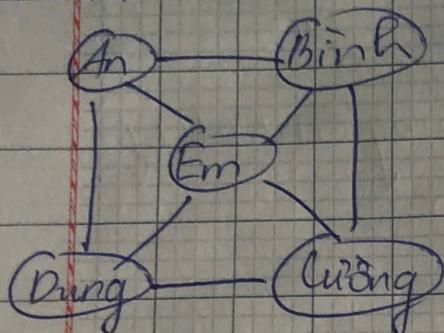


Exercise:



① Calculate density network.

$$n = 5, k_e = 8$$

$$\text{Density} = \frac{k_e}{n(n-1)/2} = \frac{8}{5 \cdot 4 / 2} = 0,8$$

\Rightarrow High Density \Rightarrow Network tends to connectivity strongly, information easily transmitted between actors.

② Identify:

- Degree centrality:

$$Co_D(v) = \frac{\deg(v)}{n-1}$$

$$Co_D(An) = \frac{3}{5-1} = \frac{3}{4} = 0,75 \quad Co_D(Dung) = \frac{3}{4} = 0,75$$

$$Co_D(Binh) = \frac{3}{4} = 0,75$$

$$Co_D(Em) = \frac{4}{4} = 1$$

$$Co_D(Cuong) = \frac{3}{4} = 0,75$$

Actor
 \Rightarrow ~~vertex~~ "Em have highest degree centrality"

\Rightarrow Em is the most important actor in network ~~network~~

~~connection to all others, best info transfer ability, effective network~~

- Closeness centrality:

$$C_c(v) = \frac{1}{\sum_{t \in V \setminus v} d_G(v, t)}$$

$$CC(v) = (n - 1) C_c(v)$$

An Binh Em Cường Dung .

0	1	1	2	1
1	0	1	1	2
1	1	0	1	1
2	1	1	0	1
1	2	1	1	0

~~$C_c(A)$~~ = ~~$\frac{1}{5}$~~

$$C_c(A) = C_c(Binh) = C_c(Cuong) = C_c(Dung) = \frac{1}{5}$$

$$C_c(Em) = \frac{1}{4}$$

$$CC(A) = CC(Binh) = CC(Cuong) = CC(Dung)$$

$$= (n - 1) C_c(v) = (5 - 1) \cdot \frac{1}{5} = \frac{4}{5} = 0,8$$

$$CC(Binh) = 4 \cdot \frac{1}{4} = 1$$

Comments: \Rightarrow Vertex "Em" has highest closeness centrality ~~level~~

~~↳~~ \Rightarrow "Em" has highest level.

• Between centrality

$$C_B(v) = \sum \frac{\delta_{S+}(v)}{\delta_{S+}}$$

$$C'_B = \frac{C_B(v)}{(n-1)(n-2)/2}$$

$$\text{An} \rightarrow \text{Cường (Em)} \Rightarrow \delta_{S+} = 3, \delta_{S+}(Em) = 1$$

$$\text{Dung} \rightarrow \text{Bình (Em)} = \delta_{S+} = 3, \delta_{S+}(Em) = 1.$$

$$C_B(Em) = \sum \frac{\delta_{S+}(Em)}{\delta_{S+}} = \frac{1}{3} + \frac{1}{3} = \frac{2}{3}$$

Normalization coef.

$$(n-1)(n-2)/2 = (5-1)(5-2)/2 = 6.$$

$$C'_B(Em) = \frac{C_B(Em)}{(n-1)(n-2)/2} = \frac{\frac{2}{3}}{6} = \cancel{\frac{2}{3}} \cancel{\frac{1}{6}} 0.11$$

- Comments:

- "Em" occupies ~~33%~~^{11/1} of the possible mediating roles in the graph

~~"Em" is less important, not the only intermediate vertex but plays an important connecting role in the network.~~

- "Em" less important, it doesn't play an important bridging role in the network.

