# **Assignment 1**

# **Question 1**

## Code:

```
timeStruct = [d['review/timeStruct'] for d in data]

def feature(datum):
    feat = [1] #the intercept vector does not have a feature and should be multiplied with 1
    feat.append(datum['year'])
    return feat

X = [feature(d) for d in timeStruct]
y = [d['review/overall'] for d in data]
theta,residuals,rank,s = numpy.linalg.lstsq(X, y)
print(theta)
print(residuals/len(y)) ##MSE
```

#### Answer:

```
[ -3.91707489e+01 2.14379786e-02]
[ 0.49004382]
```

# Question 2:

A better representation for year would be giving binary codes for various years. For ex, year 1999 could be 0,0,0,1 and year 2012 can be 1,1,0,1. Any other year not provided in the dataset could be included in the bias.

# Code

```
timeStruct = [d['review/timeStruct'] for d in data]

year = [d['year'] for d in timeStruct]

min(year) ### Answer : 1999

max(year) ### 2012

def feature(datum):

if datum['year'] == 1999:

feat = [1,0,0,0,0]

elif datum['year'] == 2000:

feat = [1,0,0,0,1]
```

```
elif datum['year'] == 2001:
  feat = [1,0,0,1,0]
 elif datum['year'] == 2002:
  feat = [1,0,0,1,1]
 elif datum['year'] == 2003:
  feat = [1,0,1,0,0]
 elif datum['year'] == 2004:
  feat = [1,0,1,0,1]
 elif datum['year'] == 2005:
  feat = [1,0,1,1,0]
 elif datum['year'] == 2006:
  feat = [1,0,1,1,1]
 elif datum['year'] == 2007:
  feat = [1,1,0,0,0]
 elif datum['year'] == 2008:
  feat = [1,1,0,0,1]
 elif datum['year'] == 2009:
  feat = [1,1,0,1,0]
 elif datum['year'] == 2010:
  feat = [1,1,0,1,1]
 elif datum['year'] == 2011:
  feat = [1,1,1,0,0]
 elif datum['year'] == 2012:
  feat = [1,1,1,0,1] # any other year will get added to the bias term
 return featX = [feature(d) for d in timeStruct]
y = [d['review/overall'] for d in data]
theta,residuals,rank,s = numpy.linalg.lstsq(X, y)
#### theta = array([ 3.70613430e+00, 1.64047010e-01, 7.07739382e-02
####
                 4.47664682e-02, -3.61124198e-03])
```

```
residuals/len(y) ##MSE
thetamat = numpy.asmatrix(theta)
Xmat = numpy.asmatrix(X)
(thetamat * Xmat.transpose()).shape
ymat = numpy.asmatrix(y)
sum(numpy.squeeze(numpy.asarray(ymat-thetamat*Xmat.transpose()))**2)/len(y) ###MSE
Answer
#### theta = array([ 3.70613430e+00,
                                                    1.64047010e-01, 7.07739382e-02
####
                 4.47664682e-02, -3.61124198e-03])
##### 0.48990915696982806
Question 3
Code
### Using pandas
df = pd.read csv('C:/Users/BHEL/Desktop/Recommendation Systems/Assignment 1/winequality-whi
te.csv',delimiter=";")
df train = df.iloc[0: int(len(df)/2)]
df test = df.iloc[int(len(df)/2) + 1 :len(df)]
y = df_train["quality"].values
X = numpy.vstack([numpy.ones(len(df train)),df train["fixed acidity"].values,df train["volatile acidit
y"],df train["citric acid"] \
         ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"], \
         df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
         df_train["alcohol"]]).T
theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
theta
#### array([ 2.56420279e+02, 1.35421303e-01, -1.72994866e+00,
            1.02651152e-01, 1.09038568e-01, -2.76775146e-01,
            6.34332168e-03, 3.85023977e-05, -2.58652809e+02, 1.19540566e+00, 8.33006285e-01, 9.79304353e-02])
y_test = df_test["quality"].values
X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile aci
dity"],df test["citric acid"] \
         ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"], \
         df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
         df test["alcohol"]]).T
theta test, residuals test, rank test, s test = numpy.linalg.lstsq(X test, y test)
print(residuals/len(y))
print(residuals test/len(y test))
```

