Special Neural Network

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Syllabus

Special Neural Networks 08 CO3

- 4.1 Cognitron, Neocognitron, Boltzman Machine, Gaussian Machine, Simulated Annealing, SVM
- #Self-Learning: Benefits of Multi-layer Neural Network

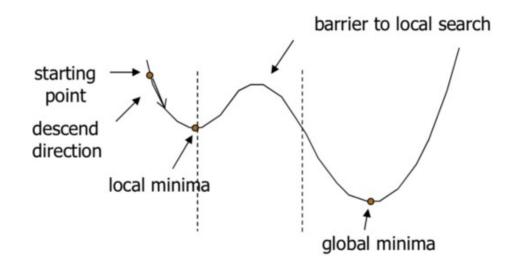
Simulated Annealing

- The Simulated Annealing algorithm is based upon Physical Annealing in real life. Physical Annealing is the process of heating up a material until it reaches an **annealing temperature** and then it will be **cooled down** slowly in order to change the material to a desired structure.
- When the material is hot, the molecular structure is weaker and is more susceptible to change.
- When the material cools down, the molecular structure is harder and is less susceptible to change.
- Another important part of this analogy is the following equation from Thermal Dynamics:

$$P(\Delta E) = e^{-\frac{\Delta E}{k*t}}$$

Simulated Annealing (cont.)

- Simulated Annealing (SA) mimics the Physical Annealing process but is used for optimizing parameters in a model.
- This process is very useful for situations where there are a lot of local minima such that algorithms like Gradient Descent would be stuck at.



Simulated Annealing (cont.)

Example – Stone and Hill (Textbook-Shivnandan)

Convergence of simulated annealing

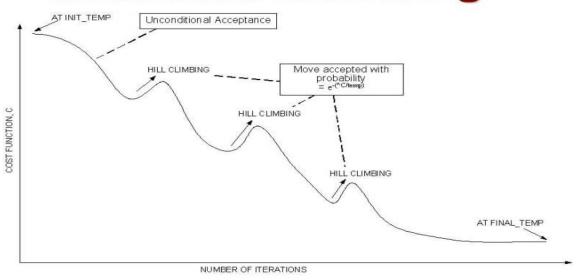


Fig- Reference - https://dev.to/swyx/unsupervised-learning-randomized-optimization-d2j

Boltzmann Machine

- When simulated annealing is applied to the Discrete Hopfield network then it becomes Boltzmann machine.
- It consists of as set of units Xi and Xj and set of bidirectional connections between pairs of units. Also, contains wij not equal to o.
- This machine can be used as an associative memory then, wij = wji. Self-connection on weights also exist.
- For unit Xi, state xi may be o or 1.

Boltzmann Machine

The maximum of the CF can be obtained by letting each unit attempt to change its state (alter between "1" and "0" or "0" and "1"). The change of state can be done either in parallel or sequential manner. However, in this case all the description is based on sequential manner. The consensus change when unit X_i changes its state is given by

$$\Delta CF(i) = (1 - 2x_i) \left(w_{ij} + \sum_{j \neq i} w_{ij} x_i \right)$$

where x_i is the current state of unit X_i . The variation in coefficient $(1-2x_i)$ is given by

$$(1 - 2x_i) = \begin{cases} +1, & X_i \text{ is currently off} \\ -1, & X_i \text{ is currently on} \end{cases}$$

Boltzmann Machine

If unit X_i were to change its activations then the resulting change in the CF can be obtained from the information that is local to unit X_i . Generally, X_i does not change its state, but if the states are changed, then this increases the consensus of the net. The probability of the network that accepts a change in the state for unit X_i is given by

$$AF(i, T) = \frac{1}{1 + \exp[-\Delta CF(i)/T]}$$

where T (temperature) is the controlling parameter and it will gradually decrease as the CF reaches the maximum value. Low values of T are acceptable because they increase the net consensus since the net accepts a change in state. To help the net not to stick with the local maximum, probabilistic functions are used widely.