- Clustering Centrality

$$c_i = \frac{2|e_{jk}|}{d_i(d_i - 1)}$$

$$c_i(A_n) = \frac{2 \cdot 2}{3(3-1)} = 0,67.$$

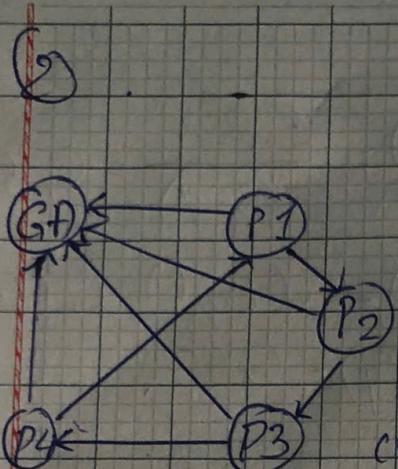
$$\bar{c} = \frac{1}{n} \sum_{i=1}^n c_i$$

$$c_i(A_n) = c_v(Binh) = c_v(Cuong) = \\ c_i(Dung) = 0,67$$

$$c_i(E_m) = \frac{2 \cdot 4}{4(4-1)} = 0,67.$$

⇒ Comments:

- The clustering coefficient (0,67) for each vertex indicates that the degree of connectivity between neighbors is similar.



6. Density network:

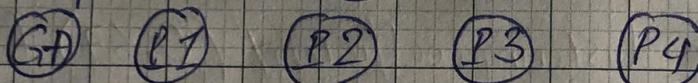
$$n = 5, h = 8.$$

$$\text{Density} = \frac{h}{n(n-1)/2} = 0,8.$$

\Rightarrow High density, \Rightarrow Network tends to connectivity strongly, information easily transmitted between actors.

② Identify input level & output level each vertex.

• Input level: ~~GA~~ = 4.



- Input level 4 1 1 1 1.

- Output level 0 2 2 2 2.

• Closeness centrality:

- Input edge:

- ~~GA~~

$$C_c(GA) = \frac{1}{\sum_{i \in V} d_G(v_i, t)} = \frac{1}{4}.$$

$$CC(GA) = (n - 1) C_c(GA) = 4 \cdot \frac{1}{4} = 1.$$

$$C_c(P_1) = \frac{1}{3 + 2 + 1} = \frac{1}{6}$$

$$CC(P_1) = 4 \cdot \frac{1}{6} = \frac{4}{6} = 0,67.$$

$$C_C(P_2) = \frac{1}{2+3+2} = \frac{1}{6}$$

$$CC(P_2) = 4 \cdot \frac{1}{6} = \frac{4}{6} = 0,67.$$

$$C_C(P_3) = \frac{1}{2+1+3} = \frac{1}{6} \Rightarrow CC(P_3) = 4 \cdot \frac{1}{6} = \frac{4}{6}$$

$$C_C(P_4) = \frac{1}{3+2+1} = \frac{1}{6} \Rightarrow CC(P_4) = 4 \cdot \frac{1}{6} = \frac{4}{6}.$$

- Output edge:

$$C_C(P_1) = \frac{1}{1+1+2+3} = \frac{1}{7}.$$

$$CC(P_1) = 4 \cdot \frac{1}{7} = \frac{4}{7} = 0,57.$$

$$C_C(P_2) = \frac{1}{3+1+2+1} = \frac{1}{7}.$$

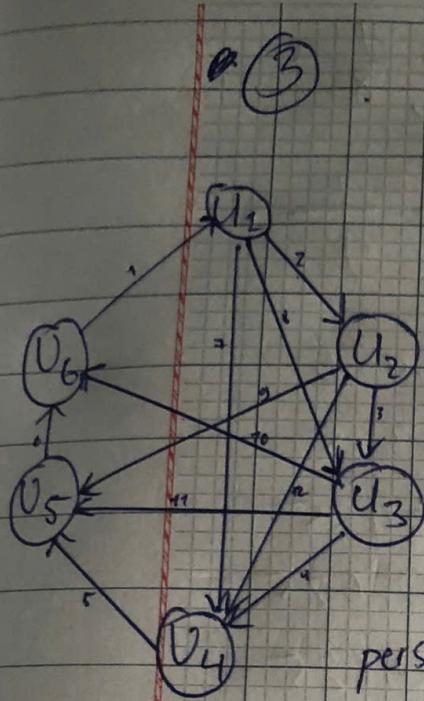
$$CC(P_2) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$

