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CS2023 - Data Structures and

Algorithms

Take Home Assignment

Week 2 Complexity Analysis

March 09, 2023

You are required to answer the below questions and submit a PDF to the submission link provided under this week before the deadline (no extensions will be provided). You can either write / type your answers, but either way your answers should be readable.

Question 1

Study the Little Oh notation (o), Big Omega Notation (Ω) and Little Omega Notation (ω).

Note.: You should define. what these symbols mean and provide examples if possible.

Question 2

What are the relationships between the θ , O , o , and ω notations?

Note.: Please use a table to compare and contrast them

Question 3

Study the optimized Bubble sort algorithms given in the next page and

1. Analyze them for worst case time complexity.

2. Is there a difference in worst case time complexities?

3. Is there an easy method to analyze only the worst- c a s e time complexity?

1

Algorithm 1 Bubble Sort Optimized

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```
if (A[i] — 1|> A[j]) then
temp = A[j]
A[j] = A[i] — 1|
A[i] — 1| = temp
swapped = true
if (! swapped) then
break;
n = newLimit
Algorithm 2 Bubble Sort Optimized - Version II
n = A.length
do
swapped = false
for i = 2 to n do
if (A[i] — 1| > A[j]) then
temp = A[j]
A[j] = A[i] - 1|
A[i] - 1| = temp
swapped = true
newLimit = i-1
```

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Question 1



Little Oh notation (o):

The little oh notation is used to describe the upper bound of the growth rate of a function. It is used to denote that a function $f(n)$ grows strictly slower than $g(n)$ as n approaches infinity. Mathematically, we say $f(n) = o(g(n))$ if for any positive constant c , there exists a value n_0 such that $f(n) < c \cdot g(n)$ for all $n > n_0$.

For example, if $f(n) = n^2$ and $g(n) = n^3$, then we can say $f(n) = o(g(n))$ because n^2 grows strictly slower than n^3 as n approaches infinity.

Big Omega Notation (Ω):

The big omega notation is used to describe the lower bound of the growth rate of a function. It is used to denote that a function $f(n)$ grows at least as fast as $g(n)$ as n approaches infinity. Mathematically, we say $f(n) = \Omega(g(n))$ if for any positive constant c , there exists a value n_0 such that $f(n) > c \cdot g(n)$ for all $n > n_0$.

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The little omega notation is used to describe the lower bound of the growth rate of a function, but strictly faster than $g(n)$. It is used to denote that a function $f(n)$ grows strictly faster than $g(n)$ as n approaches infinity. Mathematically, we say $f(n) = \omega(g(n))$ if for any positive constant c , there exists a value n_0 such that $f(n) > c \cdot g(n)$ for all $n > n_0$.

For example, if $f(n) = n^3$ and $g(n) = n^2$, then we can say $f(n) = \omega(g(n))$ because n^3 grows strictly faster than n^2 as n approaches infinity.

Question 2

The table below shows the relationships between the θ , O , o , and ω notations.

Notation	Definition	Upper Bound	Lower Bound	Tight Bound
O	$f(n)$ is	Yes	No	No
	bounded			
Ω	$f(n)$ is			No
	lower bounded			

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ω	$f(n)$ is	No	Yes	No
	tightly			
o	$f(n)$ is	Yes	No	No
	tightly			

- The big O notation (O) is an upper bound on the growth rate of a function.
- The big ω notation (Ω) is a lower bound on the growth rate of a function.
- The θ notation (θ) is a tight bound on the growth rate of a function.
- The little ω notation (ω) is a lower bound on the growth rate of a function, but strictly faster than $g(n)$.
- The little o notation (o) is an upper bound on the growth rate of a function, but strictly slower than g .

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