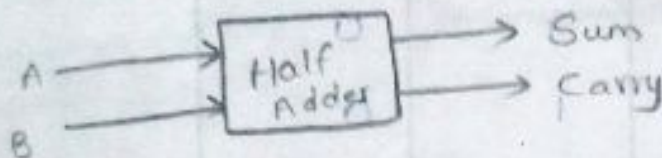


unit-3 Combinational digital Circuits

Half Adder :-

Half Adder is used for adding two bits. It contains Sum and Carry

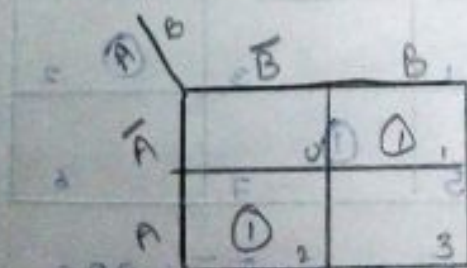
Block diagram



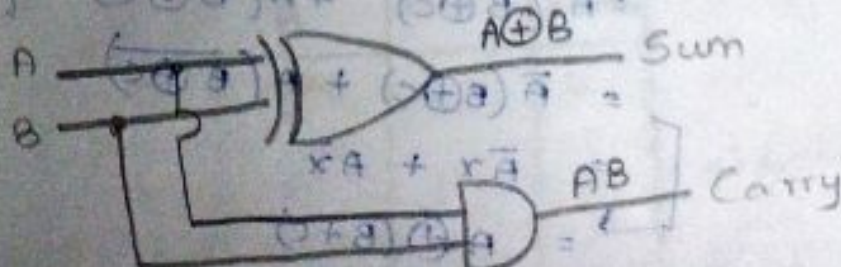
Truth Table

A	B	Sum	Carry
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

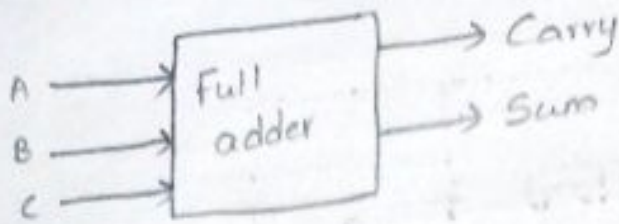
Sum :-



$$\text{Sum} = \bar{A}B + A\bar{B} = A \oplus B$$



Full adder



Truth table

A	B	C	Sum	Carry
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

K-map Simplification

A \ BC	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$
\bar{A}	0	① 1	3	① 2
A	① 4	5	① 7	6

$$\text{Sum} = \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$$

$$= \bar{A}(\bar{B}C + B\bar{C}) + A(\bar{B}\bar{C} + BC)$$

$$= \bar{A}(B \oplus C) + A(B \odot C)$$

$$= \bar{A}(B \oplus C) + A(\overline{B \oplus C})$$

$$\begin{aligned} &= \bar{A}x + A\bar{x} \\ &\rightarrow = A \oplus (B \oplus C) \end{aligned}$$

$$\text{Sum} = A \oplus B \oplus C$$

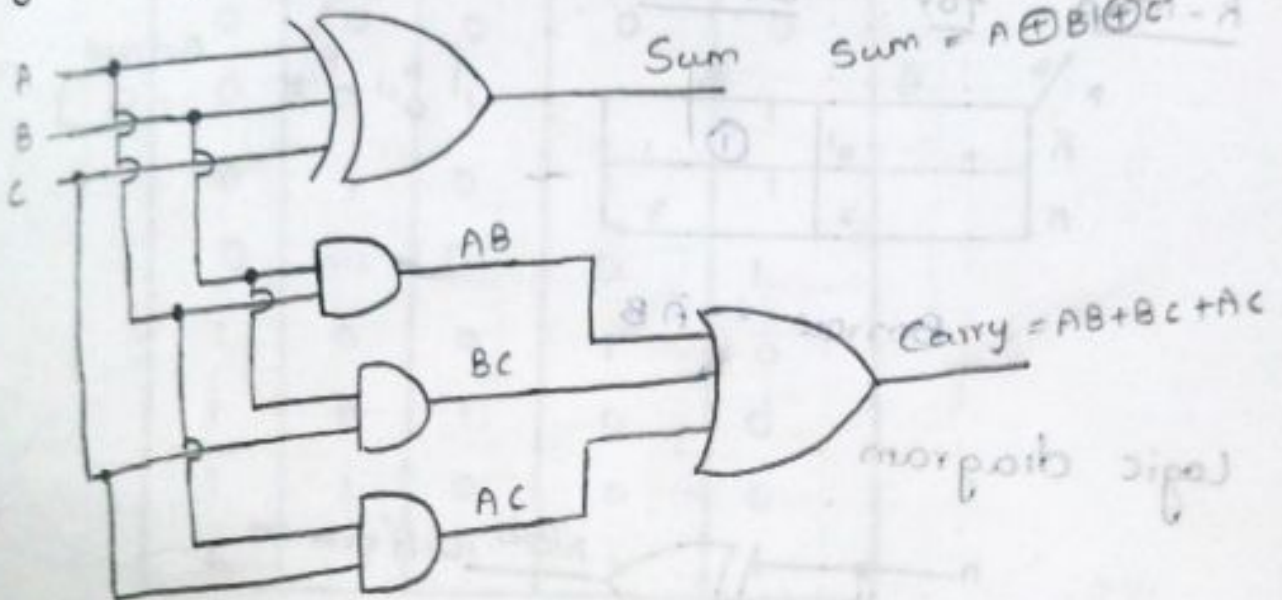
$$\begin{aligned} B \oplus C &= \bar{B}\bar{C} \\ B \odot C &= \overline{B \oplus C} \\ B \oplus C &= x \\ \overline{B \oplus C} &= \bar{x} \end{aligned}$$

for Carry

	$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	BC
\bar{A}	0	1	1	3
A	4	1	1	1

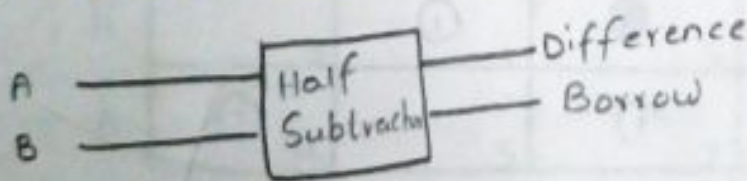
$$\text{Carry} = AB + BC + AC$$

Logic diagram



Half Subtractor :-

Half adder is used for subtracting two bits.
It contains diff and borrow



Truth table

A	B	Diff	Borrow
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$\Rightarrow 0 - 1 = -1$$

