

**Batch: D-2    Roll No.: 16010122323**

**Experiment / assignment / tutorial No. 2**

**Grade: AA / AB / BB / BC / CC / CD / DD**

**Signature of the Staff In-charge with date**

**TITLE:** To study and implement Booth's Multiplication Algorithm.

**AIM:** Booth's Algorithm for Multiplication

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**Expected OUTCOME of Experiment: (Mention CO/CO's attained here)**

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**Books/ Journals/ Websites referred:**

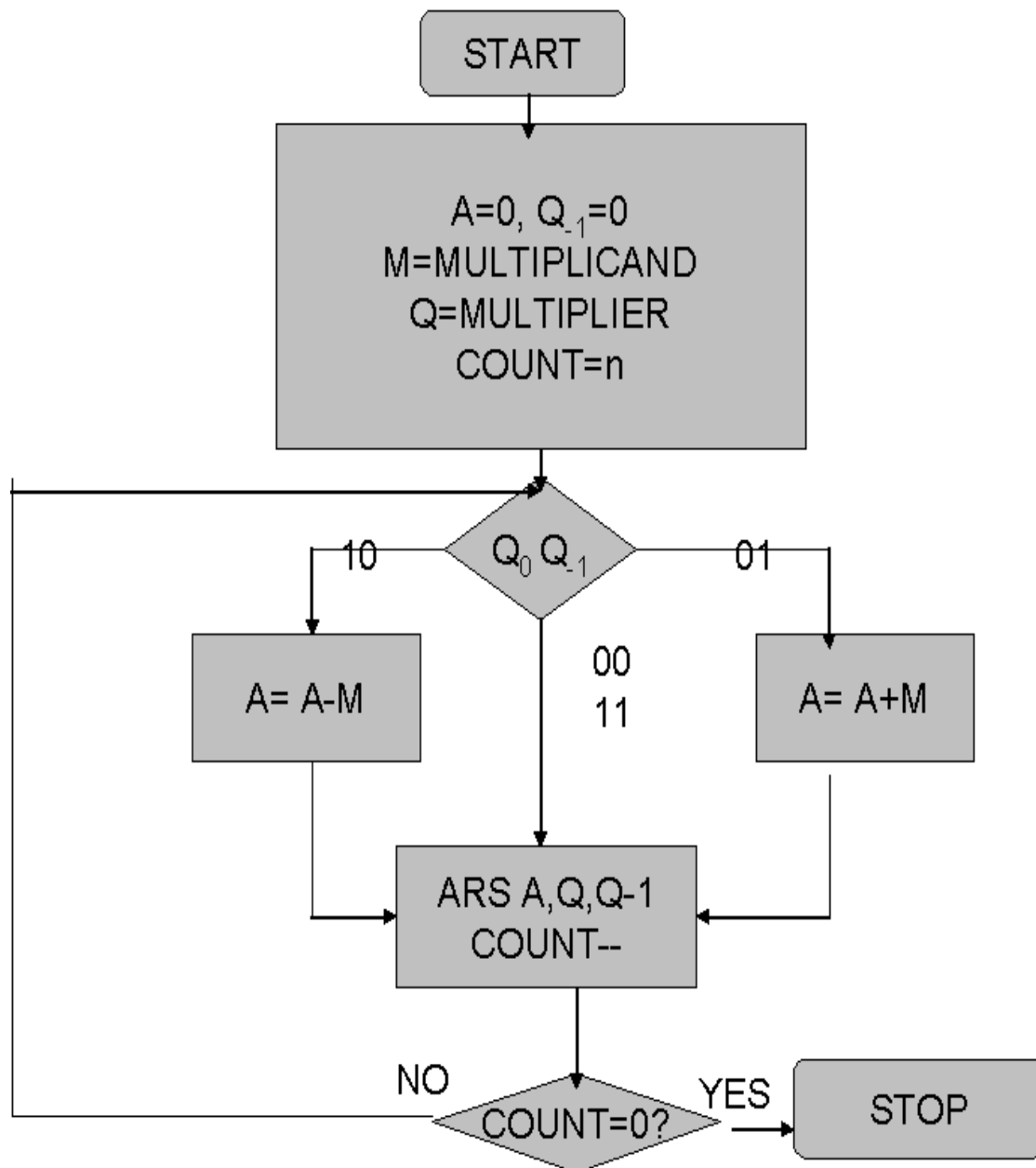
1. Carl Hamacher, Zvonko Vranesic and Safwat Zaky, "Computer Organization", Fifth Edition, TataMcGraw-Hill.
2. William Stallings, "Computer Organization and Architecture: Designing for Performance", Eighth Edition, Pearson.
3. Dr. M. Usha, T. S. Srikanth, "Computer System Architecture and Organization", First Edition, Wiley-India.

