

EE210A: Microelectronics I - Mini-Quiz 6

NAME (in capital)

Roll No

Time: 20 minutes

1) : Consider all transistors are identical. $\mu_n C_{ox} = 200 \mu A/V^2$, $W/L = 10$, $\lambda = 0.1 V^{-1}$. $I_0 = 1 mA$, $V_{tn} = 1 V$. Neglect body effect.

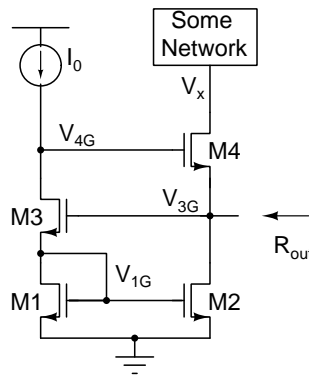


Fig. 1. Problem 1

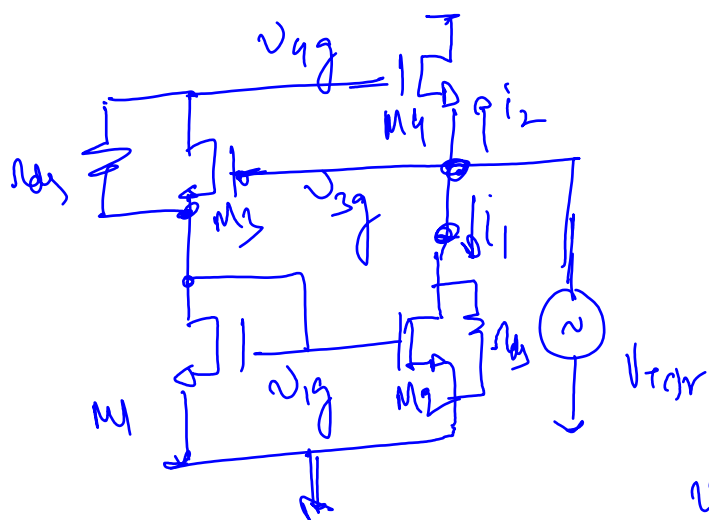
a) : Neglect channel length modulation for all transistors for this part. Find the quiescent voltages at V_{1G} , V_{3G} . You are allowed to change the aspect ratio of a single transistor to decrease V_{3G} by 500 mV. What will you change in the circuit? [2+3]

$$V_{1G} = V_{tn} + \sqrt{\frac{2 I_0}{\mu_n C_{ox} (W/L)_2}} = 2V$$

$$V_{3G} = V_{1G} + V_{tn} + \sqrt{\frac{2 I_0}{\mu_n C_{ox} (W/L)_3}} = 4V$$

To decrease V_{3G} , either decrease V_{1G} or decrease $V_{ov/3}$ (from 1V). But decreasing V_{1G} will affect current mirroring, and will need changing of $(W/L)_2$ to restore the current.
 So change $V_{ov/3}$ by increasing $(W/L)_3$ by 4X

b) : Find the output resistance R_{out} as indicated in the figure. Neglect channel length modulation for $M1$ and $M4$.



∴ No current can flow into $M1$ ∴ $v_{g1} = 0$

$$\therefore i_1 = \frac{V_{test}}{R_{ds}}$$

To find i_2 we need v_{g3} and v_{g4} .

$$v_{g3} = V_{test}$$

$$KCL @ v_{g1} \Rightarrow g_m v_{g3} + \frac{v_{g1}}{R_{ds}} = 0$$

(∴ $v_{g1} = 0$)

$$\Rightarrow v_{g1} = -g_m R_{ds} v_{g3} = -g_m R_{ds} V_{test}$$

$$\therefore i_2 = g_m (V_{test} - v_{g1})$$

$$= g_m (1 + g_m R_{ds}) V_{test}$$

$$\therefore i_{test} = \frac{V_{test}}{R_{ds}} + g_m (1 + g_m R_{ds}) V_{test}$$

$$\Rightarrow \frac{i_{test}}{V_{test}} = g_{ds} + g_m + g_m^2 R_{ds}$$

$$\Rightarrow R_{out} = \frac{1}{g_m^2 R_{ds} + g_m + g_{ds}} \approx \frac{1}{g_m^2 R_{ds}}$$