

8.2 example

1. On $t \in [0, 3]$ in seconds, we have two particles described by:

Particle	position (m)	velocity (m/s)	acceleration (m/s ²)
A	$s_A = \frac{t(1-t)^2}{t+1} + 2$	$v_A = \frac{2t^3 + t^2 - 4t + 1}{(t+1)^2}$	$a_A = \frac{2(t^3 + 3t^2 + 3t - 3)}{(t+1)^3}$
B	$s_B = t \ln(t+1)$	$v_B = \frac{t}{t+1} + \ln(t+1)$	$a_B = \frac{t+2}{(t+1)^2}$

(a) Calculate $\frac{1}{3} \int_0^3 v_A dt$ and interpret the result, including units.

(b) When is particle A slowing down?

(c) Is the distance between particles A and B increasing or decreasing at:

- (i) $t = 2$?
- (ii) $t = 3$?

(d) What are the maximum and minimum distances between particles A and B ?