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**DRAFT: THE EFFECT OF VARIYING VISCOSITY IN TURBULENT CHANNEL FLOW**

**Victor Coppo Leite**

Ken and Mary Alice Lindquist  
Department of Nuclear Engineering  
Pennsylvania State University  
State College, PA 16801  
Email: vbc5085@psu.edu

**Elia Merzari**

Ken and Mary Alice Lindquist  
Department of Nuclear Engineering  
Pennsylvania State University  
State College, PA 16801  
Email: ebm5153@psu.edu

**ABSTRACT**

*In various applications in nuclear engineering and in particular in test reactors, heat removal is carried by single-phase axial flow. In these applications, we observe sharp changes in molecular viscosity while the density presents very limited changes. As a consequence, the Reynolds number increases often by 2-3 folds across the channel, with an inlet value often transitional. In these conditions, turbulence changes significantly across the length of the channel with redistribution and thinning of the boundary layers. This is different from acceleration as the effect of changes in density is negligible. We aim to characterize in detail this phenomenon.*

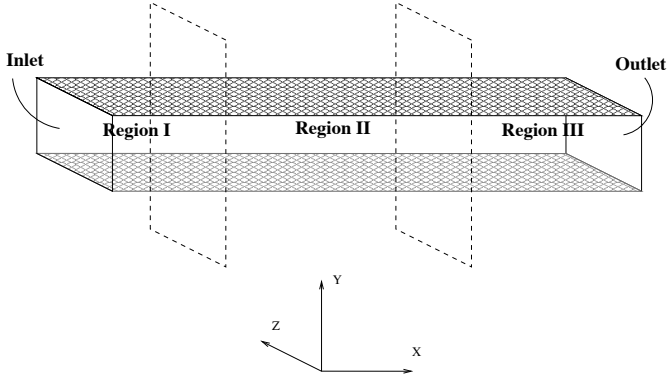
*In particular Nek5000, a spectral-element computational fluid dynamics (CFD) code, will be used to perform DNS of fluid flow in the transition regime for channel flow with varying viscosity. We set up a novel benchmark case: the channel is extended in the stream-wise direction up to  $20\pi$ . The viscosity is kept constant in the first  $4\pi$  region. This inlet region is used as a cyclic region to obtain a fully developed flow profile at the beginning of the ramping region. The ramping region ( $4\pi - 20\pi$ ) is defined as a transition region where the viscosity is linearly decreased along the channel. The flow is homogenous in the span-wise direction due to the periodic boundary conditions. Due to the cyclic and wall boundary conditions, the flow is non-homogenous in the stream-wise and wall-normal direction respectively.*

*In this study, specific focus is given to the investigation of turbulence properties and structures in the near-wall region along the flow direction. Detailed turbulence budgets are col-*

*lected and investigated. As expected, the results show that variation in the Reynolds across a channel does not cause an immediate change in the size of turbulent structures in the ramp region and a delay is in fact observed. Moreover, the results from the present study are compared with a correlation available in the literature for the friction velocity and as a function of the Reynolds-number.*

**NOMENCLATURE**

A You may include nomenclature here.  
 $\nu$  Viscosity.  
 $x$  Streamwise direction.  
 $y$  Vertical direction.  
 $z$  Spanwise direction.  
 $Re$  Reynolds number.  
 $Re_\tau$  Friction Reynolds number.  
 $DNS$  Direct Numerical Simulation.  
 $ANL$  Argonne National Laboratory.  
 $\tau_w$  Shear stress at the wall.  
 $u_\tau$  Friction velocity.  
 $Re_\tau$  Friction Reynolds number.  
 $\delta$  Height of the turbulence channel.  
 $F_{Ci}$  Delayed function of Cases  $i=I, II$  and  $III$ .  
 $a$  Viscosity linear coefficient.  
 $R$  Relaxing parameter.  
 $C$  Contraction parameter.  
 $\delta_i$  Streamwise position where Region  $i$  starts,  $i=I, II$  and  $III$ .  
 $\Lambda$  Signal contribution in the delayed function.