## **Answer**

```
#### theta
```

```
##### array([ 2.56420279e+02, 1.35421303e-01, -1.72994866e+00, 1.02651152e-01, 1.09038568e-01, -2.76775146e-01, 6.34332168e-03, 3.85023977e-05, -2.58652809e+02, 1.19540566e+00, 8.33006285e-01, 9.79304353e-02])
#### MSE of the train and test dataset
Train - [ 0.6023075]
Test - [ 0.49562901]
```

MSE of the test set is lower – this could be because the training and the test set features are not ide ntically distributed.

# **Question 4**

```
In [6]: | # Removing Fixed Acidity
                          y = df_train["quality"].values
                          X = numpy.vstack([numpy.ones(len(df_train)),df_train["volatile acidity"],df_train["citric acid"] \)
                                                                              ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"], \
                                                                            \label{lem:density} $$ df_{train}["total sulfur dioxide"], $$ df_{train}["density"], $$ df_{train}["pH"], $$ df_{train}["sulphates"], $$ $$ df_{train}["total sulfur dioxide"], $$ df_{train}["total sulfur dioxide
                                                                            df_train["alcohol"]]).T
                          theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
                          theta
Out[6]: array([ 1.59265497e+02, -1.79843308e+00, 1.53362739e-01,
                                                7.40365514e-02, -8.95644126e-01, 6.66762254e-03, -2.78710665e-04, -1.59274221e+02, 7.11764816e-01, 7.06744801e-01, 2.12169554e-01])
In [7]: y_test = df_test["quality"].values
                          X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["volatile acidity"],df_test["citric acid"] \
                                                                               ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"],
                                                                            df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                                                                            df_test["alcohol"]]).T
                          theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
In [8]: residuals/len(y)
                          residuals test/len(y test)
Out[8]: array([ 0.49593076])
```

```
In [9]: # Removing Volatile Acidity
         y = df_train["quality"].values
         df_train["alcohol"]]).T
         theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
        theta
Out[9]: array([ 2.76319617e+02, 1.70596631e-01, 3.37705416e-01, 1.11733261e-01, -1.03169500e+00, 8.78146518e-03,
                -7.94469068e-04, -2.79834990e+02, 9.14939034e-01, 4.97740129e-02])
                                                   1.46305736e+00,
In [10]: y_test = df_test["quality"].values
         df_test["alcohol"]]).T
         theta\_test, residuals\_test, rank\_test, s\_test = numpy.linalg.lstsq(X\_test, y\_test)
In [11]: residuals/len(y)
        residuals_test/len(y_test)
Out[11]: array([ 0.52603379])
 In [12]: # Removing Citric Acid
          y = df_train["quality"].values
          X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"] \
                           ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"],
                          df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
                          df_train["alcohol"]]).T
          theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
 Out[12]: array([ 2.54710681e+02, 1.37865465e-01, -1.75200556e+00,
                  1.08761156e-01, -2.16042405e-01, 6.39876960e-03, 2.76634223e-05, -2.56894507e+02, 1.18003096e+00,
                  2.76634223e-05, -2.56894507e+02,
8.35323848e-01, 1.01084607e-01])
 In [13]: y_test = df_test["quality"].values
          df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                          df_test["alcohol"]]).T
          theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
 In [14]: residuals/len(y)
          residuals_test/len(y_test)
 Out[14]: array([ 0.49575561])
 In [15]: # Removing Residual Sugar
          y = df_train["quality"].values
          X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                           ,df_train["chlorides"],df_train["free sulfur dioxide"], \
                          df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
                          df_train["alcohol"]]).T
          theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
          theta
 Out[15]: array([ -1.47920104e+01, -7.46073461e-02, -1.76142965e+00,
                  6.81139124e-02, -1.82547037e+00, 8.93883453e-03,
                 -8.05570058e-04, 1.66496148e+01,