↓
Negative

$$\Rightarrow 1 - 0 = 1$$

$$\Rightarrow 1 - 1 = 0$$

K-Map for Difference

A \ B	\bar{B}	B
\bar{A}	0	①
A	①	3

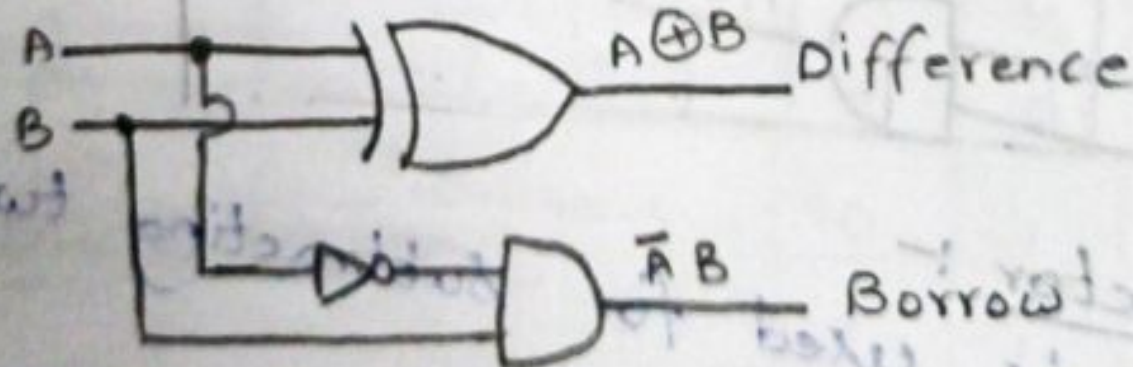
$$\begin{aligned}\text{Difference} &= A\bar{B} + \bar{A}B \\ &= A \oplus B\end{aligned}$$

K-Map for Borrow

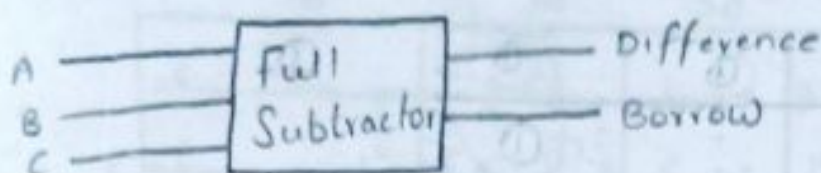
A \ B	\bar{B}	B
\bar{A}	0	①
A	2	3

$$\text{Borrow} = \bar{A}B$$

Logic diagram



full Subtractor



Truth table

A	B	C	Diff	Borrow
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

K-map Simplification for Difference

A \ BC	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$
\bar{A}		①	②	①
A	①		①	

$$\text{Difference} = A\bar{B}\bar{C} + \bar{A}\bar{B}C + ABC + \bar{A}B\bar{C}$$