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**Pre Lab/ Prior Concepts:**

It is a powerful algorithm for signed number multiplication which generates a  $2n$  bit product and treats both positive and negative numbers uniformly. Also the efficiency of the algorithm is good due to the fact that, block of 1's and 0's are skipped over and subtraction/addition is only done if pair contains 10 or 01

**Flowchart:**



### Design Steps:

1. Start
2. Get the multiplicand (M) and Multiplier (Q) from the user
3. Initialize  $A = Q_{-1} = 0$
4. Convert M and Q into binar

5. Compare  $Q_0$  and  $Q_{-1}$  and perform the respective operation.

$Q_0 Q_{-1}$	Operation
00/11	Arithmetic right shift
01	A+M and Arithmetic right shift
10	A-M and Arithmetic right shift

6. Repeat steps 5 till all bits are compared

7. Convert the result to decimal form and display

8. End

CODE :

```
#include <stdio.h>
#include <math.h>

int a = 0, b = 0, c = 0, a1 = 0, b1 = 0, com[5] = { 1, 0, 0, 0, 0};
int anum[5] = {0}, anumcp[5] = {0}, bnum[5] = {0};
int acomp[5] = {0}, bcomp[5] = {0}, pro[5] = {0}, res[5] = {0};

void binary(){
    a1 = fabs(a);
    b1 = fabs(b);
    int r, r2, i, temp;
    for (i = 0; i < 5; i++){
        r = a1 % 2;
        a1 = a1 / 2;
        r2 = b1 % 2;
        b1 = b1 / 2;
        anum[i] = r;
        anumcp[i] = r;
        bnum[i] = r2;
        if(r2 == 0){
            bcomp[i] = 1;
        }
        if(r == 0){
            acomp[i] = 1;
        }
    }
}

//part for two's complementing
c = 0;
```

```

for ( i = 0; i < 5; i++){
    res[i] = com[i] + bcomp[i] + c;
    if(res[i] >= 2){
        c = 1;
    }
    else
        c = 0;
    res[i] = res[i] % 2;
}
for (i = 4; i >= 0; i--){
    bcomp[i] = res[i];
}
//in case of negative inputs
if (a < 0){
    c = 0;
    for (i = 4; i >= 0; i--){
        res[i] = 0;
    }
    for ( i = 0; i < 5; i++){
        res[i] = com[i] + acomp[i] + c;
        if (res[i] >= 2){
            c = 1;
        }
        else
            c = 0;
        res[i] = res[i]%2;
    }
    for (i = 4; i >= 0; i--){
        anum[i] = res[i];
        anumcp[i] = res[i];
    }
}
if(b < 0){
    for (i = 0; i < 5; i++){
        temp = bnum[i];
        bnum[i] = bcomp[i];
        bcomp[i] = temp;
    }
}
}

void add(int num[]){
    int i;
    c = 0;
    for ( i = 0; i < 5; i++){
        res[i] = pro[i] + num[i] + c;
        if (res[i] >= 2){
            c = 1;
        }
        else{

```

```

        c = 0;
    }
    res[i] = res[i]%2;
}
for (i = 4; i >= 0; i--){
    pro[i] = res[i];
    printf("%d",pro[i]);
}
printf(".");
for (i = 4; i >= 0; i--){
    printf("%d", anumcp[i]);
}
}

void arshift(){//for arithmetic shift right
    int temp = pro[4], temp2 = pro[0], i;
    for (i = 1; i < 5 ; i++){//shift the MSB of product
        pro[i-1] = pro[i];
    }
    pro[4] = temp;
    for (i = 1; i < 5 ; i++){//shift the LSB of product
        anumcp[i-1] = anumcp[i];
    }
    anumcp[4] = temp2;
    printf("\nAR-SHIFT: ");//display together
    for (i = 4; i >= 0; i--){
        printf("%d",pro[i]);
    }
    printf(".");
    for(i = 4; i >= 0; i--){
        printf("%d", anumcp[i]);
    }
}
}

