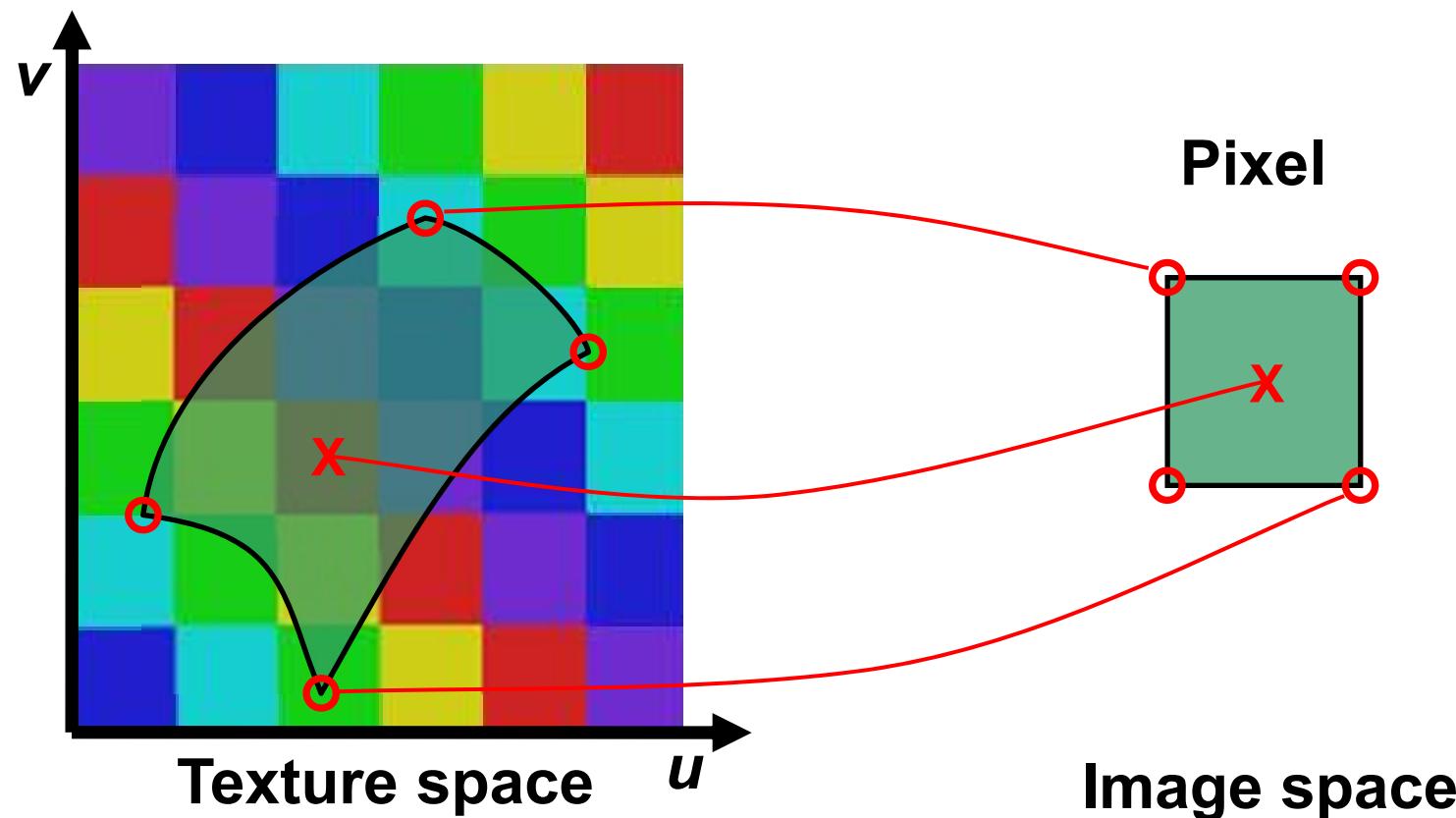
Texture Aliasing: Minification

- Caused by *undersampling*: texture information is lost



Texture Anti-Aliasing: Minification

- A good pixel value is the weighted mean of the pixel area projected into texture space



Thank you.