



Wittgenstein Centre

FOR DEMOGRAPHY AND  
GLOBAL HUMAN CAPITAL



ÖAW



# Challenges in Estimating the Case Fatality Rate: Lessons from Demography

International Workshop  
Fourth Meeting of the Advisory Board  
Excess Deaths and Life-Years Lost Due to the Covid-19 Pandemic in Denmark  
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# The CFR is particularly sensitive to <sup>1</sup>:

$$CFR_{t,a} = \frac{Deaths_{t,a}}{Reported\ Cases_{t,a}}$$

**Any** factor that impacts the number of **confirmed deaths** from a disease and the number of **reported cases** in a given time

- demographic factors
- delays in reported cases
- testing policies

[1] (Dowd et al. 2020; Rajgor et al. 2020; Goldstein and Lee 2020; Green et al. 2020; Harman et al. 2021; Smith 2021; Luo et al. 2021; Undurraga et al. 2021)

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The CFR can be expressed as the sum of age-specific CFRs weighted by the proportion of cases in a certain age group <sup>1</sup>

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**Hence, one can decompose/split the CFR into two parts:**

$$CFR_i - CFR_j = \alpha + \delta$$

with  $\alpha$  being the age-structure of detected cases and  $\delta$  the age-structure of case-fatality rates

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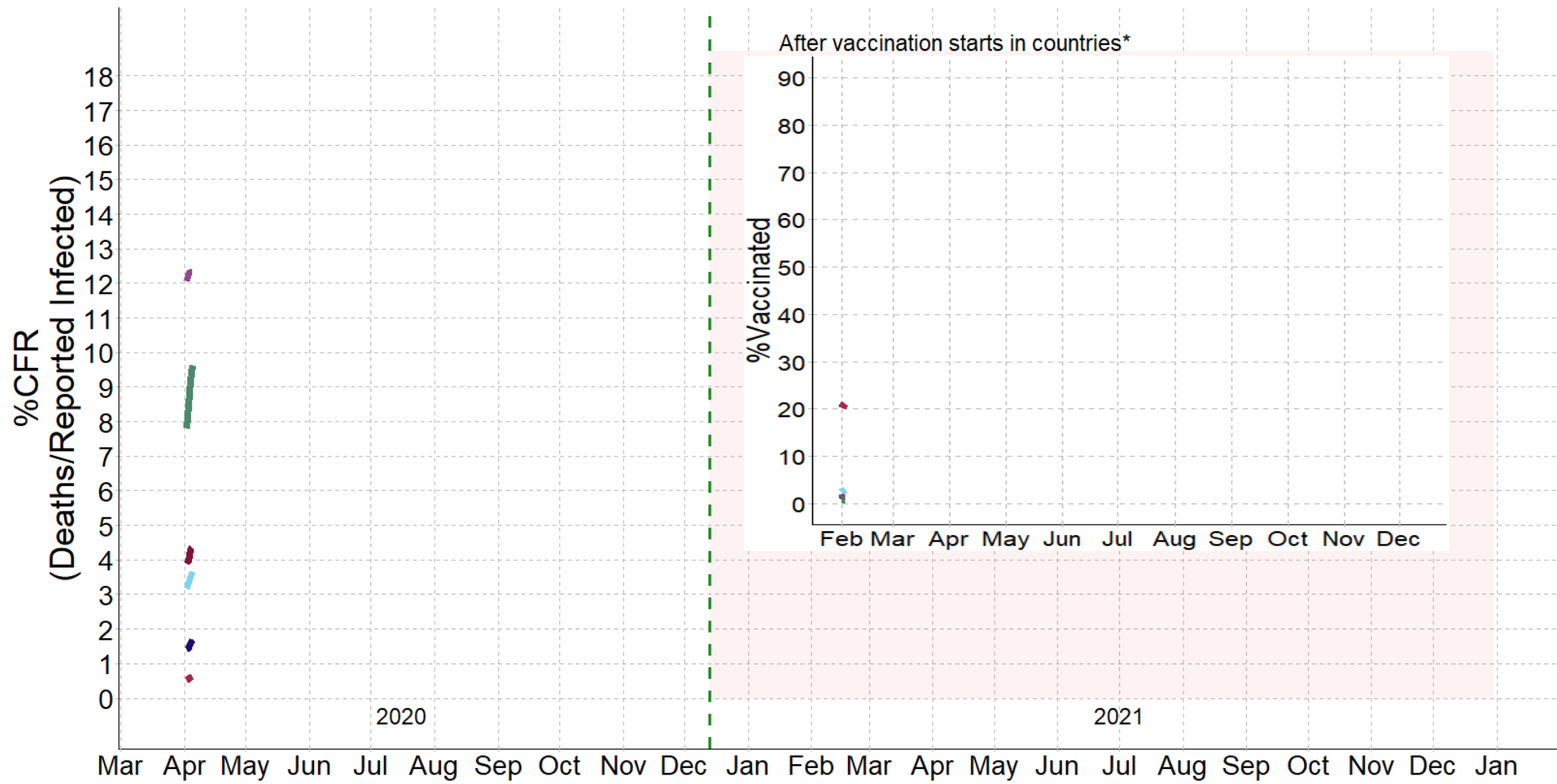
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- the age-structure of detected cases  $\alpha$  explained >60% of cross-country variation
- the age-structure of case-fatality rates  $\delta$  within countries across time - mortality due to increasing age-specific case-fatality rates.]