$$= \bar{B}(A\bar{C} + \bar{A}C) + B(AC + \bar{A}\bar{C})$$

$$= \bar{B}(A \oplus C) + B(A \odot C)$$

$$= \bar{B}(A \oplus C) + B(\overline{A \oplus C})$$

$$= B \oplus (A \oplus C)$$

$$= A \oplus B \oplus (A + C)$$

$$= A \oplus B \oplus C$$

$$A\bar{C} + \bar{A}C = A \oplus C$$

$$AC + \bar{A}\bar{C} = A \odot C$$

$$A \odot C = \overline{A \oplus C}$$

$$A \oplus C = \overline{A \odot C}$$

$$\frac{A \odot C}{A \oplus C} = \frac{x}{\bar{x}}$$

$$\bar{B}x + B\bar{x}$$

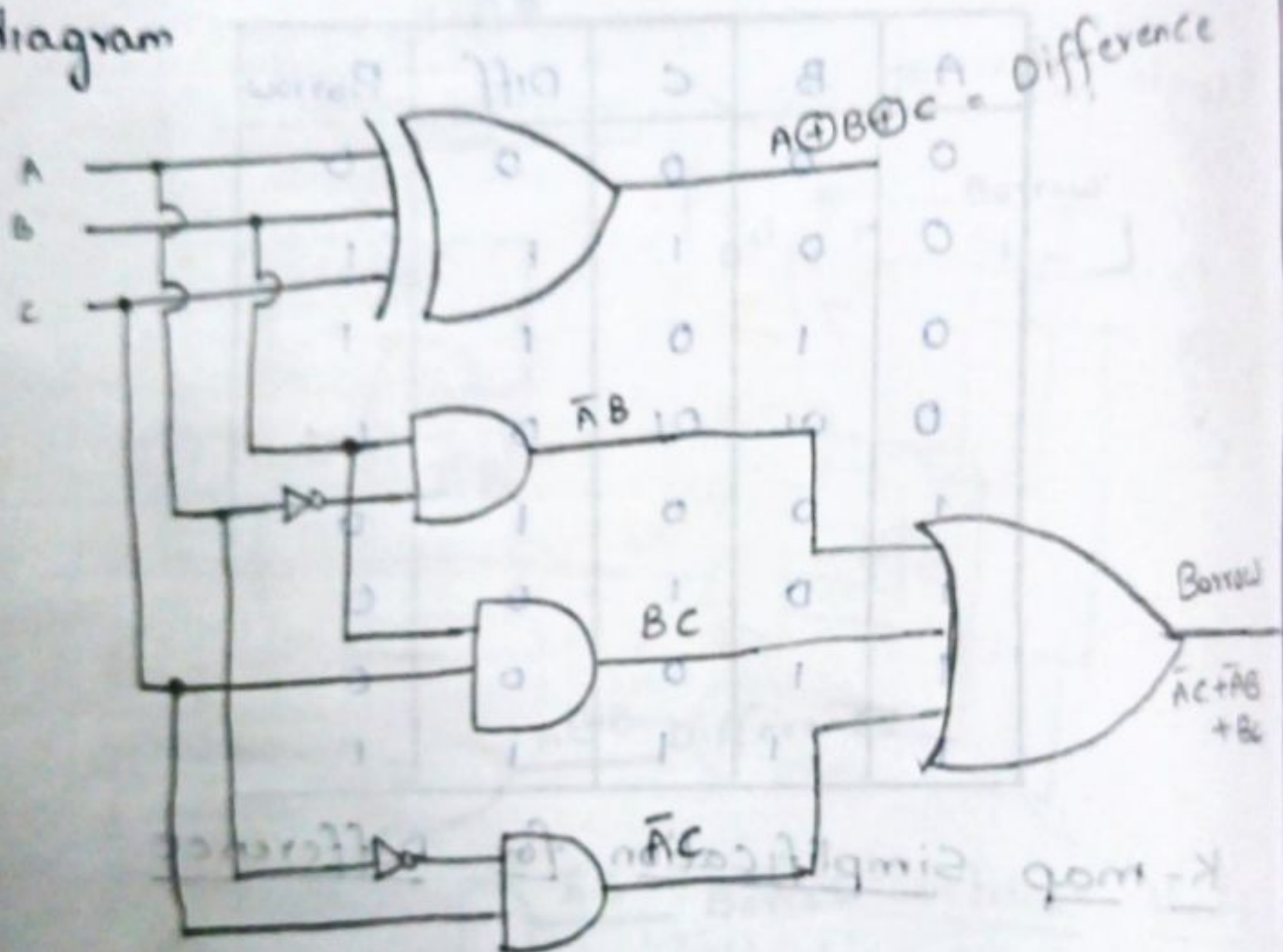
$$= B \oplus x$$

K-Map for Borrow

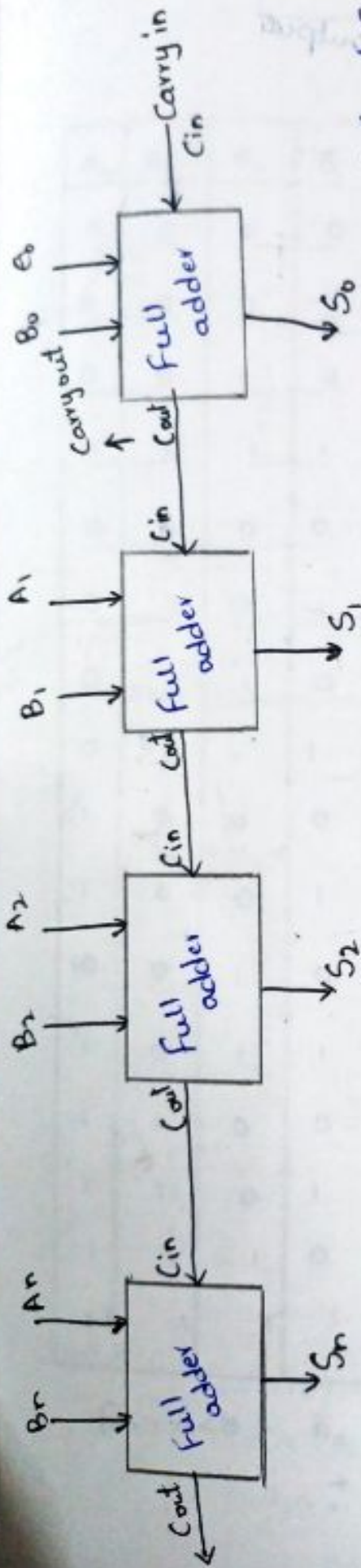
	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$A\bar{C}$
\bar{A}		① 1	① 3	① 2
A			① 7	

$$\text{Borrow} = \bar{A}C + \bar{A}B + BC$$

Logic diagram



parallel binary adder



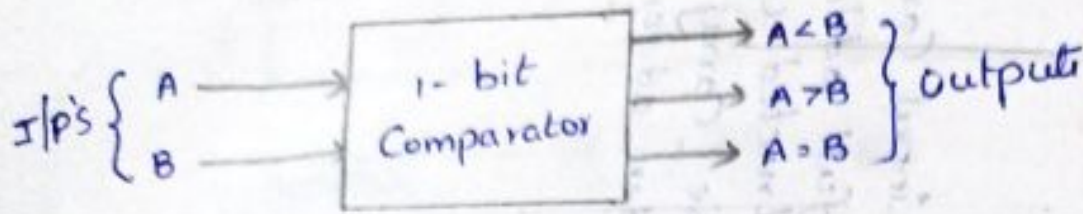
→ Single full adder is capable of adding two bit numbers and input carry. In order to add binary numbers with more than 1 bit additional full adder may be use. For this purpose a "n" bit parallel adder can be constructed using number of full adder connected in parallel. In this the Carry out of each adder is connected to the Carry input of the next higher order adder.

gf Suppose $n=4$

A_3	A_2	A_1	A_0	
1	0	0	0	
B_3	B_2	B_1	B_0	
1	1	0	0	
0	1	0	0	
Carry ← ①				

Magnitude Comparator

The Comparator is used for Comparing the number of bits.



A to Value
B to Value
Compare
Condition
denote true
as the
and false
magnitude

A	B	$A < B$	$A > B$	$A = B$
0	0	0	0	1
0	1	1	0	0
1	0	0	1	0
1	1	0	0	1

K-map

for $A < B$

$$= \bar{A}B$$

(A ki 0 karuka A)

for $A > B$

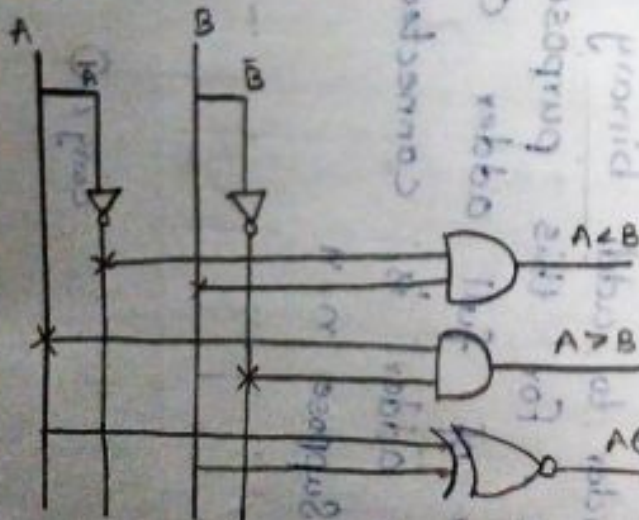
$$= A\bar{B}$$

for $A = B$

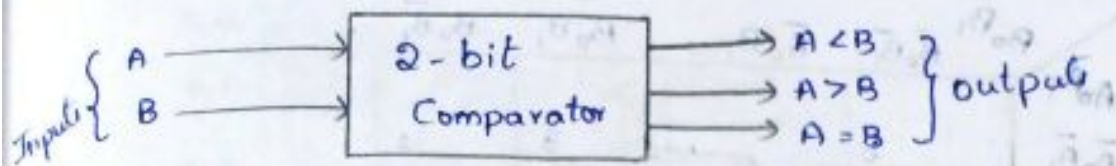
$$= \bar{A}\bar{B} + AB$$

$$= A \oplus B$$

Logic diagram



2-bit Comparator



A ₀	A ₁	B ₀	B ₁	A < B	A > B	A = B
0	0	0	0	0	0	1
0	0	0	1	1	0	0
0	0	1	0	1	0	0
0	0	1	1	1	0	0
0	1	0	0	0	1	0
0	1	0	1	0	0	1
0	1	1	0	1	0	0
0	1	1	1	1	0	0
1	0	0	0	0	1	0
1	0	0	1	0	1	0
1	0	1	0	0	0	1
1	0	1	1	1	0	0
1	1	0	0	0	1	0
1	1	0	1	0	1	0
1	1	1	0	0	1	0
1	1	1	1	0	0	1

Logic diagram

0 0 → 0
 0 1 → 1
 1 0 → 2
 1 1 → 3

for $A < B$:

