# Univariate Time Series Data and Model Card

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This report provides an automated, comprehensive analysis of univariate time series data. Generated by Cardtale, it explores basic aspects and potential challenges in your data to support informed decision-making and modeling choices.

**Generated:** 2024-11-10 11:24

Series Name: M1

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Other aspects were explored but omitted from the final report:

### **Change Detection**

No change point was found according to offline change detection methods

### **Data Overview**

This section examines the core characteristics and statistical properties of the time series. Understanding these attributes is important for assessing data quality and

gaining a preliminary context. We explore the temporal structure, summary statistics, and distribution patterns to create a baseline understanding of your data.

#### **Time Series Plot**

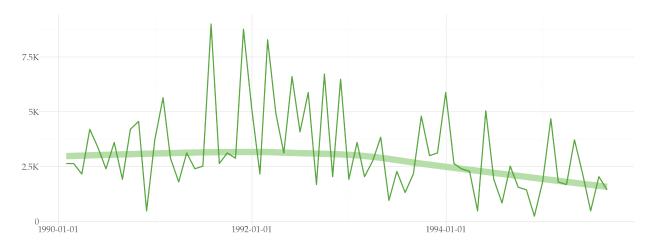


Figure 1: Time series line plot.

- A total of 68 observations which span from January 1990 to August 1995. These are collected with a monthly sampling frequency.
- The data ranges from a minimum of 240 to a maximum of 9000, starting in 2640 and ending in 1440 during the observed period. The average growth percentage per observation is 57.75% (median growth equal to -7.69%), with an average value of 3185.29. There are no missing values in the time series.

## Trend, Seasonality, and Residuals

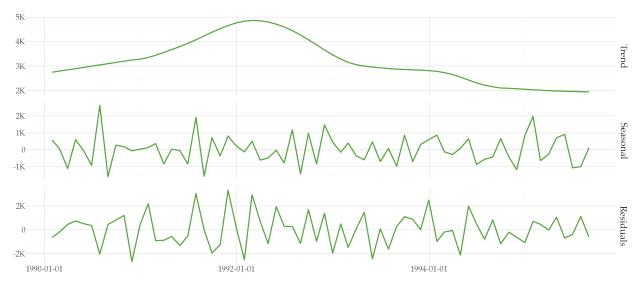


Figure 2: Seasonal, Trend, and Residuals components after decomposition on a monthly frequency using the STL (Season-Trend decomposition using LOESS) method.

• The trend strength (ranges from 0 to 1) is 0.35. The following tests indicate that the time series is non-stationary in trend or level: KPSS. On the other hand, other

tests (Augmented Dickey-Fuller and Philips-Perron) fail to reject the hypothesis that the data is stationary.

- The seasonal strength (also ranges from 0 to 1) is 0.34. The following tests indicate that the time series is non-stationary in seasonality for the specified period: OCSB. On the other hand, other tests (Wang-Smith-Hyndman) fail to reject stationarity.
- The STL decomposition residuals show balanced behavior: 50.0% of residuals are positive and 50.0% negative. The average magnitude of positive residuals is 1060.918 compared to -1046.387 for negative residuals. In terms of autocorrelation structure, the residuals show significant temporal dependency in some of the first 12 lags according to the Ljung-Box test. This suggests that the decomposition method is missing some systematic patterns.

### **Auto-Correlation**

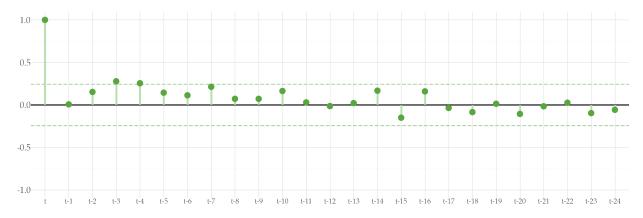


Figure 3: Auto-correlation plot up to 24 lags.

- The following lags show significant autocorrelation: t-3 and t-4. The autocorrelation is positive for all lags with a significant value.
- None of the lags relative to the seasonal period (t-12 and t-24) show any significant autocorrelation.

#### **Partial Auto-Correlation**

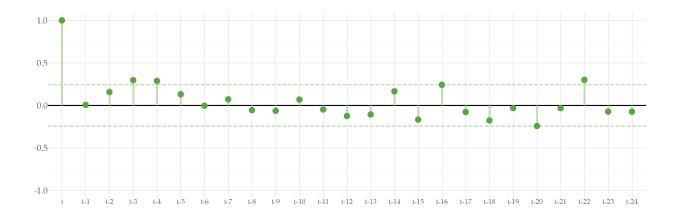


Figure 4: Partial Auto-correlation plot up to 24 lags. At each lag, the partial auto-correlation takes into account the previous correlations.