Boltzmann Machine Architecture

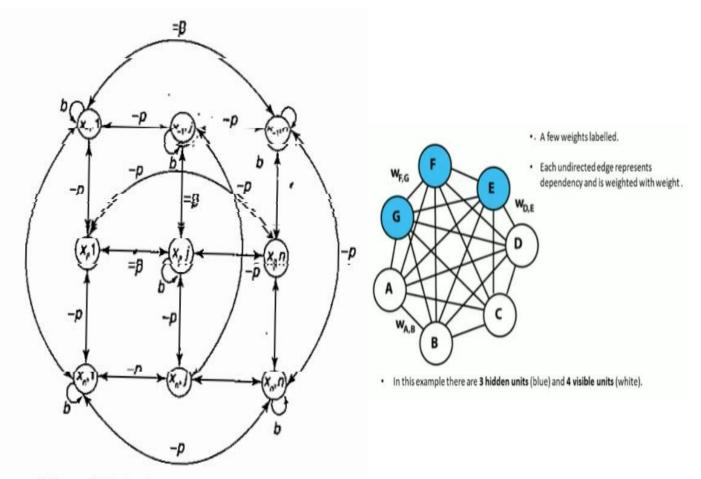


Figure 6-3 Architecture of Boltzmann machine.

Boltzmann Machine Algorithm

It is assumed here that the units are arranged in a two-dimensional array. There are n^2 units. So, the weights between unit $X_{i,j}$ and unit $X_{i,j}$ are denoted by w(i,j;l,j).

$$w(i, j : I, J) = \begin{cases} -p & \text{if } i = J \text{ or } j = J \text{ (but not both)} \\ b & \text{otherwise} \end{cases}$$

The testing algorithm is as follows.

- Step 0: Initialize the weights representing the constraints of the problem. Also initialize control parameter T and activate the units.
- Step 1: When stopping condition is false, perform Steps 2-8.
- Step 2: Perform Steps 3-6 n2 times. (This forms an epoch.)
- Step 3: Integers I and J are chosen random values between 1 and n. (Unit U_{I,J} is the current victim to change its state.)
- Step 4: Calculate the change in consensus:

$$\Delta CF = (1 - 2X_{I,f}) \left[w(I, f : I, f) + \sum_{i,j \neq I,f} \sum_{I,f} w(i,j : I,f) X_{I,f} \right]$$

Boltzmann Machine Algorithm

Step 5: Calculate the probability of acceptance of the change in state:

$$AF(T) = 1/1 + \exp[-(\Delta CF/T)]$$

Step 6: Decide whether to accept the change or not. Let R be a random number between 0 and 1. If R < AF, accept the change:

 $X_{I,f} = 1 - X_{I,f}$ (This changes the state $U_{I,f}$.) If $R \ge AF$, reject the change.

Step 7: Reduce the control parameter T.

$$T(\text{new}) = 0.95 T(\text{old})$$

Step 8: Test for stopping condition, which is:

If the temperature reaches a specified value or if there is no change of state for specified number of epochs then stop, else continue.

The initial temperature should be taken large enough for accepting the change of state quickly. Also remember that the Boltzmann machine can be applied for various optimization problems such as traveling salesman problem.

Gaussian Machine

- Gaussian machine is one which includes Boltzmann machine, Hopfield net and other neural networks.
- Gaussian machine is based on the following three parameters: (a) a slope parameter of sigmoidal function (alpha) (b) a rime step Delta *t*, (c) Temperature *T*.
- The steps involved in the operation of the Gaussian net are the following:

Gaussian Machine

Step 1: Compute the net input to unit X;:

$$net_i = \sum_{j=1}^{N} w_{ij}v_j + \theta_i + \in$$

where θ_i is the threshold and ϵ the random noise which depends on temperature T.

Step 2: Change the activity level of unit X_j :

$$\frac{\Delta x_i}{\Delta t} = -\frac{x_i}{t} + \text{net}_i$$

Step 3: Apply the activation function:

$$v_i = f(x_i) = 0.5(1 + \tanh(x_i))$$

where the binary step function corresponds to $\alpha = \infty$ (infinity).