**FIGURE 1:** Geometry of the turbulence channel, the channel is divided into three different Regions.

*BLABLABLA* Bullshit.

$\alpha$  There are two arguments for each entry of the nomenclature environment, the symbol and the definition.

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## INTRODUCTION

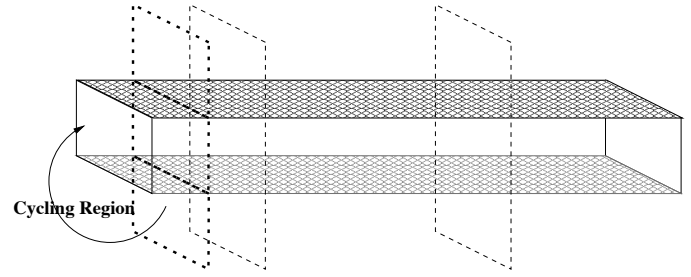
A schematic of the turbulence channels simulated are shown in Fig. 1. In this figure, Regions I, II and III are defined by two planes crossing the channel. A cycling region is implemented within Region I, Fig. 2. In this problem, the viscosity  $\nu$  is a function of  $x$ , i.e., the streamwise distance. This parameter has constants values of  $1E-4$  Pa.s and  $5E-5$  Pa.s along Regions I and III respectively, while in region II it decreases with respect to the inverse of  $x$ .

In the present work, three cases varying the length of Region II are studied. Cases I, II and III have their Region II length of respectively  $16\pi$ ,  $8\pi$  and  $4\pi$ . Fig. 3 shows the plot of the viscosity as a function of  $x$  for each one of these cases and Fig. 4 shows the plot of the Reynolds number for them.

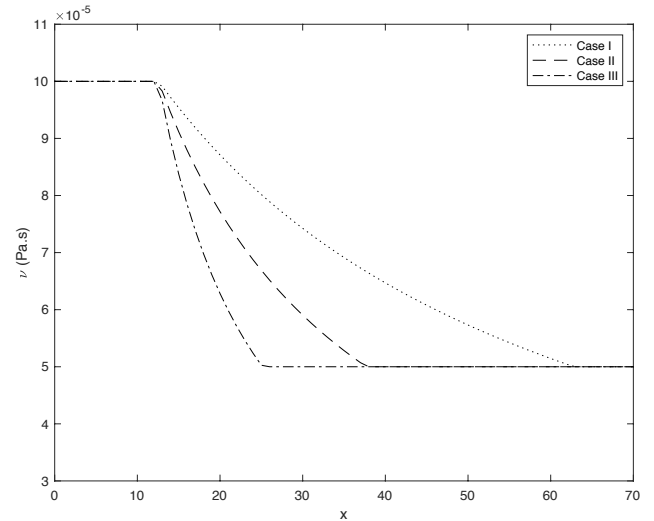
For all three Cases the inlet flow in Region I is considered to be fully developed with  $Re_\tau = 550$ , i.e., the same conditions as in [1]. Periodic condition is considered for the boundaries of the spanwise direction, i.e.,  $z$  axis, and finally wall conditions are considered for the boundaries of the vertical direction, i.e.,  $y$  axis.

## METHODS - DIRECT NUMERICAL SIMULATION

In order to resolve the finest turbulent scales, the calculations of this work has been developed through Direct Numerical Simulation (DNS). To do so Nek5000 was employed, a spectral



