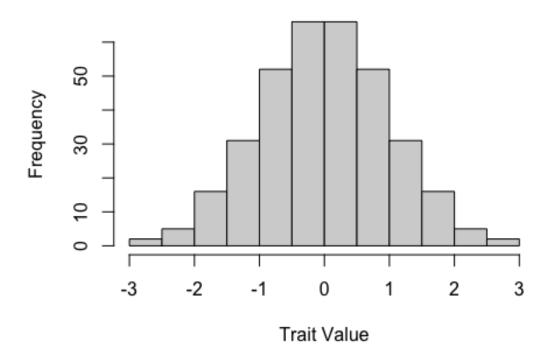
BTRY4830-Project

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```
libs = c('tidyverse', 'data.table', 'MASS',
         'ggsci', 'ggthemes', 'ggpubr', 'KEGGREST',
         'rentrez', 'tidyimpute', 'ggplot', 'ggfortify')
suppressMessages(
  suppressWarnings(sapply(libs, require, character.only = TRUE))
## tidyverse data.table
                                MASS
                                          ggsci
                                                  ggthemes
                                                                ggpubr
KEGGREST
         TRUE
                                TRUE
                                                       TRUE
##
                    TRUE
                                          FALSE
                                                                 FALSE
FALSE
##
      rentrez tidyimpute
                              ggplot ggfortify
##
        FALSE
                   FALSE
                               FALSE
                                           TRUE
rm(libs)
theme_set(theme_few(14))
1.
pheno_import <- read.csv("projectphenotypes.csv")</pre>
pheno1 <- pheno_import$ENSG00000164308.12</pre>
hist(pheno1, main = "Histogram of Phenotype 1 - ERAP2", xlab = "Trait Value",
ylab = "Frequency")
```

Histogram of Phenotype 1 - ERAP2

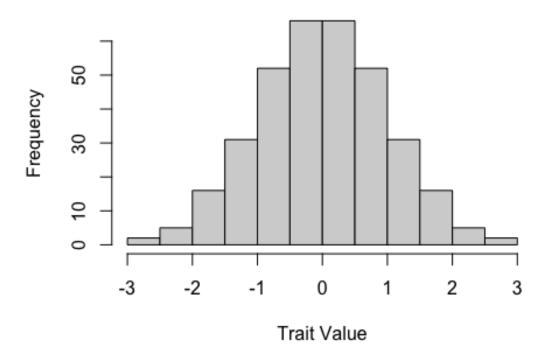


```
pheno_import <- read.csv("projectphenotypes.csv")

pheno2 <- pheno_import$ENSG00000124587.9

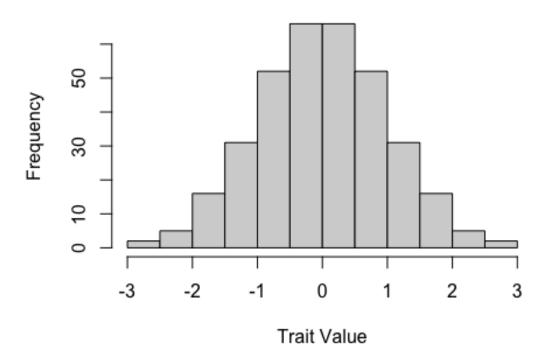
hist(pheno2, main = "Histogram of Phenotype 2 - PEX6", xlab = "Trait Value",
ylab = "Frequency")</pre>
```

Histogram of Phenotype 2 - PEX6



```
pheno_import <- read.csv("projectphenotypes.csv")
pheno3 <- pheno_import$ENSG00000180185.7
hist(pheno3, main = "Histogram of Phenotype 3 - FAHD1", xlab = "Trait Value", ylab = "Frequency")</pre>
```

Histogram of Phenotype 3 - FAHD1

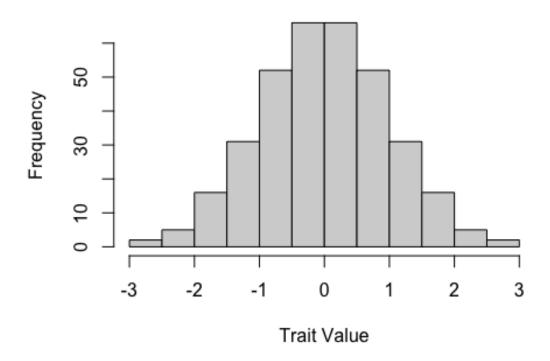


```
pheno_import <- read.csv("projectphenotypes.csv")

pheno4 <- pheno_import$ENSG00000168827.9

hist(pheno4, main = "Histogram of Phenotype 4 - GFM1", xlab = "Trait Value",
ylab = "Frequency")</pre>
```

Histogram of Phenotype 4 - GFM1

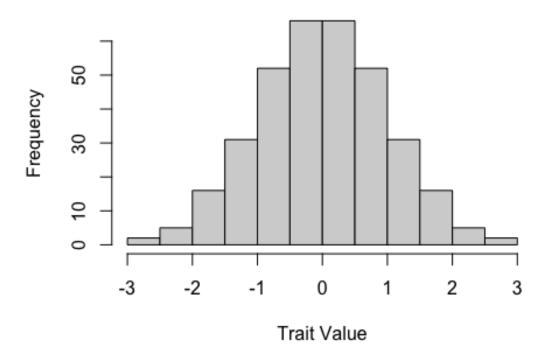


```
pheno_import <- read.csv("projectphenotypes.csv")

pheno5 <- pheno_import$ENSG00000136536.9

hist(pheno5, main = "Histogram of Phenotype 5 - MARCHF7", xlab = "Trait Value", ylab = "Frequency")</pre>
```

Histogram of Phenotype 5 - MARCHF7



```
geno_import <- read.csv("projectgenotypes.csv")

N <- ncol(geno_import) - 1

cat("Number of SNPs (N):", N, "\n")

## Number of SNPs (N): 50000

gen_import <- read.csv("projectgenotypes.csv")
gen_import<- gen_import[,-1]
colnames(gen_import) <- NULL
rownames(gen_import) <- NULL</pre>
```

GWAS Manhattan GWAS QQ plot - E Covariate NOT Include Covariate NOT Includ -log10 Observed p-val 75 75 --log₁₀ p 50 50 -25 -0 0 1000220003000040000500000 ż ż -log10 Expected p-val Index

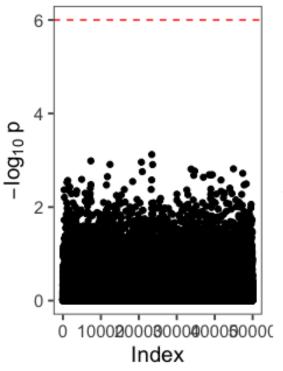
GWAS Manhattan GWAS QQ plot - P Covariate NOT Include Covariate NOT Includ 75 --log10 Observed p-val 75 --log₁₀ p 50 50 25 · 0 ż ż 0 1000200003000040000500000 -log10 Expected p-val Index

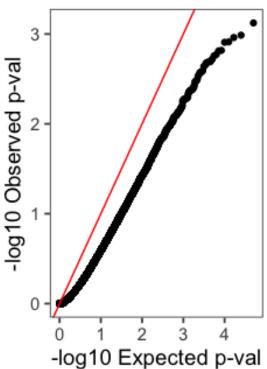
GWAS Manhattan GWAS QQ plot - F Covariate NOT Include Covariate NOT Includ 50 50 --log10 Observed p-val 40 40 d 30 -30 20 10 10 0 ż 2 -log10 Expected p-val Index

GWAS Manhattan

GWAS QQ plot - M. Covariate NOT Include:







```
# Convert genotypes to Xa & Xd
# # Details can be found in Lab 6
gen_import <- read.csv("projectgenotypes.csv")</pre>
gen_import<- gen_import[,-1]</pre>
colnames(gen_import) <- NULL</pre>
rownames(gen_import) <- NULL</pre>
xa_mat <- as.matrix(gen_import )</pre>
xd_mat <- ((2*xa_mat) - 1)
# Load in phenotype data and run GWAS
sim_pheno_mx <- read.csv("projectphenotypes.csv",</pre>
                           header = TRUE, row.names = 1)
# Read-in our covariate data
xc_mat = read.csv('projectcovars.csv')
Xc <- model.matrix(~Population + Sex, data=xc_mat)</pre>
xc mat1 <- Xc[,-1]</pre>
xc.pca<- prcomp(xa_mat %*% t(xa_mat))</pre>
```

