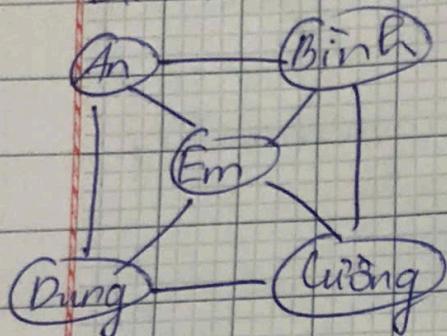


Exercise.



① Calculate density network.

$$n = 5, k = 8$$

$$\text{Density} = \frac{k}{n(n-1)/2} = \frac{8}{5 \cdot 4 / 2} = 0,8$$

\Rightarrow High Density \Rightarrow Network tends to connectivity strongly, information easily transmitted between actors.

② Identify:

- Degree centrality.

$$C_D(v) = \frac{\deg(v)}{n-1}$$

$$C_D(A_n) = \frac{3}{5-1} = \frac{3}{4} = 0,75 \quad C_D(Dung) = \frac{3}{4} = 0,75$$

$$C_D(Binh) = \frac{3}{4} = 0,75 \quad C_D(Em) = \frac{4}{4} = 1$$

$$C_D(Cuong) = \frac{3}{4} = 0,75$$

\Rightarrow Actor ~~Em~~ "Em have highest degree centrality"

\Rightarrow Em is the most important actor in network.

~~connection~~, ~~center~~, ~~best for transfer~~, ~~ability~~, ~~effect~~ ~~network~~

- Closeness centrality.

$$C_c(v) = \frac{1}{\sum_{t \in V, v} d_G(v, t)}$$

$$CC(v) = (n - 1) C_c(v)$$

Anh	Binh	Em	Cường	Dung
0	1	1	2	1
1	0	1	1	2
1	1	0	1	1
2	1	1	0	1
1	2	1	1	0

~~$C_c(v)$~~ = ~~$\frac{1}{4}$~~

$$C_c(An) = C_c(Binh) = C_c(Cuong) = C_c(Dung) = \frac{1}{5}$$

$$C_c(Em) = \frac{1}{4}$$

$$CC(An) = CC(Binh) = CC(Cuong) = CC(Dung) \\ = (n - 1) C_c(v) = (5 - 1) \cdot \frac{1}{5} = \frac{4}{5} = 0,8$$

$$CC(Em) = 4 \cdot \frac{1}{4} = 1$$

Comments: \Rightarrow Vertex "Em" has highest closeness centrality ~~level~~

~~level~~ \Rightarrow "Em" has highest level.

• Between centrality:

$$C_B(v) = \sum \frac{\delta_{S+}(v)}{\delta_{S+}}$$

$$C'_B = \frac{C_B(v)}{(n-1)(n-2)/2}$$

$$\text{An} \rightarrow \text{Giồng (Em)} \Rightarrow \delta_{S+} = 3, \delta_{S+}(\text{Em}) = 1$$

$$\text{Dung} \rightarrow \text{Bình (Em)} = \delta_{S+} = 3, \delta_{S+}(\text{Em}) = 1.$$

$$C_B(\text{Em}) = \sum \frac{\delta_{S+}(\text{Em})}{\delta_{S+}} = \frac{1}{3} + \frac{1}{3} = \underline{\underline{0}} \underline{\underline{2}} \quad \underline{\underline{0}} \frac{2}{3}$$

Normalization coef:

$$(n-1)(n-2)/2 = (5-1)(5-2)/2 = 6.$$

$$C'_B(\text{Em}) = \frac{C_B(\text{Em})}{(n-1)(n-2)/2} = \frac{\underline{\underline{0}} \underline{\underline{2}}}{6} = \cancel{\underline{\underline{0}} \cancel{\underline{\underline{2}}} \cancel{\underline{\underline{3}}}} 0.11$$

- Comments:

11/1

- "Em" occupies ~~33%~~ of the possible mediating roles in the graph.

- "Em" is ~~more~~ less important, not the only intermediate vertex but plays an important connecting role in the network.

- "Em" less important, it doesn't play an important bridging role in the network.