                                                   2.40618592e-01.
                  4.00610149e-01, 3.87434345e-01])
 In [16]: y_test = df_test["quality"].values
          X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                           ,df_test["chlorides"],df_test["free sulfur dioxide"],
                          df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                          df_test["alcohol"]]).T
          theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
 In [17]: residuals/len(y)
          residuals_test/len(y_test)
 Out[17]: array([ 0.50989045])
```

```
In [18]: # Removing Chlorides
                    y = df_train["quality"].values
                    X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                                                        ,df_train["residual sugar"],df_train["free sulfur dioxide"],
                                                     \label{train} $$ df_{train}["total sulfur dioxide"], df_{train}["density"], df_{train}["pH"], df_{train}["sulphates"], $$ $$ (a) $$ df_{train}["sulphates"], $$ (b) $$ df_{train}["sulphates"], $$ (c) $$ df_{train}["sulphates"
                                                     df_train["alcohol"]]).T
                    theta,residuals,rank,s = numpy.linalg.lstsq(X, y)
                    theta
Out[18]: array([ 2.58709684e+02, 1.37904183e-01, -1.73584539e+00,
                                     9.75957321e-02, 1.10074038e-01, 6.31755375e-03, 3.99792536e-05, -2.61016310e+02, 1.20593153e+00,
                                     8.35397592e-01, 9.72781925e-02])
In [19]: y_test = df_test["quality"].values
                     X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                                                        ,df_test["residual sugar"],df_test["free sulfur dioxide"],
                                                     df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                                                     df_test["alcohol"]]).T
                    theta\_test, residuals\_test, rank\_test, s\_test = numpy.linalg.lstsq(X\_test, y\_test)
 In [20]: residuals/len(y)
                    residuals_test/len(y_test)
 Out[20]: array([ 0.49563808])
In [21]: # Removing Free Sulfur Dioxide
                    y = df_train["quality"].values
                    X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                                                     ,df_train["residual sugar"],df_train["chlorides"], \
df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
                                                     df_train["alcohol"]]).T
                   theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
                   theta
                   4
Out[21]: array([ 2.82300292e+02, 1.44692601e-01, -1.86565663e+00,
                                     1.35540475e-01, 1.21404594e-01, -9.31572520e-02,
                                     1.55712233e-03, -2.84834933e+02, 1.29264990e+00,
                                     8.11809727e-01, 7.21620256e-02])
In [22]: y_test = df_test["quality"].values
                   X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                                                     ,df_test["residual sugar"],df_test["chlorides"], \
df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                                                     df_test["alcohol"]]).T
                    theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
                   4
In [23]: residuals/len(y)
                   residuals_test/len(y_test)
Out[23]: array([ 0.49663839])
```

```
In [25]: # Removing Total Sulfur Dioxide
         y = df train["quality"].values
         df_train["density"],df_train["pH"], df_train["sulphates"], \
df_train["alcohol"]]).T
         theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
         theta
         4
Out[25]: array([ 2.55873246e+02, 1.35090722e-01, -1.72825856e+00,
                  1.02416787e-01, 1.08891972e-01, -2.77158772e-01, 6.39868008e-03, -2.58094731e+02, 1.19355492e+00,
                  8.34256998e-01, 9.83042785e-02])
In [26]: y_test = df_test["quality"].values
          X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                            ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"], \
                           df_test["density"],df_test["pH"], df_test["sulphates"],
                           df_test["alcohol"]]).T
         theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
In [27]: residuals/len(y)
         residuals_test/len(y_test)
Out[27]: array([ 0.4957691])
   In [28]: # Removing Density
             y = df_train["quality"].values
