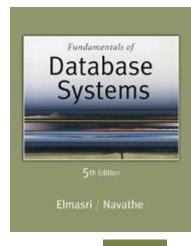


5th Edition

Elmasri / Navathe

Chapter 3

The Relational Algebra and Calculus





Chapter Outline

- Relational Algebra
 - Unary Relational Operations
 - Relational Algebra Operations From Set Theory
 - Binary Relational Operations
 - Additional Relational Operations
 - Examples of Queries in Relational Algebra
- Relational Calculus
 - Tuple Relational Calculus
 - Domain Relational Calculus
- Example Database Application (COMPANY)
- Overview of the QBE language (appendix D)

Relational Algebra Overview

- Relational algebra is the basic set of operations for the relational model
- These operations enable a user to specify basic retrieval requests (or queries)
- The result of an operation is a new relation, which may have been formed from one or more input relations
 - This property makes the algebra "closed" (all objects in relational algebra are relations)

Relational Algebra Overview (continued)

- The algebra operations thus produce new relations
 - These can be further manipulated using operations of the same algebra
- A sequence of relational algebra operations forms a relational algebra expression
 - The result of a relational algebra expression is also a relation that represents the result of a database query (or retrieval request)

Brief History of Origins of Algebra

- Muhammad ibn Musa al-Khwarizmi (800-847 CE) wrote a book titled al-jabr about arithmetic of variables
 - Book was translated into Latin.
 - Its title (al-jabr) gave Algebra its name.
- Al-Khwarizmi called variables "shay"
 - "Shay" is Arabic for "thing".
 - Spanish transliterated "shay" as "xay" ("x" was "sh" in Spain).
 - In time this word was abbreviated as x.
- Where does the word Algorithm come from?
 - Algorithm originates from "al-Khwarizmi"
 - Reference: PBS (http://www.pbs.org/empires/islam/innoalgebra.html)

Relational Algebra Overview

- Relational Algebra consists of several groups of operations
 - Unary Relational Operations
 - SELECT (symbol: σ (sigma))
 - PROJECT (symbol: π (pi))
 - RENAME (symbol: ρ (rho))
 - Relational Algebra Operations From Set Theory
 - UNION (∪), INTERSECTION (∩), DIFFERENCE (or MINUS,)
 - CARTESIAN PRODUCT (x)
 - Binary Relational Operations
 - JOIN (several variations of JOIN exist)
 - DIVISION
 - Additional Relational Operations
 - OUTER JOINS, OUTER UNION
 - AGGREGATE FUNCTIONS (These compute summary of information: for example, SUM, COUNT, AVG, MIN, MAX)

Unary Relational Operations: SELECT

- The SELECT operation (denoted by σ (sigma)) is used to select a subset of the tuples from a relation based on a selection condition.
 - The selection condition acts as a filter
 - Keeps only those tuples that satisfy the qualifying condition
 - Tuples satisfying the condition are selected whereas the other tuples are discarded (filtered out)
- Examples:
 - Select the EMPLOYEE tuples whose department number is 4:

$$\sigma_{DNO=4}$$
 (EMPLOYEE)

Select the employee tuples whose salary is greater than \$30,000:

$$\sigma_{SALARY > 30,000}$$
 (EMPLOYEE)

Unary Relational Operations: SELECT

- In general, the select operation is denoted by
 - $\sigma_{\text{selection condition}}(R)$ where
 - the symbol σ (sigma) is used to denote the select operator
 - the selection condition is a Boolean (conditional)
 expression specified on the attributes of relation R
 - tuples that make the condition true are selected
 - appear in the result of the operation
 - tuples that make the condition false are filtered out
 - discarded from the result of the operation

Unary Relational Operations: SELECT (contd.)

SELECT Operation Properties

- The SELECT operation $\sigma_{\text{selection condition}}(R)$ produces a relation S that has the same schema (same attributes) as R
- SELECT σ is commutative:
 - $\sigma_{\text{condition1}}(\sigma_{\text{condition2}}(R)) = \sigma_{\text{condition2}}(\sigma_{\text{condition1}}(R))$
- Because of commutativity property, a cascade (sequence) of SELECT operations may be applied in any order:
 - σ_{cond1} (σ_{cond2} (σ_{cond3} (R)) = σ_{cond2} (σ_{cond3} (σ_{cond1} (R)))
- A cascade of SELECT operations may be replaced by a single selection with a conjunction of all the conditions:
 - $\sigma_{\text{<cond1>}}(\sigma_{\text{<cond2>}}(\sigma_{\text{<cond3>}}(R))) = \sigma_{\text{<cond1> AND < cond2> AND < cond3>}}(R))$
- The number of tuples in the result of a SELECT is less than (or equal to) the number of tuples in the input relation R

Unary Relational Operations: PROJECT

- PROJECT Operation is denoted by π (pi)
- This operation keeps certain columns (attributes) from a relation and discards the other columns.
 - PROJECT creates a vertical partitioning
 - The list of specified columns (attributes) is kept in each tuple
 - The other attributes in each tuple are discarded
- Example: To list each employee's first and last name and salary, the following is used:

 $\pi_{\text{LNAME, FNAME,SALARY}}(\text{EMPLOYEE})$

Unary Relational Operations: PROJECT (cont.)

The general form of the *project* operation is:

$$\pi_{\text{}}(R)$$

- \bullet π (pi) is the symbol used to represent the *project* operation
- <attribute list> is the desired list of attributes from relation R.
- The project operation removes any duplicate tuples
 - This is because the result of the project operation must be a set of tuples
 - Mathematical sets do not allow duplicate elements.