```
xc.pca$sdev
     [1] 6.427237e+03 3.116876e+03 1.626246e+03 1.393769e+03 1.348115e+03
##
     [6] 1.262807e+03 1.209274e+03 1.203364e+03 1.196482e+03 1.189354e+03
##
    [11] 1.183723e+03 1.176994e+03 1.169424e+03 1.163703e+03 1.159626e+03
##
    [16] 1.154370e+03 1.152850e+03 1.148883e+03 1.141628e+03 1.138455e+03
##
##
    [21] 1.135365e+03 1.131426e+03 1.129800e+03 1.124041e+03 1.121787e+03
##
    [26] 1.119182e+03 1.117536e+03 1.113179e+03 1.111885e+03 1.109252e+03
    [31] 1.104816e+03 1.103658e+03 1.101757e+03 1.100419e+03 1.098486e+03
##
##
    [36] 1.096698e+03 1.095543e+03 1.095326e+03 1.089676e+03 1.088675e+03
    [41] 1.087383e+03 1.086510e+03 1.082802e+03 1.081972e+03 1.079094e+03
##
    [46] 1.077650e+03 1.076481e+03 1.073658e+03 1.073091e+03 1.070557e+03
    [51] 1.067799e+03 1.067384e+03 1.064559e+03 1.063028e+03 1.061835e+03
##
    [56] 1.059029e+03 1.057953e+03 1.055338e+03 1.054601e+03 1.052785e+03
##
    [61] 1.052125e+03 1.050047e+03 1.049038e+03 1.048526e+03 1.046296e+03
    [66] 1.043911e+03 1.042524e+03 1.041937e+03 1.038166e+03 1.036866e+03
##
    [71] 1.035134e+03 1.033292e+03 1.031230e+03 1.030714e+03 1.029552e+03
    [76] 1.027296e+03 1.026493e+03 1.026187e+03 1.023989e+03 1.022830e+03
##
    [81] 1.020409e+03 1.018483e+03 1.018153e+03 1.017024e+03 1.015774e+03
    [86] 1.015339e+03 1.013081e+03 1.011066e+03 1.010345e+03 1.009144e+03
    [91] 1.007144e+03 1.004131e+03 1.003394e+03 1.002108e+03 1.001168e+03
    [96] 1.000130e+03 9.990847e+02 9.977815e+02 9.966950e+02 9.953574e+02
## [101] 9.934285e+02 9.928147e+02 9.921263e+02 9.889116e+02 9.878715e+02
## [106] 9.870330e+02 9.858830e+02 9.844095e+02 9.828766e+02 9.817144e+02
## [111] 9.815441e+02 9.801736e+02 9.794226e+02 9.773364e+02 9.762718e+02
## [116] 9.747273e+02 9.743429e+02 9.733624e+02 9.721300e+02 9.694334e+02
## [121] 9.690543e+02 9.665108e+02 9.659888e+02 9.651578e+02 9.646666e+02
## [126] 9.628692e+02 9.617965e+02 9.606342e+02 9.589537e+02 9.579263e+02
## [131] 9.576399e+02 9.565771e+02 9.551647e+02 9.534546e+02 9.527577e+02
## [136] 9.513468e+02 9.510565e+02 9.497074e+02 9.475445e+02 9.472500e+02
## [141] 9.452895e+02 9.447093e+02 9.439998e+02 9.431473e+02 9.419851e+02
## [146] 9.413799e+02 9.396646e+02 9.373141e+02 9.370022e+02 9.351853e+02
## [151] 9.336451e+02 9.327803e+02 9.318289e+02 9.309163e+02 9.301936e+02
## [156] 9.289218e+02 9.275203e+02 9.272192e+02 9.248979e+02 9.237018e+02
## [161] 9.223170e+02 9.212970e+02 9.207484e+02 9.190583e+02 9.175964e+02
## [166] 9.168758e+02 9.155734e+02 9.144915e+02 9.139177e+02 9.115838e+02
## [171] 9.100090e+02 9.089549e+02 9.082701e+02 9.075609e+02 9.070621e+02
## [176] 9.061834e+02 9.037305e+02 9.031297e+02 9.026705e+02 9.015705e+02
## [181] 9.006897e+02 8.995660e+02 8.988972e+02 8.969267e+02 8.967292e+02
## [186] 8.947837e+02 8.945184e+02 8.930036e+02 8.923525e+02 8.912859e+02
## [191] 8.905865e+02 8.886448e+02 8.882295e+02 8.867257e+02 8.855461e+02
## [196] 8.846877e+02 8.830573e+02 8.825466e+02 8.818479e+02 8.814751e+02
## [201] 8.794259e+02 8.777186e+02 8.767972e+02 8.758468e+02 8.757262e+02
## [206] 8.744545e+02 8.736686e+02 8.721873e+02 8.717075e+02 8.697694e+02
## [211] 8.692546e+02 8.677861e+02 8.661287e+02 8.652436e+02 8.642717e+02
## [216] 8.633542e+02 8.617654e+02 8.611184e+02 8.597113e+02 8.594240e+02
## [221] 8.587240e+02 8.581504e+02 8.569184e+02 8.564457e+02 8.553471e+02
## [226] 8.539759e+02 8.532587e+02 8.521061e+02 8.513172e+02 8.493478e+02
## [231] 8.485337e+02 8.477899e+02 8.466858e+02 8.455183e+02 8.446625e+02
```

```
## [236] 8.424588e+02 8.415318e+02 8.411388e+02 8.405069e+02 8.389686e+02
## [241] 8.382553e+02 8.380126e+02 8.361499e+02 8.351868e+02 8.348635e+02
## [246] 8.329343e+02 8.322722e+02 8.314363e+02 8.306184e+02 8.290522e+02
## [251] 8.274878e+02 8.267802e+02 8.260722e+02 8.250299e+02 8.235588e+02
## [256] 8.224138e+02 8.219797e+02 8.203458e+02 8.194079e+02 8.182833e+02
## [261] 8.171338e+02 8.157413e+02 8.156224e+02 8.139621e+02 8.137759e+02
## [266] 8.123691e+02 8.112856e+02 8.101449e+02 8.091977e+02 8.087009e+02
## [271] 8.077159e+02 8.062131e+02 8.055174e+02 8.031145e+02 8.023779e+02
## [276] 8.010343e+02 8.007215e+02 7.984976e+02 7.981396e+02 7.966775e+02
## [281] 7.958301e+02 7.954928e+02 7.941076e+02 7.935662e+02 7.911468e+02
## [286] 7.908311e+02 7.903589e+02 7.891410e+02 7.869310e+02 7.858087e+02
## [291] 7.855454e+02 7.849577e+02 7.820512e+02 7.811003e+02 7.802921e+02
## [296] 7.796162e+02 7.790589e+02 7.770834e+02 7.754008e+02 7.753526e+02
## [301] 7.728763e+02 7.726947e+02 7.705890e+02 7.701995e+02 7.693325e+02
## [306] 7.686392e+02 7.667707e+02 7.665011e+02 7.648718e+02 7.640755e+02
## [311] 7.615802e+02 7.614540e+02 7.589987e+02 7.568496e+02 7.560320e+02
## [316] 7.550266e+02 7.538642e+02 7.529631e+02 7.526921e+02 7.492002e+02
## [321] 7.486189e+02 7.473058e+02 7.456907e+02 7.421292e+02 7.408742e+02
## [326] 7.401063e+02 7.387272e+02 7.382018e+02 7.359075e+02 7.341505e+02
## [331] 7.326539e+02 7.291693e+02 7.283385e+02 7.257851e+02 7.224219e+02
## [336] 7.202882e+02 7.180573e+02 7.160515e+02 7.140979e+02 7.082242e+02
## [341] 7.067593e+02 6.938449e+02 5.987201e+02 2.584256e-12
(xc.pca$sdev / sum(xc.pca$sdev))*100
     [1] 1.982205e+00 9.612662e-01 5.015456e-01 4.298480e-01 4.157681e-01
##
##
     [6] 3.894586e-01 3.729485e-01 3.711259e-01 3.690034e-01 3.668051e-01
    [11] 3.650685e-01 3.629930e-01 3.606586e-01 3.588940e-01 3.576369e-01
##
##
    [16] 3.560158e-01 3.555470e-01 3.543236e-01 3.520862e-01 3.511074e-01
    [21] 3.501545e-01 3.489397e-01 3.484383e-01 3.466620e-01 3.459669e-01
##
    [26] 3.451635e-01 3.446559e-01 3.433122e-01 3.429130e-01 3.421011e-01
##
    [31] 3.407328e-01 3.403757e-01 3.397894e-01 3.393770e-01 3.387808e-01
    [36] 3.382295e-01 3.378732e-01 3.378061e-01 3.360637e-01 3.357549e-01
##
    [41] 3.353566e-01 3.350872e-01 3.339438e-01 3.336879e-01 3.328002e-01
    [46] 3.323548e-01 3.319942e-01 3.311237e-01 3.309487e-01 3.301672e-01
##
    [51] 3.293167e-01 3.291886e-01 3.283173e-01 3.278452e-01 3.274773e-01
##
    [56] 3.266120e-01 3.262802e-01 3.254735e-01 3.252462e-01 3.246862e-01
    [61] 3.244827e-01 3.238418e-01 3.235307e-01 3.233727e-01 3.226850e-01
##
    [66] 3.219494e-01 3.215217e-01 3.213407e-01 3.201777e-01 3.197768e-01
    [71] 3.192426e-01 3.186745e-01 3.180386e-01 3.178795e-01 3.175211e-01
##
    [76] 3.168254e-01 3.165776e-01 3.164833e-01 3.158052e-01 3.154480e-01
    [81] 3.147013e-01 3.141074e-01 3.140056e-01 3.136574e-01 3.132717e-01
    [86] 3.131377e-01 3.124413e-01 3.118198e-01 3.115973e-01 3.112271e-01
    [91] 3.106101e-01 3.096809e-01 3.094538e-01 3.090570e-01 3.087671e-01
##
    [96] 3.084471e-01 3.081247e-01 3.077228e-01 3.073877e-01 3.069752e-01
## [101] 3.063803e-01 3.061910e-01 3.059787e-01 3.049872e-01 3.046665e-01
## [106] 3.044079e-01 3.040532e-01 3.035988e-01 3.031260e-01 3.027676e-01
## [111] 3.027150e-01 3.022924e-01 3.020608e-01 3.014174e-01 3.010890e-01
## [116] 3.006127e-01 3.004942e-01 3.001918e-01 2.998117e-01 2.989800e-01
## [121] 2.988631e-01 2.980787e-01 2.979177e-01 2.976614e-01 2.975099e-01
```