**FIGURE 2:** Cyclic region in the inlet.

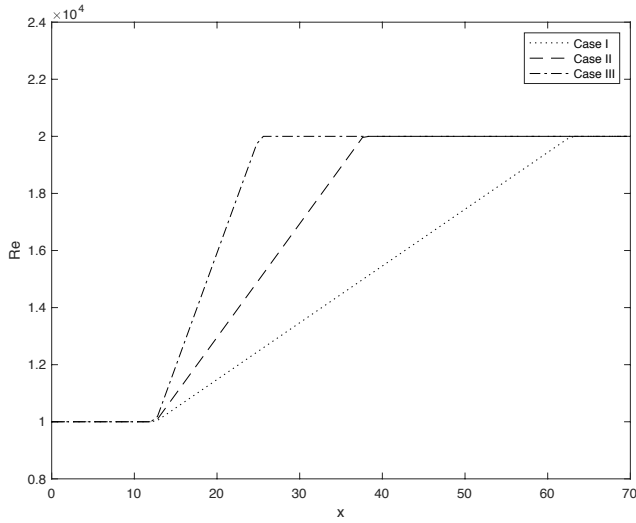


**FIGURE 3:** The viscosity of the considered Cases as a function of  $x$ .

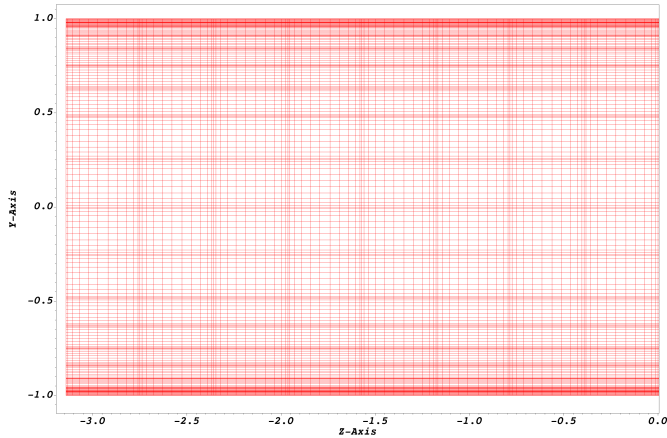
element code developed in Argonne National Laboratory (ANL). Nek5000 has been validated in references [2] and [3].

The solution of this method is given by trigonometric series, in each element a polynomial functions of up to the twelfth degree have been employed to discretize the velocity field. Fig. 5 shows an example of the grid from half of the channel's cross section. One should notice that the discretization presented by this particular area is identical through all model's domain and it is only presented half of the cross-section for better visualization of the frame.

DNS simulations are able to simulate the finest turbulent length scales without using any turbulent model. Since the present work is focused on studying the contribution of the smaller scales to the energy cascade, it is required to use DNS rather than Reynolds Average Navier-Stokes (RANS) or Large Eddy Simulations (LES), although there is a substantial growth of the computational cost.



**FIGURE 4:** The Reynolds number as a function of the  $x$  for the considered Cases.



**FIGURE 5:** The grid employed in the simulation from half of the channel's cross section.

## METHODS - CONVOLUTION ANALYSIS OF THE FRICTION REYNOLDS NUMBER

The friction Reynolds number has been calculated via numerical simulations for Cases I, II and III and this result was compared to the values obtained using an existed expression from Ref. [4] valid for fully developed turbulent flows. A delay in space can be seen between  $Re_\tau$  when comparing the simulations' results with the values yielded from the mentioned expression. This way, these results are treated as signals in the space and a convolution operation is performed over the analytical expression for fully developed turbulent flows in order to build a

function that matches with the obtained values from the simulations.

To calculate the friction Reynolds number from the simulations several velocities profiles along  $x$  were obtained from the results and the viscous stress  $\frac{d\langle U \rangle}{dy}$  for these locations are calculated. Such values can then be applied in the set of definitions given from Eqn. 1 to Eqn. 3 following presented in order to calculate  $Re_\tau$ .

$$\tau_w = \rho \nu \left( \frac{d\langle U \rangle}{dy} \right)_{y=0} \quad (1)$$

Where  $\rho$  is the density and  $\tau_w$  is the shear stress at the wall.

$$u_\tau = \sqrt{\frac{\tau_w}{\rho}} \quad (2)$$

Where  $u_\tau$  is the friction velocity. And finally,

$$Re_\tau = \frac{u_\tau \delta}{\nu} \quad (3)$$

Where  $\delta$  is the height of the simulated channels. For all Cases studied here this is a constant parameter  $\delta = 2$ .