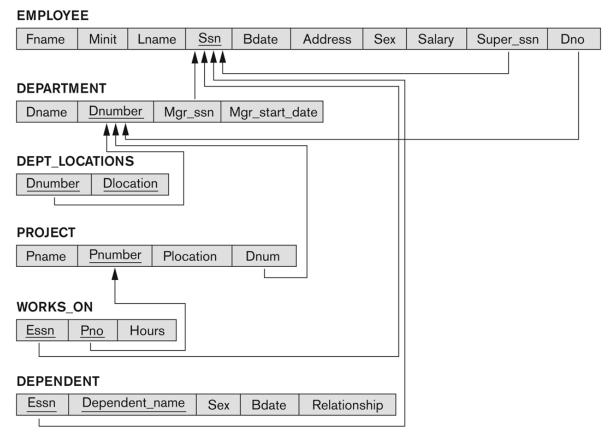
Unary Relational Operations: PROJECT (contd.)

PROJECT Operation Properties

- The number of tuples in the result of projection $\pi_{\text{<list>}}(R)$ is always less or equal to the number of tuples in R
 - If the list of attributes includes a key of R, then the number of tuples in the result of PROJECT is equal to the number of tuples in R
- PROJECT is not commutative
 - $\pi_{\langle list1\rangle}$ ($\pi_{\langle list2\rangle}$ (R)) = $\pi_{\langle list1\rangle}$ (R) as long as $\langle list2\rangle$ contains the attributes in $\langle list1\rangle$

Database State for COMPANY

All examples discussed below refer to the COMPANY database shown here.
 Figure 5.7
Referential integrity constraints displayed on the COMPANY relational database schema.



Bdate

1965-01-09

1955-12-08

1968-01-19

Address

638 Voss, Houston, TX

3321 Castle, Spring, TX

731 Fondren, Houston, TX

Ssn

123456789

333445555

999887777

Franklin

Minit

В

Т

J

Lname

Smith

Wong

Zelaya

Fname

John

Alicia

s	Wallace	98765	4321	1941-06	6-20	291 Be	erry, Bella	ire, TX	F	4300	00	8886	6555	5 4
K	Narayan	66688	34444	1962-09	9-15	975 Fire Oak, Humble, TX		M	380	00	3334	14555	5 5	
Α	English	45345	53453	1972-07	-31	5631 F	Rice, Hou	ıston, TX	F	2500	00	3334	14555	5 5
V	Jabbar	98798	37987	1969-03	3-29	980 D	allas, Hou	uston, TX	М	2500	00	9876	55432	1 4
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987	10	35.0	_	3334455	55	Joy			F	1958	8-05-	оз	Spou	ise
987	30	5.0	╛	9876543	21	Abn	er		М	1942	2-02-	28	Spou	ıse
321	30	20.0]	1234567	89	Mic	hael		м	1988	3-01-	04	Son	
321	20	15.0		12345678	89	Alic	e		F	1988	3-12-	30	Daug	hter
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Salary

30000

40000

25000

Super_ssn

333445555

888665555

987654321

Dno

5

5

4

Sex

M

М

F

Examples of applying SELECT and PROJECT operations

Figure 6.1

Results of SELECT and PROJECT operations. (a) $\sigma_{\text{(Dno=4 AND Salary>25000) OR (Dno=5 AND Salary>30000)}}$ (EMPLOYEE). (b) $\pi_{\text{Lname, Fname, Salary}}$ (EMPLOYEE). (c) $\pi_{\text{Sex, Salary}}$ (EMPLOYEE).

(a)

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5

(b)

Lname	Fname	Salary
Smith	John	30000
Wong	Franklin	40000
Zelaya	Alicia	25000
Wallace	Jennifer	43000
Narayan	Ramesh	38000
English	Joyce	25000
Jabbar	Ahmad	25000
Borg	James	55000

(c)

Sex	Salary
М	30000
М	40000
F	25000
F	43000
М	38000
М	25000
М	55000

Relational Algebra Expressions

- We may want to apply several relational algebra operations one after the other
 - Either we can write the operations as a single relational algebra expression by nesting the operations, or
 - We can apply one operation at a time and create intermediate result relations.
- In the latter case, we must give names to the relations that hold the intermediate results.

Single expression versus sequence of relational operations (Example)

- To retrieve the first name, last name, and salary of all employees who work in department number 5, we must apply a select and a project operation
- We can write a single relational algebra expression as follows:
 - $\pi_{\text{FNAME, LNAME, SALARY}}(\sigma_{\text{DNO}=5}(\text{EMPLOYEE}))$
- OR We can explicitly show the sequence of operations, giving a name to each intermediate relation:
 - DEP5_EMPS $\leftarrow \sigma_{DNO=5}(EMPLOYEE)$
 - RESULT $\leftarrow \pi$ FNAME, LNAME, SALARY (DEP5_EMPS)

Example of applying multiple operations and RENAME

(a)

Fname	Lname	Salary
John	Smith	30000
Franklin	Wong	40000
Ramesh	Narayan	38000
Joyce	English	25000

(b) TEMP

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston,TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston,TX	М	40000	888665555	5
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble,TX	М	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

R

First_name	Last_name	Salary
John	Smith	30000
Franklin	Wong	40000
Ramesh	Narayan	38000
Joyce	English	25000

Figure 6.2

Results of a sequence of operations.

(a) $\pi_{\text{Fname, Lname, Salary}}(\sigma_{\text{Dno=5}}(\text{EMPLOYEE})).$

(b) Using intermediate relations and renaming of attributes.

Unary Relational Operations: RENAME

- The RENAME operator is denoted by ρ (rho)
- In some cases, we may want to rename the attributes of a relation or the relation name or both
 - Useful when a query requires multiple operations
 - Necessary in some cases (see JOIN operation later)

Unary Relational Operations: RENAME (contd.)

- The general RENAME operation ρ can be expressed by any of the following forms:
 - ρ_{S (B1, B2, ..., Bn)}(R) changes both:
 - the relation name to S, and
 - the column (attribute) names to B1, B1,Bn
 - $\rho_{S}(R)$ changes:
 - the relation name only to S
 - ρ_(B1, B2, ..., Bn)(R) changes:
 - the column (attribute) names only to B1, B1,Bn

Unary Relational Operations: RENAME (contd.)