- The following lags show significant partial autocorrelation: t-3, t-4, t-20, and t-22.
- None of the lags relative to the seasonal period (t-12 and t-24) show any significant partial autocorrelation.

### **Trend**

Trend refers to the long-term change in the mean level of a time series. It reflects systematic and gradual changes in the data over time. Understanding the trend is important for identifying long-term growth or decline, structural changes, and making informed modeling decisions. This section examines the characteristics of the trend of the time series.

### **Trend Line Plot**

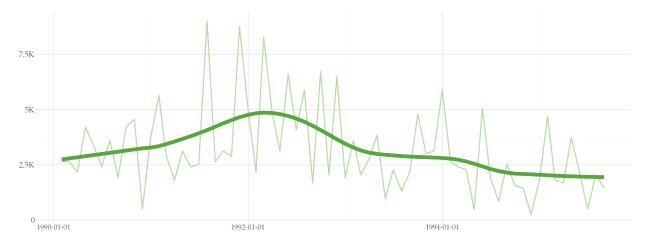


Figure 5: Time series trend plot.

- There is a slight downward trend. This trend is non-stationary (i.e. not deterministic) according to the statistical test(s): KPSS. The test(s) Augmented Dickey-Fuller and Philips-Perron did not find evidence for non-stationarity around a deterministic trend.
- The same tests were applied to analyse whether the time series is stationary around a constant level. The method(s) KPSS and Augmented Dickey-Fuller reject this hypothesis. But, the test(s) Philips-Perron fail to reject stationarity.
- **Preliminary experiments:** Including a trend explanatory variable which denotes the position (row id) of each observation improves forecasting accuracy. These experiments were conducted using a LightGBM algorithm and evaluated using SMAPE loss function. Using only lag-based features the model achieved a SMAPE of 79.33% on the test set. Including the trend variable improved the SMAPE to 64.67%.

## **Long-term Growth**

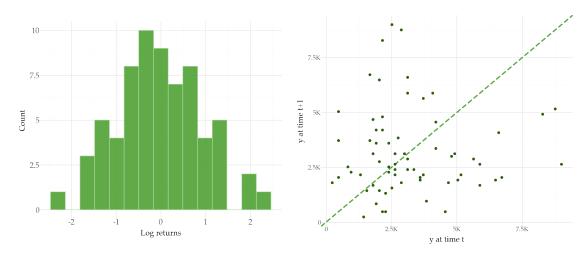


Figure 6: Distribution of log differences (left), and a Lag-plot (right). These plots help to understand how the data changes over consecutive observations. The histogram show the distribution of these changes using log returns. The lag-plot depicts the randomness in the data. The time series shows greater randomness as the points deviate from the dotted line.

- The time series has an average growth (log returns) of -0.01 (median equal to -0.08). The volatility of the returns in terms of standard deviation is 0.95. The skewness of the log differenced series is equal to 0.19, which is close to zero. This indicates a symmetric distribution, though there is a slight right skewness. The excess kurtosis of the log differenced series is equal to -0.21. This value is similar to that found from data following a Gaussian distribution.
- Concerning the symmetry of returns, 44.78% of the log differences are positive. The average of positive returns is 0.84, while the average of negative returns (53.73% of all returns) is -0.72. Overall, there are 46 return direction changes (69.7% of the data points)
- In the tails, 5.97% of returns fall beyond 2 standard deviations from the mean. The largest positive return is 2.35 on April 1994. Conversely, the largest decline is -2.25 (on October 1990).
- **Preliminary experiments:** Modeling the time series of first differences may improve forecasting accuracy. Experiments were conducted using a LightGBM algorithm and evaluated using SMAPE loss function. Using the original time series led to a 79.33% SMAPE. The scores using the differenced and log differenced time series are 87.89% and 58.15%, respectively.

## **Seasonality**

Seasonality represents recurring patterns or cycles that appear at regular intervals in time series data. These are predictable fluctuations that reflect periodic influences such as monthly, quarterly, or yearly cycles. Understanding seasonal patterns is crucial for

forecasting, trend analysis, and identifying anomalies. This section examines the presence, strength, and characteristics of seasonal components in the input time series.