- Clustering Centrality

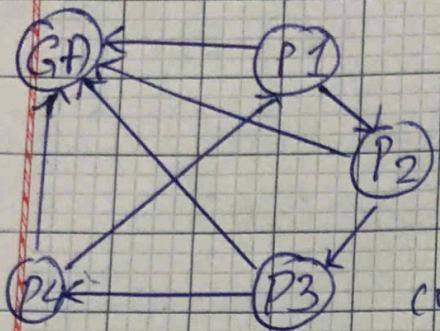
$$c_i = \frac{2|e_{ijk}|}{d_i(d_i - 1)} \quad c_i(A_n) = \frac{2 \cdot 2}{3(3-1)} = 0,67.$$

$$\bar{c} = \frac{1}{n} \sum_{i=1}^n c_i \quad c_i(Binh) = c_i(Wöng) = \\ c_i(Dung) = 0,67$$

$$c_i(E_m) = \frac{2 \cdot 4}{4(4-1)} = 0,67.$$

⇒ Comments:

- The clustering coefficient (0,67) for each vertex indicates that the degree of connectivity between neighbours is similar.



6. Density network:

$$n = 5, h = 8.$$

$$\text{Density} = \frac{h}{n(n-1)/2} = 0,8$$

\Rightarrow High density, \Rightarrow Network tends to connectivity strongly, information easily transmitted between actors.

② - Identify input level & output level each vertex.

- Input level: ~~G'D~~ = 4.

~~G'D~~ P1 P2 P3 P4

- Input level 4 1 1 1 1.

Output level 0 2 2 2 2.

- Closeness centrality:

- ~~Input edge~~:

- ~~Output edge~~:

$$CC_c(G'D) = \frac{1}{\sum_{t \in V, t \neq G'D} d_{G'D}(v,t)} = \frac{1}{4}$$

$$CC(G'D) = (n-1) C_c(G'D) = 4 \cdot \frac{1}{4} = 1.$$

$$C_c(P_1) = \frac{1}{3+2+1} = \frac{1}{6}$$

$$CC(P_1) = 4 \cdot \frac{1}{6} = \frac{4}{6} = 0,67.$$

$$C_c(P_2) = \frac{1}{1+3+2} = \frac{1}{6}$$

$$CC(P_2) = 4 \cdot \frac{1}{6} = \frac{4}{6} = 0.67.$$

$$C_c(P_3) = \frac{1}{2+1+3} = \frac{1}{6} \Rightarrow CC(P_3) = 4 \cdot \frac{1}{6} = \frac{4}{6}$$

$$C_c(P_4) = \frac{1}{3+2+1} = \frac{1}{6} \Rightarrow CC(P_4) = 4 \cdot \frac{1}{6} = \frac{4}{6}$$

- Output edge:

$$C_c(P_1) = \frac{1}{1+1+2+3} = \frac{1}{7}$$

$$CC(P_1) = 4 \cdot \frac{1}{7} = \frac{4}{7} = 0.57.$$

$$C_c(P_2) = \frac{1}{3+1+2+1} = \frac{1}{7}$$

$$CC(P_2) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$

$$C_c(P_3) = \frac{1}{2+3+1+1} = \frac{1}{7}.$$

$$CC(P_3) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$

$$C_c(P_4) = \frac{1}{1+1+2+3} = \frac{1}{7}.$$

$$CC(P_4) = 4 \cdot \frac{1}{7} = \frac{4}{7}.$$

Comments:

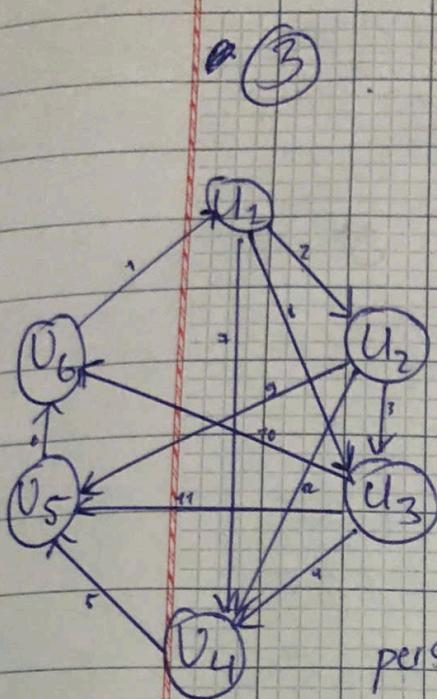
- Closeness centrality for input edges.
- $CC(GD) = 1 \Rightarrow GD$ is the intermediary receiving information from all departments.
- $CC(P_1) = CC(P_2) = CC(P_3) = CC(P_4) = 0,67 \Rightarrow$ ability ~~receiving~~ to receive information from other departments is average -.
- Closeness & centrality for output edge.
- $CC(GD)$ is not exist due to it don't have output edge.
- $CC(P_1) = CC(P_2) = CC(P_3) = CC(P_4) = 0,57 \Rightarrow$ ability to receive information from other departments is average.