- For convenience, we also use a shorthand for renaming attributes in an intermediate relation:
 - If we write:
 - RESULT $\leftarrow \pi_{\text{FNAME, LNAME, SALARY}}$ (DEP5_EMPS)
 - RESULT will have the same attribute names as DEP5_EMPS (same attributes as EMPLOYEE)
 - · If we write:
 - RESULT (FN, LN, Sal,) $\leftarrow \pi_{\text{FNAME, LNAME, SALARY}}$ (DEP5_EMPS)
 - 3 attributes of RESULT are renamed to FN, LN, Sal respectively

Relational Algebra Operations from Set Theory:

UNION Operation

- Binary operation, denoted by U
- The result of R ∪ S, is a relation that includes all tuples that are either in R or in S or in both R and S
- Duplicate tuples are eliminated
- The two operand relations R and S must be "type compatible" (or UNION compatible)
 - R and S must have same number of attributes
 - Each pair of corresponding attributes must be type compatible (have same or compatible domains)

Relational Algebra Operations from Set Theory

- Type Compatibility of operands is required for the binary set operation UNION ∪, INTERSECTION ∩, and SET DIFFERENCE –,
- R1(A1, A2, ..., An) and R2(B1, B2, ..., Bn) are type compatible if:
 - they have the same number of attributes, and
 - the domains of corresponding attributes are type compatible (i.e. dom(Ai)=dom(Bi) for i=1, 2, ..., n).
- The resulting relation for R1∪R2 (also for R1∩R2, or R1–R2, see next slides) has the same attribute names as the first operand relation R1 (by convention)

Example of the result of a UNION operation

UNION Example

Figure 6.3

Result of the UNION operation RESULT ← RESULT1 URESULT2.

RESULT1

Ssn
123456789
333445555
666884444
453453453

RESULT2

Ssn
333445555
888665555

RESULT

Ssn
123456789
333445555
666884444
453453453
888665555

Relational Algebra Operations from Set Theory: UNION

Example:

- To retrieve the social security numbers of all employees who either work in department 5 (RESULT1 below) or directly supervise an employee who works in department 5 (RESULT2 below)
- We can use the UNION operation as follows:

$$\begin{array}{c} \mathsf{DEP5_EMPS} \leftarrow \sigma_{\mathsf{DNO=5}} \; (\mathsf{EMPLOYEE}) \\ \mathsf{RESULT1} \leftarrow \pi_{\; \mathsf{SSN}} (\mathsf{DEP5_EMPS}) \\ \mathsf{RESULT2} (\mathsf{SSN}) \leftarrow \pi_{\mathsf{SUPERSSN}} (\mathsf{DEP5_EMPS}) \end{array}$$

RESULT ← RESULT1 ∪ RESULT2

 The union operation produces the tuples that are in either RESULT1 or RESULT2 or both

Relational Algebra Operations from Set Theory: INTERSECTION

- INTERSECTION is denoted by ∩
- The result of the operation R ∩ S, is a relation that includes all tuples that are in both R and S
 - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be "type compatible"

Relational Algebra Operations from Set Theory: SET DIFFERENCE (cont.)

- SET DIFFERENCE (also called MINUS or EXCEPT) is denoted by –
- The result of R S, is a relation that includes all tuples that are in R but not in S
 - The attribute names in the result will be the same as the attribute names in R
- The two operand relations R and S must be "type compatible"

Example to illustrate the result of UNION, INTERSECT, and DIFFERENCE

(a) STUDENT

Fn	Ln
Susan	Yao
Ramesh	Shah
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert

INSTRUCTOR

Fname	Lname
John	Smith
Ricardo	Browne
Susan	Yao
Francis	Johnson
Ramesh	Shah

(b)

Fn	Ln
Susan	Yao
Ramesh	Shah
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert
John	Smith
Ricardo	Browne
Francis	Johnson

(c)	Fn	Ln
	Susan	Yao
	Ramesh	Shah

(d)

Fn	Ln
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert

(e)

Fname	Lname
John	Smith
Ricardo	Browne
Francis	Johnson

Figure 6.4

The set operations UNION, INTERSECTION, and MINUS. (a) Two union-compatible relations. (b) STUDENT ∪ INSTRUCTOR. (c) STUDENT ∩ INSTRUCTOR. (d) STUDENT − INSTRUCTOR.

(e) INSTRUCTOR – STUDENT.

Some properties of UNION, INTERSECT, and DIFFERENCE

- Notice that both union and intersection are commutative operations; that is
 - $R \cup S = S \cup R$, and $R \cap S = S \cap R$
- Both union and intersection can be treated as n-ary operations applicable to any number of relations as both are associative operations; that is
 - $R \cup (S \cup T) = (R \cup S) \cup T$
 - $(R \cap S) \cap T = R \cap (S \cap T)$
- The minus operation is not commutative; that is, in general
 - $R S \neq S R$

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT

- CARTESIAN (or CROSS) PRODUCT Operation
 - This operation is used to combine tuples from two relations in a combinatorial fashion.
 - Denoted by R(A1, A2, . . ., An) x S(B1, B2, . . ., Bm)
 - Result is a relation Q with degree n + m attributes:
 - Q(A1, A2, . . ., An, B1, B2, . . ., Bm), in that order.
 - The resulting relation state has one tuple for each combination of tuples—one from R and one from S.
 - Hence, if R has n_R tuples (denoted as $|R| = n_R$), and S has n_S tuples, then R x S will have n_R * n_S tuples.
 - The two operands do NOT have to be "type compatible"

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT (cont.)

- Generally, CROSS PRODUCT is not a meaningful operation
 - Can become meaningful when followed by other operations
- Example (not meaningful):
 - FEMALE_EMPS $\leftarrow \sigma_{SEX='F'}(EMPLOYEE)$
 - EMPNAMES $\leftarrow \pi_{\text{FNAME, LNAME, SSN}}$ (FEMALE_EMPS)
 - EMP_DEPENDENTS ← EMPNAMES x DEPENDENT
- EMP_DEPENDENTS will contain every combination of EMPNAMES and DEPENDENT
 - whether or not they are actually related

Relational Algebra Operations from Set Theory: CARTESIAN PRODUCT (cont.)