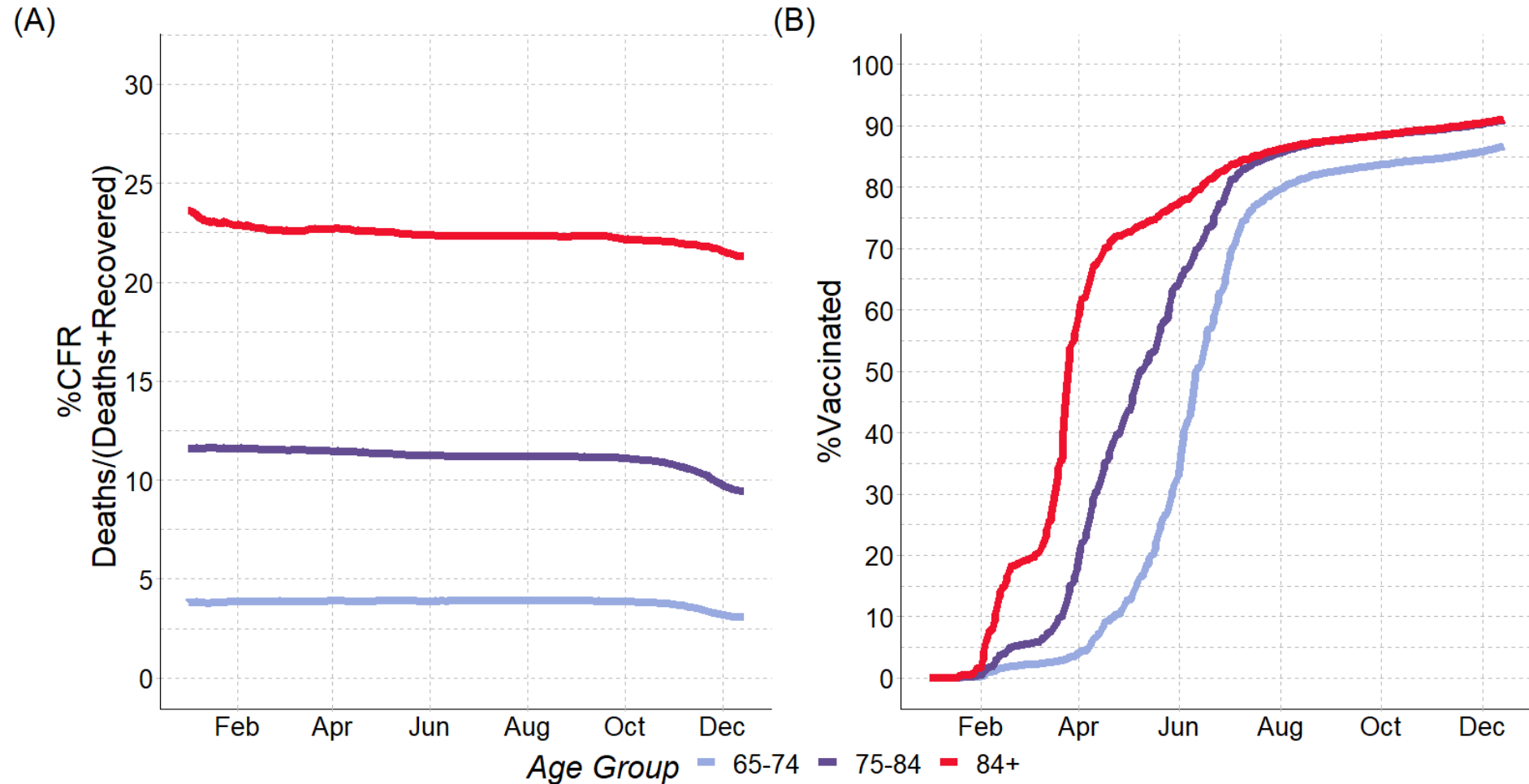
What happens in the presence of vaccines?

