

I Show that $\mathcal{L}f(ct) = \frac{1}{c}F(\frac{s}{c})$

Definition 1 (Laplace Transform). $F(s) = \mathcal{L}f(t), s > a \geq 0 \ s > ca$

$$\mathcal{L}f(ct) = \int_0^\infty e^{-st} f(ct) dt$$

$$u = ct, \frac{u}{c} = t$$

$$\frac{du}{dt} = c$$

$$\frac{1}{c} du = dt$$

$$\mathcal{L}f(ct) = \frac{1}{c} \int_0^\infty e^{-\frac{su}{c}} f(u) du$$

$$t = u$$

$$dt = du$$

$$\mathcal{L}f(ct) = \frac{1}{c}F(\frac{s}{c})$$