- To keep only combinations where the DEPENDENT is related to the EMPLOYEE, we add a SELECT operation as follows
- Example (meaningful):
 - FEMALE_EMPS $\leftarrow \sigma_{\text{SEX='F'}}(\text{EMPLOYEE})$
 - EMPNAMES $\leftarrow \pi_{\text{FNAME, LNAME, SSN}}$ (FEMALE_EMPS)
 - EMP DEPENDENTS ← EMPNAMES x DEPENDENT
 - ACTUAL_DEPS $\leftarrow \sigma_{SSN=ESSN}(EMP_DEPENDENTS)$
 - RESULT $\leftarrow \pi_{\text{FNAME, LNAME, DEPENDENT_NAME}}$ (ACTUAL_DEPS)
- RESULT will now contain the name of female employees and their dependents

Bdate

1965-01-09

1955-12-08

1968-01-19

1941-06-20

Address

638 Voss, Houston, TX

291 Berry, Bellaire, TX

3321 Castle, Spring, TX

731 Fondren, Houston, TX

Ssn

123456789

333445555

999887777

987654321

Franklin

Jennifer

Minit

В

Т

J

S

Lname

Smith

Wong

Zelaya

Wallace

Fname

John

Alicia

K	Narayan	66688	34444	1962-09	-15	975 Fi	975 Fire Oak, Humble, TX		х м	380	38000 333		3445555 5	
Α	English	45345	3453	1972-07	-31	5631 I	6631 Rice, Houston, TX		F	250	25000 333		44555	5 5
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789	1	32.5					Produc	tX	1	1	Ве	llaire		5
789	2	7.5	_				Produc	tY	1 2	2	Su	ıgarla	nd	5
144	3	40.0	_				Produc	tZ	3	3	Ho	ousto	n	5
153	1	20.0	_				Compu	terization	1	0	St	afforc	t l	4
153	2	20.0							2	0				1
555	2	10.0	_				Newbei	nefits	3	0	St	afforc	t l	4
555	3	10.0	_											
555	10	10.0		PEPENDE	NT									
555	20	10.0		Essn		De	pendent_	name	Sex	Bdate			Relationship	
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777	10	10.0	」 ┌	3334455	55	The	odore		м	1983	3-10	-25	Son	
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87	30	5.0	_	9876543	21	Abner			М	1942	1942-02-28		Spot	ıse
321	30	20.0]	12345678	89	Michael			м	1988-01-04		-04	Son	
321	20	15.0		12345678	89	Alic	е		F	1988	1988-12-30		Daug	ghter
555	20	NULL]	12345678	89	Eliza	abeth		F	1967	'-05-	-05	Spor	ıse
	A V E ENT me h tration arters ON 289 444 44 453 453 555 555 555 655 777 787 87 87 87 821 821	A English V Jabbar E Borg ENT me Dnur h Stration arters ON Pno 289 1 289 2 444 3 453 1 453 2 555 2 555 3 555 10 555 20 777 30 777 10 87 30 87 30 87 30 821 30 821 20	A English 45345 V Jabbar 98798 E Borg 88866 ENT me Dnumber h 5 tration 4 arters 1 ON Pno Hours 789 1 32.5 789 2 7.5 444 3 40.0 453 1 20.0 453 2 20.0 655 2 10.0 655 3 10.0 655 3 10.0 655 3 10.0 677 30 30.0 677 10 10.0 687 10 35.0 687 30 5.0 687 30 5.0 687 30 5.0 687 30 5.0 681 30 20.0	A English 453453453 V Jabbar 987987987 E Borg 888665555 ENT me Dnumber Mg tration 4 9876 arters 1 8886 ON Pno Hours 789 1 32.5 789 2 7.5 444 3 40.0 453 1 20.0 453 1 20.0 453 2 20.0 555 2 10.0 555 3 10.0 555 3 10.0 555 10 10.0 677 30 30.0 677 10 10.0 687 10 35.0 687 30 5.0 687 30 5.0 687 30 5.0 681 30 20.0	A English 453453453 1972-07 V Jabbar 987987987 1969-03 E Borg 888665555 1937-11 ENT Me	A English 453453453 1972-07-31 V Jabbar 987987987 1969-03-29 E Borg 888665555 1937-11-10 ENT	A English 453453453 1972-07-31 5631 I V Jabbar 987987987 1969-03-29 980 D E Borg 888665555 1937-11-10 450 Start ENT The Dnumber Mgr_ssn Mgr_star	A English 453453453 1972-07-31 5631 Rice, Hou V Jabbar 987987987 1969-03-29 980 Dallas, Hou E Borg 888665555 1937-11-10 450 Stone, Hou ENT The Dnumber Mgr_ssn Mgr_start_date h 5 333445555 1988-05-22 tration 4 987654321 1995-01-01 arters 1 888665555 1981-06-19 DN PROJECT Product Pro	A English 453453453 1972-07-31 5631 Rice, Houston, TX V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX E Borg 888665555 1937-11-10 450 Stone, Houston, TX ENT	A English 453453453 1972-07-31 5631 Rice, Houston, TX F V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M E Borg 888665555 1937-11-10 450 Stone, Houston, TX M M ENT	A English 453453453 1972-07-31 5631 Rice, Houston, TX F 250 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 250 E Borg 888665555 1937-11-10 450 Stone, Houston, TX M 550 ENT Dept. Doumber Mgr_ssn Mgr_start_date	A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000 E Borg 888665555 1937-11-10 450 Stone, Houston, TX M 55000 ENT Dept	A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 333-0 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000 9876 E Borg 888665555 1937-11-10 450 Stone, Houston, TX M 55000 NULL ENT	A English 453453453 1972-07-31 5631 Rice, Houston, TX F 25000 333445555 V Jabbar 987987987 1969-03-29 980 Dallas, Houston, TX M 25000 98765432 E Borg 888665555 1937-11-10 450 Stone, Houston, TX M 55000 NULL ENT Dept