① Calculate density network.

$$n = 6, \quad k_2 = 12$$

$$\text{Density} = \frac{k_2}{n(n-1)/2} = \frac{12}{15} = 0.8$$

\Rightarrow high density \Rightarrow Network tends to connectivity strongly, information easy to transmitted between actors.



② Identify input & output level \rightarrow find person who have the most influential

	U_1	U_2	U_3	U_4	U_5	U_6
Input level	1.	1	2	3	3	2
Output level	3	3	3	1.	1	2

~~- Person who have the most influence~~

- The most influential person: U_2, U_2, U_3
- The most concerned person: U_4, U_5 .

③ Calculate

- Closeness Centrality:

Input:

$$C_c(U_1) = \frac{1}{3+2+3+2+2} = \frac{1}{11}$$

$$C_c(U_2) = \frac{1}{1+3+4+3+2} = \frac{1}{13}$$

$$C_c(U_3) = \frac{1}{1+1+4+3+2} = \frac{1}{11}$$

$$C_c(U_4) = \frac{1}{2+2+1+1+3+2} = \frac{1}{8}$$

$$C_c(U_5) = \frac{1}{2+2+1+1+3} = \frac{1}{8}$$

$$C_c(U_6) = \frac{1}{\cancel{2+2+1+2+1}} = \frac{1}{8}$$

$$CC(U_1) = 5 \cdot \frac{1}{11} = \frac{5}{11} = 0,455$$

$$CC(U_2) = 5 \cdot \frac{1}{13} = \frac{5}{13} = 0,385$$

$$-CC(U_3) = 5 \cdot \frac{1}{11} = \frac{5}{11} = 0,455$$

$$CC(U_4) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$

$$CC(U_5) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$

$$-CC(U_6) = 5 \cdot \frac{1}{8} = \frac{5}{8} = \cancel{0,56} \cdot 0,625$$

Output :

$$C_c(U_1) = \frac{1}{1+1+1+2+2} = \frac{1}{8}$$

$$C_c(U_2) = \frac{1}{3+1+2+1+2} = \frac{1}{9}$$

$$C_c(U_3) = \frac{1}{2+3+1+2+1} = \frac{1}{8}$$

$$C_c(U_4) = \frac{1}{3+4+4+1+2} = \frac{1}{14}$$

$$C_c(U_5) = \frac{1}{2+3+3+3+2} = \frac{1}{12}$$

$$C_c(U_6) = \frac{1}{1+2+2+2+3} = \frac{1}{10}$$

~~$$CC(U_1) = \frac{1}{11} = 0,091$$~~

$$CC(U_1) = 5 \cdot \frac{1}{11} = \frac{5}{11} = 0,455$$

~~$$CC(U_2) = CC(U_3) = CC(U_4) = 5 \cdot \frac{1}{8} = \frac{5}{8} = 0,625$$~~

$$CC(U_4) = 5 \cdot \frac{1}{14} = \frac{5}{14} = 0,357.$$

$$CC(U_5) = 5 \cdot \frac{1}{12} = \frac{5}{12} = 0,41667.$$

$$CC(U_6) = 5 \cdot \frac{1}{10} = \frac{5}{10} = 0,5$$

Comments :

- Input level : $CC(U_3)$ has smallest distance ~~so it has largest transmission capacity~~.
So it has largest transmission capacity.
- Output level : $CC(U_9)$ has smallest distance
so it has largest transmission capacity.