```

```

void main(){
    int i, q = 0;
    printf("\t\tBOOTH'S MULTIPLICATION ALGORITHM");
    printf("\n\nEnter two numbers to multiply: ");
    printf("\nBoth must be less than 16");
    //simulating for two numbers each below 16
    do{
        printf("\nEnter A: ");
        scanf("%d",&a);
        printf("Enter B: ");
        scanf("%d", &b);
    }while(a >=16 || b >=16);

    printf("\nExpected product = %d", a * b);
    binary();
    printf("\n\nBinary Equivalentents are: ");
    printf("\nA = ");
}

```

```

for (i = 4; i >= 0; i--){
    printf("%d", anum[i]);
}
printf("\nB = ");
for (i = 4; i >= 0; i--){
    printf("%d", bnum[i]);
}
printf("\nB' + 1 = ");
for (i = 4; i >= 0; i--){
    printf("%d", bcomp[i]);
}
printf("\n\n");
for (i = 0; i < 5; i++){
    if (anum[i] == q){//just shift for 00 or 11
        printf("\n-->");
        arshift();
        q = anum[i];
    }
    else if (anum[i] == 1 && q == 0){//subtract and shift for 10
        printf("\n-->");
        printf("\nSUB B: ");
        add(bcomp);//add two's complement to implement subtraction
        arshift();
        q = anum[i];
    }
    else{//add ans shift for 01
        printf("\n-->");
        printf("\nADD B: ");
        add(bnum);
        arshift();
        q = anum[i];
    }
}

printf("\nProduct is = ");
for (i = 4; i >= 0; i--){
    printf("%d", pro[i]);
}
for (i = 4; i >= 0; i--){
    printf("%d", anumcp[i]);
}
}

```

## OUTPUT :

```
input
BOOTH'S MULTIPLICATION ALGORITHM
Enter two numbers to multiply:
Both must be less than 16
Enter A: 5
Enter B: 6

Expected product = 30

Binary Equivalents are:
A = 00101
B = 00110
B'+ 1 = 11010

-->
SUB B: 11010:00101
AR-SHIFT: 11101:00010
-->
ADD B: 00011:00010
AR-SHIFT: 00001:10001
-->
SUB B: 11011:10001
AR-SHIFT: 11101:11000
-->
ADD B: 00011:11000
AR-SHIFT: 00001:11100
-->
AR-SHIFT: 00000:11110
Product is = 0000011110

...Program finished with exit code 0
Press ENTER to exit console.
```

Example:  $7 \times 3 = 21$  [1010]

$N = 7 = 000111$   
 $Q = 3 = 0011$

A      Q      Q<sub>-1</sub>

1) 0000 0011 0

Operator's  
 $A - M \Rightarrow A + 2^i \text{comp}$   
 $\begin{array}{r} 0000 \\ 1001 \\ \hline 1001 \end{array} \Rightarrow A$

2)  $\begin{array}{r} 1001 \\ 1100 \\ \hline 1110 \end{array} \quad \begin{array}{r} 0011 \\ 1001 \\ \hline 0100 \end{array} \quad \begin{array}{r} 0 \\ 1 \\ 1 \end{array}$

shift operators

3)  $\begin{array}{r} 1110 \\ 0010 \\ \hline 0010 \end{array} \quad \begin{array}{r} 0100 \\ 0100 \\ \hline 0100 \end{array} \quad \begin{array}{r} 1 \\ 1 \\ 0 \end{array}$

$A + M \Rightarrow 1110$   
 $\begin{array}{r} 0111 \\ 10101 \end{array}$

4)  $\begin{array}{r} 0010 \\ 1010 \\ \hline 0001 \end{array} \quad \begin{array}{r} 1010 \\ 0101 \\ \hline 0101 \end{array} \quad \begin{array}{r} 0 \\ 0 \\ 0 \end{array}$

shift operator

$00010011$   
 $= 21$

The aim of the experiment is verified.

1. **Explain advantages and disadvantages of Booth's algorithm.**

- It handles both positive and negative numbers uniformly.
  - It achieves efficiency in the number of additions required when the multiplier has a few large blocks of 1's.
2. **Is Booth's recoding better than Booth's algorithm? Justify**
- Booth recoding there are reduced number of partial products as there are reduced number of addition and subtraction as compared to Booth's algorithm. In this case Booth recoding is better but as far as implementation is concerned the algorithm is followed.