Fig. 1 Case Fatality Rate (CFR) and %Fully Vaccinated Trajectories



Source: Our World in Data (Mathieu et al. 2021)

Fig. 2 Panel (A) %Case-Fatality Rate (CFR); Panel (B) Share of fully vaccinated persons (%). Austria, by age, from Jan to Dec 2021



What drives the patterns in the CFR in the presence of vaccines?

$$\text{CFR}_{t,a} = \frac{\mathcal{D}_{t,a}^U + \mathcal{D}_{t,a}^V}{d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V}$$

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Let  $m_a > 0$  be the COVID fatality rate for the age group  $a$  and  $\beta_a \in (0, 1)$  the effectiveness of vaccines in preventing deaths among the infected



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Then, the fatality rate of the unvaccinated can be defined as  $m_a$ , while the fatality rate of the vaccinated becomes  $m_a(1 - \beta_a)$  (by definition smaller than  $m_a$ ).

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Since the total number of deaths is given by the total number of infected times the associated fatality rate, we can rewrite  $\text{CFR}_{t,a}$  as:

$$\text{CFR}_{t,a} = \frac{m_a \mathcal{I}_{t,a}^U + m_a(1 - \beta_a) \mathcal{I}_{t,a}^V}{d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V}$$

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Taking  $m_a$  as common factor and multiplying and dividing by  $d_{t,a}^U$  gives:

$$\text{CFR}_{t,a} = \frac{m_a}{d_{t,a}^U} \frac{d_{t,a}^U \mathcal{I}_{t,a}^U + (1 - \beta_a) d_{t,a}^U \mathcal{I}_{t,a}^V}{d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V}$$

If we call  $\gamma_{t,a} = d_{t,a}^V \mathcal{I}_{t,a}^V / (d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V)$  the ratio between cases among the vaccinated and the total number of ever infected and detected cases, The case fatality rate can be rewritten as:

$$\text{CFR}_{t,a} = \frac{m_a}{d_{t,a}^U} \left( (1 - \gamma_{t,a}) + (1 - \beta_a) \frac{d_{t,a}^U}{d_{t,a}^V} \gamma_{t,a} \right)$$

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The value of  $\gamma_{t,a} \in [0, 1)$  will increase the higher is the number of cases among vaccinated individuals.

Denoting  $Z_{t,a} = d_{t,a}^V/d_{t,a}^U$  as the proportion of detected cases among the ever infected after being vaccinated and the proportion detected among the ever infected and unvaccinated and substituting in the previous equation yields

$$\text{CFR}_{t,a} = \frac{m_a}{d_{t,a}^U} \left( (1 - \gamma_{t,a}) + \frac{1 - \beta_a}{Z_{t,a}} \gamma_{t,a} \right)$$

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**This equation shows that the observed  $\text{CFR}_{t,a}$  is the weighted sum of the CFR of the unvaccinated  $\text{CFR}_{t,a}^U = m_a/d_{t,a}^U$  and the CFR of the vaccinated**

$$\text{CFR}_{t,a}^V = (m_a/d_{t,a}^U)((1 - \beta_a)/Z_{t,a}) = m_a(1 - \beta_a)/d_{t,a}^V$$



$$\text{CFR}_{t,a} = \frac{\mathcal{D}_{t,a}^U + \mathcal{D}_{t,a}^V}{d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V} = \text{CFR}_{t,a}^U (1 - \gamma_{t,a}) + \text{CFR}_{t,a}^V \gamma_{t,a}$$

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$\text{CFR}_{t,a}$  being the weighted sum of  $\text{CFR}_{t,a}^U$  and  $\text{CFR}_{t,a}^V$  with weights  $\gamma_{t,a}$ :

$$\gamma_{t,a} = \frac{d_{t,a}^V \mathcal{I}_{t,a}^V}{d_{t,a}^U \mathcal{I}_{t,a}^U + d_{t,a}^V \mathcal{I}_{t,a}^V}$$

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the ratio between the total number of COVID vaccine **breakthroughs** and the total number of COVID-associated ever infected and detected cases

$$\text{CFR}_{t,a} = \text{CFR}_{t,a}^U (1 - \gamma_{t,a}) + \text{CFR}_{t,a}^V \gamma_{t,a}$$

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$$\gamma_{t,a} = 0$$

No **breakthrough** cases:

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$$\gamma_{t,a} = 0$$

$$\gamma_{t,a} \neq 0$$

No **breakthrough** cases:

$$\text{CFR}_{t,a} = \text{CFR}_{t,a}^U$$

How does  $\text{CFR}_{t,a}^V \gamma_{t,a}$  affect the  $\text{CFR}_{t,a}$ ?

$$\text{CFR}_{t,a}^V = \text{CFR}_{t,a}^U \frac{(1 - \beta_a)}{Z_{t,a}}$$

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$\beta_a$  = effectiveness of vaccines in preventing deaths