The friction Reynolds number calculated using Eqn. 3 with the numeric simulations' results is then compared with Eqn. 4 from Ref. [4], which is valid for fully developed turbulent flows.

$$Re_\tau = 0.09 Re^{0.88} \quad (4)$$

The Reynolds numbers used to supply Eqn. 4 are those varying through  $x$  from Cases I, II and III, as presented in Fig. 4. The convolution to be performed over Eqn. 4 is given by Eqn. 5. In this equation  $Re(\chi)$  stands for the analytical approximation given by Eqn. 4,  $g(x - \chi)$  is a shifting function and  $\chi$  is simply a dummy variable for the streamwise distance.

$$F(x) = \int_{-\infty}^{+\infty} Re_\tau(\chi) g(x - \chi) d\chi \quad (5)$$

As mentioned earlier, the simulated channels in the present study are divided in three Regions, as shown in Fig. ?? and a delayed function is built for each one of those. Since there is

no delay in Region I, no special treatment is required for it, thus  $F(x) = Re_\tau(x) = 550$ . Differently, in Region II and III the results from the numerical experiments are delayed when compared to those from Eqn. 4 and because of that a convolution operator takes place. Since we are dealing with a delayed signal in both Regions, a decaying exponential has been used as a shifting function, as proposed in Ref. [5].

In Region II, the friction Reynolds number is a linear function given by Eqn. 6.

$$Re_\tau(x) = ax + 550 \quad (6)$$

Where  $a$  is the linear coefficient of the increasing viscosity for each one of the three cases in Region II. Using Eqn. 6 in conjunction to the definition from Eqn. 5, one may derive Eqn. 7, which is the delayed function valid for Region II of the considered Cases.

$$F(x) = \frac{a}{R^2} (e^{-R(x-\delta_{II})} - 1) + \frac{a}{R} (x - \delta_{II}) + 550 \quad (7)$$

Where  $\delta_{II}$  is the streamwise position that Region II starts and  $R$  is named relaxing parameter and it stands for the exponential decaying constant to be used in the shifting function  $g(x - \chi)$  when dealing with Region II.

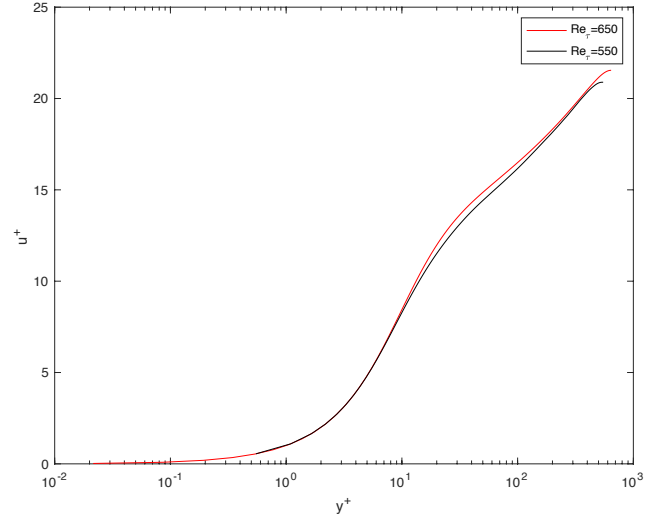
Eqn. 8 is the delayed function yielded applying Eqn. 5 over Region III, where a constant friction Reynolds number  $Re_\tau$  predicted by Eqn. 4 takes place.

$$F(x) = (20000 - \Lambda)(1 - e^{-C(x-\delta_{III})}) + \Lambda \quad (8)$$

In this equation  $\delta_{III}$  is the streamwise position that Region III starts,  $C$  is named contraction parameter and it stands for the exponential decaying constant to be used in the shifting function  $g(x - \chi)$  when dealing with Region III and finally  $\Lambda = \frac{a}{R^2} (e^{-R(\delta_{III}-\delta_{II})} - 1) + \frac{a}{R} (\delta_{III} - \delta_{II}) + 550$ , represents the contribution from Regions II to the delayed signal in Region III.