```
## [126] 2.969556e-01 2.966247e-01 2.962663e-01 2.957480e-01 2.954312e-01
## [131] 2.953428e-01 2.950151e-01 2.945795e-01 2.940521e-01 2.938371e-01
## [136] 2.934020e-01 2.933125e-01 2.928964e-01 2.922293e-01 2.921385e-01
## [141] 2.915339e-01 2.913549e-01 2.911361e-01 2.908732e-01 2.905148e-01
## [146] 2.903281e-01 2.897991e-01 2.890742e-01 2.889780e-01 2.884177e-01
## [151] 2.879427e-01 2.876760e-01 2.873825e-01 2.871011e-01 2.868782e-01
## [156] 2.864860e-01 2.860537e-01 2.859609e-01 2.852450e-01 2.848761e-01
## [161] 2.844490e-01 2.841344e-01 2.839653e-01 2.834440e-01 2.829931e-01
## [166] 2.827709e-01 2.823692e-01 2.820356e-01 2.818586e-01 2.811388e-01
## [171] 2.806531e-01 2.803280e-01 2.801168e-01 2.798981e-01 2.797443e-01
## [176] 2.794733e-01 2.787168e-01 2.785315e-01 2.783899e-01 2.780506e-01
## [181] 2.777790e-01 2.774324e-01 2.772262e-01 2.766185e-01 2.765575e-01
## [186] 2.759575e-01 2.758757e-01 2.754086e-01 2.752078e-01 2.748788e-01
## [191] 2.746631e-01 2.740643e-01 2.739362e-01 2.734724e-01 2.731086e-01
## [196] 2.728439e-01 2.723410e-01 2.721835e-01 2.719680e-01 2.718531e-01
## [201] 2.712211e-01 2.706945e-01 2.704104e-01 2.701173e-01 2.700801e-01
## [206] 2.696879e-01 2.694455e-01 2.689887e-01 2.688407e-01 2.682429e-01
## [211] 2.680842e-01 2.676313e-01 2.671201e-01 2.668472e-01 2.665474e-01
## [216] 2.662644e-01 2.657745e-01 2.655749e-01 2.651410e-01 2.650523e-01
## [221] 2.648365e-01 2.646596e-01 2.642796e-01 2.641338e-01 2.637950e-01
## [226] 2.633721e-01 2.631509e-01 2.627955e-01 2.625522e-01 2.619448e-01
## [231] 2.616937e-01 2.614643e-01 2.611238e-01 2.607637e-01 2.604998e-01
## [236] 2.598202e-01 2.595343e-01 2.594131e-01 2.592182e-01 2.587438e-01
## [241] 2.585238e-01 2.584489e-01 2.578745e-01 2.575774e-01 2.574777e-01
## [246] 2.568828e-01 2.566786e-01 2.564208e-01 2.561685e-01 2.556855e-01
## [251] 2.552030e-01 2.549848e-01 2.547664e-01 2.544450e-01 2.539913e-01
## [256] 2.536382e-01 2.535043e-01 2.530004e-01 2.527111e-01 2.523643e-01
## [261] 2.520098e-01 2.515803e-01 2.515437e-01 2.510316e-01 2.509742e-01
## [266] 2.505403e-01 2.502062e-01 2.498543e-01 2.495622e-01 2.494090e-01
## [271] 2.491052e-01 2.486418e-01 2.484272e-01 2.476861e-01 2.474589e-01
## [276] 2.470446e-01 2.469481e-01 2.462622e-01 2.461518e-01 2.457009e-01
## [281] 2.454396e-01 2.453355e-01 2.449083e-01 2.447414e-01 2.439952e-01
## [286] 2.438978e-01 2.437522e-01 2.433766e-01 2.426950e-01 2.423489e-01
## [291] 2.422677e-01 2.420864e-01 2.411901e-01 2.408968e-01 2.406475e-01
## [296] 2.404391e-01 2.402672e-01 2.396579e-01 2.391390e-01 2.391241e-01
## [301] 2.383604e-01 2.383045e-01 2.376550e-01 2.375349e-01 2.372675e-01
## [306] 2.370537e-01 2.364774e-01 2.363943e-01 2.358918e-01 2.356462e-01
## [311] 2.348766e-01 2.348377e-01 2.340805e-01 2.334177e-01 2.331655e-01
## [316] 2.328555e-01 2.324970e-01 2.322191e-01 2.321355e-01 2.310586e-01
## [321] 2.308793e-01 2.304743e-01 2.299762e-01 2.288778e-01 2.284908e-01
## [326] 2.282540e-01 2.278286e-01 2.276666e-01 2.269590e-01 2.264172e-01
## [331] 2.259556e-01 2.248809e-01 2.246247e-01 2.238372e-01 2.228000e-01
## [336] 2.221419e-01 2.214539e-01 2.208353e-01 2.202328e-01 2.184213e-01
## [341] 2.179695e-01 2.139866e-01 1.846495e-01 7.970027e-16
summary(xc.pca)
## Importance of components:
                                PC1
                                          PC2
                                                    PC3
                                                              PC4
## Standard deviation 6427.2371 3.117e+03 1.626e+03 1.394e+03 1.348e+03
```

```
## Proportion of Variance
                             0.1189 2.796e-02 7.610e-03 5.590e-03 5.230e-03
## Cumulative Proportion
                             0.1189 1.469e-01 1.545e-01 1.601e-01 1.653e-01
                                PC<sub>6</sub>
                                           PC7
                                                     PC8
                                                               PC9
                                                                         PC10
## Standard deviation
                          1.263e+03 1.209e+03 1.203e+03 1.196e+03 1.189e+03
## Proportion of Variance 4.590e-03 4.210e-03 4.170e-03 4.120e-03 4.070e-03
## Cumulative Proportion
                          1.699e-01 1.741e-01 1.782e-01 1.824e-01 1.864e-01
##
                               PC11
                                          PC12
                                                    PC13
                                                              PC14
                                                                         PC15
## Standard deviation
                          1.184e+03 1.177e+03 1.169e+03 1163.7026 1.160e+03
## Proportion of Variance 4.030e-03 3.990e-03 3.940e-03
                                                            0.0039 3.870e-03
## Cumulative Proportion
                          1.905e-01 1.945e-01 1.984e-01
                                                            0.2023 2.062e-01
##
                               PC16
                                          PC17
                                                    PC18
                                                              PC19
                                                                         PC20
## Standard deviation
                          1.154e+03 1.153e+03 1148.8830 1.142e+03 1.138e+03
## Proportion of Variance 3.840e-03 3.830e-03
                                                  0.0038 3.750e-03 3.730e-03
## Cumulative Proportion 2.100e-01 2.138e-01
                                                  0.2176 2.214e-01 2.251e-01
##
                               PC21
                                          PC22
                                                    PC23
                                                              PC24
                                                                         PC25
## Standard deviation
                          1.135e+03 1.131e+03 1.130e+03 1.124e+03 1.122e+03
## Proportion of Variance 3.710e-03 3.680e-03 3.670e-03 3.640e-03 3.620e-03
## Cumulative Proportion
                          2.288e-01 2.325e-01 2.362e-01 2.398e-01 2.434e-01
##
                               PC26
                                          PC27
                                                    PC28
                                                              PC29
## Standard deviation
                          1.119e+03 1.118e+03 1.113e+03 1.112e+03 1.109e+03
## Proportion of Variance 3.610e-03 3.590e-03 3.570e-03 3.560e-03 3.540e-03
## Cumulative Proportion 2.470e-01 2.506e-01 2.542e-01 2.578e-01 2.613e-01
##
                               PC31
                                          PC32
                                                    PC33
                                                              PC34
                                                                         PC35
                          1.105e+03 1.104e+03 1.102e+03 1.100e+03 1.098e+03
## Standard deviation
## Proportion of Variance 3.510e-03 3.510e-03 3.490e-03 3.490e-03 3.470e-03
## Cumulative Proportion
                          2.648e-01 2.683e-01 2.718e-01 2.753e-01 2.788e-01
##
                               PC36
                                          PC37
                                                    PC38
                                                              PC39
                                                                         PC40
## Standard deviation
                          1.097e+03 1.096e+03 1.095e+03 1.090e+03 1.089e+03
## Proportion of Variance 3.460e-03 3.450e-03 3.450e-03 3.420e-03 3.410e-03
## Cumulative Proportion 2.822e-01 2.857e-01 2.891e-01 2.926e-01 2.960e-01
                                                    PC43
##
                               PC41
                                          PC42
                                                              PC44
                                                                         PC45
## Standard deviation
                          1087.3834 1086.5098 1.083e+03 1.082e+03 1.079e+03
## Proportion of Variance
                             0.0034
                                        0.0034 3.370e-03 3.370e-03 3.350e-03
                                        0.3028 3.061e-01 3.095e-01 3.129e-01
## Cumulative Proportion
                             0.2994
##
                               PC46
                                          PC47
                                                    PC48
                                                              PC49
                                                                         PC50
## Standard deviation
                          1.078e+03 1.076e+03 1.074e+03 1.073e+03 1070.5568
## Proportion of Variance 3.340e-03 3.340e-03 3.320e-03 3.310e-03
                                                                       0.0033
## Cumulative Proportion 3.162e-01 3.195e-01 3.229e-01 3.262e-01
                                                                       0.3295
                               PC51
                                          PC52
                                                    PC53
                                                              PC54
                                                                         PC55
## Standard deviation
                          1.068e+03 1.067e+03 1.065e+03 1.063e+03 1.062e+03
## Proportion of Variance 3.280e-03 3.280e-03 3.260e-03 3.250e-03 3.250e-03
## Cumulative Proportion
                          3.327e-01 3.360e-01 3.393e-01 3.426e-01 3.458e-01
                                                    PC58
##
                               PC56
                                          PC57
                                                              PC59
                                                                         PC60
## Standard deviation
                          1.059e+03 1.058e+03 1.055e+03 1054.6006 1.053e+03
## Proportion of Variance 3.230e-03 3.220e-03 3.210e-03
                                                            0.0032 3.190e-03
## Cumulative Proportion 3.490e-01 3.522e-01 3.554e-01
                                                            0.3587 3.618e-01
##
                               PC61
                                          PC62
                                                    PC63
                                                              PC64
                                                                         PC65
## Standard deviation
                          1.052e+03 1.050e+03 1.049e+03 1.049e+03 1.046e+03
## Proportion of Variance 3.190e-03 3.170e-03 3.170e-03 3.160e-03 3.150e-03
## Cumulative Proportion 3.650e-01 3.682e-01 3.714e-01 3.745e-01 3.777e-01
```

