

# Thesis Outline – the problem of axisymmetric BOR

May 4, 2016

## 1

What is an axisymmetric surface of revolution? Why are these type of densities useful and sought after?

## 2

What is a modal Green's function? What is translation invariant kernel? What are the problems associated with this?

## 3

Why is an analytic FMM for a modal Green's function difficult? The problem with evaluating special functions – Bessel or Hankel functions.

## 4

So we're left to kernel-independent methods.

## 5

Why not use the typical KIFMM from Ying, Biros, and Zorin? Pre-computation is not optimal because of translation operators.

## 6

We now consider using the black-box FMM or a Chebyshev interpolation-based scheme. Consider that for each mode  $n$ , the computation of the weights is simply a matrix  $W_{m_1, m_2} = \sum_{j=1}^N \sigma_j R_n(\bar{\mathbf{y}}_{m_1, m_2}, \mathbf{y}_j)$