Sex

M

М

F

F

Salary

30000

40000

25000

43000

Super_ssn

333445555

888665555

987654321

888665555

Dno

5

5

4

4

FEMALE_EMPS

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
Alicia	J	Zelaya	999887777	1968-07-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	s	Wallace	987654321	1941-06-20	291Berry, Bellaire, TX	F	43000	888665555	4
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

EMPNAMES

Fname	Lname	Ssn
Alicia	Zelaya	999887777
Jennifer	Wallace	987654321
Joyce	English	453453453

EMP DEPENDENTS

EMP_DE							
Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Alicia	Zelaya	999887777	333445555	Alice	F	1986-04-05	
Alicia	Zelaya	999887777	333445555	Theodore	M	1983-10-25	
Alicia	Zelaya	999887777	333445555	Joy	F	1958-05-03	
Alicia	Zelaya	999887777	987654321	Abner	M	1942-02-28	
Alicia	Zelaya	999887777	123456789	Michael	M	1988-01-04	
Alicia	Zelaya	999887777	123456789	Alice	F	1988-12-30	
Alicia	Zelaya	999887777	123456789	Elizabeth	F	1967-05-05	
Jennifer	Wallace	987654321	333445555	Alice	F	1986-04-05	
Jennifer	Wallace	987654321	333445555	Theodore	M	1983-10-25	
Jennifer	Wallace	987654321	333445555	Joy	F	1958-05-03	
Jennifer	Wallace	987654321	987654321	Abner	M	1942-02-28	
Jennifer	Wallace	987654321	123456789	Michael	M	1988-01-04	
Jennifer	Wallace	987654321	123456789	Alice	F	1988-12-30	
Jennifer	Wallace	987654321	123456789	Elizabeth	F	1967-05-05	
Joyce	English	453453453	333445555	Alice	F	1986-04-05	
Joyce	English	453453453	333445555	Theodore	M	1983-10-25	
Joyce	English	453453453	333445555	Joy	F	1958-05-03	
Joyce	English	453453453	987654321	Abner	M	1942-02-28	
Joyce	English	453453453	123456789	Michael	М	1988-01-04	
Joyce	English	453453453	123456789	Alice	F	1988-12-30	
Joyce	English	453453453	123456789	Elizabeth	F	1967-05-05	

ACTUAL_DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Jennifer	Wallace	987654321	987654321	Abner	М	1942-02-28	

RESULT

	Fname	Lname	Dependent_name
Γ	Jennifer	Wallace	Abner

Binary Relational Operations: JOIN

- JOIN Operation (denoted by ⋈)
 - The sequence of CARTESIAN PRODECT followed by SELECT is used quite commonly to identify and select related tuples from two relations
 - A special operation, called JOIN combines this sequence into a single operation
 - This operation is very important for any relational database with more than a single relation, because it allows us combine related tuples from various relations
 - The general form of a join operation on two relations R(A1, A2, . . ., An) and S(B1, B2, . . ., Bm) is:

 R_{\bowtie} <join condition>S

 where R and S can be any relations that result from general relational algebra expressions.

Binary Relational Operations: JOIN (cont.)

- Example: Suppose that we want to retrieve the name of the manager of each department.
 - To get the manager's name, we need to combine each DEPARTMENT tuple with the EMPLOYEE tuple whose SSN value matches the MGRSSN value in the department tuple.
 - We do this by using the join operation.
 - DEPT_MGR ← DEPARTMENT MGRSSN=SSN EMPLOYEE
- MGRSSN=SSN is the join condition
 - Combines each department record with the employee who manages the department
 - The join condition can also be specified as DEPARTMENT.MGRSSN= EMPLOYEE.SSN

Example of applying the JOIN operation

DEPT_MGR

Dname	Dnumber	Mgr_ssn	 Fname	Minit	Lname	Ssn	
Research	5	333445555	 Franklin	Т	Wong	333445555	
Administration	4	987654321	 Jennifer	S	Wallace	987654321	
Headquarters	1	888665555	 James	E	Borg	888665555	

Figure 6.6 Result of the JOIN operation

Some properties of JOIN

- Consider the following JOIN operation:
 - R(A1, A2, ..., An)
 S(B1, B2, ..., Bm)
 R.Ai=S.Bj
 - Result is a relation Q with degree n + m attributes:
 - Q(A1, A2, . . ., An, B1, B2, . . ., Bm), in that order.
 - The resulting relation state has one tuple for each combination of tuples—r from R and s from S, but only if they satisfy the join condition r[Ai]=s[Bj]
 - Hence, if R has n_R tuples, and S has n_S tuples, then the join result will generally have less than n_R * n_S tuples.
 - Only related tuples (based on the join condition) will appear in the result

Some properties of JOIN

- The general case of JOIN operation is called a Theta-join: R
 S
 theta
- The join condition is called theta
- Theta can be any general boolean expression on the attributes of R and S; for example:
 - R.Ai<S.Bj AND (R.Ak=S.Bl OR R.Ap<S.Bq)
- Most join conditions involve one or more equality conditions "AND"ed together; for example:
 - R.Ai=S.Bj AND R.Ak=S.Bl AND R.Ap=S.Bq

Binary Relational Operations: EQUIJOIN

- EQUIJOIN Operation
- The most common use of join involves join conditions with equality comparisons only
- Such a join, where the only comparison operator used is =, is called an EQUIJOIN.
 - In the result of an EQUIJOIN we always have one or more pairs of attributes (whose names need not be identical) that have identical values in every tuple.
 - The JOIN seen in the previous example was an EQUIJOIN.

Binary Relational Operations: NATURAL JOIN Operation

NATURAL JOIN Operation

- Another variation of JOIN called NATURAL JOIN denoted by * — was created to get rid of the second (superfluous) attribute in an EQUIJOIN condition.
 - because one of each pair of attributes with identical values is superfluous
- The standard definition of natural join requires that the two join attributes, or each pair of corresponding join attributes, have the same name in both relations
- If this is not the case, a renaming operation is applied first.

Binary Relational Operations NATURAL JOIN (contd.)