```
##
                                PC66
                                          PC67
                                                     PC68
                                                               PC69
                                                                          PC70
## Standard deviation
                           1.044e+03 1.043e+03 1.042e+03 1038.1663 1.037e+03
## Proportion of Variance 3.140e-03 3.130e-03 3.120e-03
                                                             0.0031 3.090e-03
## Cumulative Proportion
                          3.808e-01 3.840e-01 3.871e-01
                                                             0.3902 3.933e-01
                                                                          PC75
##
                                PC71
                                          PC72
                                                     PC73
                                                               PC74
## Standard deviation
                           1.035e+03 1.033e+03 1.031e+03 1.031e+03 1.030e+03
## Proportion of Variance 3.080e-03 3.070e-03 3.060e-03 3.060e-03 3.050e-03
                           3.963e-01 3.994e-01 4.025e-01 4.055e-01 4.086e-01
## Cumulative Proportion
##
                                                               PC79
                                PC76
                                          PC77
                                                     PC78
## Standard deviation
                           1.027e+03 1.026e+03 1.026e+03 1.024e+03 1.023e+03
## Proportion of Variance 3.040e-03 3.030e-03 3.030e-03 3.020e-03 3.010e-03
## Cumulative Proportion 4.116e-01 4.147e-01 4.177e-01 4.207e-01 4.237e-01
                                PC81
                                          PC82
                                                     PC83
                                                               PC84
                                                                          PC85
##
## Standard deviation
                           1020.4091 1.018e+03 1.018e+03 1.017e+03 1.016e+03
## Proportion of Variance
                              0.0030 2.990e-03 2.980e-03 2.980e-03 2.970e-03
## Cumulative Proportion
                              0.4267 4.297e-01 4.327e-01 4.357e-01 4.386e-01
##
                                PC86
                                          PC87
                                                     PC88
                                                               PC89
                                                                          PC90
## Standard deviation
                           1.015e+03 1.013e+03 1.011e+03 1.010e+03 1.009e+03
## Proportion of Variance 2.970e-03 2.950e-03 2.940e-03 2.940e-03 2.930e-03
## Cumulative Proportion
                           4.416e-01 4.446e-01 4.475e-01 4.504e-01 4.534e-01
##
                                PC91
                                          PC92
                                                     PC93
                                                               PC94
                                                                          PC95
## Standard deviation
                           1.007e+03 1004.1305 1003.3942 1.002e+03 1.001e+03
## Proportion of Variance 2.920e-03
                                                   0.0029 2.890e-03 2.880e-03
                                        0.0029
## Cumulative Proportion
                           4.563e-01
                                         0.4592
                                                   0.4621 4.650e-01 4.679e-01
                                                     PC98
                                                               PC99
##
                                PC96
                                          PC97
                                                                         PC100
## Standard deviation
                           1.000e+03 999.08472 997.78146 996.69503 995.35740
## Proportion of Variance 2.880e-03
                                       0.00287
                                                  0.00287
                                                            0.00286
                                                                       0.00285
## Cumulative Proportion
                           4.707e-01
                                       0.47361
                                                  0.47648
                                                            0.47934
                                                                       0.48219
##
                                                              PC104
                               PC101
                                         PC102
                                                    PC103
                                                                         PC105
## Standard deviation
                           993.42854 992.81470 992.12632 988.91157 987.87151
## Proportion of Variance
                             0.00284
                                       0.00284
                                                  0.00283
                                                            0.00281
                                                                      0.00281
## Cumulative Proportion
                             0.48503
                                       0.48787
                                                  0.49070
                                                            0.49351
                                                                       0.49632
##
                              PC106
                                       PC107
                                                  PC108
                                                            PC109
                                                                      PC110
## Standard deviation
                           987.0330 985.8830 984.40946 982.87657 981.71439
## Proportion of Variance
                             0.0028
                                      0.0028
                                                0.00279
                                                          0.00278
                                                                     0.00277
## Cumulative Proportion
                             0.4991
                                      0.5019
                                                0.50471
                                                          0.50749
                                                                     0.51027
##
                               PC111
                                         PC112
                                                    PC113
                                                              PC114
                                                                         PC115
## Standard deviation
                           981.54406 980.17362 979.42257 977.33637 976.27183
## Proportion of Variance
                                                  0.00276
                             0.00277
                                       0.00277
                                                            0.00275
                                                                      0.00274
## Cumulative Proportion
                             0.51304
                                       0.51580
                                                  0.51856
                                                            0.52131
                                                                      0.52406
##
                               PC116
                                         PC117
                                                    PC118
                                                              PC119
                                                                        PC120
## Standard deviation
                           974.72735 974.34291 973.36240 972.13000 969.4334
## Proportion of Variance
                             0.00273
                                       0.00273
                                                  0.00273
                                                            0.00272
                                                                       0.0027
## Cumulative Proportion
                             0.52679
                                       0.52952
                                                  0.53225
                                                            0.53497
                                                                       0.5377
##
                              PC121
                                        PC122
                                                   PC123
                                                             PC124
                                                                        PC125
## Standard deviation
                           969.0543 966.51082 965.98879 965.15780 964.66663
## Proportion of Variance
                             0.0027
                                      0.00269
                                                 0.00269
                                                           0.00268
                                                                      0.00268
## Cumulative Proportion
                             0.5404
                                      0.54307
                                                 0.54575
                                                           0.54843
                                                                      0.55111
##
                               PC126
                                         PC127
                                                    PC128
                                                              PC129
                                                                         PC130
## Standard deviation
                           962.86922 961.79648 960.63423 958.95375 957.92629
```