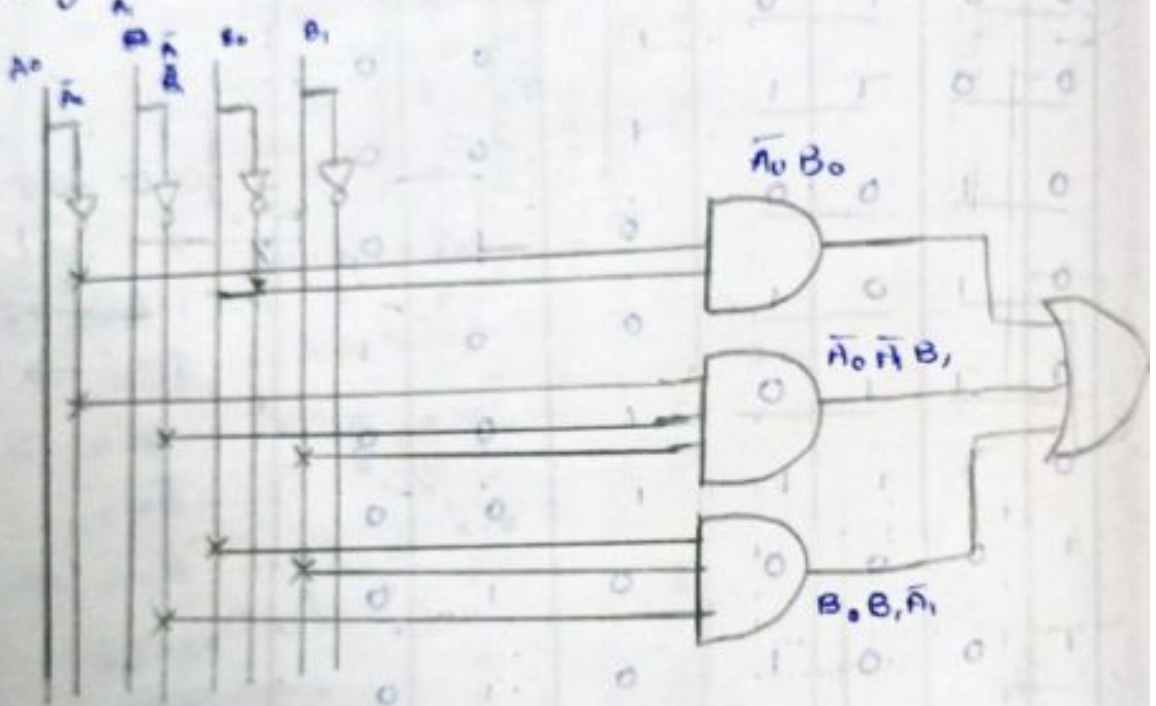
$$\bar{A}_0 \bar{A}_1 \bar{B}_0 B_1 + \bar{A}_0 \bar{A}_1 B_0 \bar{B}_1 + \bar{A}_0 \bar{A}_1 B_0 B_1 + \bar{A}_0 A_1 B_0 \bar{B}_1 + \bar{A}_0 A_1 B_0 B_1 + A_0 \bar{B}_0 \bar{B}_1$$

k-map for $A \oplus B$:-

	$B_0 B_1$	$\bar{B}_0 \bar{B}_1$	$\bar{B}_0 B_1$	$B_0 \bar{B}_1$
$A_0 \bar{A}_1$	0	1	3	2
$\bar{A}_0 \bar{A}_1$	4	5	7	6
$\bar{A}_0 A_1$	12	13	15	14
$A_0 A_1$	8	9	11	10

$$Y = \bar{A}_0 B_0 + \bar{A}_0 \bar{A}_1 B_1 + B_0 B_1 \bar{A}_1$$

Logic diagram



for $A \oplus B$:-

	$B_0 \bar{B}_1$	$\bar{B}_0 \bar{B}_1$	$B_0 B_1$	$\bar{B}_0 B_1$
$\bar{A}_0 \bar{A}_1$	0	1	3	2
$\bar{A}_0 A_1$	4	5	7	6
$A_0 \bar{A}_1$	12	13	15	14
$A_0 A_1$	8	9	11	10

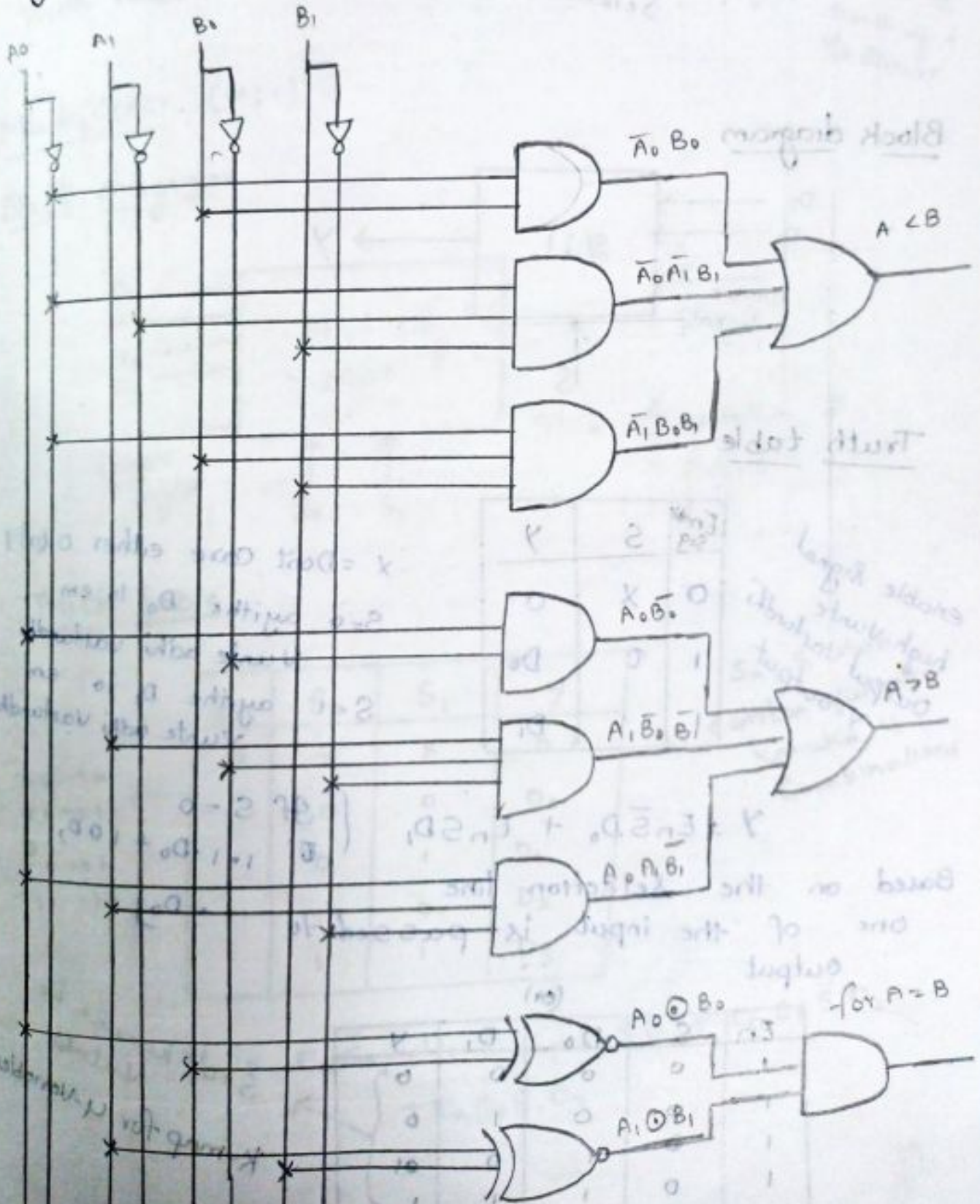
$$\begin{aligned}
 &= \bar{A}_0 \bar{A}_1 \bar{B}_0 \bar{B}_1 + \bar{A}_0 \bar{A}_1 B_0 B_1 + A_0 \bar{A}_1 B_0 \bar{B}_1 + A_0 \bar{A}_1 \bar{B}_0 B_1 \\
 &= \bar{A}_0 \bar{B}_0 (\bar{A}_1 \bar{B}_1 + A_1 B_1) + A_0 B_0 (A_1 B_1 + \bar{A}_1 \bar{B}_1) \\
 &= (\bar{A}_0 \bar{B}_0 + A_0 B_0) (\bar{A}_1 \bar{B}_1 + A_1 B_1) \\
 &= (A_0 \odot B_0) (A_1 \odot B_1)
 \end{aligned}$$