$Z_{t,a}$  = ratio of detection rates between the vaccinated and the unvaccinated

if  $Z_{t,a} = 1$ , the rate of detection among vaccinated and unvaccinated is the same



$$\text{CFR}_{t,a}^V = \text{CFR}_{t,a}^U \frac{(1 - \beta_a)}{Z_{t,a}}$$

$$(1 - \beta_a) = Z_{t,a}$$

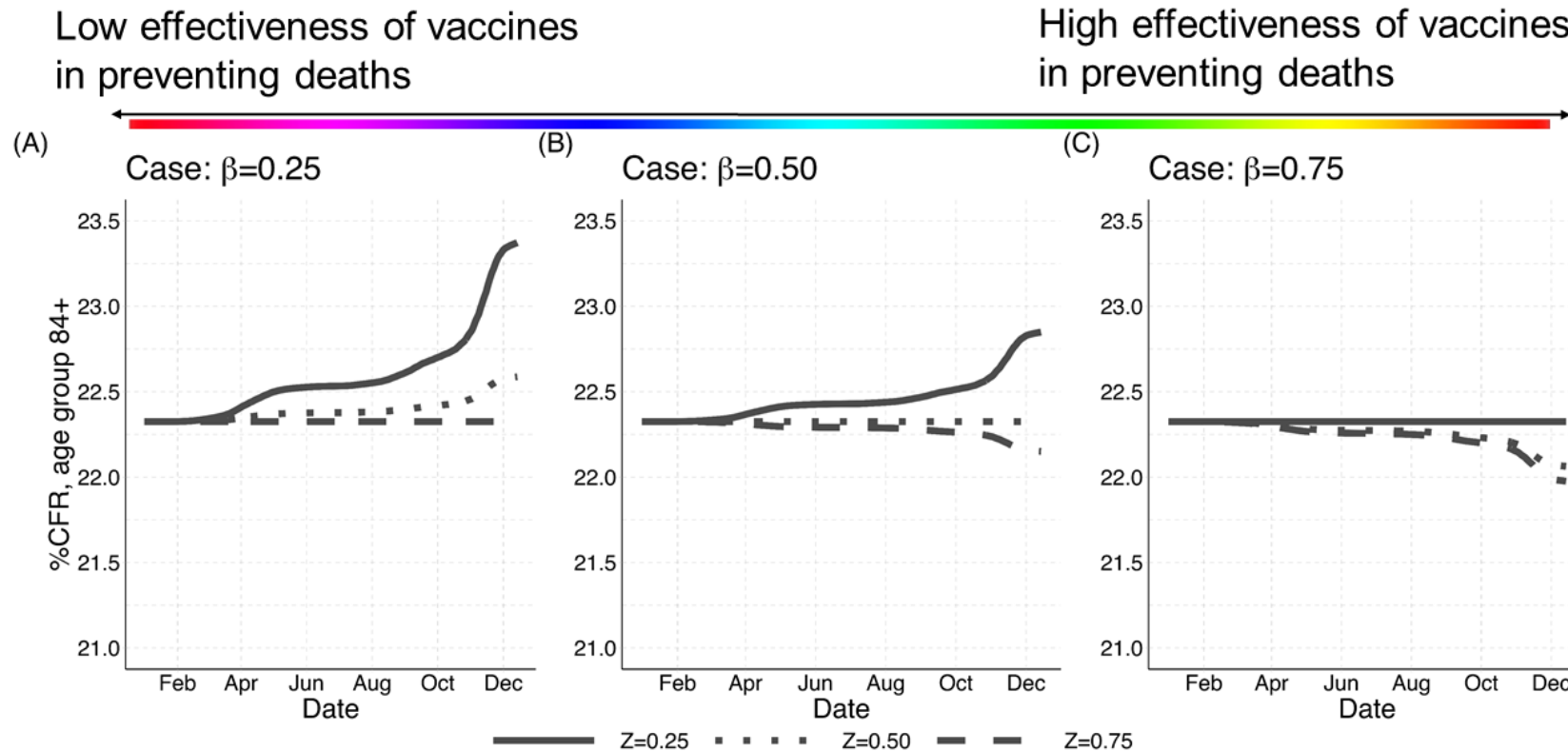
the CFR will remain **unchanged**, regardless the fact that the case fatality rate of the vaccinated is **lower** than the case fatality rate of the unvaccinated.

$\beta_a$  = effectiveness of vaccines in preventing deaths

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Figure 3. Evolution of the %CFR for the age group 84+ in Austria (Jan-Dec 2021) by three different parameter values of  $\beta_{(84+)}$  and  $Z_{(t,84+)}$



# Conclusions

- A constant CFR can **still** mean that vaccines are effective in reducing deaths
- Detecting infections among both the vaccinated and unvaccinated population is key
- Unless vaccinated people are **also** tested, it is hard to use the CFR as an indicator for monitoring the pandemic
- However - CFR still useful measure for policy makers - how to improve/alternative measures
- Excess mortality also has its issues - maybe "temporary aging"?

Thank you!