## **Seasonal Line Plot (Monthly)**

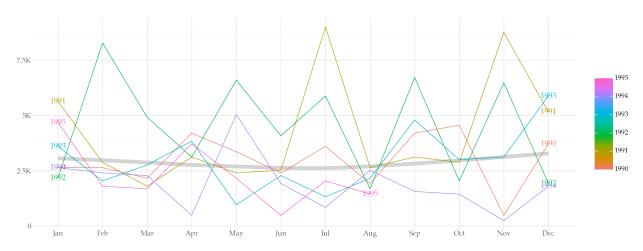


Figure 7: Seasonal plot of monthly values grouped by year.

- The following tests indicate that the time series is non-stationary in seasonality for a yearly period: OCSB. On the other hand, other tests (Wang-Smith-Hyndman) fail to reject the stationary null hypothesis.
- \*\*Forecasting experiments\*\*: Including monthly information in the predictive model decreases forecasting performance. This information was included as Fourier terms and repeating basis function terms in the explanatory variables.

## **Seasonal Sub-series Plot (Monthly)**

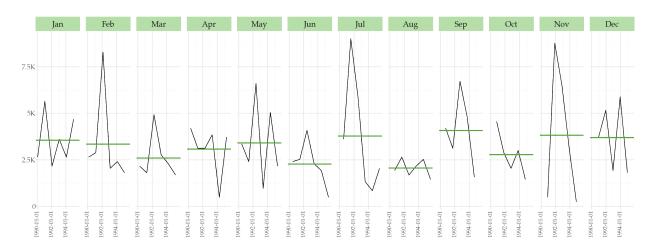


Figure 8: Monthly seasonal sub-series. This plot helps to understand how the data varies within and across monthly groups.

- Statistical tests were carried out to check for differences among means and variances across months. No significant differences were found.
- Overall, there is a reasonable evidence that the time series is not stationary around a constant level. But, the data is constant around a level in each Month.

• \*\*Forecasting experiments\*\*: There is evidence for a yearly seasonal pattern from statistical tests. Yet, including information about this period in the forecasting model decreased its performance.

# Seasonal Sub-series Plot (Quarterly)



Figure 9: Quarterly seasonal sub-series. This plot helps to understand how the data varies within and across quarterly groups.

- Statistical tests were carried out to check for differences among means and variances across quarters. No significant differences were found.
- The following tests indicate that the time series is non-stationary in seasonality for a Quarterly period: OCSB. On the other hand, other tests (Wang-Smith-Hyndman) fail to reject the stationary null hypothesis.
- Overall, there is a reasonable evidence that the time series is not stationary around a constant level. But, the data is constant around a level in each Quarter.
- \*\*Forecasting experiments\*\*: There is evidence for a quarterly seasonal pattern from statistical tests. Besides, including information about this period in the forecasting model improved its performance.

### Variance

Variance measures how data points spread around the average value in your time series. This section examines whether the variability remains stable (homoskedastic) or changes (heteroskedastic) over time. Understanding variance patterns is crucial for selecting appropriate modeling techniques, which can have a significant impact on forecasting accuracy.

# **Heteroskedasticity Testing**

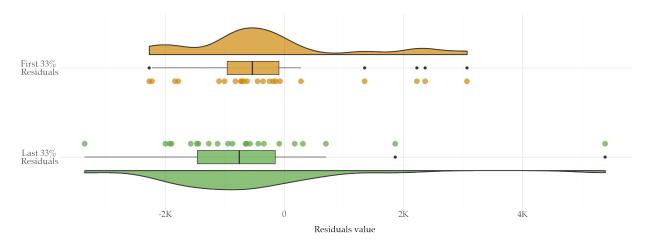


Figure 10: Time series residuals analysis. Difference in the distribution of the residuals in the first and last thirds of the series, following a Goldfeld-Quand partition.

- No statistical evidence was found for the hypothesis that the time series is heteroskedastic, according to the White, Breusch-Pagan, and Goldfeld-Quandt tests. The residuals are based on a linear trend model.
- Variance in seasonal periods according to Levene's test
  - Quarterly groups: no differences in variance
  - Monthly groups: no differences in variance
- **Preliminary experiments:** Three variance stabilization preprocessing techniques were tested to improve the forecast accuracy of an auto-regressive LightGBM (with 79.33% SMAPE using lag-based features):

∘ Log returns: 58.15% SMAPE

Log transformation: 51.58% SMAPE

∘ Box-Cox transformation: 54.87% SMAPE