```
## Proportion of Variance
                             0.00267
                                        0.00266
                                                  0.00266
                                                             0.00265
                                                                       0.00264
## Cumulative Proportion
                             0.55378
                                        0.55644
                                                  0.55910
                                                             0.56175
                                                                       0.56439
##
                               PC131
                                          PC132
                                                    PC133
                                                               PC134
                                                                         PC135
## Standard deviation
                           957.63992 956.57709 955.16471 953.45459 952.75773
## Proportion of Variance
                             0.00264
                                        0.00263
                                                  0.00263
                                                             0.00262
                                                                       0.00261
## Cumulative Proportion
                             0.56703
                                        0.56966
                                                  0.57229
                                                             0.57490
                                                                       0.57751
##
                              PC136
                                        PC137
                                                 PC138
                                                            PC139
                                                                      PC140
PC141
## Standard deviation
                           951.3468 951.0565 949.7074 947.54449 947.25003
945.28954
                                       0.0026
                                                0.0026
## Proportion of Variance
                             0.0026
                                                          0.00258
                                                                    0.00258
0.00257
## Cumulative Proportion
                                       0.5827
                                                0.5853
                                                          0.58790
                                                                    0.59048
                             0.5801
0.59306
##
                               PC142
                                          PC143
                                                    PC144
                                                               PC145
                                                                         PC146
                           944.70931 943.99979 943.14729 941.98509 941.37995
## Standard deviation
## Proportion of Variance
                             0.00257
                                        0.00256
                                                  0.00256
                                                             0.00255
                                                                       0.00255
## Cumulative Proportion
                             0.59563
                                        0.59819
                                                  0.60075
                                                             0.60330
                                                                       0.60585
##
                               PC147
                                          PC148
                                                    PC149
                                                               PC150
                                                                          PC151
## Standard deviation
                           939.66465 937.31413 937.00220 935.18535 933.64506
## Proportion of Variance
                             0.00254
                                        0.00253
                                                  0.00253
                                                             0.00252
                                                                       0.00251
## Cumulative Proportion
                             0.60840
                                        0.61092
                                                  0.61345
                                                             0.61597
                                                                       0.61848
##
                              PC152
                                        PC153
                                                  PC154
                                                             PC155
                                                                       PC156
## Standard deviation
                           932.7803 931.8289 930.91633 930.19361 928.92185
## Proportion of Variance
                             0.0025
                                       0.0025
                                                0.00249
                                                           0.00249
                                                                     0.00248
## Cumulative Proportion
                             0.6210
                                       0.6235
                                                0.62597
                                                           0.62847
                                                                     0.63095
##
                               PC157
                                          PC158
                                                    PC159
                                                               PC160
                                                                         PC161
## Standard deviation
                           927.52026 927.21918 924.89786 923.70176 922.31703
## Proportion of Variance
                             0.00248
                                        0.00247
                                                  0.00246
                                                             0.00246
                                                                       0.00245
## Cumulative Proportion
                             0.63342
                                        0.63590
                                                  0.63836
                                                             0.64082
                                                                       0.64327
##
                               PC162
                                          PC163
                                                    PC164
                                                               PC165
                                                                         PC166
## Standard deviation
                           921.29699 920.74845 919.05833 917.59636 916.87582
## Proportion of Variance
                             0.00244
                                        0.00244
                                                  0.00243
                                                             0.00242
                                                                       0.00242
## Cumulative Proportion
                             0.64571
                                        0.64815
                                                  0.65058
                                                             0.65300
                                                                       0.65542
##
                               PC167
                                          PC168
                                                   PC169
                                                              PC170
                                                                        PC171
## Standard deviation
                           915.57335 914.49148 913.9177 911.58384 910.00905
## Proportion of Variance
                             0.00241
                                        0.00241
                                                  0.0024
                                                            0.00239
                                                                      0.00238
## Cumulative Proportion
                             0.65783
                                        0.66024
                                                  0.6626
                                                            0.66504
                                                                      0.66742
##
                               PC172
                                          PC173
                                                    PC174
                                                               PC175
                                                                         PC176
## Standard deviation
                           908.95494 908.27011 907.56094 907.06211 906.18340
## Proportion of Variance
                             0.00238
                                        0.00237
                                                  0.00237
                                                             0.00237
                                                                       0.00236
## Cumulative Proportion
                             0.66980
                                        0.67217
                                                  0.67454
                                                             0.67691
                                                                       0.67927
##
                               PC177
                                          PC178
                                                    PC179
                                                               PC180
                                                                          PC181
## Standard deviation
                           903.73049 903.12970 902.67053 901.57053 900.68965
## Proportion of Variance
                             0.00235
                                        0.00235
                                                  0.00235
                                                             0.00234
                                                                       0.00233
## Cumulative Proportion
                             0.68163
                                        0.68397
                                                  0.68632
                                                             0.68866
                                                                       0.69099
##
                               PC182
                                          PC183
                                                    PC184
                                                               PC185
                                                                        PC186
## Standard deviation
                           899.56596 898.89720 896.92670 896.72921 894.7837
## Proportion of Variance
                             0.00233
                                        0.00233
                                                  0.00232
                                                             0.00231
                                                                       0.0023
## Cumulative Proportion
                             0.69332
                                       0.69565
                                                  0.69796
                                                             0.70028
                                                                       0.7026
```

```
##
                              PC187
                                        PC188
                                                  PC189
                                                             PC190
                                                                        PC191
## Standard deviation
                           894.5184 893.0036 892.35254 891.28595 890.58649
## Proportion of Variance
                             0.0023
                                       0.0023
                                                0.00229
                                                           0.00229
                                                                     0.00228
## Cumulative Proportion
                             0.7049
                                       0.7072
                                                0.70947
                                                           0.71176
                                                                     0.71404
##
                               PC192
                                          PC193
                                                    PC194
                                                               PC195
                                                                          PC196
## Standard deviation
                           888.64477 888.22955 886.72565 885.54610 884.68771
                             0.00227
## Proportion of Variance
                                        0.00227
                                                  0.00226
                                                             0.00226
                                                                        0.00225
## Cumulative Proportion
                             0.71631
                                        0.71858
                                                  0.72085
                                                             0.72310
                                                                        0.72536
                               PC197
##
                                          PC198
                                                    PC199
                                                               PC200
                                                                          PC201
## Standard deviation
                           883.05731 882.54659 881.84786 881.47513 879.42589
## Proportion of Variance
                             0.00224
                                        0.00224
                                                  0.00224
                                                             0.00224
                                                                        0.00223
## Cumulative Proportion
                             0.72760
                                        0.72984
                                                  0.73208
                                                             0.73432
                                                                        0.73654
##
                                                    PC204
                                                               PC205
                               PC202
                                          PC203
                                                                        PC206
## Standard deviation
                           877.71856 876.79720 875.84678 875.72619 874.4545
## Proportion of Variance
                             0.00222
                                                  0.00221
                                        0.00221
                                                             0.00221
                                                                        0.0022
## Cumulative Proportion
                             0.73876
                                        0.74097
                                                  0.74318
                                                             0.74539
                                                                        0.7476
##
                              PC207
                                         PC208
                                                   PC209
                                                              PC210
                                                                        PC211
## Standard deviation
                           873.6686 872.18734 871.70746 869.76936 869.25465
## Proportion of Variance
                             0.0022
                                       0.00219
                                                 0.00219
                                                            0.00218
                                                                       0.00217
## Cumulative Proportion
                             0.7498
                                       0.75197
                                                 0.75416
                                                            0.75634
                                                                       0.75851
##
                               PC212
                                          PC213
                                                    PC214
                                                               PC215
                                                                          PC216
## Standard deviation
                           867.78609 866.12867 865.24357 864.27167 863.35416
## Proportion of Variance
                             0.00217
                                        0.00216
                                                  0.00215
                                                             0.00215
                                                                        0.00215
## Cumulative Proportion
                             0.76068
                                        0.76284
                                                  0.76499
                                                             0.76714
                                                                        0.76929
##
                               PC217
                                          PC218
                                                    PC219
                                                               PC220
                                                                          PC221
## Standard deviation
                           861.76538 861.11841 859.71126 859.42395 858.72401
## Proportion of Variance
                             0.00214
                                        0.00213
                                                  0.00213
                                                             0.00213
                                                                        0.00212
## Cumulative Proportion
                             0.77143
                                        0.77356
                                                  0.77569
                                                             0.77781
                                                                        0.77994
##
                               PC222
                                          PC223
                                                    PC224
                                                               PC225
                                                                         PC226
## Standard deviation
                           858.15042 856.91837 856.44571 855.34707 853.9759
## Proportion of Variance
                             0.00212
                                        0.00211
                                                  0.00211
                                                             0.00211
                                                                        0.0021
## Cumulative Proportion
                             0.78206
                                        0.78417
                                                  0.78628
                                                             0.78839
                                                                        0.7905
##
                              PC227
                                         PC228
                                                    PC229
                                                              PC230
                                                                         PC231
## Standard deviation
                           853.2587 852.10611 851.31720 849.34779 848.53370
## Proportion of Variance
                             0.0021
                                       0.00209
                                                 0.00209
                                                            0.00208
                                                                       0.00207
## Cumulative Proportion
                             0.7926
                                       0.79467
                                                 0.79676
                                                            0.79883
                                                                       0.80091
                                          PC233
##
                               PC232
                                                    PC234
                                                               PC235
                                                                          PC236
## Standard deviation
                           847.78987 846.68578 845.51827 844.66254 842.45881
## Proportion of Variance
                             0.00207
                                        0.00206
                                                  0.00206
                                                             0.00205
                                                                        0.00204
## Cumulative Proportion
                             0.80297
                                        0.80504
                                                  0.80709
                                                             0.80915
                                                                        0.81119
##
                               PC237
                                          PC238
                                                    PC239
                                                               PC240
                                                                          PC241
## Standard deviation
                           841.53183 841.13881 840.50695 838.96856 838.25535
## Proportion of Variance
                             0.00204
                                        0.00204
                                                  0.00203
                                                             0.00203
                                                                        0.00202
## Cumulative Proportion
                             0.81323
                                        0.81527
                                                  0.81730
                                                             0.81932
                                                                        0.82135
##
                                                    PC244
                                                               PC245
                               PC242
                                          PC243
                                                                        PC246
## Standard deviation
                           838.01260 836.14987 835.18682 834.86347 832.9343
## Proportion of Variance
                             0.00202
                                        0.00201
                                                  0.00201
                                                             0.00201
                                                                        0.0020
## Cumulative Proportion
                             0.82337
                                        0.82538
                                                  0.82739
                                                             0.82939
                                                                        0.8314
##
                               PC247
                                          PC248
                                                    PC249
                                                               PC250
                                                                          PC251
## Standard deviation
                           832.27220 831.43634 830.61835 829.05215 827.48778
```