- Example: To apply a natural join on the DNUMBER attributes of DEPARTMENT and DEPT_LOCATIONS, it is sufficient to write:
 - DEPT_LOCS ← DEPARTMENT * DEPT_LOCATIONS
- Only attribute with the same name is DNUMBER
- An implicit join condition is created based on this attribute:
 DEPARTMENT.DNUMBER=DEPT_LOCATIONS.DNUMBER
- Another example: Q ← R(A,B,C,D) * S(C,D,E)
 - The implicit join condition includes each pair of attributes with the same name, "AND"ed together:
 - R.C=S.C AND R.D.S.D
 - Result keeps only one attribute of each such pair:
 - Q(A,B,C,D,E)

Example of NATURAL JOIN operation

(a)

PROJ DEPT

Pname	<u>Pnumber</u>	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01

(b)

DEPT_LOCS

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston

Figure 6.7

Results of two NATURAL JOIN operations.

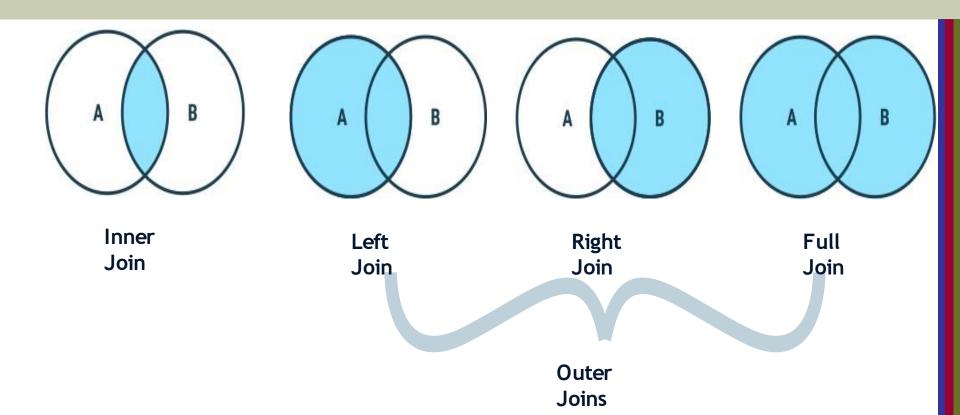
(a) PROJ_DEPT ← PROJECT * DEPT.

(b) DEPT_LOCS ← DEPARTMENT * DEPT_LOCATIONS.

Joins in SQL

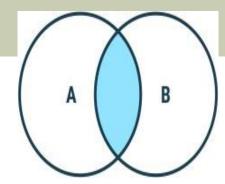
Join is used to combine rows from two or more tables, based on a related column between them.

Types of Joins



<u>Inner</u> Join

Returns records that have matching values in both tables



Syntax

SELECT

column(s)

FROM tableA

INNER JOIN

tableB

ON tableA.col_name = tableB.col_name;

<u>Inner</u> <u>Join</u>

Example

stude

student_id	name
101	adam
102	bob
103	casey

cours

e student_id	course
102	english
105	math
103	science
107	computer science

SELECT *
FROM student
INNER JOIN course

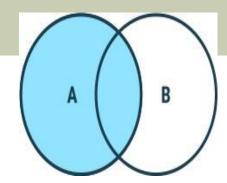
ON student.student_id =
course.student_id;

Resu

student_id	name	course
102	bob	english
103	casey	science

Left Join

Returns all records from the left table, and the matched records from the right table



Syntax

SELECT

column(s)

FROM

tableA LEFT

JOIN tableB

ON tableA.col_name =
tableB.col_name;



Example

stude

student_id	name
101	adam
102	bob
103	casey

cours

e student_id	course
102	english
105	math
103	science
107	computer science

FROM student as s LEFT JOIN course as c

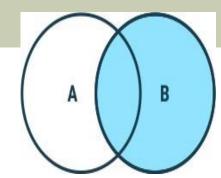
ON s.student_id =
c.student_id;

Resu

student_id	name	course
101	adam	null
102	bob	english
103	casey	science

Right Join

Returns all records from the right table, and the matched records from the left table



Syntax

SELECT

column(s)

FROM tableA

RIGHT JOIN

tableB

ON tableA.col_name =
tableB.col_name;

Right Join

Example

stude

student_id	name
101	adam
102	bob
103	casey

cours

e student_id	course
102	english
105	math
103	science
107	computer science

Resu

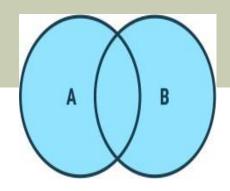
It student_id	course	name
102	english	bob
105	math	null
103	science	casey
107	computer science	null

SELECT *
FROM student as s
RIGHT JOIN course as c

ON s.student_id =
c.student_id;

Full Join

Returns all records when there is a match in either left or right table



Syntax in MySQL

SELECT * FROM student as a LEFT JOIN course as b ON a.id = b.id UNION SELECT * FROM student as a RIGHT JOIN course as b ON a.id = b.id;

LEFT JOIN
UNION
RIGHT
JOIN

Full Join

Exampl

e

student

student_id	name
101	adam
102	bob
103	casey

cours

e student_id	course
102	english
105	math
103	science
107	computer science

Resu

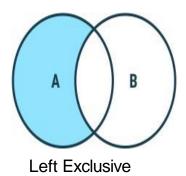
14			
student_id	name	course	
101	adam	null	
102	bob	english	
103	casey	science	
105	null	math	
107	null	computer science	

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Think & Ans



Qs: Write SQL commands to display the right exclusive join :



Join

 $\left(\begin{array}{c}
A \\
B
\end{array}\right)$

Right Exclusive Join

```
SELECT *
FROM student as a
LEFT JOIN course as b
ON a.id = b.id
WHERE b.id IS NULL;
```

Self Join

It is a regular join but the table is joined with itself.