for $A > B$

$A_1 \backslash B_1$	$\bar{B}_1 \bar{B}_0$	$\bar{B}_1 B_0$	$B_1 \bar{B}_0$	$B_1 B_0$
$\bar{A}_0 \bar{A}_1$	0	1	3	2
$\bar{A}_0 A_1$	4	5	7	6
$A_0 \bar{A}_1$	12	13	15	14
$A_0 A_1$	8	9	11	10

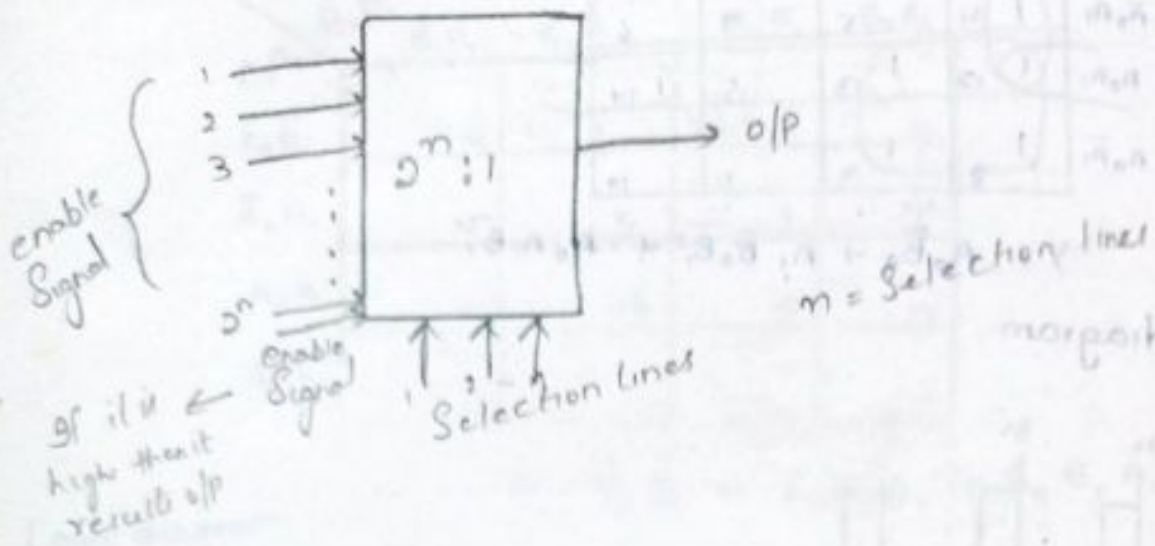
$$Y = A_0 \bar{B}_0 + A_1 \bar{B}_0 \bar{B}_1 + A_0 A_1 \bar{B}_1$$

Logic diagram

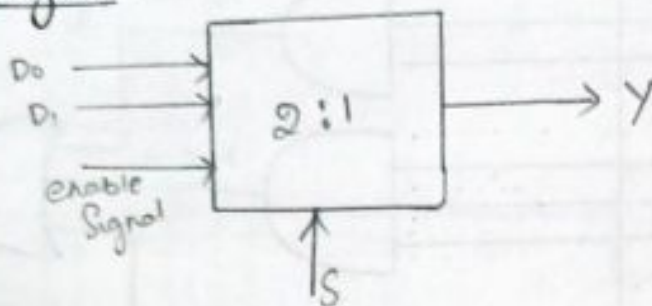


Multiplexer :- (MUX)

(2:1)



Block diagram



Truth table

enable signal
high vante
output vartundhi
Y-output

Enable Sig	S	Y
0	X	0
1	0	D_0
1	1	D_1

X = Don't care either 0 or 1
 $S=0$ ayithe D_0 lo em
 vunte adhi vartundhi
 $S=1$ ayithe D_1 lo em
 vunte adhi vartundhi

$$Y = E_n \bar{S} D_0 + E_n S D_1$$

if $S=0$
 $0 = 0 \cdot 1 \cdot D_0 + 1 \cdot 0 \cdot D_1$
 $= D_0$

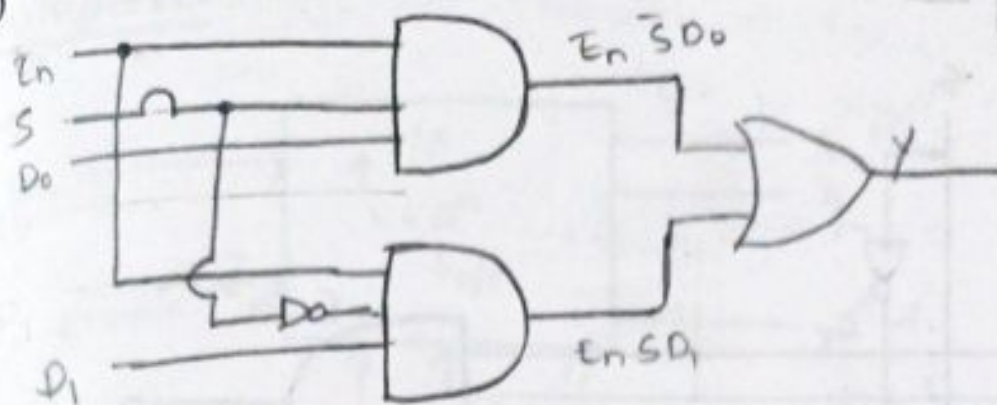
Based on the Selection line
 one of the input is passed to
 output