             X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                               df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"],
                              df_train["total sulfur dioxide"],df_train["pH"], df_train["sulphates"], \
                              df_train["alcohol"]]).T
             theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
             theta
             4
    Out[28]: array([ 1.35278847e+00, -6.30214557e-02, -1.81229926e+00,
                      2.98038927e-02, 1.74234814e-02, -1.45313766e+00,
8.17207399e-03, -1.03082385e-03, 3.24191788e-01,
4.57723912e-01, 3.87103702e-01])
    In [29]: y_test = df_test["quality"].values
             X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                               df_test["total sulfur dioxide"],df_test["pH"], df_test["sulphates"], \
                              df_test["alcohol"]]).T
             theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
             4
    In [30]: residuals/len(y)
             residuals_test/len(y_test)
    Out[30]: array([ 0.50117674])
  In [31]: # Removing pH
           y = df_train["quality"].values
           X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                            ,df_train["residual sugan"],df_train["chlorides"],df_train["free sulfur dioxide"], \
df_train["total sulfur dioxide"],df_train["density"], df_train["sulphates"], \
df_train["alcohol"]]).T
           theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
           4
  Out[31]: array([ 1.03156070e+02, -3.95816093e-02, -1.91850711e+00,
                   -1.27755184e-02, 5.14623196e-02, -1.22611859e+00, 7.57413959e-03, -6.04094775e-04, -1.00780974e+02, 7.57619203e-01, 2.83982725e-01])
  In [32]: y_test = df_test["quality"].values
           df_test["alcohol"]]).T
           theta\_test, residuals\_test, rank\_test, s\_test = numpy.linalg.lstsq(X\_test, y\_test)
  In [33]: residuals/len(y)
           residuals_test/len(y_test)
  Out[33]: array([ 0.49564268])
```

```
In [34]: # Removing Sulphates
           y = df_train["quality"].values
          X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                             ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"],
                            df_train["total sulfur dioxide"],df_train["density"],df_train["pH"],
                           df_train["alcohol"]]).T
           theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
          theta
 Out[34]: array([ 2.02754232e+02, 9.89499345e-02, -1.77602652e+00,
                    1.16540757e-01, 8.82235158e-02, -4.48945940e-01,
                   6.12915393e-03, 3.85168935e-04, -2.04365676e+02, 1.13522515e+00, 1.59797632e-01])
 In [35]: y_test = df_test["quality"].values
           X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                             ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"], \
                            df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], \
                           df test["alcohol"]]).T
           theta_test,residuals_test,rank_test,s_test = numpy.linalg.lstsq(X_test, y_test)
          4
 In [36]: residuals/len(y)
          residuals_test/len(y_test)
 Out[36]: array([ 0.50020054])
In [37]: # Removing Alcohol
          y = df_train["quality"].values
         X = numpy.vstack([numpy.ones(len(df_train)),df_train["fixed acidity"].values,df_train["volatile acidity"],df_train["citric acid"]
                            ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"],
                           df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
                          1).T
          theta, residuals, rank, s = numpy.linalg.lstsq(X, y)
         4
Out[37]: array([ 3.25993179e+02,
                                    1.90940672e-01, -1.68438300e+00,
                  1.34455930e-01,
                                    1.32486181e-01, -1.97765161e-01,
                  5.90527049e-03,
                                    2.12840502e-04, -3.29032181e+02,
                  1.44529192e+00, 9.37096269e-01])
In [38]: y_test = df_test["quality"].values
          X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["fixed acidity"].values,df_test["volatile acidity"],df_test["citric acid"
                            ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"],
                           df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
                          1).T
         theta test, residuals test, rank test, s test = numpy.linalg.lstsq(X test, y test)
In [39]: residuals/len(y)
          residuals_test/len(y_test)
Out[39]: array([ 0.50846051])
```