```
## Proportion of Variance
                             0.00199
                                        0.00199
                                                  0.00199
                                                             0.00198
                                                                       0.00197
## Cumulative Proportion
                             0.83338
                                        0.83537
                                                  0.83736
                                                             0.83934
                                                                       0.84131
##
                               PC252
                                          PC253
                                                    PC254
                                                               PC255
                                                                         PC256
## Standard deviation
                           826.78021 826.07222 825.02992 823.55881 822.41380
                                                  0.00196
## Proportion of Variance
                             0.00197
                                        0.00196
                                                             0.00195
                                                                       0.00195
## Cumulative Proportion
                             0.84328
                                        0.84524
                                                  0.84720
                                                             0.84915
                                                                       0.85110
##
                              PC257
                                         PC258
                                                   PC259
                                                              PC260
                                                                        PC261
## Standard deviation
                           8.22e+02 820.34579 819.40790 818.28326 817.13380
## Proportion of Variance 1.94e-03
                                       0.00194
                                                 0.00193
                                                            0.00193
                                                                      0.00192
## Cumulative Proportion
                           8.53e-01
                                       0.85498
                                                 0.85691
                                                            0.85884
                                                                      0.86076
##
                               PC262
                                          PC263
                                                    PC264
                                                               PC265
                                                                        PC266
## Standard deviation
                           815.74132 815.62244 813.96213 813.77593 812.3691
## Proportion of Variance
                             0.00192
                                        0.00191
                                                  0.00191
                                                             0.00191
                                                                       0.0019
## Cumulative Proportion
                             0.86268
                                        0.86459
                                                  0.86650
                                                             0.86840
                                                                       0.8703
##
                                                    PC269
                                                               PC270
                               PC267
                                          PC268
                                                                         PC271
## Standard deviation
                           811.28565 810.14490 809.19772 808.70092 807.71591
## Proportion of Variance
                             0.00189
                                        0.00189
                                                  0.00188
                                                             0.00188
                                                                       0.00188
## Cumulative Proportion
                                                  0.87597
                             0.87220
                                        0.87409
                                                             0.87785
                                                                       0.87973
##
                               PC272
                                          PC273
                                                    PC274
                                                               PC275
                                                                        PC276
## Standard deviation
                           806.21314 805.51739 803.11445 802.37787 8.01e+02
## Proportion of Variance
                             0.00187
                                        0.00187
                                                  0.00186
                                                             0.00185 1.85e-03
## Cumulative Proportion
                             0.88160
                                        0.88347
                                                  0.88532
                                                             0.88718 8.89e-01
##
                               PC277
                                          PC278
                                                    PC279
                                                               PC280
                                                                         PC281
## Standard deviation
                           800.72148 798.49763 798.13957 796.67753 795.83013
## Proportion of Variance
                             0.00185
                                        0.00184
                                                  0.00183
                                                             0.00183
                                                                       0.00182
## Cumulative Proportion
                             0.89087
                                        0.89270
                                                  0.89454
                                                             0.89637
                                                                       0.89819
                                                    PC284
##
                               PC282
                                          PC283
                                                              PC285
                                                                       PC286
PC287
## Standard deviation
                           795.49283 794.10760 793.56622 791.1468 790.8311
790.3589
## Proportion of Variance
                             0.00182
                                       0.00181
                                                  0.00181
                                                             0.0018
                                                                      0.0018
0.0018
## Cumulative Proportion
                             0.90001
                                       0.90182
                                                  0.90364
                                                             0.9054
                                                                      0.9072
0.9090
##
                               PC288
                                          PC289
                                                    PC290
                                                               PC291
                                                                         PC292
## Standard deviation
                           789.14105 786.93102 785.80873 785.54538 784.95766
## Proportion of Variance
                             0.00179
                                        0.00178
                                                  0.00178
                                                             0.00178
                                                                       0.00177
## Cumulative Proportion
                             0.91083
                                        0.91261
                                                  0.91439
                                                             0.91616
                                                                       0.91794
##
                               PC293
                                          PC294
                                                    PC295
                                                               PC296
                                                                         PC297
## Standard deviation
                           782.05124 781.10025 780.29212 779.61622 779.05885
## Proportion of Variance
                             0.00176
                                        0.00176
                                                  0.00175
                                                             0.00175
                                                                       0.00175
## Cumulative Proportion
                             0.91970
                                        0.92145
                                                  0.92321
                                                             0.92496
                                                                       0.92670
##
                                          PC299
                               PC298
                                                    PC300
                                                               PC301
                                                                         PC302
## Standard deviation
                           777.08340 775.40078 775.35255 772.87626 772.69474
## Proportion of Variance
                             0.00174
                                        0.00173
                                                  0.00173
                                                             0.00172
                                                                       0.00172
## Cumulative Proportion
                             0.92844
                                        0.93017
                                                  0.93190
                                                             0.93362
                                                                       0.93534
##
                               PC303
                                          PC304
                                                   PC305
                                                             PC306
                                                                       PC307
## Standard deviation
                           770.58903 770.19950 769.3325 768.6392 766.77070
## Proportion of Variance
                             0.00171
                                        0.00171
                                                  0.0017
                                                            0.0017
                                                                     0.00169
## Cumulative Proportion
                             0.93705
                                       0.93875
                                                  0.9405
                                                            0.9422
                                                                     0.94385
```

```
##
                               PC308
                                          PC309
                                                     PC310
                                                               PC311
                                                                          PC312
## Standard deviation
                           766.50114 764.87184 764.07549 761.58017 761.45398
## Proportion of Variance
                             0.00169
                                        0.00168
                                                  0.00168
                                                             0.00167
                                                                        0.00167
## Cumulative Proportion
                             0.94554
                                        0.94723
                                                  0.94891
                                                                        0.95224
                                                             0.95058
##
                               PC313
                                          PC314
                                                     PC315
                                                               PC316
                                                                          PC317
## Standard deviation
                           758.99870 756.84958 756.03198 755.02663 753.86420
## Proportion of Variance
                                                  0.00165
                             0.00166
                                        0.00165
                                                             0.00164
                                                                        0.00164
## Cumulative Proportion
                             0.95390
                                        0.95555
                                                  0.95720
                                                             0.95884
                                                                        0.96047
##
                               PC318
                                          PC319
                                                     PC320
                                                               PC321
                                                                          PC322
## Standard deviation
                           752.96305 752.69211 749.20016 748.61892 747.30583
## Proportion of Variance
                                                  0.00162
                                                             0.00161
                             0.00163
                                        0.00163
                                                                        0.00161
## Cumulative Proportion
                             0.96210
                                        0.96373
                                                  0.96535
                                                             0.96696
                                                                        0.96857
##
                              PC323
                                         PC324
                                                   PC325
                                                              PC326
                                                                         PC327
## Standard deviation
                           745.6907 742.12923 740.87419 740.10633 738.72716
## Proportion of Variance
                             0.0016
                                       0.00159
                                                 0.00158
                                                            0.00158
                                                                       0.00157
## Cumulative Proportion
                             0.9702
                                       0.97176
                                                 0.97334
                                                            0.97491
                                                                       0.97648
##
                               PC328
                                          PC329
                                                     PC330
                                                               PC331
                                                                          PC332
## Standard deviation
                           738.20175 735.90746 734.15054 732.65389 729.16925
## Proportion of Variance
                             0.00157
                                        0.00156
                                                  0.00155
                                                             0.00154
                                                                        0.00153
## Cumulative Proportion
                                        0.97961
                             0.97805
                                                  0.98116
                                                             0.98271
                                                                        0.98424
##
                                          PC334
                                                   PC335
                                                              PC336
                               PC333
                                                                         PC337
## Standard deviation
                           728.33855 725.78514 722.4219 720.28823 718.05731
## Proportion of Variance
                             0.00153
                                        0.00152
                                                  0.0015
                                                            0.00149
                                                                       0.00148
## Cumulative Proportion
                                        0.98728
                                                  0.9888
                                                            0.99027
                                                                       0.99176
                             0.98576
##
                               PC338
                                          PC339
                                                     PC340
                                                               PC341
                                                                          PC342
## Standard deviation
                           716.05153 714.09795 708.22422 706.75925 693.84489
## Proportion of Variance
                                                  0.00144
                                                             0.00144
                             0.00148
                                        0.00147
                                                                        0.00139
## Cumulative Proportion
                             0.99323
                                        0.99470
                                                  0.99615
                                                             0.99758
                                                                        0.99897
##
                               PC343
                                          PC344
## Standard deviation
                           598.72011 2.584e-12
## Proportion of Variance
                             0.00103 0.000e+00
## Cumulative Proportion
                             1.00000 1.000e+00
Xc.just.sex <- model.matrix(~ Sex, data=xc mat)</pre>
xc.pca.and.sex <- cbind(xc.pca, Xc.just.sex)</pre>
## Warning in cbind(xc.pca, Xc.just.sex): number of rows of result is not a
## multiple of vector length (arg 1)
gene_info <- read.csv('gene_info.csv')</pre>
SNP_info <- read.csv('SNP_info.csv')</pre>
# Define our function to run GWAS and get p-values
pval calculator w covars <- function(pheno input, xa_input, xd input,</pre>
xz input){
  n_samples <- length(xa_input) # calculate your number of samples</pre>
  X_mx <- cbind(rep(1,length(xa_input)),xa_input, xd_input, xz_input) #create</pre>
your X matrix under H1
```