(en)

En	S	D_0	D_1	Y
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$S=0$ kanuka D_0
 Valid
 K-map for 4-Variable

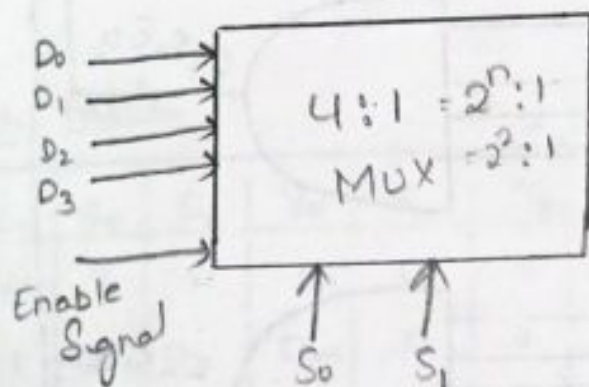
Logic diagram



Truth Table

Multiplexer (4:1)

Block diagram



$n=2$ Karuka 2 Signals

Truth table

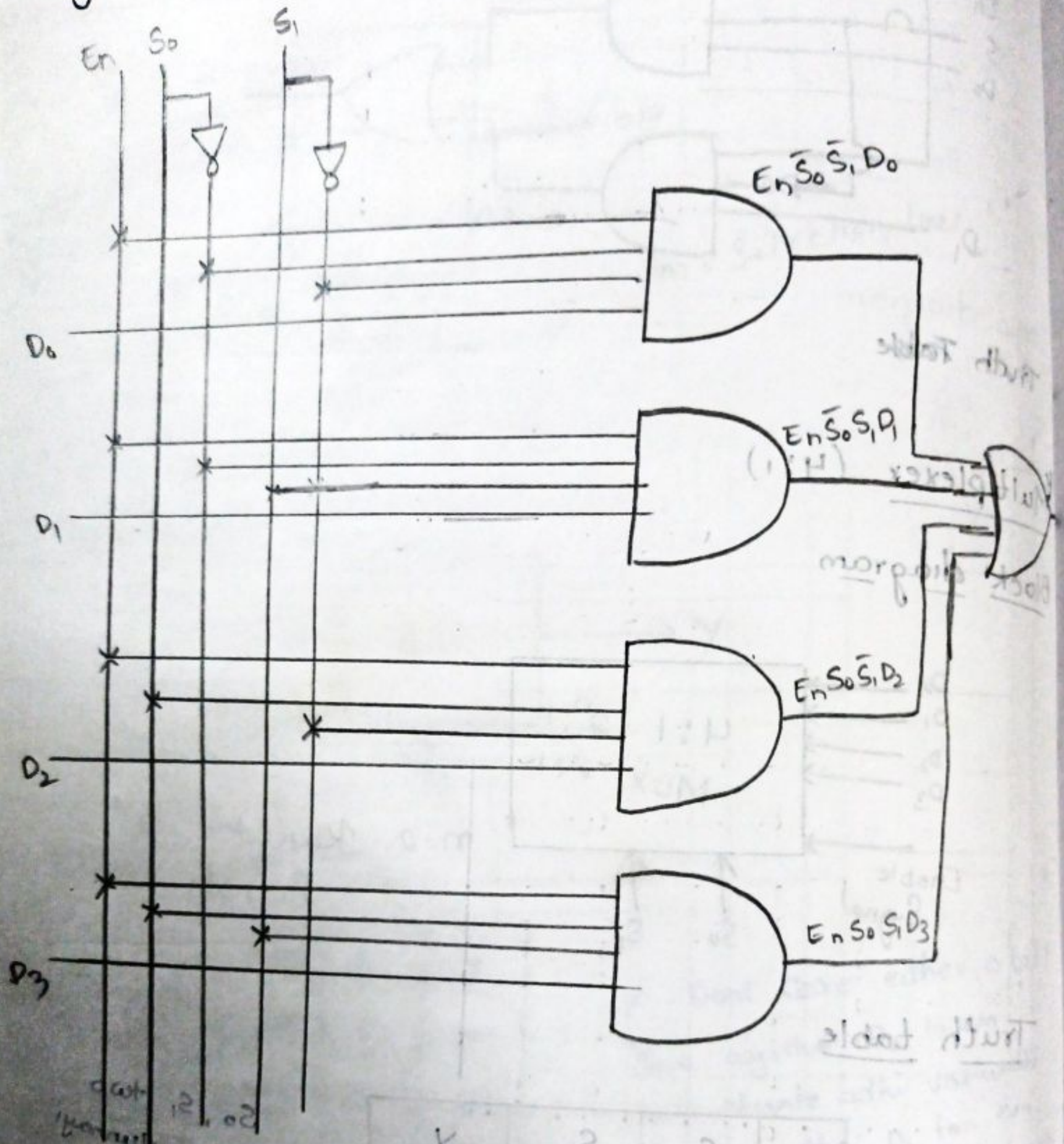
00 → 0
01 → 1
10 → 2
11 → 3

En	S ₀	S ₁	Y
0	x	x	0
1	0	0	D ₀
1	0	1	D ₁
1	1	0	D ₂
1	1	1	D ₃

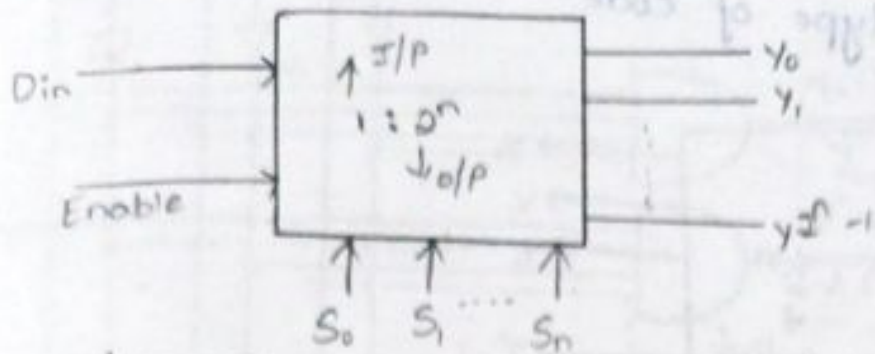
S₀, S₁ two combinations Vannayi Karuka 4 combinations

$$Y = E_n \bar{S}_0 \bar{S}_1 D_0 + E_n \bar{S}_0 S_1 D_1 + E_n S_0 \bar{S}_1 D_2 + E_n S_0 S_1 D_3$$

