Show that the solution of the initial value problem

$$L[y] = y" + p(t)y' + q(t)y = g(t), y(t_0) = y_0, y'(t_0) = y_0' \tag{1}$$