In summary, Eqn. (9) express the delayed function for  $Re_\tau$  over the different Regions of the turbulence channels in the present work.

$$F(x) = \begin{cases} 550 & \text{(Region I)} \\ \frac{a}{R^2} (e^{-R(x-\delta_{II})} - 1) + \frac{a}{R} (x - \delta_{II}) + 550 & \text{(Region II)} \\ (20000 - \Lambda)(1 - e^{-C(x-\delta_{III})}) + \Lambda & \text{(Region III)} \end{cases} \quad (9)$$



**FIGURE 6:** Comparing  $u^+$  from Region I in Case I with already existed data in Ref [6].

## RESULTS

Results from the three considered Cases in the present work are shown in this section. First, a comparison between the results in Region I from Case I with an existed data from Ref [6] is done in order to verify the model. Second, the  $Re_\tau$  results obtained via numerical models, through Eqn. 4 and by the derived delayed function  $F(x)$  are presented. Third, low velocity streaks are presented following it by the  $s < u >$  and  $< uu >$  profiles along the streamwise direction for Case I are presented,

### Model verification

#### The friction Reynolds number along $x$ Turbulent structures

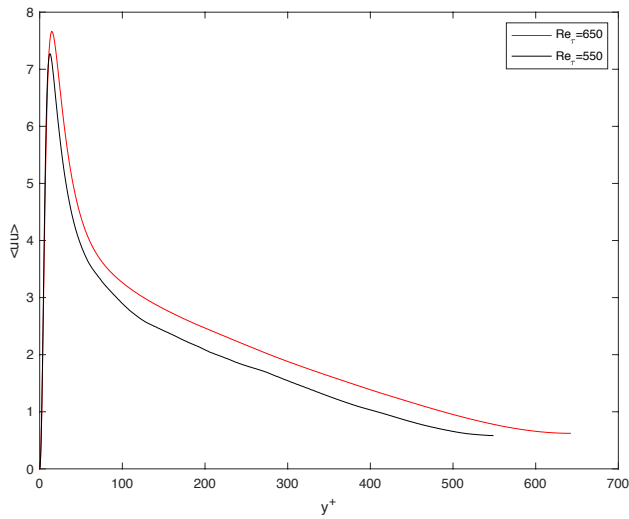
### CONCLUSIONS

### ACKNOWLEDGMENT

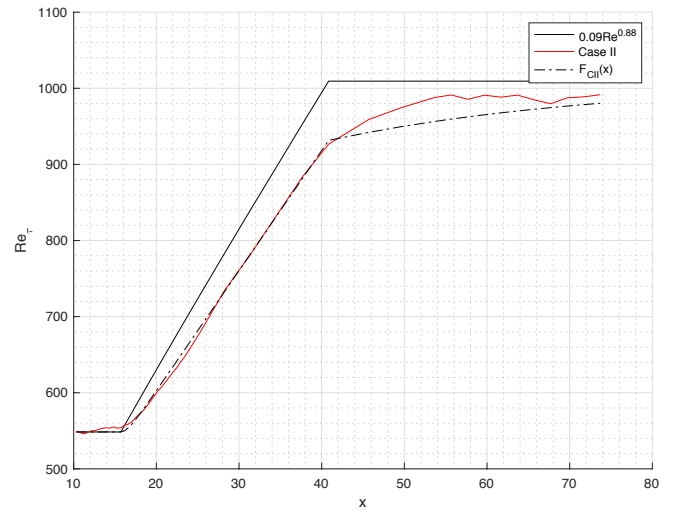
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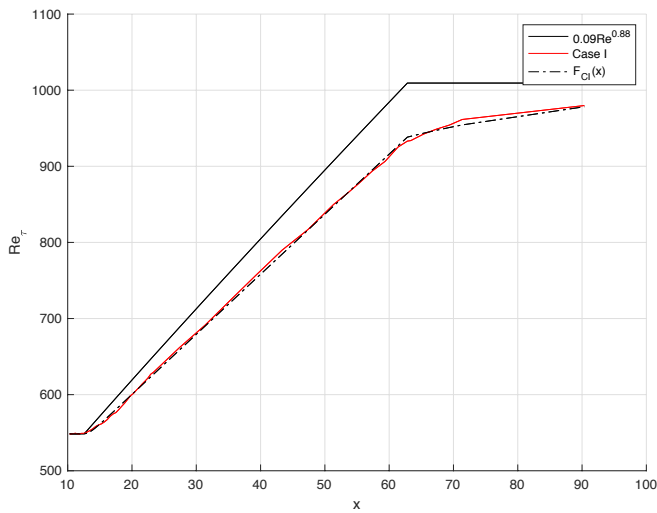
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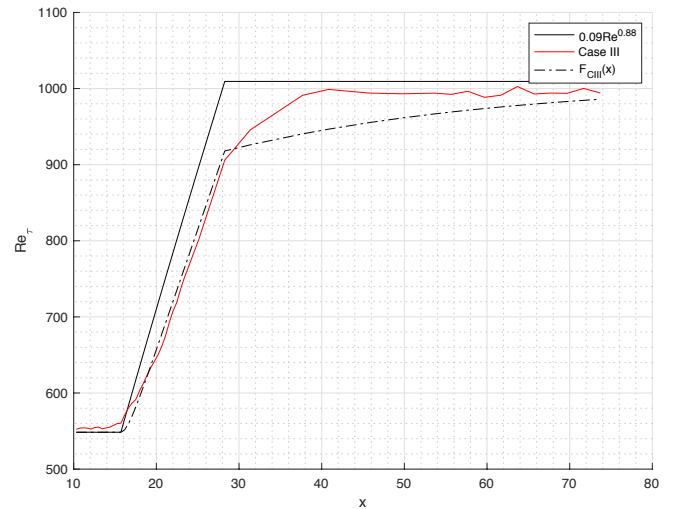
**FIGURE 7:** Comparing  $\langle uu \rangle$  from Region I in Case I with already existed data in Ref [6].



**FIGURE 9:** Friction Reynolds number through  $x$  for Case II.



**FIGURE 8:** Friction Reynolds number through  $x$  for Case I.



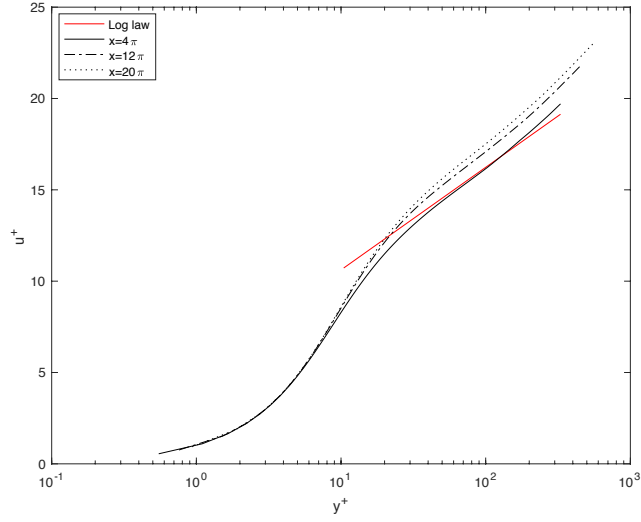
**FIGURE 10:** Friction Reynolds number through  $x$  for Case III.