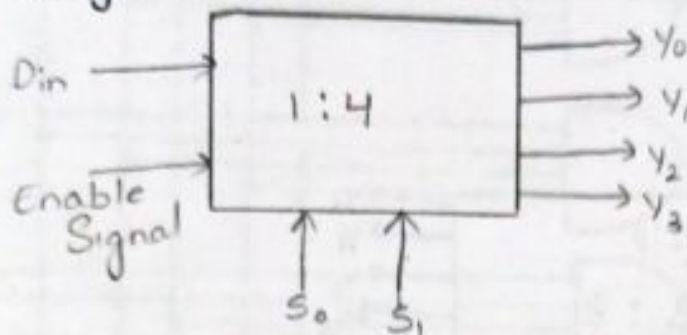
Logic diagram



Demultiplexer:-



Block diagram



Truth table

En	S ₀	S ₁	y ₀	y ₁	y ₂	y ₃
0	x	x	0	0	0	0
1	0	0	Din	0	0	0
1	0	1	0	Din	0	0
1	1	0	0	0	Din	0
1	1	1	0	0	0	Din

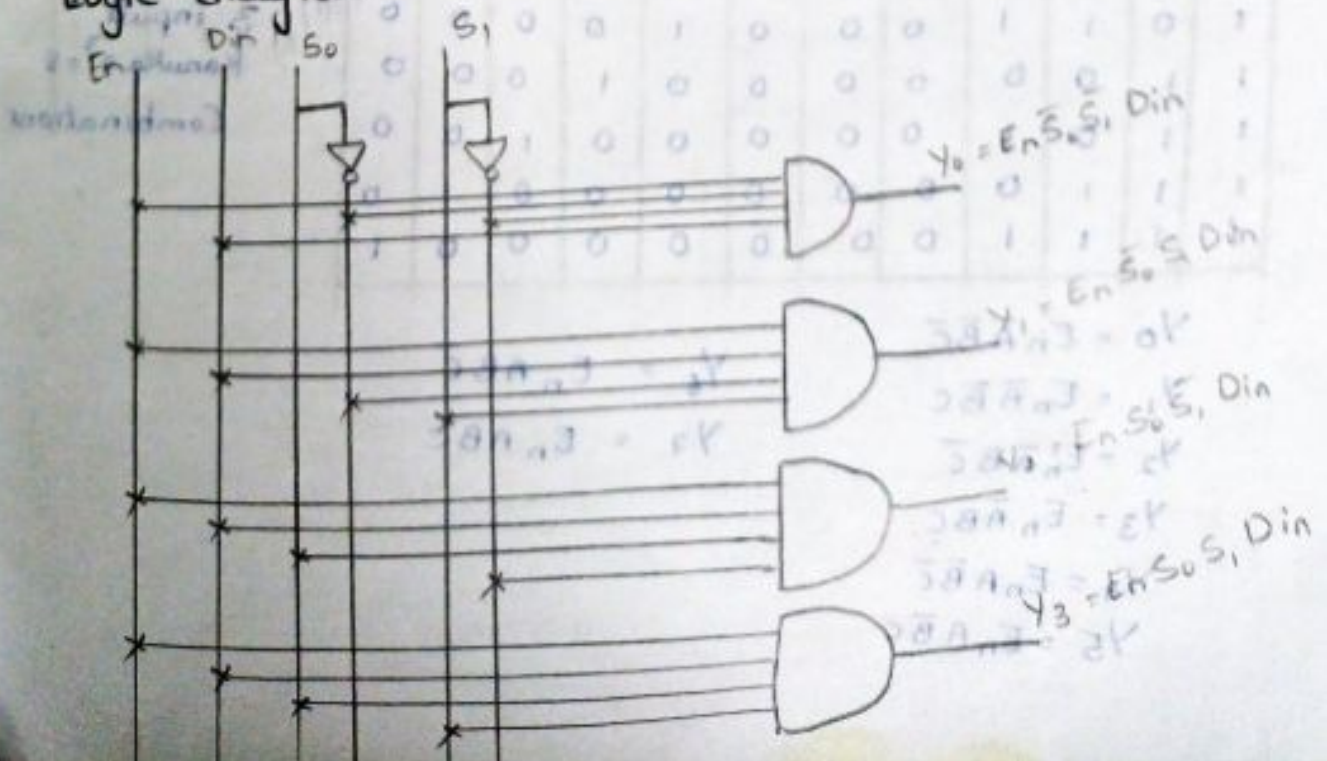
$$y_0 = E_n \bar{S}_0 \bar{S}_1 \text{ Din}$$

$$y_1 = E_n \bar{S}_0 S_1 \text{ Din}$$

$$y_2 = E_n S_0 \bar{S}_1 \text{ Din}$$

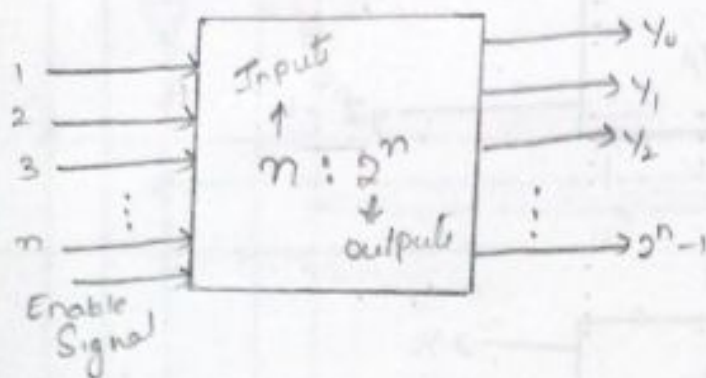
$$y_3 = E_n S_0 S_1 \text{ Din}$$

Logic diagram

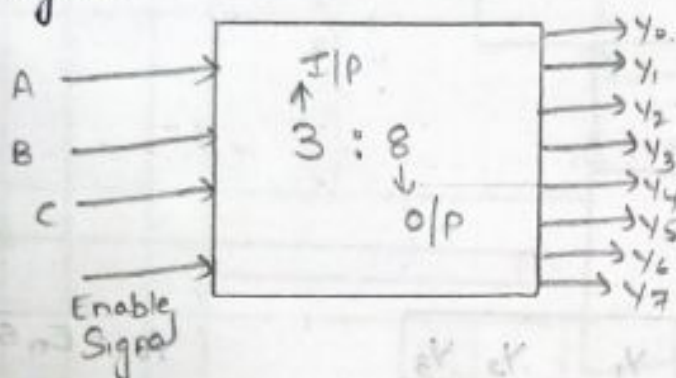


Decoder :-

Decoder are used to Convert one type of code to another type of code.