The Gaussian machine with T=0 corresponds the Hopfield net. The Boltzmann machine can be obtained by setting $\Delta t = r = 1$ to get

$$\Delta x_i = -x_i + \text{net}_i$$

or
$$x_i(\text{new}) = \text{net}_i = \sum_{j=1}^N \hat{w}_{ij}v_j + \theta_i + \epsilon$$

The approximate Boltzmann acceptance function is obtained by integrating the Gaussian noise distribution

$$\int_{0}^{\infty} \frac{1}{\sqrt{2\pi \sigma^2}} \exp \frac{(x - x_i^2)}{2\sigma^2} dx \approx AF(t, T) = \frac{1}{1 + \exp(-x_i/T)}$$

where $x_i = \Delta CF(t)$. The noise which is found to obey a logistic rather than a Gaussian distribution produces a Gaussian machine that is identical to Boltzmann machine having Metropolis acceptance function, i.e., the output set to 1 with probability,

$$AF(i, T) = \frac{1}{1 + \exp(-x_i/T)}$$

This does not bother about the unit's original state. When noise is added to the net input of a unit then using probabilistic state transition gives a method for extending the Gaussian machine into Cauchy machine.

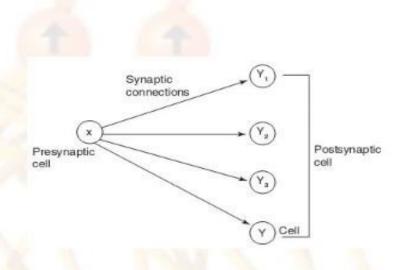
Cognitron Neural Network

Cognitron network was proposed by Fukushima in 1975.

The synaptic strength from cell X to cell Y is reinforced if and only if the following two conditions are true:

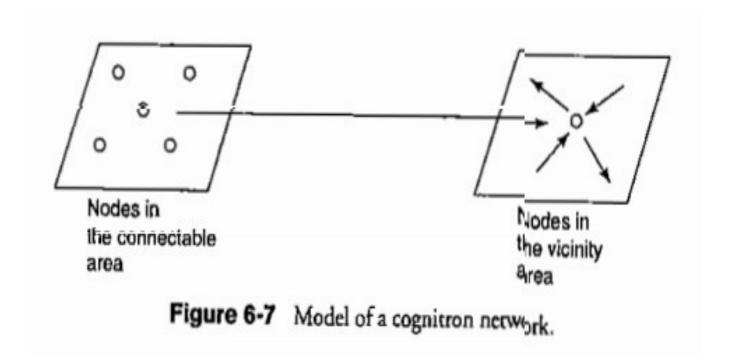
- Cell X: presynaptic cell fires.
- None of the postsynaptic cells present near cell Y fire stronger than Y.

The connection between presynaptic and postsynaptic cells is as follows:



Model of Cognitron Neural Network

• Application - Cognitron network can be used in neurophysiolog and psychology, visual and suditory information processing system.

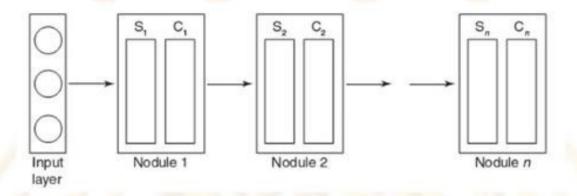


Neocognitron Neural Network

- Neocognitron is a multilayer feedforward network model for visual pattern recognition.
- It is an extension of cognitron network.
- Neocognitron net can be used for recognizing handwritten characters.
- The algorithm used in cognitron and neocognitron is same, except that neocognitron model can recognize patterns that are positionshifted or shape-distorted.
- The cells used in neocognitron are of two types:
 - S-cell: Cells that are trained suitably to respond to only certain features in the previous layer.
 - C-cell: A C-cell displaces the result of an S-cell in space, i.e., sort of "spreads" the features recognized by the S-cell.

Neocognitron Neural Network

The model of neocognitron network is as given below:



Training is found to progress layer by layer. The weights from the input units to the first layer are first trained and then frozen. Then the next trainable weights are adjusted and so on. When the net is designed, the weights between some layers are fixed as they are connection patterns.

Neocognitron Neural Network