### **Answer**

Based on the MSE values, removing **Volatile acidity** resulted in the highest increase in MSE of 0.5260. So Volatile acidity is an important variable.

Chlorides adds the least value to the MSE of 0.495638. So, it's not very important.

## **Question 5**

Code

df = pd.read\_csv('C:/Users/BHEL/Desktop/Recommendation Systems/Assignment 1/winequality-white.csv',delimiter=";")

```
df.loc[df['quality'] <= 5, 'quality'] = 0
df.loc[df['quality'] > 5, 'quality'] = 1
df_{train} = df.iloc[0: int(len(df)/2)]
df_{test} = df.iloc[int(len(df)/2) + 1 :len(df)]
X_train = numpy.vstack([numpy.ones(len(df_train)),df_train["volatile acidity"],df_train["citric acid"] \
          ,df_train["residual sugar"],df_train["chlorides"],df_train["free sulfur dioxide"], \
         df_train["total sulfur dioxide"],df_train["density"],df_train["pH"], df_train["sulphates"], \
         df_train["alcohol"]]).T
y_train = df_train["quality"].values
clf = svm.SVC(C=1000)
clf.fit(X_train, y_train)
y_test = df_test["quality"].values
X_test = numpy.vstack([numpy.ones(len(df_test)),df_test["volatile acidity"],df_test["citric acid"] \
          ,df_test["residual sugar"],df_test["chlorides"],df_test["free sulfur dioxide"], \
         df_test["total sulfur dioxide"],df_test["density"],df_test["pH"], df_test["sulphates"], \
         df_test["alcohol"]]).T
train_predictions = clf.predict(X_train)
test_predictions = clf.predict(X_test)
accuracy_train = sum(z[0] == z[1] for z in zip(train_predictions, y_train))/len(train_predictions)
accuracy\_test = sum(z[0] == z[1] for z in zip(test\_predictions, y\_test))/len(test\_predictions)
Answer
Accuracy train - 0.99959167006941607
Accuracy test - 0.64991830065359479
Question 6
Code
def fprime(theta, X, y, lam):
```

```
dl = [0.0]*len(theta)
for i in range(len(X)):
    logit = inner(X[i],theta)
    logitsigm = 1- sigmoid(logit)
    for k in range(len(theta)):
        dl[k] += X[i,k]*logitsigm
        if not y[i]:
            dl[k] -= X[i,k]
for m in range(len(theta)):
        dl[m] -= 2*lam*theta[m]
# Negate the return value since we're doing gradient *ascent*
    return numpy.array([-x for x in dl])
```

```
In [159]: theta,l,info = scipy.optimize.fmin_l_bfgs_b(f, [0]*len(X_train[0]), fprime, args = (X_train, y_train, 1.0))
          print("Final log likelihood =", -1)
          11 = -1394.92260272
          11 = -1394.92403627
          11 = -1394.92259383
          11 = -1394.92251155
          11 = -1394.92237783
          11 = -1394.92220392
          11 = -1394.92201748
          11 = -1394.92174875
          11 = -1394.92206472
          11 = -1394.92162681
          11 = -1394.92133886
          11 = -1394.92103647
          11 = -1396.72495648
          11 = -1394.92070764
          11 = -1394.92032856
          11 = -1394.9202579
          11 = -1394.92025439
          11 = -1394.92025248
          Final log likelihood = -1394.92025248
```

```
theta = numpy.matrix(theta).transpose()
X_train = numpy.matrix(X_train)
y_pred_train = (X_train * theta)
for i in range(len(y_pred_train)):
    if(y_pred_train[i,0]<0):
        y_pred_train[i,0] = 0
    else:
        y_pred_train[i,0] = 1
accuracy_train = sum(z[0] == z[1] for z in zip(y_pred_train, y_train))/len(y_pred_train)
X_test = numpy.matrix(X_test)</pre>
```

```
y_pred_test = (X_test * theta)
for i in range(len(y_pred_test)):
  if(y_pred_test[i,0]<0):</pre>
    y_pred_test[i,0] = 0
  else:
    y_pred_test[i,0] = 1
accuracy_test = sum(z[0] == z[1] for z in zip(y_pred_test, y_test))/len(y_pred_test)
Answer
```

Final log – likelihood value converged at -1394.92

```
Training accuracy - matrix([[ 0.70600245]])
Testing accuracy - matrix([[ 0.76062092]])
```

Testing accuracy is greater than training accuracy which might be due to the fact that training and testing datasets are not identically distributed.