```
MLE beta <- ginv(t(X mx) %*% X mx) %*% t(X mx) %*% pheno input #calculate
your MLE of the betas
  x h0 = cbind(rep(1,length(xa input)), xz input) #calculate your x under H0
  MLE_h0 = ginv(t(x_h0) %*% x_h0) %*% t(x_h0) %*% pheno_input #calculate your
MLE under h0
  y_hat_0 = x_h0 %*% MLE_h0 #calculate y_hat under the null hypothesis
  y_hat_1 = X_mx%*% MLE_beta #calculate y_hat under H1
  SSE theta 0 = sum((pheno input-y hat 0)^2) #calculate SSE under null
  SSE theta 1 = sum((pheno input-y hat 1)^2) #calculate SSE under H1
  df M <- 2
  df E <- n samples - 4
  numerator <- (SSE theta 0-SSE theta 1) / df M #calculate your F statistic
  denom <- SSE theta 1 / df E
  Fstatistic <-numerator / denom
  # to check if it is correct
  pval <- pf(Fstatistic, df M, df E,lower.tail = FALSE) #calculate your p</pre>
value and return it
  return(pval)
}
# Run the functions
results.1 <- lapply(1:ncol(xa mat), function(column.counter){</pre>
  data.table(pval_calculator_w_covars(pheno_input = sim_pheno_mx[,1],
                                      xa_input = as.matrix(xa_mat[,
column.counter]),
                                      xd input = as.matrix(xd mat[,
column.counter]),
                                       xz input = as.matrix(xc mat1)))
              }) %>% rbindlist() %>% mutate(p=V1, index = 1:ncol(xa mat))
indices1 <- which(p.adjust(results.1$p, method = "bonferroni") <= 0.05)</pre>
hits1 <- sort(SNP_info$position[indices1])</pre>
length(hits1)
## [1] 71
results.2 <- lapply(1:ncol(xa_mat), function(column.counter){
  data.table(pval_calculator_w_covars(pheno_input = sim_pheno_mx[,2],
                                      xa input = as.matrix(xa mat[,
column.counter]),
                                      xd input = as.matrix(xd mat[,
column.counter]),
                                      xz input = as.matrix(xc mat1)))
              }) %>% rbindlist() %>% mutate(p=V1, index = 1:ncol(xa_mat))
```

```
indices2 <- which(p.adjust(results.2$p, method = "bonferroni") <= 0.05)</pre>
hits2 <- sort(SNP info$position[indices2])</pre>
hits2
## [1] 42889467 42893842 42896182 42903013 42904736 42907726 42911587
42916172
## [9] 42919954 42924756 42938645 42942927 42946612 42949278 42952810
42953822
## [17] 42954621 42956454 42957216 42962100 42964461 42969161 42972496
42973585
## [25] 42977844 43108015 98486048
results.3 <- lapply(1:ncol(xa_mat), function(column.counter){</pre>
  data.table(pval_calculator_w_covars(pheno_input = sim_pheno_mx[,3],
                                      xa_input = as.matrix(xa_mat[,
column.counter]),
                                      xd input = as.matrix(xd mat[,
column.counter]),
                                      xz_input = as.matrix(xc_mat1)))
              }) %>% rbindlist() %>% mutate(p=V1, index = 1:ncol(xa mat))
indices3 <- which(p.adjust(results.3$p, method = "bonferroni") <= 0.05)</pre>
hits3 <- sort(SNP info$position[indices3])</pre>
hits3
## [1] 1524250 1604317 1614929 1780619 1785391 1789021 1792207 1794224
1798982
## [10] 1804934 1806080 1806559 1807707 1808392 1809480 1810194 1810803
## [19] 1812168 1813518 1816100 1819604 1820639 1824144 1825190 1826990
1828065
## [28] 1829958 1831143 1831554 1832328 1832761 1835286 1836231 1837572
1839643
## [37] 1842605 1842970 1845028 1845980 1846938 1848043 1849190 1850033
1852576
## [46] 1854320 1854638 1855229 1856231 1857300 1858216 1858666 1859725
1860371
## [55] 1861583 1862683 1862993 1864524 1864887 1865581 1866730 1867504
1868123
## [64] 1868857 1869663 1870120 1871282 1872310 1873062 1873933 1874763
1883987
## [73] 1892929 1895185 1897411 1898338 1899224 1901135 1902367 1904506
1911549
## [82] 1916400 1919081 1921599 1923514 1926150 1926998 1928485 1929366
results.4 <- lapply(1:ncol(xa mat), function(column.counter){</pre>
  data.table(pval_calculator_w_covars(pheno_input = sim_pheno_mx[,4],
                                      xa_input = as.matrix(xa_mat[,
column.counter]),
                                      xd_input = as.matrix(xd_mat[,
```

```
column.counter]),
                                       xz input = as.matrix(xc mat1)))
              }) %>% rbindlist() %>% mutate(p=V1, index = 1:ncol(xa_mat))
indices4 <- which(p.adjust(results.4$p, method = "bonferroni") <= 0.05)</pre>
hits4 <- sort(SNP info$position[indices4])</pre>
results.5 <- lapply(1:ncol(xa_mat), function(column.counter){
  data.table(pval_calculator_w_covars(pheno_input = sim_pheno_mx[,5],
                                       xa_input = as.matrix(xa_mat[,
column.counter]),
                                      xd input = as.matrix(xd mat[,
column.counter]),
                                      xz input = as.matrix(xc mat1)))
              }) %>% rbindlist() %>% mutate(p=V1, index = 1:ncol(xa_mat))
indices5 <- which(p.adjust(results.5$p, method = "bonferroni") <= 0.05)</pre>
hits5 <- sort(SNP_info$position[indices5])</pre>
# Manhattan Plot
## phenotype 1 - ERAP2
my.alpha = 0.05/ncol(xa_mat)
man1 <- ggplot(results.1, aes(x = index, y = -\log 10(p))) +
  geom_point() +
  geom hline(yintercept = -log10(my.alpha), color = 'red', lty = 2) +
  labs(x = 'Index', y = expression(-log[10]~p),
       title = 'GWAS Manhattan Plot- ERAP2', subtitle='Covariates Included')
## phenotype 2 - PEX6
my.alpha = 0.05/ncol(xa_mat)
man2 <- ggplot(results.2, aes(x = index, y = -log10(p))) +
  geom_point() +
  geom_hline(yintercept = -log10(my.alpha), color = 'red', lty = 2) +
  labs(x = 'Index', y = expression(-log[10]~p),
       title = 'GWAS Manhattan Plot - PEX6', subtitle='Covariates Included')
## phenotype 3 - FAHD1
my.alpha = 0.05/ncol(xa_mat)
man3 <- ggplot(results.3, aes(x = index, y = -log10(p))) +
  geom point() +
  geom_hline(yintercept = -log10(my.alpha), color = 'red', lty = 2) +
  labs(x = 'Index', y = expression(-log[10]~p),
       title = 'GWAS Manhattan Plot - FAHD1', subtitle='Covariates Included')
## phenotype 4 - GFM1
my.alpha = 0.05/ncol(xa_mat)
```

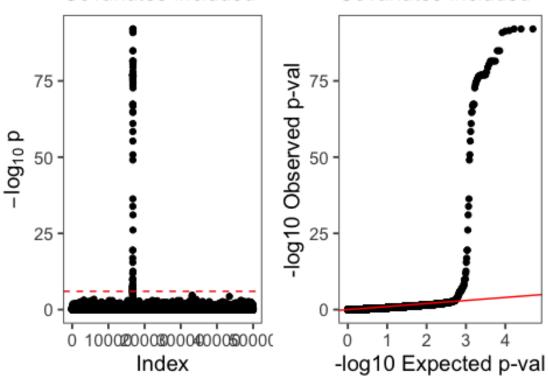
```
man4 <- ggplot(results.4, aes(x = index, y = -log10(p))) +
  geom point() +
  geom_hline(yintercept = -log10(my.alpha), color = 'red', lty = 2) +
  labs(x = 'Index', y = expression(-log[10]~p),
       title = 'GWAS Manhattan Plot - GFM1', subtitle='Covariates Included')
## phenotype 5 - MARCHF7
my.alpha = 0.05/ncol(xa mat)
man5 <- ggplot(results.5, aes(x = index, y = -log10(p))) +
  geom_point() +
  geom_hline(yintercept = -log10(my.alpha), color = 'red', lty = 2) +
  labs(x = 'Index', y = expression(-log[10]~p),
       title = 'GWAS Manhattan Plot - MARCHF7', subtitle='Covariates
Included')
# 00 plot
## phenotype 1 - ERAP2
observed pvals = sort(results.1$p)
expected_pvals = qunif(seq(0, 1, length.out = length(observed_pvals) + 2),
min = 0, max = 1) ## Generate expected values. Note that we are using
Length+2
expected_pvals = expected_pvals[expected_pvals != 0 & expected_pvals != 1]
## Remove the two extra values since they are 0 and 1
p df = data.frame(observed = -log10(observed pvals),
                  expected = -log10(expected pvals))
qq <- ggplot(p_df, aes(x = expected, y = observed)) +
  geom point() +
  geom_abline(intercept = 0, slope = 1, color = 'red') +
  labs(x = '-log10 Expected p-val',
       y = '-log10 Observed p-val'
       title = 'GWAS QQ plot - ERAP2',
       subtitle = 'Covariates Included')
grid.arrange(man1,qq, ncol=2)
```

GWAS Manhattan

GWAS QQ plot - E

Covariates Included

Covariates Included