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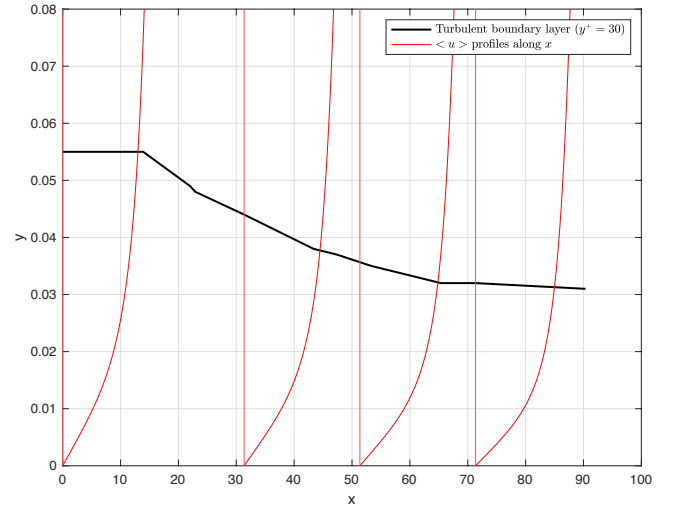
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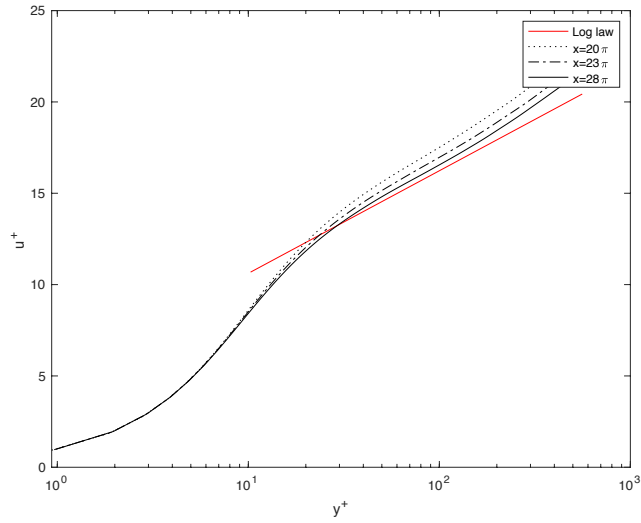
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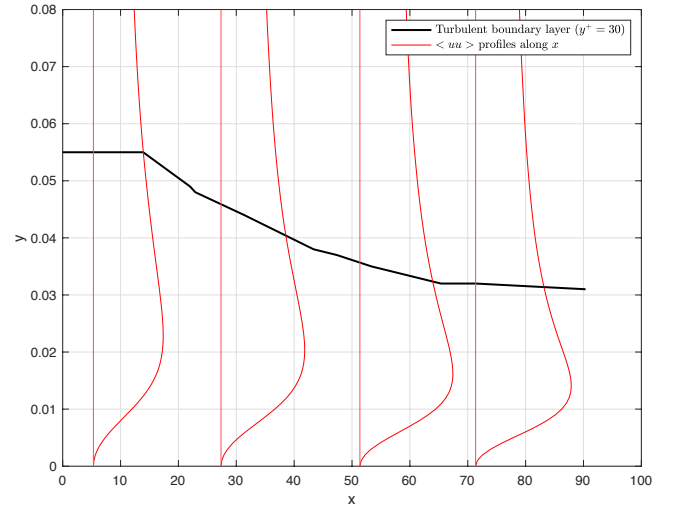
**FIGURE 11:**  $u^+$  versus  $y^+$  obtained from Case I at  $x = 4\pi$  (end of Region I),  $x = 12\pi$  (middle of Region II) and  $x = 20\pi$  (end of Region II) compared to the log law.