$$C_C(P_3) = \frac{1}{2+3+1+1} = \frac{1}{7}.$$

$$CC(P_3) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$

$$C_C(P_4) = \frac{1}{1+1+2+3} = \frac{1}{7}.$$

$$CC(P_4) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$



① Calculate density network

$$n = 6, \quad t_k = 12$$

$$\text{Density} = \frac{t_k}{n(n-1)/2} = \frac{12}{15} = 0,8$$

\Rightarrow High density \Rightarrow Network tends to connectivity strongly, information easy to transmitted between actors.

② Identify input & output level \rightarrow find person who have the most influential.

	U_1	U_2	U_3	U_4	U_5	U_6
Input level	1	1	2	3	3	2
Output level	3	3	3	1	1	1

~~- Person who have the most influence~~

- The most influential person: U_1, U_2, U_3
- The most concerned person: U_4, U_5 .

③ Calculate

- Closeness Centrality:

Input:

$$C_c(U_1) = \frac{1}{3+2+3+2+1} = \frac{1}{11}$$

$$C_c(U_2) = \frac{1}{1+3+4+3+2} = \frac{1}{13}$$

$$C_c(U_3) = \frac{1}{1+1+4+3+2} = \frac{1}{11}$$

$$C_c(U_4) = \frac{1}{2+1+1+1+3+2} = \frac{1}{8}$$

$$C_c(U_5) = \frac{1}{2+1+1+1+2+3} = \frac{1}{8}$$

$$C_c(U_6) = \frac{1}{3+2+1+2+1} = \frac{1}{9}$$

$$CC(U_1) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$

$$CC(U_2) = 5 \cdot \frac{1}{11} = \frac{5}{11} = 0,455$$

$$CC(U_3) = 5 \cdot \frac{1}{13} = \frac{5}{13} = 0,385$$

$$CC(U_4) = 5 \cdot \frac{1}{11} = \frac{5}{11} = 0,455$$

$$CC(U_5) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$

$$CC(U_6) = 5 \cdot \frac{1}{9} = \frac{5}{9} = 0,56$$

Output :

$$C_c(U_1) = \frac{1}{1+1+1+2+3} = \frac{1}{8}$$

$$C_c(U_2) = \frac{1}{3+1+1+1+2} = \frac{1}{8}$$

$$C_c(U_3) = \frac{1}{2+3+1+1+1} = \frac{1}{8}$$

$$C_c(U_4) = \frac{1}{3+4+4+1+2} = \frac{1}{14}$$

$$C_c(U_5) = \frac{1}{2+3+3+3+2} = \frac{1}{12}$$

$$C_c(U_6) = \frac{1}{1+2+2+2+3} = \frac{1}{10}$$

~~$$CC(U_1) = \frac{1}{8}$$~~

$$CC(U_1) = CC(U_2) = CC(U_3) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$

$$CC(U_4) = 5 \cdot \frac{1}{14} = \frac{5}{14} = 0,357$$

$$CC(U_5) = 5 \cdot \frac{1}{12} = \frac{5}{12} = 0,41667$$

$$CC(U_6) = 5 \cdot \frac{1}{10} = \frac{5}{10} = 0,5$$

Comments :

- Input level : $CC(U_3)$ has smallest distance
so it has largest transmission capacity .
- Output level : $CC(U_4)$ has smallest distance
so it has largest transmission capacity .