```
## phenotype 2 - PEX6
observed pvals = sort(results.2$p)
expected_pvals = qunif(seq(0, 1, length.out = length(observed_pvals) + 2),
min = 0, max = 1) ## Generate expected values. Note that we are using
Length+2
expected_pvals = expected_pvals[expected_pvals != 0 & expected_pvals != 1]
## Remove the two extra values since they are 0 and 1
p_df = data.frame(observed = -log10(observed_pvals),
                  expected = -log10(expected pvals))
qq <- ggplot(p_df, aes(x = expected, y = observed)) +
  geom_point() +
  geom_abline(intercept = 0, slope = 1, color = 'red') +
  labs(x = '-log10 Expected p-val',
       y = '-log10 Observed p-val',
       title = 'GWAS QQ plot - PEX6',
       subtitle = 'Covariates Included')
grid.arrange(man2,qq, ncol=2)
```

GWAS Manhattan GWAS QQ plot - P Covariates Included Covariates Included 75 · 75 -log10 Observed p-val -log₁₀ p 50 25 . 0 0 1000200003000040000500000 2 3 -log10 Expected p-val

Index

```
## phenotype 3 - FAHD1
observed pvals = sort(results.3$p)
expected_pvals = qunif(seq(0, 1, length.out = length(observed_pvals) + 2),
min = 0, max = 1) ## Generate expected values. Note that we are using
Length+2
expected_pvals = expected_pvals[expected_pvals != 0 & expected_pvals != 1]
## Remove the two extra values since they are 0 and 1
p_df = data.frame(observed = -log10(observed_pvals),
                  expected = -log10(expected pvals))
qq <- ggplot(p_df, aes(x = expected, y = observed)) +
  geom_point() +
  geom_abline(intercept = 0, slope = 1, color = 'red') +
  labs(x = '-log10 Expected p-val',
       y = '-log10 Observed p-val',
       title = 'GWAS QQ plot - FAHD1',
       subtitle = 'Covariates Included')
grid.arrange(man3,qq, ncol=2)
```

GWAS QQ plot - F GWAS Manhattan Covariates Included Covariates Included 50 • 50 -log10 Observed p-val 40 40 · -log₁₀ p 30 30 20 20 10 10

0

0 1000200003000040000500000

Index

```
## phenotype 4 - GFM1
observed pvals = sort(results.4$p)
expected_pvals = qunif(seq(0, 1, length.out = length(observed_pvals) + 2),
min = 0, max = 1) ## Generate expected values. Note that we are using
Length+2
expected_pvals = expected_pvals[expected_pvals != 0 & expected_pvals != 1]
## Remove the two extra values since they are 0 and 1
p_df = data.frame(observed = -log10(observed_pvals),
                  expected = -log10(expected pvals))
qq <- ggplot(p_df, aes(x = expected, y = observed)) +
  geom_point() +
  geom_abline(intercept = 0, slope = 1, color = 'red') +
  labs(x = '-log10 Expected p-val',
       y = '-log10 Observed p-val',
       title = 'GWAS QQ plot - GFM1',
       subtitle = 'Covariates Included')
grid.arrange(man4,qq, ncol=2)
```

2

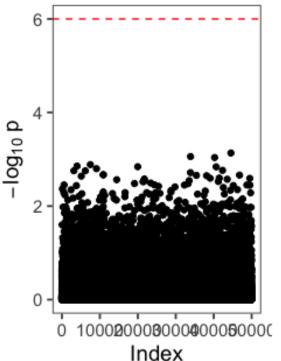
-log10 Expected p-val

3

GWAS Manhattan

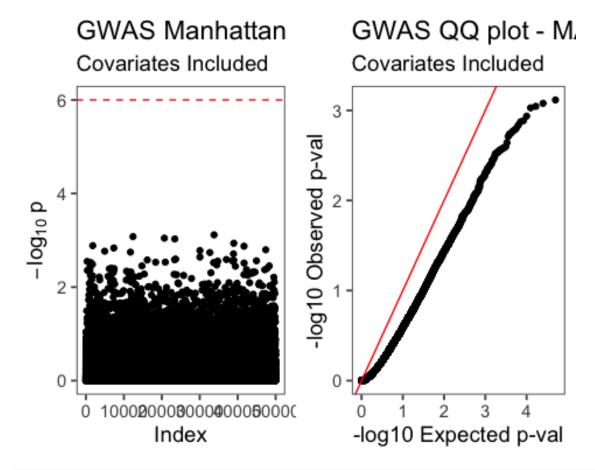
GWAS QQ plot - Gl Covariates Included

Covariates Included

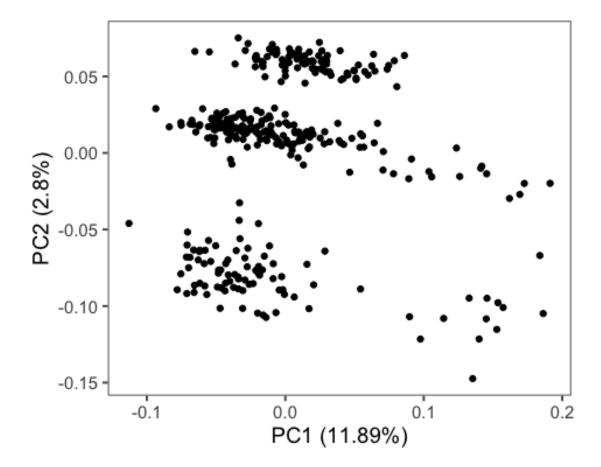


log10 Opserved b-val

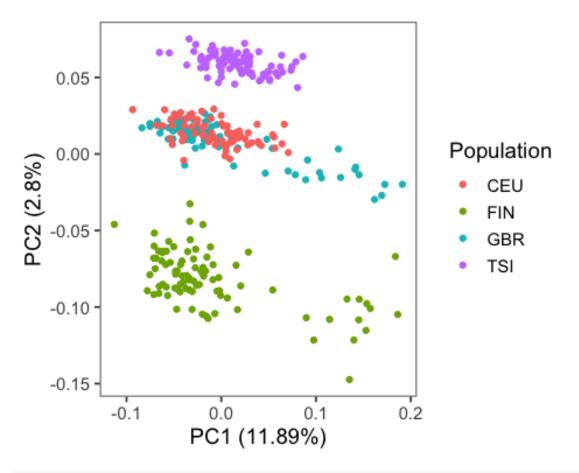
```
## phenotype 5 - MARCHF7
observed pvals = sort(results.5$p)
expected_pvals = qunif(seq(0, 1, length.out = length(observed_pvals) + 2),
min = 0, max = 1) ## Generate expected values. Note that we are using
Length+2
expected_pvals = expected_pvals[expected_pvals != 0 & expected_pvals != 1]
## Remove the two extra values since they are 0 and 1
p_df = data.frame(observed = -log10(observed_pvals),
                  expected = -log10(expected pvals))
qq <- ggplot(p_df, aes(x = expected, y = observed)) +
  geom_point() +
  geom_abline(intercept = 0, slope = 1, color = 'red') +
  labs(x = '-log10 Expected p-val',
       y = '-log10 Observed p-val',
       title = 'GWAS QQ plot - MARCHF7',
       subtitle = 'Covariates Included')
grid.arrange(man5,qq, ncol=2)
```



library(ggfortify)
xc.pca<- prcomp(xa_mat %*% t(xa_mat))
autoplot(xc.pca)</pre>



autoplot(xc.pca, data = xc_mat, colour = "Population")



autoplot(xc.pca, data = xc_mat, colour = "Sex")