Block diagram



Truth table

En	A	B	C	y_0	y_1	y_2	y_3	y_4	y_5	y_6	y_7
0	x	x	x	0	0	0	0	0	0	0	0
1	0	0	0	1	0	0	0	0	0	0	0
1	0	0	1	0	1	0	0	0	0	0	0
1	0	1	0	0	0	1	0	0	0	0	0
1	0	1	1	0	0	0	1	0	0	0	0
1	1	0	0	0	0	0	0	1	0	0	0
1	1	0	1	0	0	0	0	0	1	0	0
1	1	1	0	0	0	0	0	0	0	1	0
1	1	1	1	0	0	0	0	0	0	0	1

$$y_0 = E_n \bar{A} \bar{B} \bar{C}$$

$$y_1 = E_n \bar{A} \bar{B} C$$

$$y_2 = E_n \bar{A} B \bar{C}$$

$$y_3 = E_n \bar{A} B C$$

$$y_4 = E_n A \bar{B} \bar{C}$$

$$y_5 = E_n A \bar{B} C$$

$$y_6 = E_n A B \bar{C}$$

$$y_7 = E_n A B C$$

$$000 \rightarrow 0$$

$$001 \rightarrow 1$$

$$010 \rightarrow 2$$

$$\vdots$$

$$111 \rightarrow 7$$

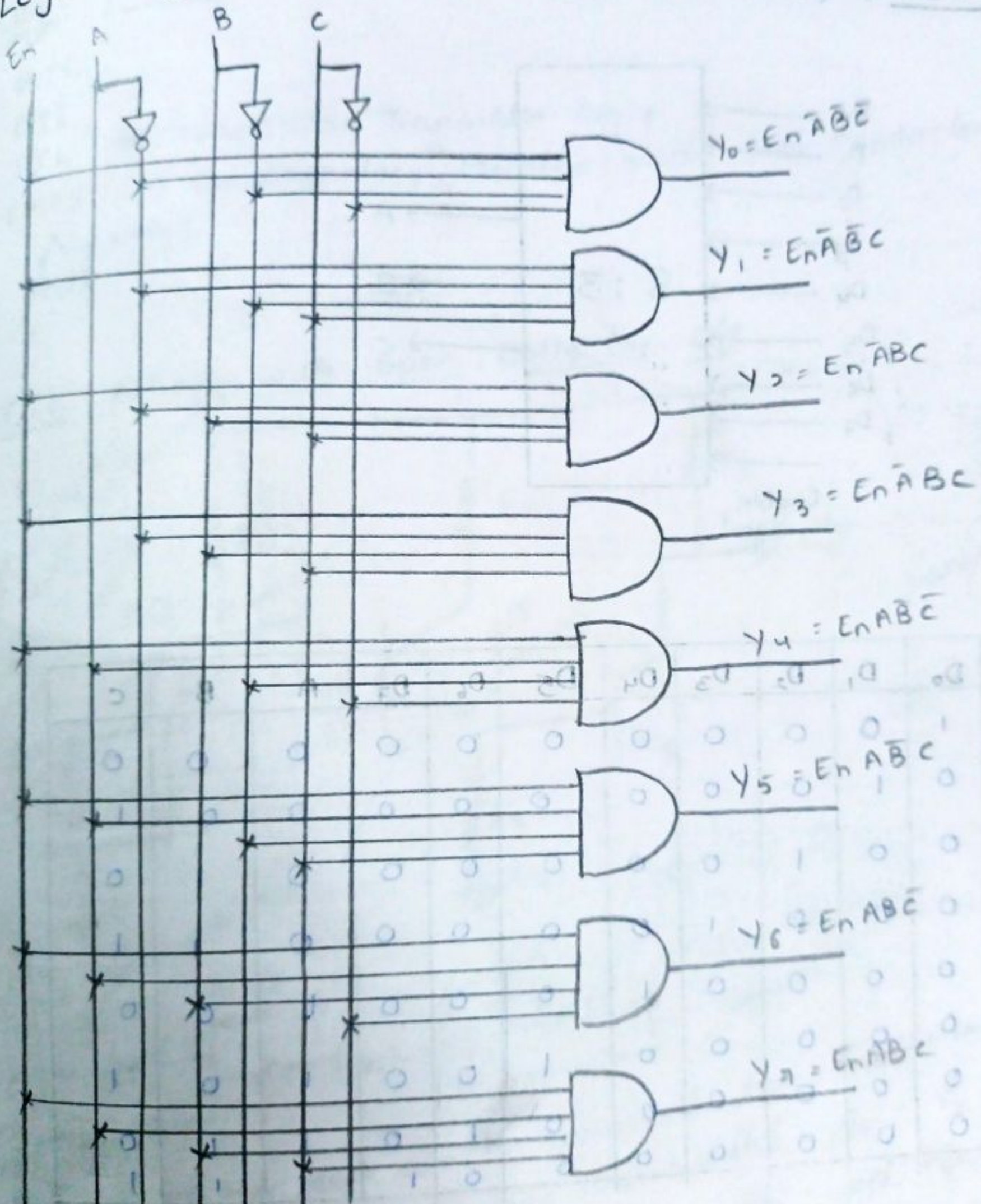
3 inputs

$$\text{Karnaugh } 2^3 = 8$$

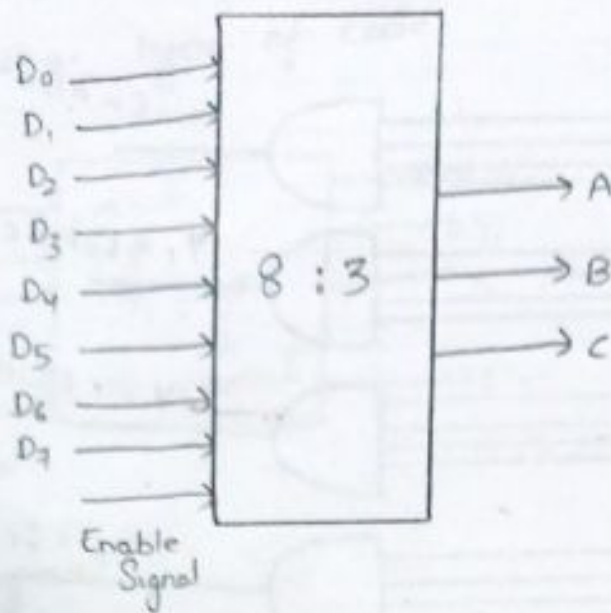
Combinations

Logic diagram

Encoder: (8 to 3)



Encoder :- (8 to 3)



$D_0 \rightarrow 000$
 $D_1 \rightarrow 001$

	D_0	D_1	D_2	D_3	D_4	D_5	D_6	D_7	A	B	C
	1	0	0	0	0	0	0	0	0	0	0
	0	1	0	0	0	0	0	0	0	0	1
	0	0	1	0	0	0	0	0	0	1	0
	0	0	0	1	0	0	0	0	0	1	1
	0	0	0	0	1	0	0	0	1	0	0
	0	0	0	0	0	1	0	0	1	0	1
	0	0	0	0	0	0	1	0	1	1	0
	0	0	0	0	0	0	0	1	1	1	1

$$A = D_4 + D_5 + D_6 + D_7$$

$$B = D_2 + D_3 + D_6 + D_7$$

$$C = D_1 + D_3 + D_5 + D_7$$