Syntax

SELECT

column(s)

FROM table

as a JOIN

table as b

ON a.col_name =
b.col_name;

Self Join

Example

Employe

е

id	name	manager_id
101	adam	103
102	bob	104
103	casey	null
104	donald	103

Resu It

```
SELECT a.name as manager_name, b.name
FROM employee as a
JOIN employee as b
ON a.id = b.manager_id;
```

Complete Set of Relational Operations

- The set of operations including SELECT σ , PROJECT π , UNION \cup , DIFFERENCE -, RENAME ρ , and CARTESIAN PRODUCT X is called a *complete set* because any other relational algebra expression can be expressed by a combination of these five operations.
- For example:
 - $R \cap S = (R \cup S) ((R S) \cup (S R))$
 - R $\bowtie_{< join condition>} S = \sigma_{< join condition>} (R X S)$

Binary Relational Operations: DIVISION

DIVISION Operation

- The division operation is applied to two relations
- R(Z) ÷ S(X), where X subset Z. Let Y = Z X (and hence Z = X ∪ Y); that is, let Y be the set of attributes of R that are not attributes of S.
- The result of DIVISION is a relation T(Y) that includes a tuple t if tuples t_R appear in R with t_R [Y] = t, and with
 - $t_R[X] = t_s$ for every tuple t_s in S.

 For a tuple t to appear in the result T of the DIVISION, the values in t must appear in R in combination with every tuple in S.

Example of DIVISION

(a) SSN_PNOS

Essn	Pno
123456789	1
123456789	2
666884444	3
453453453	1
453453453	2
333445555	2
333445555	3
333445555	10
333445555	20
999887777	30
999887777	10
987987987	10
987987987	30
987654321	30
987654321	20
888665555	20

SMITH_PNOS

Pno
1
2

SSNS

Ssn
123456789
453453453

(b)

R

Α	В
a1	b1
a2	b1
аЗ	b1
a4	b1
a1	b2
аЗ	b2
a2	b3
аЗ	b3
a4	b3
a1	b4
a2	b4
аЗ	b4

S

Α
a1
a2
аЗ

Т



Figure 6.8

The DIVISION operation. (a) Dividing SSN_PNOS by SMITH_PNOS. (b) $T \leftarrow R \div S$.

Recap of Relational Algebra Operations

Table 6.1Operations of Relational Algebra

Operation	Purpose	Notation
SELECT	Selects all tuples that satisfy the selection condition from a relation R .	$\sigma_{\langle \text{selection condition} \rangle}(R)$
PROJECT	Produces a new relation with only some of the attributes of <i>R</i> , and removes duplicate tuples.	$\pi_{< attribute \ list>}(R)$
THETA JOIN	Produces all combinations of tuples from R_1 and R_2 that satisfy the join condition.	$R_1 \bowtie_{< \text{join condition}>} R_2$
EQUIJOIN	Produces all the combinations of tuples from R_1 and R_2 that satisfy a join condition with only equality comparisons.	$R_1 \bowtie_{<\text{join condition}>} R_2,$ OR $R_1 \bowtie_{(<\text{join attributes 1>}),}$ $(<\text{join attributes 2>})$
NATURAL JOIN	Same as EQUIJOIN except that the join attributes of R_2 are not included in the resulting relation; if the join attributes have the same names, they do not have to be specified at all.	$\begin{array}{c} R_1*_{< \text{join condition}>} R_2, \\ \text{OR } R_1*_{(< \text{join attributes 1>}),} \\ (< \text{join attributes 2>}) R_2 \\ \text{OR } R_1*R_2 \end{array}$
UNION	Produces a relation that includes all the tuples in R_1 or R_2 or both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cup R_2$
INTERSECTION	Produces a relation that includes all the tuples in both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cap R_2$
DIFFERENCE	Produces a relation that includes all the tuples in R_1 that are not in R_2 ; R_1 and R_2 must be union compatible.	$R_1 - R_2$
CARTESIAN PRODUCT	Produces a relation that has the attributes of R_1 and R_2 and includes as tuples all possible combinations of tuples from R_1 and R_2 .	$R_1 \times R_2$
DIVISION	Produces a relation $R(X)$ that includes all tuples $t[X]$ in $R_1(Z)$ that appear in R_1 in combination with every tuple from $R_2(Y)$, where $Z = X \cup Y$.	$R_1(Z) \div R_2(Y)$

Additional Relational Operations: Aggregate Functions and Grouping

- A type of request that cannot be expressed in the basic relational algebra is to specify mathematical aggregate functions on collections of values from the database.
- Examples of such functions include retrieving the average or total salary of all employees or the total number of employee tuples.
 - These functions are used in simple statistical queries that summarize information from the database tuples.
- Common functions applied to collections of numeric values include
 - SUM, AVERAGE, MAXIMUM, and MINIMUM.
- The COUNT function is used for counting tuples or values.

Aggregate Function Operation

- Use of the Aggregate Functional operation \mathcal{F}
 - $\mathcal{F}_{\text{MAX Salary}}$ (EMPLOYEE) retrieves the maximum salary value from the EMPLOYEE relation
 - $\mathcal{F}_{\text{MIN Salary}}$ (EMPLOYEE) retrieves the minimum Salary value from the EMPLOYEE relation
 - $\mathcal{F}_{SUM\ Salary}$ (EMPLOYEE) retrieves the sum of the Salary from the EMPLOYEE relation
 - $\mathcal{F}_{\text{COUNT SSN, AVERAGE Salary}}$ (EMPLOYEE) computes the count (number) of employees and their average salary
 - Note: count just counts the number of rows, without removing duplicates

Using Grouping with Aggregation

- The previous examples all summarized one or more attributes for a set of tuples
 - Maximum Salary or Count (number of) Ssn
- Grouping can be combined with Aggregate Functions
- Example: For each department, retrieve the DNO, COUNT SSN, and AVERAGE SALARY
- A variation of aggregate operation \mathcal{F} allows this:
 - Grouping attribute placed to left of symbol
 - Aggregate functions to right of symbol
 - DNO $\mathcal{F}_{\text{COUNT SSN, AVERAGE Salary}}$ (EMPLOYEE)
- Above operation groups employees by DNO (department number) and computes the count of employees and average salary per department

Examples of applying aggregate functions and grouping

Figure 6.10

The aggregate function operation.