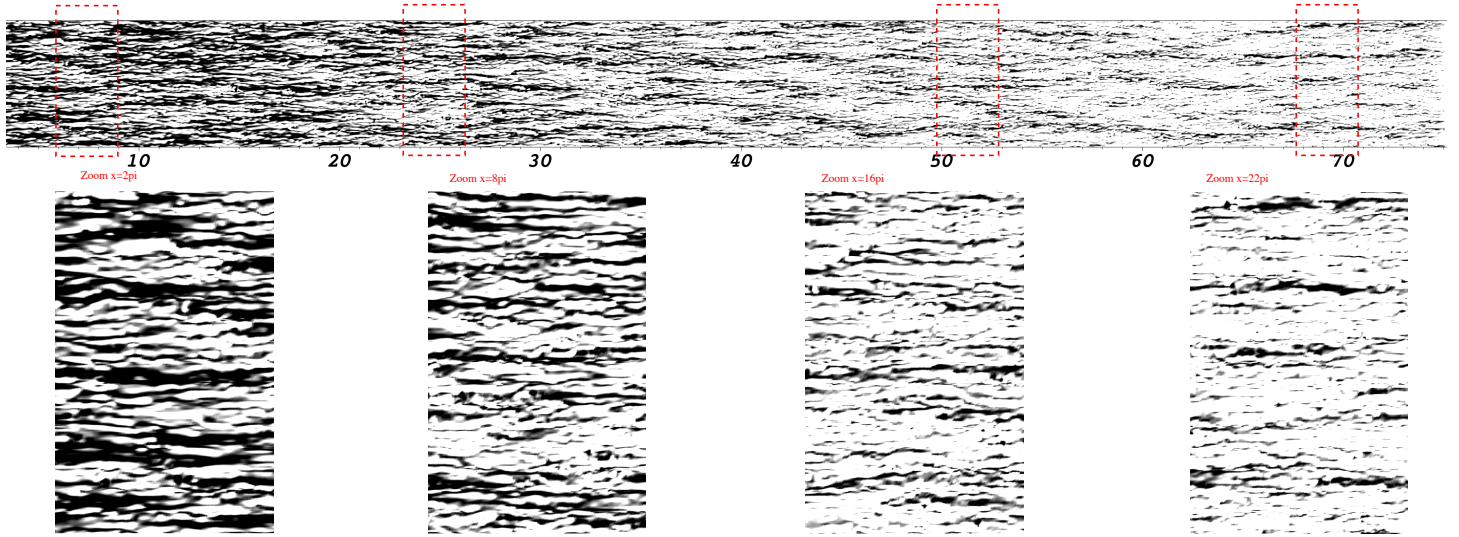
**FIGURE 13:**  $\langle u \rangle$  profiles along the streamwise direction and the turbulent boundary layer ( $y^+ = 30$ ).



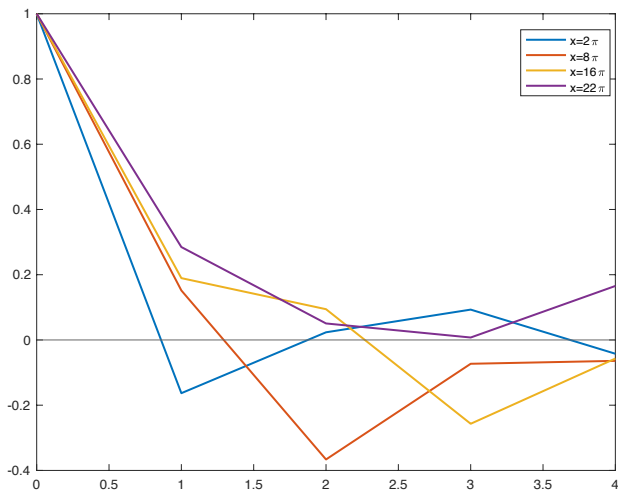
**FIGURE 12:**  $u^+$  versus  $y^+$  obtained from Case I at  $x = 20\pi$  (end of Region I),  $x = 23\pi$  (Region III) and  $x = 28\pi$  (Region III) compared to the log law.



**FIGURE 14:**  $\langle uu \rangle$  profiles along the streamwise direction and the turbulent boundary layer ( $y^+ = 30$ ).



**FIGURE 15:** A cross section of the instantaneous streamwise velocity field at 0.01 from the wall.



**FIGURE 16:** Two-point correlation of  $u$  over the spanwise direction at different streamwise distances.