(a) $\rho_{R(\text{Dno, No_of_employees, Average_sal})}$ (ρ_{Dno} count ssn, Average salary (EMPLOYEE)). (b) ρ_{Dno} count ssn, Average salary (EMPLOYEE). (c) $\rho_{\text{COUNT Ssn, AVERAGE Salary}}$ (EMPLOYEE).

٠		•
r	-	•
ı	7	

Dno	No_of_employees	Average_sal
5	4	33250
4	3	31000
1	1	55000

(b)

)	Dno	Count_ssn	Average_salary		
	5	4	33250		
	4	3	31000		
	1	1	55000		

(c)

Count_ssn	Average_salary		
8	35125		

Illustrating aggregate functions and grouping

Figure 8.6 Results of GROUP BY and HAVING. (a) Q24. (b) Q26.

(a)	Fname	Minit	Lname	<u>Ssn</u>		Salary	Super_ssn	Dno				Dno	Count (*)	Avg (Salary)
	John	В	Smith	123456789		30000	333445555	5		Г	-	5	4	33250
	Franklin	Т	Wong	333445555		40000	888665555	5			-	4	3	31000
	Ramesh	K	Narayan	666884444		38000	333445555	5	$ \ $		├ ►	1	1	55000
	Joyce	Α	English	453453453]	25000	333445555	5				Result	of Q24	
	Alicia	J	Zelaya	999887777		25000	987654321	4	\Box					
	Jennifer	S	Wallace	987654321		43000	888665555	4	1	_]			
	Ahmad	٧	Jabbar	987987987		25000	987654321	4						
	James	Е	Bong	888665555		55000	NULL	1		_				

Grouping EMPLOYEE tuples by the value of Dno

- Recursive Closure Operations
 - Another type of operation that, in general, cannot be specified in the basic original relational algebra is recursive closure.
 - This operation is applied to a recursive relationship.
 - An example of a recursive operation is to retrieve all SUPERVISEES of an EMPLOYEE e at all levels — that is, all EMPLOYEE e' directly supervised by e; all employees e' directly supervised by each employee e'; all employees e'' directly supervised by each employee e''; and so on.

- Although it is possible to retrieve employees at each level and then take their union, we cannot, in general, specify a query such as "retrieve the supervisees of 'James Borg' at all levels" without utilizing a looping mechanism.
 - The SQL3 standard includes syntax for recursive closure.

(Borg's SSN is 888665555)

(SSN) (SUPERSSN)

SSN1	SSN2		
123456789	333445555		
333445555	888665555		
999887777	987654321		
987654321	888665555		
666884444	333445555		
453453453	333445555		
987987987	987654321		
	123456789 333445555 999887777 987654321 666884444 453453453		

RESULT 1	SSN		
	333445555		
	987654321		

(Supervised by Borg)

SSN
123456789
999887777
666884444
453453453
987987987

(Supervised by Borg's subordinates)

SSN		
123456789		
999887777		
666884444		
453453453		
987987987		
333445555		
987654321		

(RESULT1 ∪ RESULT2)

- The OUTER JOIN Operation
 - In NATURAL JOIN and EQUIJOIN, tuples without a matching (or related) tuple are eliminated from the join result
 - Tuples with null in the join attributes are also eliminated
 - This amounts to loss of information.
 - A set of operations, called OUTER joins, can be used when we want to keep all the tuples in R, or all those in S, or all those in both relations in the result of the join, regardless of whether or not they have matching tuples in the other relation.

- The left outer join operation keeps every tuple in the first or left relation R in R →S; if no matching tuple is found in S, then the attributes of S in the join result are filled or "padded" with null values.
- A similar operation, right outer join, keeps every tuple in the second or right relation S in the result of R ⋉ S.
- A third operation, full outer join, denoted by keeps all tuples in both the left and the right relations when no matching tuples are found, padding them with null values as needed.

RESULT

Fname	Minit	Lname	Dname	
John	В	Smith	NULL	
Franklin	Т	Wong	Research	
Alicia	J	Zelaya	NULL	
Jennifer	S	Wallace	Administration	
Ramesh	K	Narayan	NULL	
Joyce	Α	English	NULL	
Ahmad	V	Jabbar	NULL	
James	E	Borg	Headquarters	

Figure 6.12

The result of a LEFT OUTER JOIN operation.

OUTER UNION Operations

- The outer union operation was developed to take the union of tuples from two relations if the relations are not type compatible.
- This operation will take the union of tuples in two relations R(X, Y) and S(X, Z) that are partially compatible, meaning that only some of their attributes, say X, are type compatible.
- The attributes that are type compatible are represented only once in the result, and those attributes that are not type compatible from either relation are also kept in the result relation T(X, Y, Z).

- Example: An outer union can be applied to two relations whose schemas are STUDENT(Name, SSN, Department, Advisor) and INSTRUCTOR(Name, SSN, Department, Rank).
 - Tuples from the two relations are matched based on having the same combination of values of the shared attributes— Name, SSN, Department.
 - If a student is also an instructor, both Advisor and Rank will have a value; otherwise, one of these two attributes will be null.
 - The result relation STUDENT_OR_INSTRUCTOR will have the following attributes:

STUDENT_OR_INSTRUCTOR (Name, SSN, Department, Advisor, Rank)

Examples of Queries in Relational Algebra

• Q1: Retrieve the name and address of all employees who work for the 'Research' department.

Q6: Retrieve the names of employees who have no dependents.

```
ALL_EMPS \leftarrow \pi ssn(EMPLOYEE)

EMPS_WITH_DEPS(SSN) \leftarrow \pi essn(DEPENDENT)

EMPS_WITHOUT_DEPS \leftarrow (ALL_EMPS - EMPS_WITH_DEPS)

RESULT \leftarrow \pi lname, fname (EMPS_WITHOUT_DEPS * EMPLOYEE)
```

Chapter Summary

- Relational Algebra
 - Unary Relational Operations
 - Relational Algebra Operations From Set Theory
 - Binary Relational Operations
 - Additional Relational Operations
 - Examples of Queries in Relational Algebra